sheet06

December 2, 2024

1 Sheet 6

1.1 1 Autoencoders: theory and practice

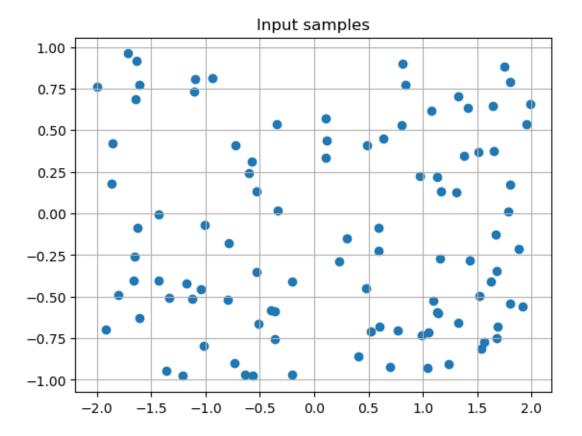
by Oliver Sange, Sam Rouppe van der Voort and Elias Huber

```
[7]: import torch
import matplotlib.pyplot as plt
import numpy as np

# create 100 uniform samples from a rectangle [-2, 2] x [-1, 1]
num_samples = 100
data = torch.zeros(num_samples, 2)
data[:, 0] = torch.rand(num_samples) * 4 - 2
data[:, 1] = torch.rand(num_samples) * 2 - 1

# plot the samples
plt.scatter(data[:, 0], data[:, 1])
plt.title("Input samples")
plt.grid(True)
plt.show()

max_epochs_run = 1000
```



```
[8]: from torch.utils.data import DataLoader, TensorDataset

# Prepare data loader
dataset = TensorDataset(data, data)
data_loader = DataLoader(dataset, batch_size=8, shuffle=True, drop_last=True)

# get batched data from the data loader
x, y = next(iter(data_loader))
print("x.shape:", x.shape)
print("y.shape:", y.shape)
print("y.shape:", y.shape)
print("all x == y:", torch.all(x == y).item())

x.shape: torch.Size([8, 2])
y.shape: torch.Size([8, 2])
```

all x == y: True

1.2 (a)

```
[9]: # TODO: define the Autoencoder architecture
     import torch
     from torch import nn
     import pytorch_lightning as pl
     class Autoencoder(nn.Module):
         def __init__(self, hidded_channels, latent_dim=1, input_dim=2,activation=nn.
      →ReLU,PCA=False):
             super().__init__()
             if not PCA:
                 # TODO: implement the encoder and decoder
                 layers_encoder = []
                 layers_decoder = []
                 n_layers = len(hidded_channels)
                 layers_encoder.append(nn.Linear(input_dim,hidded_channels[0])) #__
      ⇔adding input layer
                 #layers_encoder.append(input_dim)
                 layers_encoder.append(activation())
                 pass_latent = False
                 for i, (l_in,l_out) in enumerate(zip(hidded_channels[:
      →-1],hidded_channels[1:])):
                     if pass_latent:
                         layers_decoder.append(nn.Linear(l_in,l_out))
                         if i != n_layers-2: # no relu activation of output?
                             layers_decoder.append(activation())
                     else:
                         if l_out == latent_dim:
                             pass_latent = True
                         layers_encoder.append(nn.Linear(l_in,l_out))
                         if not pass_latent: # no activation applied on the latent_{\sqcup}
      ⇔space
                             layers_encoder.append(activation())
                 self.encoder = nn.Sequential(*layers_encoder)
                 self.decoder = nn.Sequential(*layers_decoder)
             else:
                 # Linear encoder
                 self.encoder = nn.Linear(input_dim, latent_dim)
                 # Linear decoder
                 self.decoder = nn.Linear(latent_dim, input_dim)
         def forward(self, x):
```

```
x = self.encoder(x)
        x = self.decoder(x)
        return x
    def encode(self, x):
        x_encoded = self.encoder(x)
        return x_encoded
    def decode(self, x):
        x_decoded = self.decoder(x)
        return x_decoded
11 11 11
            #self.encoder = nn.ModuleList(layers_encoder)
            #self.decoder = nn.ModuleList(layers_decoder)
# when using the nn.ModuleList one must define the forward pass explicitly as \Box
in understood, example with loop like:
        # def forward(self, x):
             for layer in self.encoder:
                  x = layer(x)
        #
        #
          for layer in self.decoder:
                  x = layer(x)
            return x
11 11 11
class AutoencoderModule(pl.LightningModule):
    def __init__(self, **model_kwargs):
        super().__init__()
        self.autoencoder = Autoencoder(**model_kwargs)
        self.loss_curve = []
    def forward(self, x):
        return self.autoencoder(x)
    def configure_optimizers(self):
        # as default use Adam optimizer:
        optimizer = torch.optim.Adam(self.parameters())#, weight_decay=1e-5)
        return optimizer
    def on_train_start(self):
        self.loss_curve = []
        return super().on_train_start()
    def training_step(self, batch):
        x, _ = batch
```

```
x_hat = self.autoencoder(x)
loss = nn.MSELoss()(x_hat, x)
self.loss_curve.append(loss.item())
return loss
```

