tag OCaml type for struct/union tag $impl_const$ implementation-defined constant x, y, ident OCaml type variable for symbols

ty_mem_int memory integer value

mem_val memory value

member C struct/union member name

au C type annots annotations

nat OCaml arbitrary-width natural number

n, i index variables

loc OCaml type for C source

mem_iv_c OCaml type for memory constraints on integer values

UB_name undefined behaviour

string OCaml string

 $tyvar_{-}TY$ OCaml type variable for types

 τ OCaml type for an annotated C type

 sym_prefix OCaml type for symbol prefix mem_order OCaml type for memory order

linux_mem_order OCaml type for Linux memory order

k OCaml fixed-width integer

```
\beta
                                          Core base types
                                            unit
                    unit
                                            boolean
                    bool
                    integer
                                            integer
                                            rational numbers?
                    real
                                            location
                    loc
                    [\beta]
                                            list
                    (\beta_1,\ldots,\beta_n)
                                            tuple
                    \mathtt{struct}\,tag
                                            struct
                     \{\beta\}
                                            \operatorname{set}
                    \mathtt{opt}\left(eta
ight)
                                            option
                    \beta_1, \ldots, \beta_n \to \beta
                                            parameter types
                                          binary operators
binop
                                            addition
                                            subtraction
                                            multiplication
                                            division
                                            modulus
                    rem_t
                                            remainder
                    rem_f
                                            exponentiation
                                            equality, defined both for integer and C types
                                            greater than
                                            less than
                     <
                                            greater than or equal to
                    >=
                                            less than or equal to
                     <=
                    /\
                                            conjucttion
                    \/
                                            disjunction
polarity
                                          memory action polarities
              ::=
```

		Pos Neg	sequenced by let weak and let strong only sequenced by let strong
ident	::=	ident	Ott-hack, ignore
name	::= 	$ident \\ impl_const$	Core identifier implementation-defined constant
ptrval	::= 	$\begin{array}{c} \mathtt{nullptr} \\ \mathtt{funcptr} ident \\ \mathtt{concptr} nat \end{array}$	pointer values null pointer function pointer concrete pointer
$object_value$::=	$\begin{array}{l} ty_mem_int \\ ptrval \\ \texttt{array} \ (loaded_value_1, \ \ , loaded_value_n) \\ (\ \texttt{struct} \ ident) \{ \ \overline{.member_i : \tau_i = mem_val_i}^i \ \} \\ (\ \texttt{union} \ ident) \{ .member = mem_val \} \end{array}$	C object values integer value pointer value C array value C struct value C union value
$loaded_value$::=	$\verb specified (object_value)$	potentially unspecified C object values specified loaded value
β	::=	eta	Ott-hack, ignore
value	::=	$object_value$	Core values C object value

		$loaded_value$ Unit True False $\beta[value_1,, value_i]$ $(value_1,, value_i)$	loaded C object value unit boolean true boolean false list tuple
ctor	::=		data constructors
		$\mathtt{Nil}\beta$	empty list
	ĺ	Cons	list cons
	ĺ	Tuple	tuple
		Array	C array
		Ivmax	max integer value
		Ivmin	min integer value
		Ivsizeof	sizeof value
		Ivalignof	alignof value
		IvCOMPL	bitwise complement
		IvAND	bitwise AND
		IvOR	bitwise OR
		IvXOR	bitwise XOR
		Specified	non-unspecified loaded value
		Unspecified	unspecified loaded value
		Fvfromint	cast integer to floating value
		Ivfromfloat	cast floating to integer value
$ident_opt_eta$::=	$_{-}:eta \ ident:eta$	type annotated optional identifier
$pattern_aux$::=		

```
ident\_opt\_eta \ ctor(\overline{pattern_i}^i)
pattern
                              loc\ annots\ pattern\_aux
ident\_or\_pattern
                              ident
                              pattern
ident
                                                                             Ott-hack, ignore
                              ident
                                                                             pure expressions
                        ::=
pexpr\_aux
                              ident
                              impl\_const
                                                                                implementation-defined constant
                              value
                              constrained (\overline{mem\_iv\_c_i, ident_i}^i)
                                                                                constrained value
                              error(string, ident)
                                                                                impl-defined static error
                              ctor(\overline{ident_i}^i)
                                                                                data constructor application
                              array\_shift(ident_1, \tau, ident_2)
                                                                                pointer array shift
                              member_shift(ident, ident, member)
                                                                                pointer struct/union member shift
                                                                                boolean not
                              not(ident)
                              ident_1 \ binop \ ident_2
                                                                                binary operations
                              (\mathtt{struct}\,ident)\{\overline{.member_i = ident_i}^i\}
                                                                                C struct expression
                              (union ident)\{.member = ident\}
                                                                                C union expression
                              memberof (ident, member, ident)
                                                                                C struct/union member access
                              name(ident_1, ..., ident_n)
                                                                                pure function call
                              assert_undef (ident, loc, UB_name)
                              bool_to_integer (ident)
```

