Departamento de Engenharia Informática, FCTUC, 2023/2024

Experimental Methods in Computer Science

(Metodologias Experimentais em Informática)

Henrique Madeira

Master in Informatics Engineering

Departamento de Engenharia Informática Faculdade de Ciências e Tecnologia da Universidade de Coimbra 2023/2024

Henrique Madeira, DEI-FCTUC,

 $Experimental\ Methods\ in\ Computer\ Science, Master\ in\ Informatics\ Engineering\ , DEI-FCTUC\ , 2023/2024$

1

Hypothesis Testing

COC 0100 CHILDRIAN TOXA

Hypothesis testing slides are mainly based on chapter 8 of the book "Essentials of Social Statistics for a Diverse Society" Second Edition by Anna Leon-Guerrero, Chava Frankfort-Nachmias, SAGE Publications, Inc, 2010.

2

1

Departamento de Engenharia Informática, FCTUC, 2023/2024

Hypothesis testing scenario 1 (test for a mean)

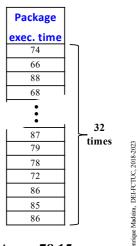
Assume you are the database administrator of a big information system and you are unhappy with the execution time of a given SQL package.

From historical data (thousands of previous package executions), you know that the average execution time of the package is 83.54 seconds with a standard deviation of 16.36.

You change the tuning of the database and run the package several times to check the effect.

Questions:

- Has the new tuning any effect?
- Is the new configuration better?
- Is the new configuration worse?



Avg = 78.15

Experimental Methods in Computer Science, Master in Informatics Engineering, DEI-FCTUC, 2023/2024

3

Hypothesis testing scenario 2 (test for means)

Assume you are the database administrator of a big information system. The database has just been installed and you are trying two tuning configurations: Conf. A and Conf. B.

You use a given SQL package to test the execution time for each configuration.

After running several times the SQL package in both configurations you want to take a decision.

Question	what is	the best	configur	otion?
Ouestion :	wnatis	the best	conngur	auon :

Conf. A	Conf. B		
exec. time	exec. time		
74	69		
66	71		
88	80		
68	88		
79	64		
68	65		
87	74		
79	76		
78	89		
72	68		
86	67		
85	72		
86			

Avg A = 78.15 Avg B = 73.58 n = 13 n = 12

Experimental Methods in Computer Science, Master in Informatics Engineering , DEI-FCTUC, 2023/2024

Henrique Madeira, DEI-FCTUC,

Departamento de Engenharia Informática, FCTUC, 2023/2024

Hypothesis

• What is an hypothesis?

- A proposed explanation for a given phenomenon
- An assumption about the efficiency of a given component/system
- A statement about the parameters of a population (statistical view)
- Scope
 - Abstract: about the world (lato senso)
 - Concrete: about a given design or apparatus

An hypothesis is a tentative answer!

Types

- Explanatory: explains the phenomenon, identifies relations and/or causality between variable/elements of the phenomenon
- Predictive: predicts the observation of a phenomenon, anticipates the outcome of an experiment,...

outer Science, Master in Informatics Engineering , DEI-FCTUC, 2023/2024

5

Hypothesis

What is an hypothesis?

- A proposed explanation for a given phenomenon
- An assumption about the efficiency of a given component/system
- A statement about the parameters of a population (statistical view)

Scope

- Abstract: abo
- Concrete: abd •
- Types
 - Explanatory: between varia
 - Predictive: pr an experiment
- An hypothesis requires evaluation to be considered true. It can be rejected or, in the absence of rejection, it is confirmed.
- True hypothesis means the probability of it being correct is 'high' and the probability of it being incorrect is 'low'.
- Statistics is necessary to quantify the meaning of "high" and "low" and to decide about the validity of the hypothesis.
- Hypotheses are rejected or accepted with some degree of certainty

Henrique Madeira, DEI-FCTUC, 2018-2023

Departamento de Engenharia Informática, FCTUC, 2023/2024

Hypothesis: put it into perspective

Topic, problem and hypothesis

- **Topic:** Subject (focused area) of interest, where the gap or difficulty to be solved is included. Essential to provide context to the hypothesis.
- **Problem:** Object of the study. Presumes clear and explicit **questions** that formulate the problem to be solved.
- **Hypothesis:** Provisional answer to the question(s). If the hypotheses is confirmed, the answer is considered correct (to a given degree of certainty).

