Social network Graph Link Prediction - Facebook Challenge

```
In [1]:
         #Importing Libraries
         # please do go through this python notebook:
         import warnings
         warnings.filterwarnings("ignore")
         import csv
         import pandas as pd#pandas to create small dataframes
         import datetime #Convert to unix time
         import time #Convert to unix time
         # if numpy is not installed already : pip3 install numpy
         import numpy as np#Do aritmetic operations on arrays
         # matplotlib: used to plot graphs
         import matplotlib
         import matplotlib.pylab as plt
         import seaborn as sns#Plots
         from matplotlib import rcParams#Size of plots
         from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
         import math
         import pickle
         import os
         # to install xgboost: pip3 install xgboost
         import xgboost as xgb
         import warnings
         import networkx as nx
         import pdb
         import pickle
         from pandas import HDFStore,DataFrame
         from pandas import read hdf
         from scipy.sparse.linalg import svds, eigs
         import qc
         from tqdm import tqdm
```

1. Reading Data

2. Similarity measures

2.1 Jaccard Distance:

http://www.statisticshowto.com/jaccard-index/

$$j = \frac{|X \cap Y|}{|X \cup Y|} \tag{1}$$

```
In [4]:
         #one test case
         print(jaccard for followees(273084,1505602))
        0.0
In [5]:
         #node 1635354 not in graph
         print(jaccard for followees(273084,1505602))
        0.0
In [6]:
         #for followers
         def jaccard for followers(a,b):
             try:
                 if len(set(train_graph.predecessors(a))) == 0 | len(set(g.predecessors(b))) == 0:
                     return 0
                 sim = (len(set(train graph.predecessors(a)).intersection(set(train graph.predecessors(b)))))/\
                                          (len(set(train graph.predecessors(a)).union(set(train graph.predecessors(b)))))
                 return sim
             except:
                 return 0
In [7]:
         print(jaccard for followers(273084,470294))
        0
In [8]:
         #node 1635354 not in graph
         print(jaccard for followees(669354,1635354))
```

2.2 Cosine distance

$$CosineDistance = \frac{|X \cap Y|}{|X| \cdot |Y|} \tag{2}$$

```
In [9]:
          #for followees
          def cosine for followees(a,b):
              try:
                  if len(set(train graph.successors(a))) == 0 | len(set(train graph.successors(b))) == 0:
                      return 0
                  sim = (len(set(train graph.successors(a)).intersection(set(train graph.successors(b)))))/\
                                               (math.sqrt(len(set(train graph.successors(a)))*len((set(train graph.successors(b)))
                  return sim
              except:
                  return 0
In [10]:
          print(cosine for followees(273084,1505602))
         0.0
In [11]:
          print(cosine for followees(273084,1635354))
In [12]:
          def cosine for followers(a,b):
              try:
                  if len(set(train graph.predecessors(a))) == 0 | len(set(train graph.predecessors(b))) == 0:
                      return 0
                  sim = (len(set(train graph.predecessors(a)).intersection(set(train graph.predecessors(b)))))/
                                                (math.sqrt(len(set(train graph.predecessors(a))))*(len(set(train graph.predecess)))
                  return sim
              except:
                  return 0
In [13]:
          print(cosine for followers(2,470294))
         0.02886751345948129
In [14]:
          print(cosine for followers(669354,1635354))
```

3. Ranking Measures

https://networkx.github.io/documentation/networkx-1.10/reference/generated/networkx.algorithms.link_analysis.pagerank_alg.pagerank.html

PageRank computes a ranking of the nodes in the graph G based on the structure of the incoming links.



Mathematical PageRanks for a simple network, expressed as percentages. (Google uses a logarithmic scale.) Page C has a higher PageRank than Page E, even though there are fewer links to C; the one link to C comes from an important page and hence is of high value. If web surfers who start on a random page have an 85% likelihood of choosing a random link from the page they are currently visiting, and a 15% likelihood of jumping to a page chosen at random from the entire web, they will reach Page E 8.1% of the time. (The 15% likelihood of jumping to an arbitrary page corresponds to a damping factor of 85%.) Without damping, all web surfers would eventually end up on Pages A, B, or C, and all other pages would have PageRank zero. In the presence of damping, Page A effectively links to all pages in the web, even though it has no outgoing links of its own.