For the Network architecture we used the ReLU activation function since we want to handle a regression problem and the ReLU is the state of the art for these classes of problems. We also decided to not put an activation function on the latent space since it would only half the space and project the negative encoder output to zero.

```
[10]: hidded_channels_small = [20, 10, 1, 10, 20, 2]
      autoencoder_module_small =_
       AutoencoderModule(hidded_channels=hidded_channels_small,latent_dim=1,_
       →input_dim=2, activation=nn.ReLU) #Autoencoder(hidded_channels_small)# #_U
       → TODO: specify the model here
      print("small Model overview:", autoencoder_module_small)
      hidded_channels_big = [50, 50, 50, 1, 50, 50, 50, 2]
      autoencoder_module_big =
       AutoencoderModule(hidded channels=hidded channels_big,latent_dim=1,_
       →input_dim=2, activation=nn.ReLU )
      print("big Model overview:", autoencoder_module_big)
      PCA_autoencoder = AutoencoderModule(hidded_channels=None, PCA=True, latent_dim=1,_
       →input_dim=2)
      print("pca like Model overview:", PCA_autoencoder)
     small Model overview: AutoencoderModule(
       (autoencoder): Autoencoder(
         (encoder): Sequential(
           (0): Linear(in_features=2, out_features=20, bias=True)
           (1): ReLU()
           (2): Linear(in_features=20, out_features=10, bias=True)
           (3): ReLU()
           (4): Linear(in_features=10, out_features=1, bias=True)
         (decoder): Sequential(
           (0): Linear(in_features=1, out_features=10, bias=True)
           (1): ReLU()
           (2): Linear(in_features=10, out_features=20, bias=True)
           (3): ReLU()
           (4): Linear(in_features=20, out_features=2, bias=True)
         )
       )
```

```
big Model overview: AutoencoderModule(
       (autoencoder): Autoencoder(
         (encoder): Sequential(
           (0): Linear(in features=2, out features=50, bias=True)
           (1): ReLU()
           (2): Linear(in features=50, out features=50, bias=True)
           (3): ReLU()
           (4): Linear(in features=50, out features=50, bias=True)
           (5): ReLU()
           (6): Linear(in_features=50, out_features=1, bias=True)
         (decoder): Sequential(
           (0): Linear(in_features=1, out_features=50, bias=True)
           (1): ReLU()
           (2): Linear(in_features=50, out_features=50, bias=True)
           (3): ReLU()
           (4): Linear(in_features=50, out_features=50, bias=True)
           (5): ReLU()
           (6): Linear(in features=50, out features=2, bias=True)
         )
       )
     pca like Model overview: AutoencoderModule(
       (autoencoder): Autoencoder(
         (encoder): Linear(in_features=2, out_features=1, bias=True)
         (decoder): Linear(in_features=1, out_features=2, bias=True)
       )
     )
     1.3 (b)
[11]: # start the training using a PyTorch Lightning Trainer
      trainer small = pl.Trainer(max epochs=max epochs run,
       →enable_checkpointing=False) # was max_epochs=max_epochs_run (1000 for test)
      trainer_small.fit(autoencoder_module_small, data_loader)
     GPU available: False, used: False
     TPU available: False, using: 0 TPU cores
     HPU available: False, using: 0 HPUs
     /home/elias/miniconda3/envs/mlph3/lib/python3.9/site-packages/pytorch_lightning/
     trainer/connectors/logger_connector/logger_connector.py:75: Starting from
     v1.9.0, `tensorboardX` has been removed as a dependency of the
     `pytorch_lightning` package, due to potential conflicts with other packages in
     the ML ecosystem. For this reason, `logger=True` will use `CSVLogger` as the
     default logger, unless the `tensorboard` or `tensorboardX` packages are found.
     Please `pip install lightning[extra]` or one of them to enable TensorBoard
```

