

## Model selection concepts

*In class exercise: Week 5*

1. Which of the following is correct when comparing LASSO to an ordinary least squares linear regression:
  - (a) It is more flexible and hence will give improved prediction accuracy when its increase in bias is less than its decrease in variance.
  - (b) It is more flexible and hence will give improved prediction accuracy when its increase in variance is less than its decrease in bias.
  - (c) It is less flexible and hence will give improved prediction accuracy when its increase in bias is less than its decrease in variance.
  - (d) It is less flexible and hence will give improved prediction accuracy when its increase in variance is less than its decrease in bias.
2. Which of the following is correct when comparing a non-linear regression method to an ordinary least squares linear regression:
  - (a) It is more flexible and hence will give improved prediction accuracy when its increase in bias is less than its decrease in variance.
  - (b) It is more flexible and hence will give improved prediction accuracy when its increase in variance is less than its decrease in bias.
  - (c) It is less flexible and hence will give improved prediction accuracy when its increase in bias is less than its decrease in variance.
  - (d) It is less flexible and hence will give improved prediction accuracy when its increase in variance is less than its decrease in bias.
3. Suppose we estimate the regression coefficients in a linear regression model by minimizing

$$\sum_{i=1}^n \left( y_i - \beta_0 - \sum_{j=1}^p \beta_j x_{ij} \right)^2 \quad \text{subject to} \quad \sum_{j=1}^p |\beta_j| \leq s$$

for a particular value of  $s$ . For parts (a) to (d), indicate which of (i) through (v) is correct and justify your answer.

- (a) As we increase  $s$  from 0, the *training* RSS will:
- (b) As we increase  $s$  from 0, the *test* RSS will:
- (c) As we increase  $s$  from 0, the variance will:
- (d) As we increase  $s$  from 0, the (squared) bias will:

The options that you can choose from are:

- (i) Increase initially, and then eventually start decreasing in an inverted U shape.
- (ii) Decrease initially, and then eventually start increasing in a U shape.
- (iii) Steadily increase.
- (iv) Steadily decrease.
- (v) Remain constant.