3.1 Page Ranking

https://en.wikipedia.org/wiki/PageRank

```
In [15]:
    if not os.path.isfile('data/fea_sample/page_rank.p'):
        pr = nx.pagerank(train_graph, alpha=0.85)
        pickle.dump(pr,open('data/fea_sample/page_rank.p','wb'))
    else:
        pr = pickle.load(open('data/fea_sample/page_rank.p','rb'))

In [16]:
    print('min',pr[min(pr, key=pr.get)])
    print('max',pr[max(pr, key=pr.get)])
    print('mean',float(sum(pr.values())) / len(pr))

min 1.6556497245737814e-07
max 2.7098251341935827e-05
mean 5.615699699389075e-07
```

```
In [17]: #for imputing to nodes which are not there in Train data
    mean_pr = float(sum(pr.values())) / len(pr)
    print(mean_pr)

5.615699699389075e-07

In []:
```

4. Other Graph Features

4.1 Shortest path:

Getting Shortest path between twoo nodes, if nodes have direct path i.e directly connected then we are removing that edge and calculating path.

```
In [18]:
          #if has direct edge then deleting that edge and calculating shortest path
          def compute shortest path length(a,b):
              p=-1
              try:
                  if train graph.has edge(a,b):
                      train graph.remove edge(a,b)
                      p= nx.shortest path length(train graph,source=a,target=b)
                      train graph.add edge(a,b)
                  else:
                      p= nx.shortest path length(train graph,source=a,target=b)
                  return p
              except:
                  return -1
In [19]:
          #testing
          compute shortest_path_length(77697, 826021)
Out[19]: 10
In [20]:
          #testing
```

```
compute_shortest_path_length(669354,1635354)
```

Out[20]: -1

4.2 Checking for same community

```
In [21]:
          #getting weekly connected edges from graph
          wcc=list(nx.weakly_connected_components(train graph))
          def belongs to same wcc(a,b):
              index = []
              if train graph.has edge(b,a):
                  return 1
              if train graph.has edge(a,b):
                      for i in wcc:
                           if a in i:
                               index= i
                               break
                      if (b in index):
                          train graph.remove_edge(a,b)
                          if compute shortest path length(a,b)==-1:
                              train graph.add edge(a,b)
                               return 0
                           else:
                              train graph.add edge(a,b)
                               return 1
                      else:
                           return 0
              else:
                      for i in wcc:
                           if a in i:
                               index= i
                               break
                      if(b in index):
                           return 1
                      else:
                           return 0
In [22]:
          belongs_to_same_wcc(861, 1659750)
```

```
Out[22]: 0
In [23]: belongs_to_same_wcc(669354,1635354)
Out[23]: 0
```

4.3 Adamic/Adar Index:

Adamic/Adar measures is defined as inverted sum of degrees of common neighbours for given two vertices.

$$A(x,y) = \sum_{u \in N(x) \cap N(y)} rac{1}{log(|N(u)|)}$$

```
In [24]:
          #adar index
          def calc adar in(a,b):
              sum=0
              try:
                  n=list(set(train graph.successors(a)).intersection(set(train graph.successors(b))))
                  if len(n)!=0:
                      for i in n:
                          sum=sum+(1/np.log10(len(list(train graph.predecessors(i)))))
                      return sum
                  else:
                       return 0
              except:
                  return 0
In [25]:
          calc_adar_in(1,189226)
Out[25]: 0
In [26]:
          calc adar in(669354,1635354)
```

4.4 Is persion was following back:

```
In [27]: def follows_back(a,b):
    if train_graph.has_edge(b,a):
        return 1
    else:
        return 0

In [28]: follows_back(1,189226)

Out[28]: 1

In [29]: follows_back(669354,1635354)
Out[29]: 0
```

4.5 Katz Centrality:

https://en.wikipedia.org/wiki/Katz_centrality

https://www.geeksforgeeks.org/katz-centrality-centrality-measure/ Katz centrality computes the centrality for a node based on the centrality of its neighbors. It is a generalization of the eigenvector centrality. The Katz centrality for node i

$$x_i = lpha \sum_j A_{ij} x_j + eta,$$

where A is the adjacency matrix of the graph G with eigenvalues

 λ

The parameter

 β

controls the initial centrality and

$$\alpha < \frac{1}{\lambda_{max}}$$

```
In [30]:
          if not os.path.isfile('data/fea sample/katz.p'):
              katz = nx.katz.katz centrality(train graph,alpha=0.005,beta=1)
              pickle.dump(katz,open('data/fea sample/katz.p','wb'))
          else:
              katz = pickle.load(open('data/fea_sample/katz.p','rb'))
In [31]:
          print('min',katz[min(katz, key=katz.get)])
          print('max', katz[max(katz, key=katz.get)])
          print('mean',float(sum(katz.values())) / len(katz))
         min 0.0007313532484065916
         max 0.003394554981699122
         mean 0.0007483800935562018
In [32]:
          mean katz = float(sum(katz.values())) / len(katz)
          print(mean katz)
         0.0007483800935562018
```

4.6 Hits Score

The HITS algorithm computes two numbers for a node. Authorities estimates the node value based on the incoming links. Hubs estimates the node value based on outgoing links.

https://en.wikipedia.org/wiki/HITS_algorithm

In [33]:

```
if not os.path.isfile('data/fea_sample/hits.p'):
    hits = nx.hits(train_graph, max_iter=100, tol=1e-08, nstart=None, normalized=True)
    pickle.dump(hits,open('data/fea_sample/hits.p','wb'))
else:
    hits = pickle.load(open('data/fea_sample/hits.p','rb'))

In [34]:
    print('min',hits[0][min(hits[0], key=hits[0].get)])
    print('max',hits[0][max(hits[0], key=hits[0].get)])
    print('mean',float(sum(hits[0].values())) / len(hits[0]))

min 0.0
    max 0.004868653378780953
    mean 5.615699699344123e-07
```