support by default

```
| Name
                     | Type
                                  | Params | Mode
     0 | autoencoder | Autoencoder | 563 | train
     _____
     563
               Trainable params
     0
               Non-trainable params
     563
               Total params
               Total estimated model params size (MB)
     0.002
     /home/elias/miniconda3/envs/mlph3/lib/python3.9/site-
     packages/pytorch_lightning/trainer/connectors/data_connector.py:424: The
     'train_dataloader' does not have many workers which may be a bottleneck.
     Consider increasing the value of the `num_workers` argument` to `num_workers=7`
     in the `DataLoader` to improve performance.
     /home/elias/miniconda3/envs/mlph3/lib/python3.9/site-
     packages/pytorch_lightning/loops/fit_loop.py:298: The number of training batches
     (12) is smaller than the logging interval Trainer(log every n steps=50). Set a
     lower value for log_every_n_steps if you want to see logs for the training
     epoch.
                                                              | 0/? [00:00<?, ?it/s]
     Training: |
     IOPub message rate exceeded.
     The Jupyter server will temporarily stop sending output
     to the client in order to avoid crashing it.
     To change this limit, set the config variable
     `--ServerApp.iopub_msg_rate_limit`.
     Current values:
     ServerApp.iopub_msg_rate_limit=1000.0 (msgs/sec)
     ServerApp.rate_limit_window=3.0 (secs)
     `Trainer.fit` stopped: `max_epochs=1000` reached.
[12]: # start the training using a PyTorch Lightning Trainer
     trainer_big = pl.Trainer(max_epochs=max_epochs_run, enable_checkpointing=False)
     trainer_big.fit(autoencoder_module_big, data_loader)
     GPU available: False, used: False
     TPU available: False, using: 0 TPU cores
     HPU available: False, using: 0 HPUs
       | Name
                     | Type
                                  | Params | Mode
     0 | autoencoder | Autoencoder | 10.6 K | train
     10.6 K
               Trainable params
```

```
10.6 K
              Total params
     0.042
              Total estimated model params size (MB)
     Training: |
                                                              | 0/? [00:00<?, ?it/s]
     `Trainer.fit` stopped: `max_epochs=1000` reached.
[13]: # start the training using a PyTorch Lightning Trainer
     PCA_trainer = pl.Trainer(max_epochs=max_epochs_run, enable_checkpointing=False)
     PCA_trainer.fit(PCA_autoencoder, data_loader)
     GPU available: False, used: False
     TPU available: False, using: 0 TPU cores
     HPU available: False, using: 0 HPUs
                    | Type
                                  | Params | Mode
       | Name
     0 | autoencoder | Autoencoder | 7 | train
     ______
               Trainable params
     0
               Non-trainable params
               Total params
               Total estimated model params size (MB)
     0.000
                                                              | 0/? [00:00<?, ?it/s]
     Training: |
     IOPub message rate exceeded.
     The Jupyter server will temporarily stop sending output
     to the client in order to avoid crashing it.
     To change this limit, set the config variable
     `--ServerApp.iopub_msg_rate_limit`.
     Current values:
     ServerApp.iopub_msg_rate_limit=1000.0 (msgs/sec)
     ServerApp.rate_limit_window=3.0 (secs)
     IOPub message rate exceeded.
     The Jupyter server will temporarily stop sending output
     to the client in order to avoid crashing it.
     To change this limit, set the config variable
     `--ServerApp.iopub_msg_rate_limit`.
     Current values:
     ServerApp.iopub_msg_rate_limit=1000.0 (msgs/sec)
     ServerApp.rate_limit_window=3.0 (secs)
     IOPub message rate exceeded.
     The Jupyter server will temporarily stop sending output
```

Non-trainable params

to the client in order to avoid crashing it. To change this limit, set the config variable `--ServerApp.iopub_msg_rate_limit`.

Current values:

ServerApp.iopub_msg_rate_limit=1000.0 (msgs/sec)
ServerApp.rate_limit_window=3.0 (secs)

IOPub message rate exceeded.

The Jupyter server will temporarily stop sending output to the client in order to avoid crashing it.

To change this limit, set the config variable

`--ServerApp.iopub_msg_rate_limit`.

Current values:

ServerApp.iopub_msg_rate_limit=1000.0 (msgs/sec)
ServerApp.rate_limit_window=3.0 (secs)

IOPub message rate exceeded.

The Jupyter server will temporarily stop sending output to the client in order to avoid crashing it.

To change this limit, set the config variable

`--ServerApp.iopub_msg_rate_limit`.

Current values:

ServerApp.iopub_msg_rate_limit=1000.0 (msgs/sec)
ServerApp.rate_limit_window=3.0 (secs)

IOPub message rate exceeded.

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To change this limit, set the config variable

`--ServerApp.iopub_msg_rate_limit`.

Current values:

ServerApp.iopub_msg_rate_limit=1000.0 (msgs/sec)
ServerApp.rate_limit_window=3.0 (secs)

IOPub message rate exceeded.

The Jupyter server will temporarily stop sending output to the client in order to avoid crashing it.

To change this limit, set the config variable

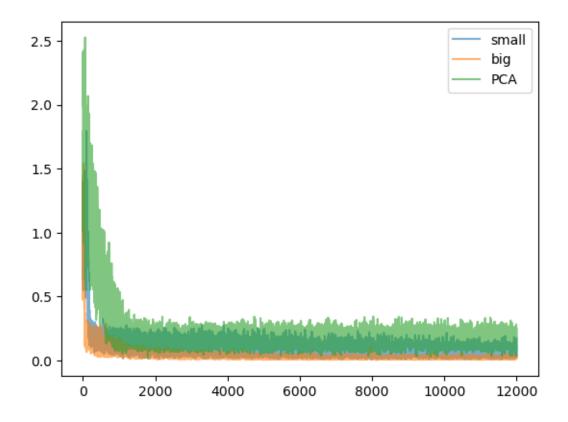
`--ServerApp.iopub_msg_rate_limit`.

Current values:

ServerApp.iopub_msg_rate_limit=1000.0 (msgs/sec)
ServerApp.rate_limit_window=3.0 (secs)

```
The Jupyter server will temporarily stop sending output
     to the client in order to avoid crashing it.
     To change this limit, set the config variable
     `--ServerApp.iopub msg rate limit`.
     Current values:
     ServerApp.iopub_msg_rate_limit=1000.0 (msgs/sec)
     ServerApp.rate limit window=3.0 (secs)
     IOPub message rate exceeded.
     The Jupyter server will temporarily stop sending output
     to the client in order to avoid crashing it.
     To change this limit, set the config variable
     `--ServerApp.iopub_msg_rate_limit`.
     Current values:
     ServerApp.iopub_msg_rate_limit=1000.0 (msgs/sec)
     ServerApp.rate_limit_window=3.0 (secs)
     `Trainer.fit` stopped: `max_epochs=1000` reached.
[14]: # len(autoencoder_module_big.loss_curve)
      ## here im not completely sure what i should actually plot, probably average,
       ⇔over each epoch makes more sense,
      # i dont understand why the loss_curve length is so long.
      plt.plot(range(len(autoencoder_module_small.
       ⇔loss_curve)),autoencoder_module_small.loss_curve,label="small",alpha = 0.6)
      plt.plot(range(len(autoencoder_module_big.loss_curve)),autoencoder_module_big.
       ⇔loss_curve,label="big",alpha = 0.6)
      plt.plot(range(len(PCA_autoencoder.loss_curve)),PCA_autoencoder.
       →loss_curve,label="PCA",alpha = 0.6)
      plt.legend()
[14]: <matplotlib.legend.Legend at 0x7fda4c5076a0>
```

IOPub message rate exceeded.



