



جامعة الطائف
TAIF UNIVERSITY



PRINCIPLES OF DATA SCIENCE

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CHAPTER 5: IMPOSSIBLE OR IMPROBABLE – A GENTLE INTRODUCTION TO PROBABILITY

- BASIC DEFINITIONS
 - PROBABILITY
 - BAYESIAN VERSUS FREQUENTIST
 - COMPOUND EVENTS
 - CONDITIONAL PROBABILITY
 - THE RULES OF PROBABILITY
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BASIC DEFINITIONS

Basic definitions

- **A procedure** is an act that leads to a result. For example,
 - throwing a dice
 - visiting a website.
- **An event** is a collection of the outcomes of a procedure, such as
 - getting a heads on a coin flip
 - leaving a website after only 4 seconds.
- **A simple event** is an outcome/event of a procedure that cannot be broken down further.
 - For example, rolling two dice can be broken down into two simple events: rolling die 1 and rolling die 2.
- **The sample space** of a procedure is the set of all possible simple events. For example, an experiment is performed, in which a coin is flipped three times in succession.
 - **What is the size of the sample space for this experiment?**
 - The answer is eight, because the results could be any one of the possibilities in the following sample space—{HHH, HHT, HTT, HTH, TTT, TTH, THH, or THT}.



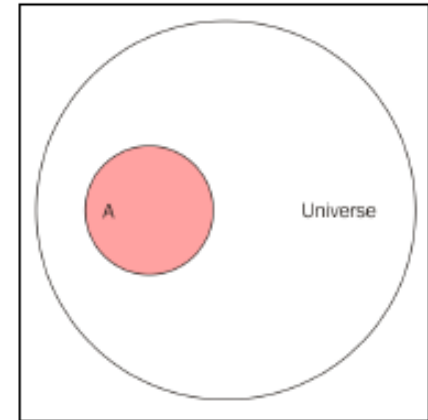
PROBABILITY

Probability

- The **probability of an event** represents the frequency, or chance, that the event will happen.
- For notation, if A is an event, $P(A)$ is the probability of the occurrence of the event.
- We can define the actual probability of an event, A , as follows:

$$P(A) = \frac{\text{number of ways A occur}}{\text{size of sample space}}$$

- Here, A is the event in question. Think of an entire universe of events where anything is possible, and let's represent it as a circle. We can think of a single event, A , as being a smaller circle within that larger universe, as shown in the following diagram:



Probability

- The maximum probability of any event is 1. This can be understood as the red circle grows so large that it is the size of the universe (the larger circle).
- **Example 1:** Let's now pretend that our universe involves a research study on humans, and the A event is people in that study who have cancer. If our study has 100 people and A has 25 people, the probability of A or $P(A)$ is $25/100$.
- **Example 2:** Let's say we have two coins and we want the probability that we will roll two heads. First, let's define A . It is the event in which two heads occur. The number of ways that A can occur is 1. Second, The sample space of the experiment is $\{HH, HT, TH, TT\}$, where each two-letter word indicates the outcome of the first and second coin simultaneously. The size of the sample space is four. So, $P(\text{getting two heads}) = 1/4$.



BAYESIAN VERSUS FREQUENTIST

Bayesian versus Frequentist

- **In a Frequentist approach**, the probability of an event is calculated through experimentation. It uses the past in order to predict the future chance of an event.
- The basic formula is as follows:

$$P(A) = \frac{\text{number of times A occurred}}{\text{number of times the procedure was repeated}}$$