5. Featurization

5. 1 Reading a sample of Data from both train and test

```
In [35]:
          import random
          if os.path.isfile('data/after eda/train after eda.csv'):
              filename = "data/after eda/train after eda.csv"
              # you uncomment this line, if you dont know the lentgh of the file name
              # here we have hardcoded the number of lines as 15100030
              # n train = sum(1 for line in open(filename)) #number of records in file (excludes header)
              n train = 15100028
              s = 100000 #desired sample size
              skip train = sorted(random.sample(range(1, n train+1), n train-s))
              #https://stackoverflow.com/a/22259008/4084039
In [36]:
          if os.path.isfile('data/after eda/train after eda.csv'):
              filename = "data/after eda/test after eda.csv"
              # you uncomment this line, if you dont know the lentgh of the file name
              # here we have hardcoded the number of lines as 3775008
              # n test = sum(1 for line in open(filename)) #number of records in file (excludes header)
              n test = 3775006
              s = 50000 #desired sample size
```

```
skip test = sorted(random.sample(range(1, n test+1), n test-s))
              #https://stackoverflow.com/a/22259008/4084039
In [37]:
          print("Number of rows in the train data file:", n train)
          print("Number of rows we are going to elimiate in train data are",len(skip train))
          print("Number of rows in the test data file:", n test)
          print("Number of rows we are going to elimiate in test data are",len(skip test))
         Number of rows in the train data file: 15100028
         Number of rows we are going to elimiate in train data are 15000028
         Number of rows in the test data file: 3775006
         Number of rows we are going to elimiate in test data are 3725006
In [38]:
          df final train = pd.read csv('data/after eda/train after eda.csv', skiprows=skip train, names=['source node', 'destir
          df final train['indicator link'] = pd.read csv('data/train y.csv', skiprows=skip train, names=['indicator link'])
          print("Our train matrix size ",df final train.shape)
          df final train.head(2)
         Our train matrix size (100002, 3)
            source_node destination_node indicator_link
Out[38]:
         0
                273084
                              1505602
                 53024
                               470337
In [39]:
          df final test = pd.read csv('data/after eda/test after eda.csv', skiprows=skip test, names=['source node', 'destinati
          df final test['indicator link'] = pd.read csv('data/test y.csv', skiprows=skip test, names=['indicator link'])
          print("Our test matrix size ",df final test.shape)
          df final test.head(2)
         Our test matrix size (50002, 3)
            source_node destination_node indicator_link
Out[39]:
         0
                848424
                               784690
         1
                120585
                               539098
```

5.2 Adding a set of features

we will create these each of these features for both train and test data points

```
1. jaccard followers
          2. jaccard_followees
          3. cosine followers
          4. cosine_followees
          5. num_followers_s
          6. num_followees_s
          7. num followers d
          8. num followees d
          9. inter followers
         10. inter followees
In [42]:
          if not os.path.isfile('data/fea sample/storage sample stage1.h5'):
              #mapping jaccrd followers to train and test data
              df final train['jaccard followers'] = df final train.apply(lambda row:
                                                        jaccard for followers(row['source node'],row['destination node']),axis=1]
              df final test['jaccard followers'] = df final test.apply(lambda row:
                                                       jaccard for followers(row['source node'],row['destination node']),axis=1]
              #mapping jaccrd followees to train and test data
              df final train['jaccard followees'] = df final train.apply(lambda row:
                                                        jaccard for followees(row['source node'],row['destination node']),axis=1]
              df final test['jaccard followees'] = df final test.apply(lambda row:
                                                       jaccard for followees(row['source node'],row['destination node']),axis=1]
                  #mapping jaccrd followers to train and test data
              df final train['cosine followers'] = df final train.apply(lambda row:
                                                       cosine for followers(row['source node'],row['destination node']),axis=1)
              df final test['cosine followers'] = df final test.apply(lambda row:
                                                        cosine for followers(row['source node'],row['destination node']),axis=1)
              #mapping jaccrd followees to train and test data
              df final train['cosine followees'] = df final train.apply(lambda row:
```

```
cosine for followees(row['source node'],row['destination node']),axis=1)
              df final test['cosine followees'] = df final test.apply(lambda row:
                                                      cosine for followees(row['source node'],row['destination node']),axis=1)
In [48]:
          def compute features stage1(df final):
              #calculating no of followers followees for source and destination
              #calculating intersection of followers and followees for source and destination
              num followers s=[]
              num followees s=[]
              num followers d=[]
              num followees d=[]
              inter followers=[]
              inter followees=[]
              for i,row in df_final.iterrows():
                  try:
                      sl=set(train graph.predecessors(row['source node']))
                      s2=set(train graph.successors(row['source node']))
                  except:
                      s1 = set()
                      s2 = set()
                  trv:
                      dl=set(train graph.predecessors(row['destination node']))
                      d2=set(train graph.successors(row['destination node']))
                  except:
                      d1 = set()
                      d2 = set()
                  num followers s.append(len(s1))
                  num followees s.append(len(s2))
                  num followers d.append(len(d1))
                  num followees d.append(len(d2))
                  inter followers.append(len(s1.intersection(d1)))
                  inter followees.append(len(s2.intersection(d2)))
              return num followers s, num followers d, num followees s, num followees d, inter followers, inter followees
```