		$\begin{aligned} &\texttt{conv_int} \ (\tau, ident) \\ &\texttt{wrapI} \ (\tau, ident) \end{aligned}$	
pexpr	::= 	$loc\ annots\ tyvar_TY\ pexpr_aux$	pure expressions with location and annotations
$tpexpr_aux$::= 	$\begin{array}{l} \text{undef } loc \ UB_name \\ \text{case } ident \ \text{of } \overline{ pattern_i \Rightarrow tpexpr_i }^i \ \text{end} \\ \text{let } ident_or_pattern = tpexpr_1 \ \text{in } tpexpr_2 \\ \text{if } ident \ \text{then } tpexpr_1 \ \text{else } tpexpr_2 \\ \text{done } ident \end{array}$	top-level pure expressions undefined behaviour pattern matching pure let pure if pure done
tpexpr	::=	$loc\ annots\ tyvar_TY\ tpexpr_aux$	pure top-level pure expressions with location and annotations
m_kill_kind	::= 	$\begin{array}{l} \operatorname{dynamic} \\ \operatorname{static} \tau \end{array}$	
bool	::=	true false	OCaml booleans
$action_aux$::= 	$\begin{array}{l} \texttt{create}(ident,\tau)sym_prefix\\ \texttt{create_readonly}(ident_1,\tau,ident_2)sym_prefix\\ \texttt{alloc}(ident_1,ident_2)sym_prefix\\ \texttt{kill}(m_kill_kind,ident)\\ \texttt{store}(bool,\tau,ident_1,ident_2,mem_order) \end{array}$	memory actions the boolean indicates whether the action is dynamic (i.e. free()) the boolean indicates whether the store is locking

```
load(\tau, ident, mem\_order)
                   rmw(\tau, ident_1, ident_2, ident_3, mem\_order_1, mem\_order_2)
                   fence (mem\_order)
                   cmp\_exch\_strong(\tau, ident_1, ident_2, ident_3, mem\_order_1, mem\_order_2)
                   cmp_exch_weak(\tau, ident_1, ident_2, ident_3, mem_order_1, mem_order_2)
                   linux_fence (linux_mem_order)
                   linux\_load(\tau, ident, linux\_mem\_order)
                   linux\_store(\tau, ident_1, ident_2, linux\_mem\_order)
                   linux_rmw(\tau, ident_1, ident_2, linux_mem_order)
action
             ::=
                   loc\ action\_aux
                                                                                                  operations involving the memory state
memop
                   ident_1 == ident_2
                                                                                                     pointer equality comparison
                   ident_1 \neq ident_2
                                                                                                     pointer inequality comparison
                   ident_1 < ident_2
                                                                                                     pointer less-than comparison
                   ident_1 > ident_2
                                                                                                     pointer greater-than comparison
                   ident_1 \leq ident_2
                                                                                                     pointer less-than comparison
                   ident_1 \geq ident_2
                                                                                                     pointer greater-than comparison
                   ident_1 -_{\tau} ident_2
                                                                                                     pointer subtraction
                   intFromPtr(\tau_1, \tau_2, ident)
                                                                                                     cast of pointer value to integer value
                   ptrFromInt (\tau_1, \tau_2, ident)
                                                                                                     cast of integer value to pointer value
                   ptrValidForDeref(\tau, ident)
                                                                                                     dereferencing validity predicate
                   ptrWellAligned (\tau, ident)
                   ptrArrayShift (ident_1, \tau, ident_2)
                   memcpy(ident_1, ident_2, ident_3)
                   memcmp(ident_1, ident_2, ident_3)
                   realloc(ident_1, ident_2, ident_3)
                                                                                                     TODO: not sure about this
                   va\_start(ident_1, ident_2)
```

```
va\_copy(ident)
                       va\_arg(ident, \tau)
                       va\_end(ident)
paction
                                                                                memory actions with polarity
                       polarity action
                                                                                   positive, sequenced by both let weak and let strong
                       action
                                                                            M
                       \neg (action)
                                                                            Μ
                                                                                   negative, only sequenced by let strong
                                                                                 (effectful) expressions
expr\_aux
                       pure (pexpr)
                      memop(memop)
                                                                                   pointer op involving memory
                                                                                   memory action
                      paction
                       skip
                       \operatorname{ccall}(\tau, ident, \overline{ident_i}^i)
                                                                                   C function call
                       pcall(name, \overline{ident_i}^i)
                                                                                   Core procedure call
                                                                                 (effectful) expressions with location and annotations
expr
                 ::=
                       loc\ annots\ expr\_aux
                                                                                top-level expressions
texpr\_aux
                       let ident\_or\_pattern = pexpr in texpr
                       let weak pattern = expr in texpr
                                                                                   weak sequencing
                       \texttt{let strong} \, ident\_or\_pattern = expr \, \texttt{in} \, texpr
                                                                                   strong sequencing
                       {	t case} \, ident \, {	t with} \, \overline{|pattern_i \Rightarrow texpr_i|^i} \, {	t end}
                                                                                   pattern matching
                       if ident then texpr_1 else texpr_2
                       bound [k](texpr)
                                                                                   ...and boundary
                       unseq(expr_1, ..., expr_n)
                                                                                   unsequenced expressions
                       nd(texpr_1, .., texpr_n)
                                                                                   nondeterministic sequencing
                       done ident
```

