Quiz II

Discrete Structures IIIT Hyderabad, Monsoon 2022

October 20, 2023

Consider the following system of congruent-recurrences:

$$a_n \equiv a_{n-1} + 3n^2 \qquad \text{with} \quad a_0 \equiv 4 \qquad \pmod{5}$$

$$a_n \equiv 6a_{n-2} - a_{n-1} \qquad \text{with} \quad a_0 \equiv -1, a_1 \equiv 8 \pmod{11}$$

$$a_n \equiv 4a_{n-1} - 3a_{n-2} - 2 \qquad \text{with} \quad a_0 \equiv 2, a_0 \equiv 5 \pmod{7}$$

$$\alpha_0 \equiv 2, \alpha_1 \equiv 5 \pmod{7}$$

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Answer the following:

1. What is $a_0 \mod 385$?	5 marks
2. What is a ₂ mod 385?	5 marks
3. What is $(a_{100} \mod 5)$?	15 marks
4. What is $(a_{150} \mod 35)$?	20 marks
5. What is $(a_{200} \mod 385)$?	25 marks

- 6. With the same initial/boundary conditions, how many values between 0 and 384 can ($a_3 \mod 385$) take, if:
 - all the three congruences are satisfied?
 none of the three congruences are satsfied?
 exactly one of the three congruences are satsfied?
 12 marks
 15 marks