In [54]:

```
if not os.path.isfile('data/fea sample/storage sample stage1.h5'):
               df final train['num followers s'], df final train['num followers d'], \
               df final train['num followees s'], df final train['num followees d'], \
               df final train['inter followers'], df final train['inter followees']= compute features stage1(df final train)
               df final test['num followers s'], df final test['num followers d'], \
               df final test['num followees s'], df final test['num followees d'], \
               df final test['inter followers'], df final test['inter followees'] = compute features stage1(df final test)
               hdf = HDFStore('data/fea sample/storage sample stage1.h5')
               hdf.put('train df',df final train, format='table', data columns=True)
               hdf.put('test df',df final test, format='table', data columns=True)
               hdf.close()
          else:
               df final train = read hdf('data/fea sample/storage sample stage1.h5', 'train df',mode='r')
               df final test = read hdf('data/fea sample/storage sample stage1.h5', 'test df',mode='r')
In [55]:
          df final train.head()
             source_node destination_node indicator_link jaccard_followers jaccard_followees cosine_followers cosine_followees num_followers_s num_fo
Out[55]:
          0
                 273084
                                1505602
                                                                  0
                                                                            0.000000
                                                                                           0.000000
                                                                                                           0.000000
                                                                                                                               11
                 832016
                                1543415
                                                                  0
                                                                            0.187135
                                                                                           0.028382
                                                                                                           0.343828
                                                                                                                               17
          2
                1325247
                                 760242
                                                                  0
                                                                            0.369565
                                                                                           0.156957
                                                                                                           0.566038
                                                                                                                               35
          3
                 1368400
                                1006992
                                                  1
                                                                            0.000000
                                                                                           0.000000
                                                                                                           0.000000
          4
                 140165
                                1708748
                                                                  0
                                                                            0.000000
                                                                                           0.000000
                                                                                                           0.000000
                                                                                                                                5
In [56]:
          df final test.head(3)
                        destination_node indicator_link jaccard_followers jaccard_followees cosine_followers cosine_followees num_followers_s num_fo
Out[56]:
             source_node
          0
                 848424
                                 784690
                                                                                 0.0
                                                                                           0.029161
                                                                                                               0.0
                 483294
                                1255532
                                                                                 0.0
                                                                                           0.000000
                                                                                                               0.0
          2
                 626190
                                1729265
                                                  1
                                                                  0
                                                                                 0.0
                                                                                           0.000000
                                                                                                               0.0
                                                                                                                               15
```

Preferential_attachment

```
In [60]:
           def preferential attachment(src, dest):
               lst=[]
               for i in range(len(src)):
                    lst.append(src[i]*dest[i])
                return lst
In [61]:
           np.array(df final train['num followers s'])
Out[61]: array([11, 17, 35, ..., 3, 1, 16], dtype=int64)
In [62]:
           len(np.array(df final train['num followers s']))
          100002
Out[62]:
In [63]:
           df final train['pref attach followers']=preferential attachment(np.array(df final train['num followers s']), np.array
           df final train['pref attach followees']=preferential attachment(np.array(df final train['num followees s']), np.array
In [64]:
           df final test['pref attach followers']=preferential attachment(np.array(df final test['num followers s']), np.array(df final test['num followers s'])
           df final test['pref attach followees']=preferential attachment(np.array(df final test['num followees s']), np.array(df final test['num followees'])
In [65]:
           df final train.head()
Out[65]:
             source_node
                         destination_node indicator_link jaccard_followers jaccard_followees cosine_followers
                                                                                                      cosine_followees num_followers_s num_fo
          0
                  273084
                                 1505602
                                                                              0.000000
                                                                                              0.000000
                                                                                                              0.000000
                                                                                                                                   11
          1
                  832016
                                 1543415
                                                                              0.187135
                                                                                              0.028382
                                                                                                              0.343828
                                                                                                                                   17
```

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_followers	cosine_followees	num_followers_s	num_fo
2	1325247	760242	1	0	0.369565	0.156957	0.566038	35	
3	1368400	1006992	1	0	0.000000	0.000000	0.000000	2	
4	140165	1708748	1	0	0.000000	0.000000	0.000000	5	
4									>

