## ML Homework4

## **Description:**

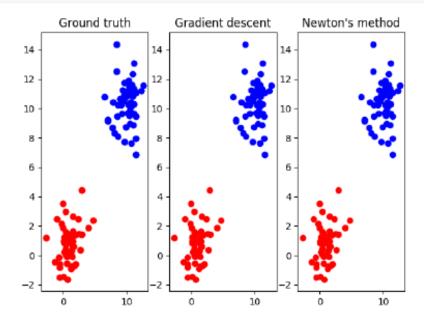
## 1. Logistic regression

- Input:
  - 1. N (number of data points)
  - 2.  $mx_1, vx_1, my_1, vy_1, mx_2, vx_2, my_2, vy_2$  (m: mean, v: variance)
- · Function:
  - 1. Generate n data point:  $D1 = (x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$ , where x and y are independently sampled from  $N(mx_1, vx_1)$  and  $N(my_1, vy_1)$  respectively.
  - 2. Generate n data point:  $D2 = (x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$ , where x and y are independently sampled from  $N(mx_2, vx_2)$  and  $N(my_2, vy_2)$  respectively.
  - 3. Use Logistic regression to separate D1 and D2. You should implement both Newton's and steepest gradient descent method during optimization.
    - In other words, when the Hessian is singular, use steepest descent for instead. You should come up with a reasonable rule to determine convergence.(a simple run out of the loop should be used as the ultimatum)
- Output:
  - 1. The confusion matrix and the **sensitivity** and **specificity** of the logistic regression applied to the training data *D*.
  - 2. Visualization
    - Plot the ground truth
    - Plot the predict result
      - Gradient descent
      - Newton's method

Use the Gaussian random number generator in homework 3.

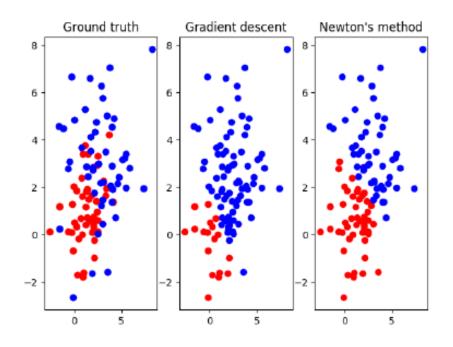
- · Sample input & output (for reference only)
  - $\circ$  Case 1: N = 50,  $mx_1 = my_1 = 1$ ,  $mx_2 = my_2 = 10$ ,  $vx_1 = vy_1 = vx_2 = vy_2 = 2$

```
Gradient descent:
2
3
   w:
4
    -78.1766393662
5
      6.7233419236
      11.2430677919
7
8
   Confusion Matrix:
                Predict cluster 1 Predict cluster 2
9
                      50
10
   Is cluster 1
                       0
11
   Is cluster 2
                                        50
12
13 Sensitivity (Successfully predict cluster 1): 1.00000
   Specificity (Successfully predict cluster 2): 1.00000
14
15
17
    Newton's method:
18
19
   w:
20
   -118.3601516394
      8.7747332848
21
     10.1954120077
22
23
   Confusion Matrix:
24
               Predict cluster 1 Predict cluster 2
25
   Is cluster 1
                      50
   Is cluster 2
                       0
27
28
29 Sensitivity (Successfully predict cluster 1): 1.00000
30 Specificity (Successfully predict cluster 2): 1.00000
```



```
1 Gradient descent:
3
    -71.1902536008
4
     46.0123814025
    54.6803199701
 6
   Confusion Matrix:
         Predict cluster 1 Predict cluster 2
                  16
10 Is cluster 1
11
   Is cluster 2
12
13 Sensitivity (Successfully predict cluster 1): 0.32000
14 Specificity (Successfully predict cluster 2): 0.94000
15
16
17
   Newton's method:
18
19 W:
20
    -1.9045831451
21
     0.3940876974
     0.5695243849
22
24 Confusion Matrix:
        Predict cluster 1 Predict cluster 2
25
26 Is cluster 1 40
27 Is cluster 2 10
                                    40
```

```
28
29 Sensitivity (Successfully predict cluster 1): 0.80000
30 Specificity (Successfully predict cluster 2): 0.80000
```