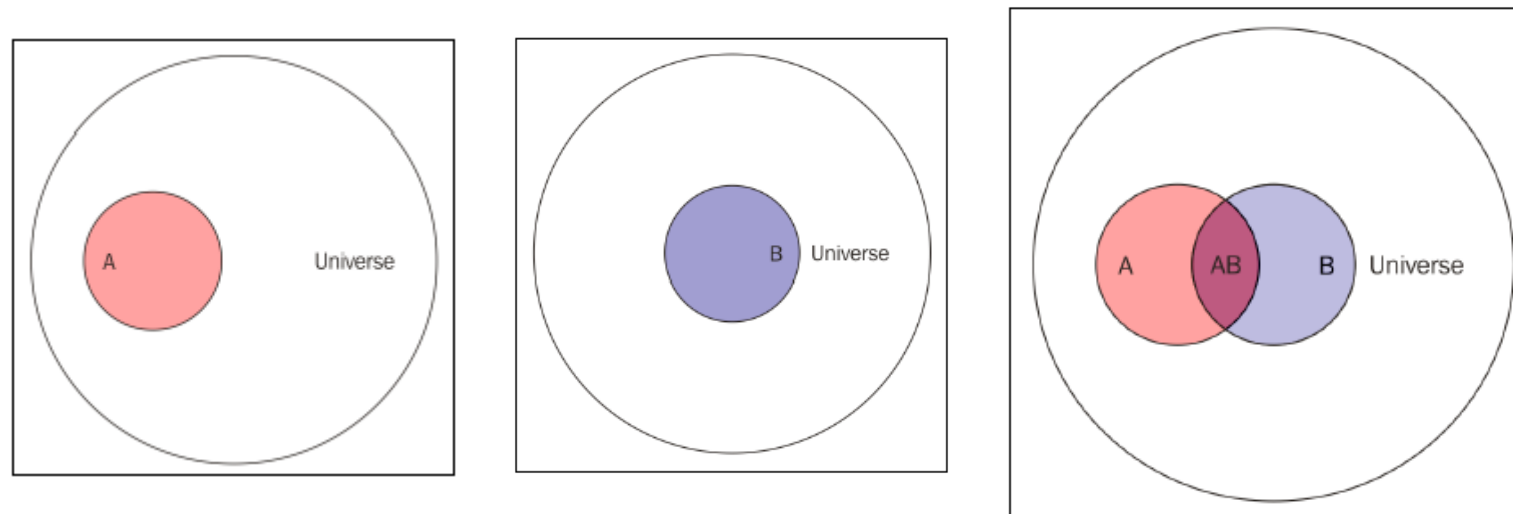
- Basically, we observe several instances of the event and count the number of times A was satisfied. The division of these numbers is an approximation of the probability.
- **The Bayesian approach** differs by dictating that probabilities must be discerned using theoretical means. Using the Bayes approach, we would have to think a bit more critically about events and why they occur.
- **The relative frequency of an event** is how often an event occurs divided by the total number of observations.



COMPOUND EVENTS

Compound events

- Sometimes, we need to deal with two or more events. These are called **compound events**.
- A compound event is any event that combines two or more simple events.
- When this happens, we need some special notation. Given events A and B:
 - The probability that A and B occur is $P(A \cap B) = P(A \text{ and } B)$
 - The probability that either A or B occurs is $P(A \cup B) = P(A \text{ or } B)$



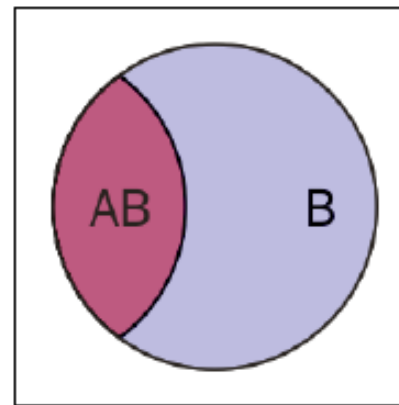


CONDITIONAL PROBABILITY

Conditional probability

- A **conditional probability** of A given B or $P(A|B)$, it is asking you to calculate the probability of an event given that another event has already happened.
- The formula can be given as follows:

$$P(A|B) = P(A \text{ and } B) / P(B)$$





THE RULES OF PROBABILITY

The rules of probability

- **The addition rule:** The addition rule is used to calculate the probability of *either or* events.

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

- **Mutual exclusivity:** We say that two events are mutually exclusive if they cannot occur at the same time. This means that $A \cap B = \emptyset$ or just that the *intersection* of the events is the empty set.

$$P(A \cup B) = P(A \text{ or } B) = P(A) + P(B) - P(A \cap B) = P(A) + P(B)$$

- **The multiplication rule:** The multiplication rule is used to calculate the probability of *and* events.

$$P(A \cap B) = P(A \text{ and } B) = P(A) \cdot P(B|A)$$

- **Independence:** Two events are independent if one event *does not* affect the outcome of the other, that is $P(B|A) = P(B)$ and $P(A|B) = P(A)$. If two events are independent, then: $P(A \cap B) = P(A) \cdot P(B|A) = P(A) \cdot P(B)$

- **Complementary events:** The complement of A is the *opposite* or *negation* of A.

$$P(\bar{A}) = 1 - P(A)$$



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