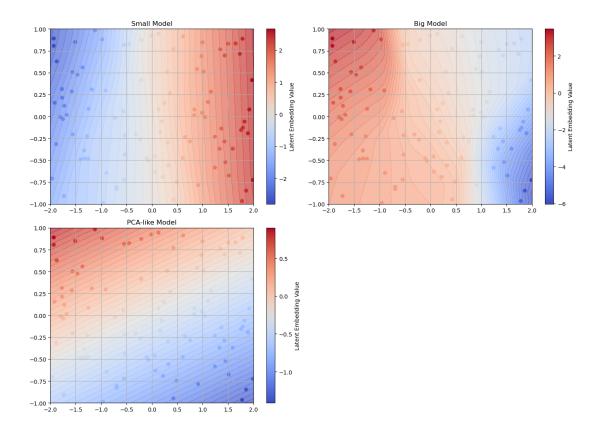
```
[40]: latent_embedding small = autoencoder_module_small.autoencoder.encode(data)
      latent_embedding_big = autoencoder_module_big.autoencoder.encode(data)
      latent_embedding_PCA = PCA_autoencoder.autoencoder.encode(data)
      # Flatten the grid for encoding
      x_{grid}, y_{grid} = np.meshgrid(np.linspace(-2, 2, 100), np.linspace(-1, 1, 100))
      # Convert grid to PyTorch tensors
      x_tensor = torch.from_numpy(x_grid).float() # Shape: (100, 100)
      y_tensor = torch.from_numpy(y_grid).float() # Shape: (100, 100)
      # Step 2: Combine x and y into a grid tensor for encoding
      grid = torch.stack((x_tensor, y_tensor), dim=-1)
      grid_flat = grid.view(-1, 2) # Flatten to shape (10000, 2)
      # Encode the grid points using the autoencoders
      contour_values1 = autoencoder_module_small.autoencoder.encode(grid_flat)
      contour_values2 = autoencoder_module_big.autoencoder.encode(grid_flat)
      contour_values3 = PCA_autoencoder.autoencoder.encode(grid_flat)
      # Reshape the encoded values back to a 2D grid for contourf
      contour_values1 = contour_values1.view(100, 100).detach().numpy()
```

```
contour_values2 = contour_values2.view(100, 100).detach().numpy()
contour_values3 = contour_values3.view(100, 100).detach().numpy()
# Plot
fig, axes = plt.subplots(2, 2, figsize=(14, 10)) # Adjust figsize for better_
 \hookrightarrow layout
# Plot latent embeddings for each model
contour1 = axes[0, 0].contourf(x_grid, y_grid, contour_values1, levels=50, u
 ⇔cmap='coolwarm', alpha=0.7)
contour2 = axes[0, 1].contourf(x_grid, y_grid, contour_values2, levels=50, u
⇔cmap='coolwarm', alpha=0.7)
contour3 = axes[1, 0].contourf(x_grid, y_grid, contour_values3, levels=50,_
 ⇔cmap='coolwarm', alpha=0.7)
scatter1 = axes[0, 0].scatter(data[:, 0], data[:, 1], c=latent_embedding_small.

detach().numpy(), cmap='coolwarm')
scatter2 = axes[0, 1].scatter(data[:, 0], data[:, 1], c=latent_embedding_big.

detach().numpy(), cmap='coolwarm')
scatter3 = axes[1, 0].scatter(data[:, 0], data[:, 1], c=latent_embedding_PCA.

detach().numpy(), cmap='coolwarm')
fig.colorbar(scatter1, ax=axes[0, 0], label="Latent Embedding Value")
fig.colorbar(scatter2, ax=axes[0, 1], label="Latent Embedding Value")
fig.colorbar(scatter3, ax=axes[1, 0], label="Latent Embedding Value")
axes[0, 0].set_title("Small Model")
axes[0, 1].set_title("Big Model")
axes[1, 0].set_title("PCA-like Model")
axes[0, 0].grid(True)
axes[0, 1].grid(True)
axes[1, 0].grid(True)
# Hide the empty subplot (bottom-right) as we only need 3 plots
axes[1, 1].axis('off')
plt.tight_layout()
plt.show()
```



The PCA model prefers a color gradient around the X2 axis, the X1 axis seems to influence the embedding less. This can be due to getting the X2 axis wrong leads to a higher loss than for the X1 axis, due to the stretch in the sample space.

1.4 (c)

1.5 also make a prediciton before looking at plots below

If we sample points from an interval in the latent space, the decoder can attempt to map them to a curve in the ambient/input space. Guess what these curves may look like: i) After random initialization of the MLP parameters, and ii) After training the respective architecture.