5.3 Adding new set of features

we will create these each of these features for both train and test data points

- 1. adar index
- 2. is following back
- 3. belongs to same weakly connect components
- 4. shortest path between source and destination

```
#mapping shortest path on train
               df final train['shortest path'] = df final train.apply(lambda row: compute shortest path length(row['source node
              #mapping shortest path on test
               df final test['shortest path'] = df final test.apply(lambda row: compute shortest path length(row['source node']
              hdf = HDFStore('data/fea sample/storage sample stage2.h5')
              hdf.put('train df',df final train, format='table', data columns=True)
               hdf.put('test df',df final test, format='table', data columns=True)
               hdf.close()
          else:
               df final train = read hdf('data/fea sample/storage sample stage2.h5', 'train df',mode='r')
               df final test = read hdf('data/fea sample/storage sample stage2.h5', 'test df',mode='r')
In [67]:
          df final train.head(3)
            source_node destination_node indicator_link jaccard_followers jaccard_followees cosine_followers cosine_followees num_followers_s num_fo
Out[67]:
          0
                 273084
                               1505602
                                                                 0
                                                                                          0.000000
                                                                                                         0.000000
                                                                          0.000000
                                                                                                                             11
                 832016
                               1543415
                                                                           0.187135
                                                                                          0.028382
                                                                                                         0.343828
                                                                                                                             17
          2
                1325247
                                760242
                                                                 0
                                                                           0.369565
                                                                                          0.156957
                                                                                                         0.566038
                                                                                                                             35
```

5.4 Adding new set of features

we will create these each of these features for both train and test data points

- 1. Weight Features
 - · weight of incoming edges
 - · weight of outgoing edges
 - weight of incoming edges + weight of outgoing edges
 - weight of incoming edges * weight of outgoing edges
 - 2*weight of incoming edges + weight of outgoing edges
 - weight of incoming edges + 2*weight of outgoing edges

- 2. Page Ranking of source
- 3. Page Ranking of dest
- 4. katz of source
- 5. katz of dest
- 6. hubs of source
- 7. hubs of dest
- 8. authorities_s of source
- 9. authorities_s of dest

Weight Features

In order to determine the similarity of nodes, an edge weight value was calculated between nodes. Edge weight decreases as the neighbor count goes up. Intuitively, consider one million people following a celebrity on a social network then chances are most of them never met each other or the celebrity. On the other hand, if a user has 30 contacts in his/her social network, the chances are higher that many of them know each other.

| Credit | Graph-based Features for Supervised Link Prediction William Cukierski, Benjamin Hamner, Bo Yang