## 2. EM algorithm

- Input: MNIST training data and label sets. (Same as HW02)
- · Function:
  - Binning the gray level value into two bins. Treating all pixels as random variables following Bernoulli distributions. Note that each pixel follows a different Binomial distribution independent to others.
  - Use EM algorithm to cluster each image into ten groups. You should come up with a reasonable rule to determine convergence. (a simple run out of the loop should be used as the ultimatum)
- Output:
  - For each digit, output a confusion matrix and the sensitivity and specificity of the clustering applied to the training data.
  - 2. Print out the imagination of numbers in your classifier
    - Just like before, about the details please refer to HW02
- Hint: The algorithm is a kind of unsupervised learning, so the labels are not used during training. But you can use these labels to help you to figure out which class belongs to which number.
  - In other words, you should find a way to assign label to each class which you classified before you compute the confusion matrix
- · Sample input & output (for reference only)

1	c1	las	18	0:																								
2						0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
4	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
6	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
7	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
8	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
9	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
10	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
11	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
12	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
13	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
14	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0
15	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	0	0	0	0	0	0	0	0	0	0
16	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	0	0	0	0	0	0	0	0	0	0
17	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	0	0	0	0	0	0	0	0	0	0	0
18	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0	0
19	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0
20	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
21	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0
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26																						0						
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29																						0						
30	Ĭ	Ĭ	Ĭ	Ĭ	Ĭ	Ĭ	Ĭ	Ĭ	Ĭ	Ĭ	Ĭ	Ĭ	Ĭ	Ĭ	Ĭ	•	Ĭ	Ĭ	Ĭ	Ĭ	Ĭ	Ĭ	Ĭ	Ĭ	Ĭ	Ĭ	Ĭ	
31	cl	as	18	1:																								
32	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
33	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
34	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
35	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
36	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
37	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
38	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
39	0	0	0	0	0	0	0	0	0	0	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
40	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	0	0	0	0	0	0	0	0	0
41	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	0	0	0	0	0	0	0	0	0
42	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	0	0	0	0	0	0	0	0	0
43																						0						
44																						0						
45																						0						
46																						0						
47																						0						
48																						0						
43	0		0	9			0					0	-	_	_	-	_	_	_		0							