1.5.1 i)

A random walk like line.

1.5.2 ii)

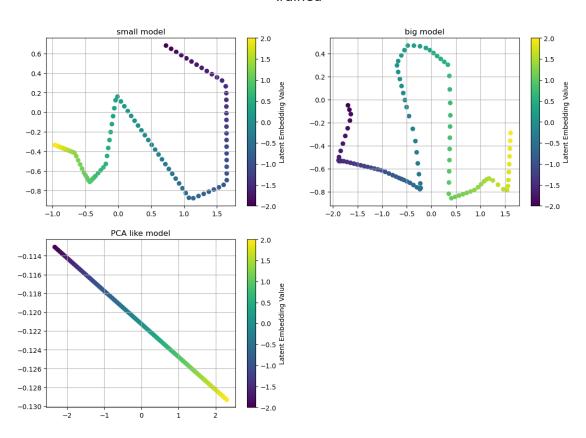
We think its a line following the color change seen above.

1.6 (d)

```
[15]: import numpy as np
      latent_space_samples = np.linspace(-2, 2, 100) # somewhat arbitrary choice for
      →ReLu maybe, shoud just inlude origin
      # if we change the non linearity to sigmoid, then from -1 to 1 i would say,
      # but also we need to think if we should have a non linearity in latent space
      # for this random num task i dont see why not but idk
      latent_space_samples = torch.tensor(latent_space_samples,dtype=torch.float32).
       \rightarrowview(100, 1)
      samples_decoded_trained_small = autoencoder_module_small.autoencoder.
       →decode(latent_space_samples)
      samples_decoded_trained_big = autoencoder_module_big.autoencoder.
       →decode(latent_space_samples)
      samples decoded trained PCA = PCA autoencoder.autoencoder.
       →decode(latent_space_samples)
      fig, axes = plt.subplots(2, 2, figsize=(14, 10)) # Adjust figsize for better_
       \hookrightarrow layout
      # Plot latent embeddings for each model
      scatter1 = axes[0,0].scatter(samples decoded trained small[:, 0].detach().
       →numpy(), samples_decoded_trained_small[:, 1].detach().
       anumpy(),c=latent_space_samples.detach().numpy(), cmap='viridis')
      scatter2 = axes[0,1].scatter(samples decoded trained big[:, 0].detach().
       →numpy(), samples decoded trained big[:, 1].detach().
       anumpy(),c=latent_space_samples.detach().numpy(), cmap='viridis')
      scatter3 = axes[1,0].scatter(samples_decoded_trained_PCA[:, 0].detach().
       umpy(), samples_decoded_trained_PCA[:, 1].detach().
       anumpy(),c=latent_space_samples.detach().numpy(), cmap='viridis')
      fig.colorbar(scatter1, ax=axes[0, 0], label="Latent Embedding Value")
      fig.colorbar(scatter2, ax=axes[0, 1], label="Latent Embedding Value")
      fig.colorbar(scatter3, ax=axes[1, 0], label="Latent Embedding Value")
      axes[0,0].set title("small model")
      axes[0,1].set_title("big model")
      axes[1,0].set_title("PCA like model")
      axes[0,0].grid(True)
      axes[0,1].grid(True)
      axes[1,0].grid(True)
```

```
fig.suptitle('Trained',fontsize=20)
# Hide the empty subplot (bottom-right) as we only need 3 plots
axes[1, 1].axis('off')
plt.show()
```

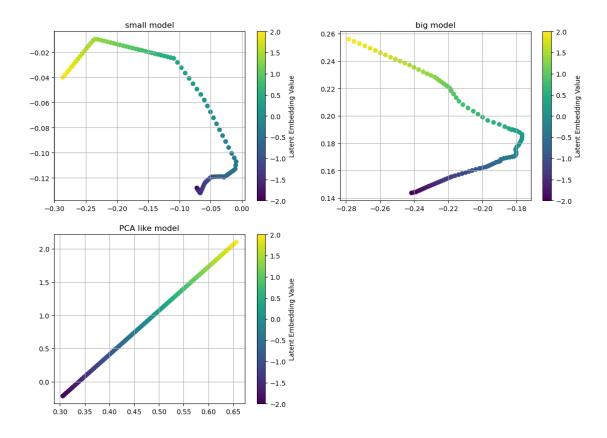
Trained



```
{\tt samples\_decoded\_untrained\_PCA = untrained\_PCA\_autoencoder.autoencoder.}

decode(latent_space_samples)
fig, axes = plt.subplots(2, 2, figsize=(14, 10)) # Adjust figsize for better
 \hookrightarrow layout
scatter1 = axes[0,0].scatter(samples_decoded_untrained_small[:, 0].detach().
 →numpy(), samples_decoded_untrained_small[:, 1].detach().
 anumpy(),c=latent_space_samples.detach().numpy(), cmap='viridis')
scatter2 = axes[0,1].scatter(samples_decoded_untrained_big[:, 0].detach().
 →numpy(), samples decoded untrained big[:, 1].detach().
 anumpy(),c=latent_space_samples.detach().numpy(), cmap='viridis')
scatter3 = axes[1,0].scatter(samples decoded untrained PCA[:, 0].detach().
 →numpy(), samples_decoded_untrained_PCA[:, 1].detach().
 anumpy(),c=latent_space_samples.detach().numpy(), cmap='viridis')
fig.colorbar(scatter1, ax=axes[0, 0], label="Latent Embedding Value")
fig.colorbar(scatter2, ax=axes[0, 1], label="Latent Embedding Value")
fig.colorbar(scatter3, ax=axes[1, 0], label="Latent Embedding Value")
axes[0,0].set_title("small model")
axes[0,1].set_title("big model")
axes[1,0].set_title("PCA like model")
axes[0,0].grid(True)
axes[0,1].grid(True)
axes[1,0].grid(True)
fig.suptitle('Untrained',fontsize=20)
# Hide the empty subplot (bottom-right) as we only need 3 plots
axes[1, 1].axis('off')
plt.show()
```