$$W = \frac{1}{\sqrt{1+|X|}}\tag{3}$$

it is directed graph so calculated Weighted in and Weighted out differently

```
1780722/1780722 [00:15<00:00, 114291.08it/
         100%
In [69]:
          if not os.path.isfile('data/fea sample/storage sample stage3.h5'):
              #mapping to pandas train
              df final train['weight in'] = df final train.destination node.apply(lambda x: Weight in.get(x,mean weight in))
              df final train['weight out'] = df final train.source node.apply(lambda x: Weight out.get(x,mean weight out))
              #mapping to pandas test
              df final test['weight in'] = df final test.destination node.apply(lambda x: Weight in.get(x,mean weight in))
              df final test['weight out'] = df final test.source node.apply(lambda x: Weight out.get(x,mean weight out))
              #some features engineerings on the in and out weights
              df final train['weight f1'] = df final train.weight in + df final train.weight out
              df final train['weight f2'] = df final train.weight in * df final train.weight out
              df final train['weight f3'] = (2*df final train.weight in + 1*df final train.weight out)
              df final train['weight f4'] = (1*df final train.weight in + 2*df final train.weight out)
              #some features engineerings on the in and out weights
              df final test['weight f1'] = df final test.weight in + df final test.weight out
              df final test['weight f2'] = df final test.weight in * df final test.weight out
              df final test['weight f3'] = (2*df final test.weight in + 1*df final test.weight out)
              df final test['weight f4'] = (1*df final test.weight in + 2*df final test.weight out)
In [70]:
          if not os.path.isfile('data/fea sample/storage sample stage3.h5'):
              #page rank for source and destination in Train and Test
              #if anything not there in train graph then adding mean page rank
              df final train['page rank s'] = df final train.source node.apply(lambda x:pr.get(x,mean pr))
              df final train['page rank d'] = df final train.destination node.apply(lambda x:pr.get(x,mean pr))
              df final test['page rank s'] = df final test.source node.apply(lambda x:pr.get(x,mean pr))
              df final test['page rank d'] = df final test.destination node.apply(lambda x:pr.get(x,mean pr))
              #Katz centrality score for source and destination in Train and test
              #if anything not there in train graph then adding mean katz score
              df final train['katz s'] = df final train.source node.apply(lambda x: katz.get(x,mean katz))
```

```
df final train['katz d'] = df final train.destination node.apply(lambda x: katz.get(x,mean katz))
              df final test['katz s'] = df final test.source node.apply(lambda x: katz.get(x,mean katz))
              df final test['katz d'] = df final test.destination node.apply(lambda x: katz.get(x,mean katz))
              #Hits algorithm score for source and destination in Train and test
              #if anything not there in train graph then adding 0
              df final train['hubs s'] = df final train.source node.apply(lambda x: hits[0].get(x,0))
              df final train['hubs d'] = df final train.destination node.apply(lambda x: hits[0].qet(x,0))
              df final test['hubs s'] = df final test.source node.apply(lambda x: hits[0].qet(x,0))
              df final test['hubs d'] = df final test.destination node.apply(lambda x: hits[0].get(x,0))
              #Hits algorithm score for source and destination in Train and Test
              #if anything not there in train graph then adding 0
              df final train['authorities s'] = df final train.source node.apply(lambda x: hits[1].get(x,0))
              df final train['authorities d'] = df final train.destination node.apply(lambda x: hits[1].get(x,0))
              df final test['authorities s'] = df final test.source node.apply(lambda x: hits[1].get(x,0))
              df final test['authorities d'] = df final test.destination node.apply(lambda x: hits[1].get(x,0))
              hdf = HDFStore('data/fea sample/storage sample stage3.h5')
              hdf.put('train df',df final train, format='table', data columns=True)
              hdf.put('test df',df final test, format='table', data columns=True)
              hdf.close()
          else:
              df final train = read hdf('data/fea sample/storage sample stage3.h5', 'train df',mode='r')
              df final test = read hdf('data/fea sample/storage sample stage3.h5', 'test df',mode='r')
In [71]:
          df final train.head(3)
            source_node destination_node indicator_link jaccard_followers jaccard_followees cosine_followers cosine_followees num_followers_s num_fo
Out[71]:
                                               1
         0
                273084
                              1505602
                                                                        0.000000
                                                                                      0.000000
                                                                                                     0.000000
                                                                                                                         11
         1
                832016
                              1543415
                                               1
                                                              0
                                                                        0.187135
                                                                                      0.028382
                                                                                                     0.343828
                                                                                                                        17
```

```
source_node destination_node indicator_link jaccard_followers jaccard_followees cosine_followers cosine_followees num_followers_s num_fo
          2
                1325247
                                760242
                                                 1
                                                                          0.369565
                                                                                         0.156957
                                                                                                        0.566038
                                                                                                                            35
         3 rows × 33 columns
In [72]:
          df final train.columns
Out[72]: Index(['source node', 'destination node', 'indicator link',
                 'jaccard followers', 'jaccard followees', 'cosine followers',
                 'cosine_followees', 'num_followers_s', 'num_followees_s',
                 'num followees d', 'inter followers', 'inter followees',
                 'num_followers_d', 'pref_attach_followers', 'pref_attach_followees',
                 'adar_index', 'follows_back', 'same_comp', 'shortest path', 'weight in',
                 'weight out', 'weight f1', 'weight f2', 'weight f3', 'weight f4',
                 'page_rank_s', 'page_rank_d', 'katz_s', 'katz_d', 'hubs_s', 'hubs_d',
                 'authorities_s', 'authorities d'],
                dtype='object')
```