7

Hypothesis: put it into perspective

Topic, problem and hypothesis

- Topic: Subject (focused area) of interest, where the gap or difficulty to be solved is included. Essential to provide context to the hypothesis.
- Problem: Object of the formulate the problem to Quality of the code (absence of bugs) produced
- **Hypothesis:** Provisional by programmers. es is confirmed, the answer is considered correct (to a given degree of certainty).

Tenrique M

8

Departamento de Engenharia Informática, FCTUC, 2023/2024

Hypothesis: put it into perspective

Topic, problem and hypothesis

Example:

- Topic: Subject (focused area) of solved is included. Essential
- Is the software development methodology related to the number of bugs in deployed software?
- **Problem:** Object of the study. Presumes clear and explicit **questions** that formulate the problem to be solved.
- **Hypothesis:** Provisional answer to the question(s). If the hypotheses is confirmed, the answer is considered correct (to a given degree of certainty).

9

Hypothesis: put it into perspective

Example:

Topic, problem and hypothesis

- **Topic:** Subject (focused are solved is included. Essential
- H_0 Software developed and deployed using CMMi 5 has the same bug density of software developed using Scrum.
- **Problem:** Object of the formulate the problem
- **H**₁ Software developed and deployed using CMMi 5 has **not** the same bug density of software developed using Scrum.
- **Hypothesis:** Provisional answer to the question(s). If the hypotheses is confirmed, the answer is considered correct (to a given degree of certainty).

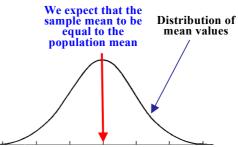
Experimental Methods in Computer Science, Master in Informatics Engineering , DEI-FCTUC, 2023/2024

_{be}

Departamento de Engenharia Informática, FCTUC, 2023/2024

Inferential statistics and hypothesis testing

- Allows us to evaluate the behavior in samples to learn more about the behavior in the entire population
- Quite often, the entire population is too large (or even infinite) or is not accessible
- From the central limit theorem, we know that the probability of selecting any other sample mean value from this population is normally distributed.

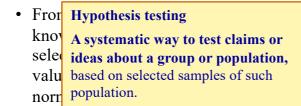


Experimental Methods in Computer Science, Master in Informatics Engineering, DEI-FCTUC, 2023/202-

23

Inferential statistics and hypothesis testing

- Allows us to evaluate the behavior in samples to learn more about the behavior in the entire population
- Quite often, the entire population is too large (or even infinite) or is not accessible



We expect that the sample mean to be equal to the population mean

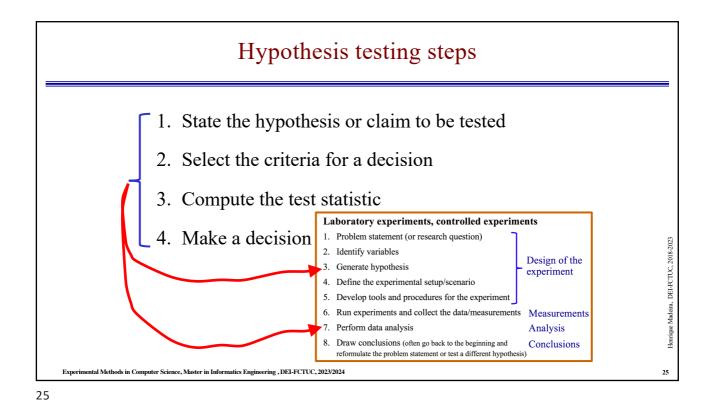
Distribution of mean values

Experimental Methods in Computer Science, Master in Informatics Engineering , DEI-FCTUC, 2023/202

24

Henrique Madeira, DEI-FCTUC, 2018-2023

Departamento de Engenharia Informática, FCTUC, 2023/2024



Hypothesis testing scenario 1 (test for a mean)

Assume you are the database administrator of a big information system and you are unhappy with the execution time of a given SQL package.

From historical data (thousands of previous package executions), you know that the average execution time of the package is 83.54 seconds with a standard deviation of 16.36.