Untrained



We observe that the trained model curve tries to cover most of the space where the data points are placed. This is contrary to the untrained model where the region where the path goes is stretched on a smaller region.

1.7 (e) and (f) discussion

1.7.1 (e)

Given enough parameters, the encoder can reconstruct the finite number of points by fitting the intepolation polynimal that fits all the points. This representation however is not very useful due to extreme overfitting.

An MLP autoencoder with a bottleneck dimension of 1 can theoretically reconstruct all data points given a sufficiently complex architecture and effective training. Since MLPs are universal approximators, they can approximate the necessary mappings if they have enough width and depth. However, practical challenges, such as optimization difficulties or finite numerical precision, can affect the model's performance. While perfect reconstruction theoretically possible, achieving it in practice is often very difficult.

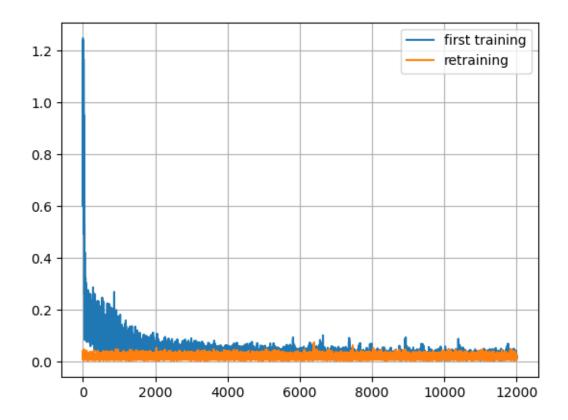
1.7.2 (f)

The encoder will with high likelyhood converge to a embedding close to the original encoder. But due to inefficiencies during training and the now less possible output values (since the decoder is fixed) the result will be less accurate then the original encoder.

```
[17]: hidded_channels_big = [50, 50, 50, 1, 50, 50, 50, 2]
      autoencoder_module_big_retrain =_
       AutoencoderModule(hidded_channels=hidded_channels_big,latent_dim=1,_u
       →input_dim=2, activation=nn.ReLU )
      # start the training using a PyTorch Lightning Trainer
      retrain_trainer = pl.Trainer(max_epochs=max_epochs_run,_
       ⇔enable_checkpointing=False)
      retrain_trainer.fit(autoencoder_module_big_retrain, data_loader)
      plt.plot(autoencoder_module_big_retrain.loss_curve,label="first training")
      latent_space_data_trained = autoencoder_module_big_retrain.autoencoder.
       →encoder(data).detach().numpy()
      #now fix decoder parameters
      for parameter in autoencoder_module_big_retrain.autoencoder.decoder.
       →parameters():
          parameter.requires_grad = False
      # reinitialize parameters for the encoder
      for parameter in autoencoder_module_big_retrain.autoencoder.encoder.
       →parameters():
          if isinstance(parameter,nn.Linear):
              nn.init.normal (parameter.weight,mean=0.0,std=1)
              nn.init.zeros_(parameter.bias)
      retrain_trainer = pl.Trainer(max_epochs=max_epochs_run,__
       →enable_checkpointing=False)
      retrain_trainer.fit(autoencoder_module_big_retrain, data_loader)
      plt.plot(autoencoder_module_big_retrain.loss_curve,label="retraining")
      plt.legend()
      plt.grid()
      plt.show()
      latent_space_data_retrained = autoencoder_module_big_retrain.autoencoder.
       →encoder(data).detach().numpy()
```

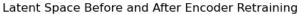
```
GPU available: False, used: False
TPU available: False, using: 0 TPU cores
HPU available: False, using: 0 HPUs
```