5.5 Adding new set of features

we will create these each of these features for both train and test data points

1. SVD features for both source and destination

```
In [73]:
    def svd(x, S):
        try:
            z = sadj_dict[x]
            return S[z]
        except:
            return [0,0,0,0,0,0]

In [74]:
#for svd features to get feature vector creating a dict node val and inedx in svd vector
sadj_col = sorted(train_graph.nodes())
sadj_dict = { val:idx for idx,val in enumerate(sadj_col)}
```

```
In [75]:
          Adj = nx.adjacency matrix(train graph,nodelist=sorted(train graph.nodes())).asfptype()
In [76]:
          U, s, V = svds(Adj, k = 6)
          print('Adjacency matrix Shape', Adj.shape)
          print('U Shape',U.shape)
          print('V Shape', V.shape)
          print('s Shape',s.shape)
         Adjacency matrix Shape (1780722, 1780722)
         U Shape (1780722, 6)
         V Shape (6, 1780722)
         s Shape (6,)
In [77]:
          if not os.path.isfile('data/fea sample/storage sample stage4.h5'):
              df final train[['svd u s 1', 'svd u s 2', 'svd u s 3', 'svd u s 4', 'svd u s 5', 'svd u s 6']] = \
              df final train.source node.apply(lambda x: svd(x, U)).apply(pd.Series)
              df final train[['svd u d 1', 'svd u d 2', 'svd u d 3', 'svd u d 4', 'svd u d 5', 'svd u d 6']] = \
              df final train.destination node.apply(lambda x: svd(x, U)).apply(pd.Series)
              df final train[['svd v s 1','svd v s 2', 'svd v s 3', 'svd v s 4', 'svd v s 5', 'svd v s 6',]] = \
              df final train.source node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
              df_final_train[['svd_v_d_1', 'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6']] = \\
              df final train.destination node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
              df final test[['svd u s 1', 'svd u s 2', 'svd u s 3', 'svd u s 4', 'svd u s 5', 'svd u s 6']] = \setminus
              df final test.source node.apply(lambda x: svd(x, U)).apply(pd.Series)
              df final test[['svd u d 1', 'svd u d 2', 'svd u d 3', 'svd u d 4', 'svd u d 5','svd u d 6']] = \
              df final test.destination node.apply(lambda x: svd(x, U)).apply(pd.Series)
```

```
df final test[['svd v s 1','svd v s 2', 'svd v s 3', 'svd v s 4', 'svd v s 5', 'svd v s 6',]] = \setminus
               df final test.source node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
               df final test[['svd v d 1', 'svd v d 2', 'svd v d 3', 'svd v d 4', 'svd v d 5','svd v d 6']] = \
               df final test.destination node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
               hdf = HDFStore('data/fea sample/storage sample stage4.h5')
               hdf.put('train df',df final train, format='table', data columns=True)
               hdf.put('test df',df final test, format='table', data columns=True)
               hdf.close()
In [78]:
           # prepared and stored the data from machine learning models
           # pelase check the FB Models.ipvnb
In [79]:
           df final train = read hdf('data/fea sample/storage sample stage4.h5', 'train df',mode='r')
           df final test = read hdf('data/fea sample/storage sample stage4.h5', 'test df',mode='r')
In [81]:
          df final train.columns
Out[8]]: Index(['source node', 'destination node', 'indicator link',
                  'jaccard followers', 'jaccard followees', 'cosine followers',
                  'cosine_followees', 'num_followers_s', 'num_followees_s', 'num_followees_d', 'inter_followers', 'inter_followees',
                  'num_followers_d', 'pref_attach_followers', 'pref_attach_followees',
                  'adar_index', 'follows_back', 'same_comp', 'shortest_path', 'weight in',
                  'weight out', 'weight f1', 'weight f2', 'weight f3', 'weight f4',
                  'page rank s', 'page rank d', 'katz s', 'katz d', 'hubs s', 'hubs d',
                  'authorities s', 'authorities d', 'svd u s 1', 'svd u s 2', 'svd u s 3',
                 'svd_u_s_4', 'svd_u_s_5', 'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1',
                  'svd v s 2', 'svd v s 3', 'svd v s 4', 'svd v s 5', 'svd v s 6',
                  'svd v d 1', 'svd v d 2', 'svd v d 3', 'svd v d 4', 'svd v d 5',
                  'svd v d 6'l,
                dtype='object')
In [126...
          df final train
```

Out[126		source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_followers	cosine_followees	num_followers_s	nι	
	0	273084	1505602	1	0	0.000000	0.000000	0.000000	11		
	1	832016	1543415	1	0	0.187135	0.028382	0.343828	17		
	2	1325247	760242	1	0	0.369565	0.156957	0.566038	35		
	3	1368400	1006992	1	0	0.000000	0.000000	0.000000	2		
	4	140165	1708748	1	0	0.000000	0.000000	0.000000	5		
	99997	139353	893843	0	0	0.000000	0.000000	0.000000	0		
	99998	910842	704068	0	0	0.000000	0.000000	0.000000	2		
	99999	794228	1172755	0	0	0.000000	0.000000	0.000000	3		
	100000	949992	1854931	0	0	0.000000	0.000000	0.000000	1		
	100001	1642037	1090977	0	0	0.000000	0.000000	0.000000	16		
	100002 i	rows × 57 colu	ımns								
	4									•	
In [139	<pre>In [139 u_source=np.array(df_final_train.iloc[:,33:39])</pre>										
<pre>In [142 v_source=np.array(df_final_train.iloc[:,45:51])</pre>											
In [144	<pre>In [144 u_dest=np.array(df_final_train.iloc[:,39:45])</pre>										
In [146	v_des ⁻	t=np.array(d	df_final_train.	iloc[:,51:5	7])						

```
In [147...
          print(u_source.shape, v_source.shape, u_dest.shape, v_dest.shape)
          (100002, 6) (100002, 6) (100002, 6) (100002, 6)
In [150...
          source=np.hstack((u source, v source))
          destination=np.hstack((u dest, v dest))
In [151...
          source.shape
Out[151... (100002, 12)
In [152...
          destination.shape
Out[152... (100002, 12)
In [153...
          svd dot mat=np.multiply(source, destination)
In [154...
          svd dot mat.shape
Out[154... (100002, 12)
In [155...
          source[1]
Out[155... array([7.05229303e-13, -8.25055109e-11, -1.71771729e-10, 3.70501564e-02,
                 1.03241105e-11, 7.20749666e-10, 2.68630901e-13, -3.31684501e-11,
                 -6.23610302e-11, 1.34572641e-02, 3.70353335e-12, 2.25173744e-10])
In [156...
          destination[1]
Out[156... array([ 1.64461774e-12, -2.04774953e-10, -3.94397001e-10, 8.61754055e-02,
                  2.39957899e-11, 1.73868180e-09, 1.24530633e-12, -1.63694547e-10,
```

```
-3.11267741e-10, 6.73890242e-02, 2.60782653e-11, 2.37290370e-09])
In [157...
           svd dot mat[1]
Out[157... array([1.15983263e-24, 1.68950621e-20, 6.77462547e-20, 3.19281225e-03,
                 2.47735187e-22, 1.25315432e-18, 3.34527762e-25, 5.42949441e-21,
                 1.94109770e-20, 9.06871897e-04, 9.65817252e-23, 5.34315610e-19])
In [158...
           svd dot final=svd dot mat.sum(axis=1)
In [159...
           svd dot final.shape
Out[159... (100002,)
In [160...
          svd dot final[1]
          0.00409968414625671
Out[160...
In [161...
           svd dot final
Out[161... array([1.33883532e-11, 4.09968415e-03, 4.64132750e-33, ...,
                 4.15853413e-22, 6.25342466e-26, 1.63939130e-15])
In [162...
          df_final_train['svd_dot']=svd_dot final.tolist()
In [163...
           df final train
Out[163...
                 source_node
                             destination_node indicator_link jaccard_followers jaccard_followees cosine_followers cosine_followees num_followers_s nu
               0
                                                       1
                                                                                                                                     11
                      273084
                                     1505602
                                                                                 0.000000
                                                                                                0.000000
                                                                                                                0.000000
                                     1543415
                                                                                 0.187135
                                                                                                0.028382
                                                                                                                0.343828
                                                                                                                                     17
                      832016
```