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0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 0 0 0 1 1 0 0 0 0 0 0 0 0 0
51
 52
 5.4
 55
 57
 5.8
 60
 ... all other unlabeled imagination of numbers goes here ...
61
62
 class 9:
63
 6.4
 65
 67
 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0 0
68
 7.0
 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0
71
 72
73
 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0
 74
 7.6
 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 0 0 0 0 0 0 0
77
7.8
 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 0 0 0 0 0 0 0
79
 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0
 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0
80
81
 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 1 1 0 0 0 0 0 0 0
82
 0 0 0 0 0 0 0 1 1 0 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0
 0 0 0 0 0 0 0 1 1 0 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0
83
 0 0 0 0 0 0 0 1 1 1 0 0 0 1 0 0 1 1 0 0 0 0 0 0 0 0 0
84
85
 86
87
 8.9
 9.0
 91
92
9.3
 No. of Iteration: 1, Difference: 3176.579389514846
95
96
97
 class 0:
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100	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
101	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
102	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
103	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
104	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
105	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
106	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
107																										0		
108	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
109																										0		
110																										0		
111																										0		
112																										0		
113																										0		
114																										0		
115																										0		
116																										0		
																										0		
117																												
118																										0		
119																										0		
120	0																									0		
121																										0		
122	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0							0	0	0	0	0		
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123 124 125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		0	0
123 124 125 126	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
123 124 125 126 127	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
123 124 125 126 127 128	0	0	0 0 a.l	0	o o ot	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
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123 124 125 126 127 128 129 130	0 0 	0 0  Las	0 0 al 38 0	0 0 11 9: 0	0 0 ot	0 0 the	0 0 er	0 0 it	0 0 0 0 0	0 0 rat	0 0	0 0 0 0	0 0	0 0 0	0 0	0 0 he	0 0 0 0	0 0	0 0	0 0	0 0	0 0	0 0 0	0 0 0	0 0	0 0	0 0	0 0
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123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0	0 all ss 0 0 0 0 0 0 0 0 0	9: 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 1 1 1	0 0 0 0 0 0 1 1 1	0 0 0 0 0 0 0 0 1 1 1 0 0	0 0 0 0 0 0 1 1 1 0 0	0 0 0 0 0 0 1 1 0 0 0	0 0 0 0 1 1 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0
123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 140	0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	all ss o o o o o o o o	9: 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 1 1 1	0 0 0 0 0 0 0 1 1 1	0 0 0 0 0 0 0 0 1 1 1 0 0	0 0 0 0 0 0 1 1 1 0 0	0 0 0 0 0 0 1 1 0 0 0	0 0 0 0 1 1 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	00000000000	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0
123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 140	0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	all 38 0 0 0 0 0 0 0 0 0 0 0	9: 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 1 1 1 1	0 0 0 0 0 1 1 1 1	0 0 0 0 0 0 0 0 1 1 1 0 0 0	0 0 0 0 0 0 1 1 1 0 0 0 0	0 0 0 0 0 0 1 1 0 0 0 0	0 0 0 0 1 1 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0	0000000000000	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0	00000000000
123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 140 141	0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 all ss 0 0 0 0 0 0 0 0 0 0 0 0 0	9: 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 1	0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 1	0 0 0 0 0 0 0 1 1 1 1 1 1	0 0 0 0 0 1 1 1 1	0 0 0 0 0 1 1 1 0 0 0 0 0 0 0	0 0 0 0 0 0 1 1 1 0 0 0 0	0 0 0 0 0 0 1 1 0 0 0 0 0	0 0 0 0 1 1 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 1	0000000000000	0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0	000000000000
123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 140 141 142	0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	all 38 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 1 1 9 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 1 1	0 0 0 0 0 0 0 0 0 0 0 0 1 1 1	0 0 0 0 0 0 0 1 1 1 1 1 1 0	0 0 0 0 0 1 1 1 1 1 0 0	0 0 0 0 0 0 0 0 1 1 1 0 0 0 0 0	0 0 0 0 0 0 0 1 1 0 0 0 0 0 0	0 0 0 0 0 0 0 1 1 0 0 0 0 0 1 1 1	0 0 0 0 1 1 0 0 0 0 0 1	0 0 0 0 0 0 0 0 0 0 0 1 1	000000000000000	0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0	0000000000000
123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 140 141 142 143 144	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	al ss 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	9:0000000000000000000000000000000000000	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	000000000000000000000000000000000000000	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 1 1 1	0 0 0 0 0 0 0 0 1 1 1 1 1 1 1	0 0 0 0 0 0 0 1 1 1 1 1 1 0 0	0 0 0 0 0 0 0 0 0 1 1 1 1 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0	0 0 0 0 0 0 0 1 1 0 0 0 0 0 1 1 1	0 0 0 0 0 0 0 0 0 0 1 1 1	0 0 0 0 0 0 0 0 0 0 0 1 1 1	000000000000000	00000000000000000	0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0	00000000000000000	00000000000000