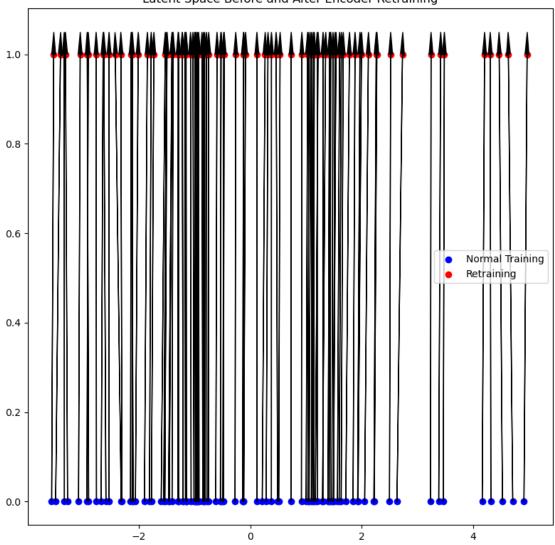
```
| Type
                     | Params | Mode
 l Name
_____
0 | autoencoder | Autoencoder | 10.6 K | train
______
10.6 K
       Trainable params
        Non-trainable params
10.6 K Total params
0.042
        Total estimated model params size (MB)
                                                   | 0/? [00:00<?, ?it/s]
Training: |
`Trainer.fit` stopped: `max_epochs=1000` reached.
GPU available: False, used: False
TPU available: False, using: 0 TPU cores
HPU available: False, using: 0 HPUs
 l Name
             | Type | Params | Mode
_____
0 | autoencoder | Autoencoder | 10.6 K | train
_____
5.3 K
        Trainable params
5.3 K
        Non-trainable params
10.6 K
        Total params
0.042
        Total estimated model params size (MB)
                                                   | 0/? [00:00<?, ?it/s]
Training: |
IOPub message rate exceeded.
The Jupyter server will temporarily stop sending output
to the client in order to avoid crashing it.
To change this limit, set the config variable
`--ServerApp.iopub_msg_rate_limit`.
Current values:
ServerApp.iopub_msg_rate_limit=1000.0 (msgs/sec)
ServerApp.rate_limit_window=3.0 (secs)
IOPub message rate exceeded.
The Jupyter server will temporarily stop sending output
to the client in order to avoid crashing it.
To change this limit, set the config variable
`--ServerApp.iopub_msg_rate_limit`.
Current values:
ServerApp.iopub_msg_rate_limit=1000.0 (msgs/sec)
ServerApp.rate_limit_window=3.0 (secs)
`Trainer.fit` stopped: `max_epochs=1000` reached.
```



```
[21]: fig, ax = plt.subplots(figsize=(8, 8))
      ax.scatter(latent_space_data_trained[:, 0], np.
       \sizeros_like(latent_space_data_trained[:, 0]), color='blue',
                 label='Normal Training')
      ax.scatter(latent_space_data_retrained[:, 0], np.

¬zeros_like(latent_space_data_retrained[:, 0])+1,
                 color='red', label='Retraining')
      # Add arrows showing how the encoder's output changed after retraining
      for i in range(len(latent_space_data_trained)):
          ax.arrow(latent_space_data_trained[i, 0], 0, latent_space_data_retrained[i, u]
       ⇔0] -
                   latent_space_data_trained[i,0], 1, head_width=0.07, head_length=0.
      ⇔05, fc='black', ec='black')
      ax.set_title('Latent Space Before and After Encoder Retraining')
      ax.legend()
      plt.tight_layout()
      plt.show()
```