 ${\tt undef}\ loc\ UB_name$ $\mathtt{run}\,ident\,ident_1,\,\dots,ident_n$ run from label top-level expressions with location and annotations texpr::= $loc\ annots\ texpr_aux$ terminalsП

::=

z

OCaml arbitrary-width integer

```
\texttt{of\_mem\_int}\ ty\_mem\_int
                                                                                       Μ
                                \mathtt{of\_nat}\, nat
                                                                                       Μ
lit
                          ::=
                                ident
                                ()
                                bool
                                \mathtt{int}\,z
                                \operatorname{\mathtt{ptr}} z
bool\_op
                          ::=
                                \neg index\_term
                                index\_term_1 = index\_term_2
                                \bigwedge(index\_term_1, ..., index\_term_n)
list\_op
                          ::=
                                [index\_term_1, ..., index\_term_n]
                                index\_term^{(k)}
tuple\_op
                          ::=
                                (index\_term_1, ..., index\_term_n)
                                index\_term^{(k)}
pointer\_op
                          ::=
                                nullop
param\_op
                          ::=
                                index\_term(index\_term_1, ..., index\_term_n)
index\_term\_aux
```

::=

```
bool\_op
                        list\_op
                        pointer\_op
                        param\_op
                                                                                             OCaml type variable for base types
bt
                  ::=
                                                                                                Ott-hack, ignore
index\_term
                        index\_term\_aux\ bt
                                                                                        S
                                                                                                parentheses
                        (index\_term)
                        index\_term[index\_term_1/ident_1, ..., index\_term_n/ident_n]
                                                                                             argument types
arg
                        \Pi ident: \beta.arg
                        \forall ident: logSort.arg
                        resource → arg
                        index\_term \supset arg
                       Ι
ret
                                                                                             return types
                        \Sigma ident: \beta.ret
                        \exists ident : logSort.ret
                        \texttt{resource} \, \star ret
                        index\_term \land ret
                        Ι
\Gamma
                                                                                             computational var env
                  ::=
                        empty
```

```
\Gamma, x : \beta
Λ
                                                                                         logical var env
                       ::=
                               {\tt empty}
                               \Lambda, x
Ξ
                                                                                         constraints env
                               empty
                               Ξ, phi
formula
                               judgement
                               \begin{array}{l} \texttt{not} \ (formula) \\ ident : \beta \in \Gamma \end{array}
                               formula_1 .. formula_n
Jtype
                               \Gamma; \Lambda; \Xi \vdash value : ident, \beta, index\_term
                               \Gamma; \Lambda; \Xi \vdash pexpr\_aux : ret
judgement
                                Jtype
user\_syntax
                               tag
                               impl\_const
                               ty\_mem\_int
                               mem\_val
                               member
```

```
	au
annots
nat
n
loc
mem\_iv\_c
UB\_name
string
tyvar_{-}TY
sym\_prefix
mem\_order
linux\_mem\_order
k
\beta
binop
polarity
ident
name
ptrval
object\_value
loaded\_value
value
ctor
ident\_opt\_\beta
pattern\_aux
pattern
ident\_or\_pattern
```