		source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_followers	cosine_followees	num_followers_s	nι
	2	1325247	760242	1	0	0.369565	0.156957	0.566038	35	
	3	1368400	1006992	1	0	0.000000	0.000000	0.000000	2	
	4	140165	1708748	1	0	0.000000	0.000000	0.000000	5	
	99997	139353	893843	0	0	0.000000	0.000000	0.000000	0	
	99998	910842	704068	0	0	0.000000	0.000000	0.000000	2	
	99999	794228	1172755	0	0	0.000000	0.000000	0.000000	3	
	100000	949992	1854931	0	0	0.000000	0.000000	0.000000	1	
	100001	1642037	1090977	0	0	0.000000	0.000000	0.000000	16	
	100002	rows × 58 colu	ımns							
	4									•
In [165	df_final_test.shape									
Out[165	(50002, 57)									
In [166	<pre>u_source=np.array(df_final_test.iloc[:,33:39]) v_source=np.array(df_final_test.iloc[:,45:51]) u_dest=np.array(df_final_test.iloc[:,39:45]) v_dest=np.array(df_final_test.iloc[:,51:57])</pre>									
In [167	source=np.hstack((u_source, v_source))									

```
destination=np.hstack((u_dest, v_dest))
In [168...
                                           svd dot mat=np.multiply(source, destination)
In [169...
                                           svd dot final=svd dot mat.sum(axis=1)
In [170...
                                           svd dot final.shape
                                       (50002,)
Out[170...
In [171...
                                           df_final_test['svd_dot']=svd_dot_final.tolist()
In [172...
                                           df_final_test
Out[172...
                                                                 source_node destination_node indicator_link jaccard_followers jaccard_followees cosine_followers cosine_followees num_followers_s num_follower
                                                      0
                                                                                    848424
                                                                                                                                                 784690
                                                                                                                                                                                                                                                                                0
                                                                                                                                                                                                                                                                                                                                          0.0
                                                                                                                                                                                                                                                                                                                                                                                   0.029161
                                                                                                                                                                                                                                                                                                                                                                                                                                               0.000000
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                                                      1
                                                                                    483294
                                                                                                                                             1255532
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                                                                                                                                                                                                                                                                                                                                          0.0
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                                                                                    626190
                                                                                                                                             1729265
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                                                      3
                                                                                   947219
                                                                                                                                                425228
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                                                      4
                                                                                    991374
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                                                                                                                                                                                                                                                                                                                                          0.2
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                                                                                                                                                 975044
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                                         49997
                                                                                 1167544
                                                                                                                                                 310247
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                                         49998
                                                                                    656027
                                                                                                                                             1761965
                                                                                                                                                                                                                   0
                                                                                                                                                                                                                                                                                0
                                                                                                                                                                                                                                                                                                                                          0.0
                                                                                                                                                                                                                                                                                                                                                                                   0.000000
                                                                                                                                                                                                                                                                                                                                                                                                                                               0.000000
```

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_followers	cosine_followees	num_followers_s nur
49999	1304926	958643	0	0	0.0	0.000000	0.000000	0
50000	773347	1488855	0	0	0.0	0.000000	0.000000	0
50001	1253866	281538	0	0	0.0	0.000000	0.000000	0

50002 rows × 58 columns

```
In [173... hdf = HDFStore('data/fea_sample/storage_sample_stage5.h5')
    hdf.put('train_df',df_final_train, format='table', data_columns=True)
    hdf.put('test_df',df_final_test, format='table', data_columns=True)
    hdf.close()
In []:
```