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148 0 0 0 0 0 0 0 0 0 0 1 1 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0
149
 150
 0 0 0 0 0 0 0 0 0 0 1 1 1 1 1 1 1 1 0 0 0 0 0 0 0 0 0 0
151
152
 153
 154
 155
156
 157
158
 No. of Iteration: 10, Difference: 19.89546432548733
159
160
161
162
163
164
 labeled class 0:
165
 166
 167
168
 169
 170
 171
 172
 173
 174
 0 0 0 0 0 0 0 0 1 1 1 1 1 1 0 0 0 0 0 1 1 1 1 0 0 0 0 0
175
 0 0 0 0 0 0 0 1 1 1 1 1 0 0 0 0 0 0 0 1 1 1 1 0 0 0 0 0
177
 178
179
 180
 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0 0 0 1 1 1 0 0 0 0 0
181
182
 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0 0 0 1 1 1 0 0 0 0 0
183
 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0 0 1 1 1 0 0 0 0 0
184
 0 0 0 0 0 0 1 1 1 1 1 0 0 0 0 0 0 0 1 1 1 1 0 0 0 0 0 0
185
 0 0 0 0 0 0 0 1 1 1 1 1 0 0 0 0 0 1 1 1 1 1 1 0 0 0 0 0 0
186
 0 0 0 0 0 0 0 0 0 1 1 1 1 1 1 1 1 1 1 0 0 0 0 0 0 0 0 0 0
187
188
 0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0
189
 190
 191
 192
193
194
 labeled class 1:
 195
196
```

```
198
  199
  200
  201
  0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 0 0 0 0 0 0 0 0 0 0
202
203
  0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0 0 0
  0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0 0 0
204
  0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0 0 0
  0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0 0 0
207
  0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 0 0 0 0 0 0 0 0 0 0 0
  208
  0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0 0 0 0
209
210
  211
  0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0 0 0 0
212
  214
  216
  217
  218
219
  220
  221
  223
224
  ... all other labeled imagination of numbers goes here ...
225
  labeled class 9:
226
227
  228
  230
231
  232
233
  234
  235
  0 0 0 0 0 0 0 0 0 1 1 1 0 0 0 0 0 1 1 0 0 0 0 0 0 0 0
236
237
  0 0 0 0 0 0 0 0 1 1 1 1 0 0 0 0 0 1 1 0 0 0 0 0 0 0 0
  0 0 0 0 0 0 0 0 1 1 0 0 0 0 0 0 1 1 0 0 0 0 0 0 0
238
239
  0 0 0 0 0 0 0 0 1 1 0 0 0 0 0 0 0 1 1 0 0 0 0 0 0 0 0
240
  0 0 0 0 0 0 0 0 1 1 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0
  0 0 0 0 0 0 0 0 1 1 0 0 0 0 0 1 1 1 1 0 0 0 0 0 0 0 0
  243
  0 0 0 0 0 0 0 0 0 1 1 1 1 1 1 1 1 1 1 0 0 0 0 0 0 0 0 0
244
  0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0
  0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 0 0 0 0 0 0 0 0
245
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246 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 0 0 0 0 0 0 0 0
247 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 0 0 0 0 0 0 0 0
248 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 0 0 0 0 0 0 0 0
   249
250 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0
251
   253
255
256
257
258 Confusion Matrix 0:
              Predict number 0 Predict not number 0
259
                  3023
260 Is number 0
261 Isn't number 0
                   113
                                53964
262
263 Sensitivity (Successfully predict number 0) : 0.51038
264 Specificity (Successfully predict not number 0): 0.99791
265
266
267
268 Confusion Matrix 1:
         Predict number 1 Predict not number 1
269
270 Is number 1
                  5986
                                 756
   Isn't number 1
                   800
271
                                 52458
272
273 Sensitivity (Successfully predict number 1) : 0.88787
274 Specificity (Successfully predict not number 1): 0.98498
275
276
277
278 ... all other confusion matrix goes here ...
279
280
281
282 Confusion Matrix 9:
              Predict number 9 Predict not number 9
283
284 Is number 9
                  2718
                                 3231
285 Isn't number 9
                  5147
                                 48904
286
287 Sensitivity (Successfully predict number 9) : 0.45688
288 Specificity (Successfully predict not number 9): 0.90478
289
290 Total iteration to converge: 10
291 Total error rate: 0.5081666666666667
```