You change the tuning of the database and run the package several times to check the effect.

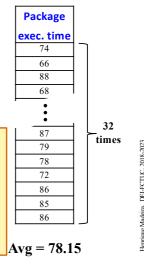
Questions:

- · Has the new tuning any effect?
- Is the new configuration better?
- Is the new configuration worse?

We consider the data distribution normal because:

- Each execution is independent from previous executions;
- The variability in the measurements results from random changes in the execution conditions.

If we are not sure that the data follows a normal distribution, we must test it for normality.



perimental Methods in Computer Science, Master in Informatics Engineering , DEI-FCTUC, 2023/2024

26

Departamento de Engenharia Informática, FCTUC, 2023/2024

Step 1 - State the hypothesis

Null hypothesis (H_0) is a statement about the population parameter (e.g., the population mean) that is assumed to be true.

This is a provisional answer to the research question or problem under study. For example:

H₀- The new configuration has no effect on the execution time of the SQL packaged

• Alternative hypothesis (H₁) is a statement that directly contradicts the null hypothesis by stating that the actual value of the population is not equal to the value stated in the null hypothesis.

This is what we think is wrong about the null hypothesis. For example:

H₁ – The execution time of the SQL packaged is different in the new configuration (could be smaller or bigger)

27

Step 1 - State the hypothesis

Null hypothesis (H_0) is a statement about the population parameter (e.g., the population mean) that is assumed to be true.

This is a provisional answer to the research question or problem under study. For example: ed

The decision made in hypothesis testing centers on the null hypothesis H₀

The idea is to show evidences that H_0 is unlikely, in order to reject the null hypothesis. If failing to do so, the null hypothesis is retained.

• The bias is do nothing. In other words, the burden is put on the researcher to demonstrate that H_0 is not likely to be true. \rightarrow The experiments must be defined to collect data to show that H₀ is not true

alue

Step 2 - Select the criteria for a decision

- To set a criteria means to state the significance level for the test.
- **Significance level** refers to a criterion of judgment upon which a decision is made regarding the value stated in a null hypothesis.
- A typical significance level is 5%. This means that when the probability of obtaining a given sample mean is less than 5%, supposing that the null hypothesis is true, then we conclude that the sample used to calculate the mean is too unlikely, and so we reject the null hypothesis.

Ienrique Madeira, DEI-FCTU

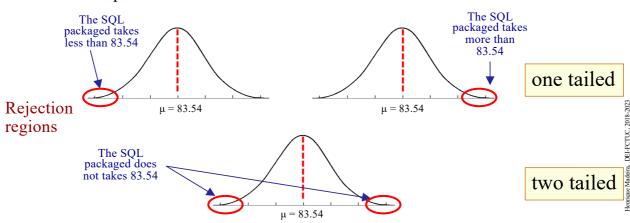
Experimental Methods in Computer Science, Master in Informatics Engineering, DEI-FCTUC, 2023/202-

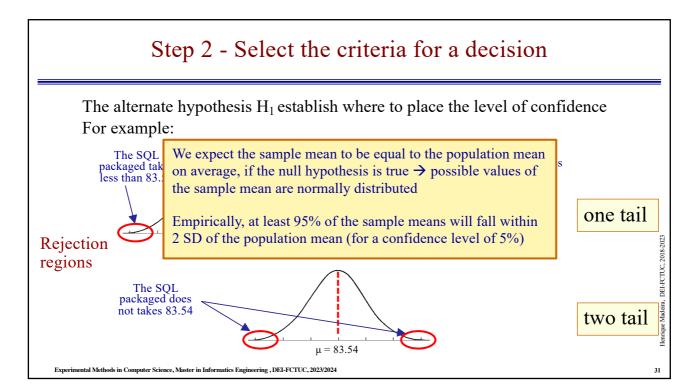
29

29

Step 2 - Select the criteria for a decision

The alternate hypothesis H_1 establish where to place the level of confidence For example:





31

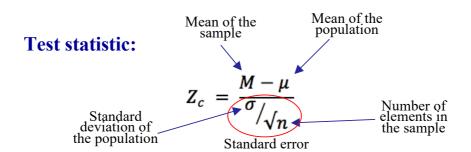
Step 3 – Compute the test statistics

- Select a random sample from the population and measure the sample mean. For example: execute the SQL package n times and measure a mean = 78.15
- To make a decision we need to evaluate how likely this sample outcome is, if the population mean stated by the null hypothesis (83.54) is true.
- **Test statistic** is a formula to determine the likelihood of obtaining sample outcomes if the null hypothesis is true. The value of the test statistic is used to make a decision regarding the null hypothesis.

enrique Madeira. DEL-FCTUC. 2018

Departamento de Engenharia Informática, FCTUC, 2023/2024

Step 3 – Compute the test statistics (test for means, normal distribution)



Measures how far the sample mean is from the population mean under H_0 . The larger the value of $|Z_c|$ the more it will indicate that H_0 is not true.

Experimental Methods in Computer Science, Master in Informatics Engineering , DEI-FCTUC, 2023/2024

3

33

Step 4 – Make a decision

- The value of the test statistic (Z_c) is the key to make a decision about the null hypothesis. The decision is based on the probability of obtaining a sample mean, given that the value stated in the null hypothesis is true.
- **P** value is the probability of obtaining a sample outcome, given that the value stated in the null hypothesis is true.
- Example:
 - P < 5% → reject the null hypothesis (reach significance)
 - $-P > 5\% \rightarrow$ retain the null hypothesis (fail reaching significance)

Experimental Methods in Computer Science, Master in Informatics Engineering , DEI-FCTUC, 2023/202

Departamento de Engenharia Informática, FCTUC, 2023/2024

Hypothesis testing scenario 1 (test for a mean)

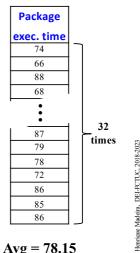
Assume you are the database administrator of a big information system and you are unhappy with the execution time of a given SQL package.

From historical data (thousands of previous package executions), you know that the average execution time of the package is 83.54 seconds with a standard deviation of 16.36.

You change the tuning of the database and run the package several times to check the effect.

Questions:

- Has the new tuning any effect?
- Is the new configuration better?
- Is the new configuration worse?



Avg = 78.15

35

Example 1: non-directional (two tailed) **Step 1- State the hypothesis**

- H_0 The new configuration has no effect on the execution time of the SQL packaged.
- H_1 The execution time of the SQL packaged is different in the new configuration (could be smaller or bigger)

We are testing whether the null hypothesis H_0 is true

Departamento de Engenharia Informática, FCTUC, 2023/2024

Example 1: non-directional (two tailed) Step 2 - Set the criteria for a decision

- Consider the level of significance of 5% $\rightarrow \alpha = 0.05$. $\rightarrow 1 \alpha = 0.95$
- Locate the Z score (in the table for the standard normal distribution) that represents the **critical values**
- A **critical value** is a cutoff value that sets the boundaries beyond which less than 5% of sample means can be obtained if the null hypothesis is true.

Henrique Madeira, DEI-FCTUC, 2018-202

Experimental Methods in Computer Science, Master in Informatics Engineering, DEI-FCTUC, 2023/202-

37

Example 1: non-directional (two tailed) Step 2 - Set the criteria for a decision

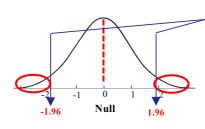
- Consider the level of significance of 5% $\rightarrow \alpha = 0.05$. $\rightarrow 1 \alpha = 0.95$
- Locate the Z score (in the table for the standard not the **critical values**
- A **critical value** is a cutoff value that sets the bou 5% of sample means can be obtained if the null h

Significance	Z score	Z score		
Level	(two tailed)	(one tailed)		
0.70	1.04	-0.525 or 0.525		
0.75	1.15	-0.675 or 0.675		
0.80	1.28	-0.84 or 0.84		
0.85	1.44	-1.036 or 1.036		
0.90	1.645	-1.28 or 1.28		
0.91	1.70	-1.34 or 1.34 -1.41 or 1.41 -1.476 or 1.476		
0.92	1.75	-1.41 or 1.41		
0.93	1.81	-1.476 or 1.476		
0.94	1.88	-1.556 or 1.556		
0.95	1.96	-1.645 or 1.645		
0.96	2.05	-1.751 or 1.751		
0.97	2.17	-1.881 or 1.881		
0.98	2.33	-2.054 or 2.054		
0.99	2.575	-2.326 or 2.326		