ident $pexpr_aux$ pexpr $tpexpr_aux$ tpexpr m_kill_kind bool $action_aux$ actionmemoppaction $expr_aux$ expr $texpr_aux$ texprterminalszlit $bool_op$ $list_op$ $tuple_op$ $pointer_op$ $param_op$ $index_term_aux$ bt $index_term$ argretΓ

```
\begin{array}{c|c} & \Lambda \\ & \Xi \\ & formula \end{array}
```

```
\Gamma; \Lambda; \Xi \vdash value : ident, \beta, index\_term
```

```
\overline{\Gamma;\Lambda;\Xi\vdash ty\_mem\_int:y,\mathtt{integer},y=\mathtt{intof\_mem\_int}\,ty\_mem\_int}
                                                                                                                                                                                                            Val_Obj_Int
                                                                                    \overline{\Gamma;\Lambda;\Xi\vdash \mathtt{nullptr}:y,\mathtt{loc},y=\mathtt{nullop}} \quad \text{Val\_Obj\_Ptr\_Null}
                                                                                 \overline{\Gamma;\Lambda;\Xi\vdash \mathtt{funcptr}\, ident:y,\mathtt{loc},y=ident} \quad \text{Val\_Obj\_Ptr\_Func}
                                                                          \frac{}{\Gamma;\Lambda;\Xi\vdash\mathsf{concptr}\,nat:y,\mathsf{loc},y=\mathsf{ptr}\,\mathsf{of}\,\mathtt{\_nat}\,nat}\quad\mathsf{Val\_Obj\_Ptr\_Conc}
                                      \Gamma; \Lambda; \Xi \vdash loaded\_value_1 : y_1, \beta, index\_term_1 \quad .. \quad \Gamma; \Lambda; \Xi \vdash loaded\_value_n : y_n, \beta, index\_term_n
                                                                                                                                                                                                                                                                            Val_Obj_Arr
\overline{\Gamma;\Lambda;\Xi\vdash \mathtt{array}\left(loaded\_value_1, \dots, loaded\_value_n\right):y,\mathtt{integer} \rightarrow \beta, \bigwedge(index\_term_1, \dots, index\_term_n)\left[y(\mathtt{int}\,z)\,/y_1, \dots, y(\mathtt{int}\,z)\,/y_n\right]}
                                                                                                        \Gamma; \Lambda; \Xi \vdash \text{Unit} : y, \text{unit}, y = () VAL_UNIT
                                                                                                    \frac{}{\Gamma;\Lambda;\Xi\vdash \mathtt{True}:y,\mathtt{bool},y=\mathtt{true}}\quad \mathsf{VAL\_TRUE}
                                                                                                 \Gamma; \Lambda; \Xi \vdash \mathtt{False} : y, \mathtt{bool}, y = \mathtt{false} VAL_FALSE
                                           \frac{\Gamma; \Lambda; \Xi \vdash value_1 : y_1, \beta, index\_term_1 \quad .. \quad \Gamma; \Lambda; \Xi \vdash value_n : y_n, \beta, index\_term_n}{\Gamma; \Lambda; \Xi \vdash \beta[value_1, \dots, value_n] : y, [\beta], \left(\bigwedge(index\_term_1, \dots, index\_term_n)\right)[y^{(k)} / y_1, \dots, y^{(k)} / y_n]} \quad \text{VAL\_LIST}
                                                      \Gamma; \Lambda; \Xi \vdash value_1: y_1, \beta_1, index\_term_1 \quad .. \quad \Gamma; \Lambda; \Xi \vdash value_n: y_n, \beta_n, index\_term_n
                                                                                                                                                                                                                                             Val_Tuple
                                   \Gamma ; \Lambda ; \Xi \vdash \overline{\left(value_1, \ldots, value_n\right) : y, (\beta_1, \ldots, \beta_n), \bigwedge(index\_term_1, \ldots, index\_term_n) \left[y^{(k)} \left/ y_1, \ldots, y^{(k)} \left/ y_n \right]\right]}
\Gamma; \Lambda; \Xi \vdash pexpr\_aux : ret
                                                                                                               \frac{x:\beta\in\Gamma}{\Gamma;\Lambda;\Xi\vdash x:\Sigma\,y:\beta.\mathsf{I}}\quad\mathsf{PEXPR\_VAR}
```

 $\frac{\Gamma; \Lambda; \Xi \vdash value: y, \beta, index_term}{\Gamma; \Lambda; \Xi \vdash value: \Sigma \ y: \beta. index_term \land \mathtt{I}} \quad \mathsf{PExpr_Val}$

 $\frac{x : \mathtt{bool} \, \in \, \Gamma}{\Gamma; \Lambda; \Xi \vdash \mathtt{not} \, (x) : \Sigma \, y : \mathtt{bool}. y = (\neg \, x \,) \, \wedge \mathbf{I}} \quad \mathsf{PEXPR_NOT}$

Definition rules: 13 good 0 bad Definition rule clauses: 19 good 0 bad