1.8 (h)

```
[22]: # define model that uses SGD
class AutoencoderModuleSGD(pl.LightningModule):
    def __init__(self, **model_kwargs):
        super().__init__()
        self.autoencoder = Autoencoder(**model_kwargs)
        self.loss_curve = []

    def forward(self, x):
        return self.autoencoder(x)
```

```
def configure_optimizers(self):
    # as default use Adam optimizer:
    optimizer = torch.optim.SGD(self.parameters(), weight_decay=1e-5)

    return optimizer

def on_train_start(self):
    self.loss_curve = []
    return super().on_train_start()

def training_step(self, batch):
    x, _ = batch
    x_hat = self.autoencoder(x)
    loss = nn.MSELoss()(x_hat, x)
    self.loss_curve.append(loss.item())
    return loss
```

```
[26]: hidded_channels_big = [50, 50, 50, 1, 50, 50, 50, 2]
     autoencoder_module_big_retrain =_
       AutoencoderModule(hidded_channels=hidded_channels_big,latent_dim=1,_
       →input_dim=2, activation=nn.ReLU)
     dataset = TensorDataset(data, data)
     data_loader = DataLoader(dataset, batch_size=100, shuffle=True, drop_last=True)
     num_training examples = [list(range(8, 8*12*max_epochs_run+1, 8)),__
       →list(range(100,100*1*max_epochs_run+1, 100))]
      #num training samples given by step=num batch size, and total,
      → train_data_seen=batch_size*num_batches*epochs
      # start the training using a PyTorch Lightning Trainer
     retrain_trainer = pl.Trainer(max_epochs=max_epochs_run,__
       ⇔enable_checkpointing=False)
     retrain_trainer.fit(autoencoder_module_big_retrain, data_loader)
     plt.plot(num_training_examples[1],autoencoder_module_big_retrain.
       ⇔loss_curve,label="first training GD",alpha = 0.6)
      #now fix decoder parameters
     for parameter in autoencoder_module_big_retrain.autoencoder.decoder.
       →parameters():
         parameter.requires_grad = False
      # reinitialize parameters for the encoder
     for parameter in autoencoder_module_big_retrain.autoencoder.encoder.
       →parameters():
          if isinstance(parameter,nn.Linear):
```

```
nn.init.normal_(parameter.weight,mean=0.0,std=1)
       nn.init.zeros_(parameter.bias)
retrain_trainer = pl.Trainer(max_epochs=max_epochs_run,__
 →enable_checkpointing=False)
retrain trainer fit (autoencoder module big retrain, data loader)
plt.plot(num_training_examples[1],autoencoder_module_big_retrain.
 ⇔loss_curve, label="retraining GD", alpha=0.6)
## now the same task for SGD_
 dataset = TensorDataset(data, data)
data_loader = DataLoader(dataset, batch_size=8, shuffle=True, drop_last=True)
autoencoder_module_big_retrain = __
 -AutoencoderModuleSGD(hidded_channels=hidded_channels_big,latent_dim=1,_
 →input_dim=2, activation=nn.ReLU)
# start the training using a PyTorch Lightning Trainer
retrain_trainer = pl.Trainer(max_epochs=max_epochs_run,_
 →enable_checkpointing=False)
retrain_trainer.fit(autoencoder_module_big_retrain, data_loader)
plt.plot(num_training_examples[0],autoencoder_module_big_retrain.
 ⇔loss_curve, label="first training SGD", alpha = 0.6)
#now fix decoder parameters
for parameter in autoencoder module big retrain.autoencoder.decoder.
 →parameters():
   parameter.requires_grad = False
# reinitialize parameters for the encoder
for parameter in autoencoder_module_big_retrain.autoencoder.encoder.
 →parameters():
   if isinstance(parameter,nn.Linear):
       nn.init.normal_(parameter.weight,mean=0.0,std=1)
       nn.init.zeros_(parameter.bias)
retrain_trainer = pl.Trainer(max_epochs=max_epochs_run,__
 ⇔enable_checkpointing=False)
retrain_trainer.fit(autoencoder_module_big_retrain, data_loader)
plt.plot(num_training_examples[0],autoencoder_module_big_retrain.
 →loss_curve,label="retraining SGD", alpha = 0.6)
```

```
plt.legend()
plt.grid()
plt.show()
GPU available: False, used: False
TPU available: False, using: 0 TPU cores
HPU available: False, using: 0 HPUs
 | Name
              | Type
                       | Params | Mode
0 | autoencoder | Autoencoder | 10.6 K | train
_____
10.6 K
        Trainable params
        Non-trainable params
10.6 K
        Total params
        Total estimated model params size (MB)
0.042
                                                    | 0/? [00:00<?, ?it/s]
Training: |
`Trainer.fit` stopped: `max_epochs=1000` reached.
GPU available: False, used: False
TPU available: False, using: 0 TPU cores
HPU available: False, using: 0 HPUs
 | Name
              | Type
                         | Params | Mode
0 | autoencoder | Autoencoder | 10.6 K | train
_____
5.3 K
         Trainable params
5.3 K
         Non-trainable params
10.6 K
        Total params
0.042
         Total estimated model params size (MB)
                                                    | 0/? [00:00<?, ?it/s]
Training: |
`Trainer.fit` stopped: `max_epochs=1000` reached.
GPU available: False, used: False
TPU available: False, using: 0 TPU cores
HPU available: False, using: 0 HPUs
 | Name
              | Type
                           | Params | Mode
0 | autoencoder | Autoencoder | 10.6 K | train
-----
10.6 K
        Trainable params
         Non-trainable params
10.6 K
        Total params
0.042
         Total estimated model params size (MB)
```

```
Training: |
                                                         | 0/? [00:00<?, ?it/s]
`Trainer.fit` stopped: `max_epochs=1000` reached.
GPU available: False, used: False
TPU available: False, using: 0 TPU cores
HPU available: False, using: 0 HPUs
  | Name
               | Type
                             | Params | Mode
0 | autoencoder | Autoencoder | 10.6 K | train
______
5.3 K
         Trainable params
5.3 K
         Non-trainable params
10.6 K
         Total params
0.042
         Total estimated model params size (MB)
                                                         | 0/? [00:00<?, ?it/s]
Training: |
IOPub message rate exceeded.
The Jupyter server will temporarily stop sending output
to the client in order to avoid crashing it.
To change this limit, set the config variable
`--ServerApp.iopub_msg_rate_limit`.
Current values:
ServerApp.iopub msg rate limit=1000.0 (msgs/sec)
ServerApp.rate_limit_window=3.0 (secs)
IOPub message rate exceeded.
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Current values:
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ServerApp.rate_limit_window=3.0 (secs)
```

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Current values:

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IOPub message rate exceeded.

The Jupyter server will temporarily stop sending output to the client in order to avoid crashing it.

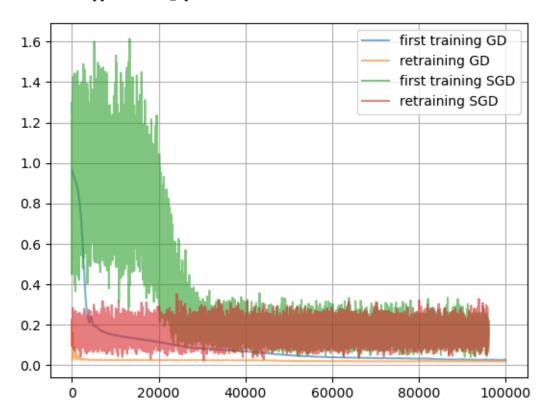
To change this limit, set the config variable

`--ServerApp.iopub msg_rate_limit`.

Current values:

ServerApp.iopub_msg_rate_limit=1000.0 (msgs/sec)
ServerApp.rate_limit_window=3.0 (secs)

`Trainer.fit` stopped: `max_epochs=1000` reached.



We see the gradient descent algorithm trains the network faster, when comapring to the examples seen, while in return taking more computing time.

[]:[