Departamento de Engenharia Informática, FCTUC, 2023/2024

Example 1: non-directional (two tailed) Step 2 - Set the criteria for a decision

- Consider the level of significance of 5% $\rightarrow \alpha = 0.05$. $\rightarrow 1 \alpha = 0.95$
- Locate the Z score (in the table for the standard normal distribution) that represents the **critical values**
- A **critical value** is a cutoff value that sets the boundaries beyond which less than 5% of sample means can be obtained if the null hypothesis is true.



Critical values for nondirectional (two tailed) test with $\alpha = 5\%$

 \rightarrow Z score = 1.96

Rejection regions

Experimental Methods in Computer Science, Master in Informatics Engineering , DEI-FCTUC, 2023/202

_

39

Example 1: non-directional (two-tailed) Step 3 - Compute the test statistic

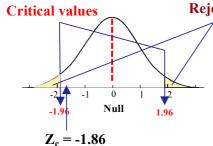
Test statistic:

$$Z_c = \frac{M - \mu}{\sigma/\sqrt{n}} = \frac{78.15 - 83.54}{16.36/\sqrt{32}} = -1.86$$

Jennique Madeira, DEI-FCTUC, 20

Departamento de Engenharia Informática, FCTUC, 2023/2024

Example 1: non-directional (two-tailed) Step 4 - Make a decision



Rejection regions

The probability of obtaining $Z_c = -1.86$ is given by the *P* value. To obtain *P* value for look for 1.86 in the standard normal table.

 \rightarrow the p value for $Z_c = -1.86$ is 0.0314

Henrique Madeira, DEI-FCTUC, 2

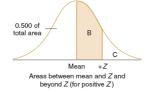
Experimental Methods in Computer Science, Master in Informatics Engineering , DEI-FCTUC, 2023/202

41

Example 1 — Step 3: Obtain the p value

(test for a mean, non-directional, known population; normal Z distribution)

Standard normal table example



To obtain **P** value for look for 1.86 in the standard normal table. → the value is 0.0314

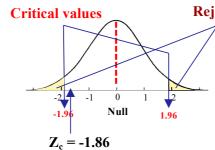
As it is a two-tailed

 $p = 0.0314 \times 2 = 0.0628 \rightarrow p = 6.28\%$

	A	В	С	A	В			В	С
		Area	Area		Area			Area	Area
		Between	Beyond		Between /			Between	Beyond
	Z	Mean and Z	Z	Z	Mean and		Z	Mean and Z	Z
	0.00	0.0000	0.5000	0.11	0/	0.4562	0.21	0.0832	0.4168
	0.01	0.0040	0.4960	0.12	6	0.4522	0.22	0.0871	0.4129
	0.02	0.0080	0.4920	0.13	10517	0.4483	0.23	0.0910	
	1.84	0.4671	0.0329	224	0.4875	0.0125	2.64	0.4959	0.0041
	1.05	0.4678	0.0322	2.25	0.4878	0.0122	2.65	0.4960	0.0040
C	1.86	0.4686	0.0314	2.26	0.4881	0.0119	2.66	0.4961	0.0039
	1.87	0.4693	0.0307	2.27	0.4884	0.0116	2.67	0.4962	0.0038

Experimental Methods in Computer Science, Master in Informatics Engineering , DEI-FCTUC, 2023/202

Example 1: non-directional (two-tailed) Step 4 - Make a decision



Rejection regions

The probability of obtaining $Z_c = -1.86$ is given by the **P** value. To obtain **P** value for look for 1.86 in the standard normal table.

 \rightarrow the p value for $Z_c = -1.86$ is 0.0314

As it is a two-tailed

 $P = 0.0314 \times 2 = 0.0628 \rightarrow P = 6.28\%$

Means that the probability of getting an average of 78.15 if H₀ is true is 6.28%

As P > 5%

43

Retain the null hypothesis (fail reach significance)

Experimental Methods in Computer Science, Master in Informatics Engineering , DEI-FCTUC, 2023/202

.

Henrique Madeira, DEI-FCTUC, 2018-2023