

<i>ident, x, y, y_p, v, v_p, -</i>	v is for values, subscript p is for pointers, rest are identifiers
<i>impl_const</i>	implementation-defined constant
<i>mem_int</i>	memory integer value
<i>member</i>	C struct/union member name
<i>annots</i>	annotations
<i>nat</i>	OCaml arbitrary-width natural number
<i>n, i</i>	index variables
<i>loc</i>	OCaml type for C source
<i>mem_iv_c</i>	OCaml type for memory constraints on integer values
<i>UB_name</i>	undefined behaviour
<i>string</i>	OCaml string
<i>tyvar_TY</i>	OCaml type variable for types
	OCaml type for symbol prefix
<i>mem_order, -</i>	OCaml type for memory order
<i>linux_mem_order</i>	OCaml type for Linux memory order
<i>k</i>	OCaml fixed-width integer
<i>bt,</i>	Ott-hack, ignore

$Sctypes_t, \tau$	$::=$ τ^*	C type pointer to type τ
tag	$::=$ $ident$	OCaml type for struct/union tag
β	$::=$ unit bool integer real loc array β $[\beta]$ $(\beta_1, \dots, \beta_n)$ struct tag $\{\beta\}$ opt (β) $\beta_1, \dots, \beta_n \rightarrow \beta$ of_ctype (τ) M	base types unit boolean integer rational numbers? location array list tuple struct set option parameter types of a C type
$binop$	$::=$ + - * / rem_t rem_f ^ =	binary operators addition subtraction multiplication division modulus remainder exponentiation equality, defined both for integer and C types

		>	greater than
		<	less than
		>=	greater than or equal to
		<=	less than or equal to
		&\	conjunction
		\/	disjunction
<i>polarity</i>	::=		memory action polarities
		Pos	sequenced by let weak and let strong
		Neg	only sequenced by let strong
<i>name</i>	::=		
		<i>ident</i>	Core identifier
		<i>impl_const</i>	implementation-defined constant
<i>mem_ptr</i>	::=		pointer values
		nullptr	null pointer
		funcptr <i>ident</i>	function pointer
		concptr <i>nat</i>	concrete pointer
<i>mem_val</i>	::=		memory value
		int <i>mem_int</i>	
		<i>mem_ptr</i>	
		array ($\overline{mem_val_i}^i$)	
		(struct <i>ident</i>) { $\overline{member_i = mem_val_i}^i$ }	
		union <i>ident member</i>	
<i>object_value</i>	::=		C object values (inhabitants of object types), which can be read/stored
		<i>mem_int</i>	integer value
		<i>mem_ptr</i>	pointer value

		$\text{array}(\overline{\text{loaded_value}_i}^i)$	C array value
		$(\text{struct } ident)\{\overline{\text{member}_i : \tau_i = \text{mem_val}_i}^i\}$	C struct value
		$(\text{union } ident)\{\text{member} = \text{mem_val}\}$	C union value
<i>loaded_value</i>	::=		potentially unspecified C object values
		<i>specified object_value</i>	specified loaded value
<i>value</i>	::=		Core values
		<i>object_value</i>	C object value
		<i>loaded_value</i>	loaded C object value
		Unit	unit
		True	boolean true
		False	boolean false
		$\beta[\text{value}_1, \dots, \text{value}_i]$	list
		$(\text{value}_1, \dots, \text{value}_i)$	tuple
<i>ctor</i>	::=		data constructors
		Nil β	empty list
		Cons	list cons
		Tuple	tuple
		Array	C array
		Ivmax	max integer value
		Ivmin	min integer value
		Ivsizeof	sizeof value
		Ivalignof	alignof value
		IvCOMPL	bitwise complement
		IvAND	bitwise AND
		IvOR	bitwise OR
		IvXOR	bitwise XOR
		Specified	non-unspecified loaded value

		Fvfromint	cast integer to floating value
		Ivfromfloat	cast floating to integer value
<i>ident_opt_β</i>	::=		type annotated optional identifier
		<i>_</i> : β	
		<i>ident</i> : β	
<i>pattern_aux</i>	::=		
		<i>ident_opt_β</i>	
		<i>ctor</i> ($\overline{pattern_i}^i$)	
<i>pattern</i>	::=		
		<i>loc annots pattern_aux</i>	
<i>ident_or_pattern</i>	::=		
		<i>ident</i>	
		<i>pattern</i>	
<i>pexpr_aux</i>	::=		pure expressions
		<i>ident</i>	[V]
		<i>impl_const</i>	[V] implementation-defined constant
		<i>value</i>	[V]
		constrained ($\overline{mem_iv_c_i, ident_i}^i$)	[V] constrained value
		error (<i>string</i> , <i>ident</i>)	[V] impl-defined static error
		<i>ctor</i> ($\overline{ident_i}^i$)	data constructor application
		array_shift (<i>ident</i> ₁ , τ, <i>ident</i> ₂)	pointer array shift
		member_shift (<i>ident</i> , <i>ident</i> , <i>member</i>)	pointer struct/union member shift
		not (<i>ident</i>)	boolean not
		<i>ident</i> ₁ <i>binop</i> <i>ident</i> ₂	binary operations
		(struct <i>ident</i>){ $\overline{.member_i = ident_i}^i$ }	[V] C struct expression

	<code>(union ident){.member = ident}</code> <code>memberof (ident, member, ident)</code> <code>name(ident₁, .., ident_n)</code> <code>assert_undef (ident, loc, UB_name)</code> <code>bool_to_integer (ident)</code> <code>conv_int (τ, ident)</code> <code>wrapI (τ, ident)</code>	[V] C union expression C struct/union member access pure function call
<i>pexpr</i>	::= <i>loc annots tyvar_TY pexpr_aux</i>	pure expressions with location and annotations [V]
<i>tpexpr_aux</i>	::= <code>undef loc UB_name</code> <code>case ident of pattern_i ⇒ tpexpr_i end</code> <code>let ident_or_pattern = pexpr in tpexpr</code> <code>if ident then tpexpr₁ else tpexpr₂</code> <code>done ident</code>	top-level pure expressions [V] undefined behaviour pattern matching pure let pure if [V] pure done
<i>tpexpr</i>	::= <i>loc annots tyvar_TY tpexpr_aux</i> $[C/C']tpexpr$	pure top-level pure expressions with location and annotations [V] M
<i>m_kill_kind</i>	::= <code>dynamic</code> <code>static τ</code>	
<i>bool, -</i>	::= <code>true</code> <code>false</code>	OCaml booleans

<i>action_aux</i>	$::=$ <code>create</code> (<i>ident</i> , τ) <code>create_readonly</code> (<i>ident</i> ₁ , τ , <i>ident</i> ₂) <code>alloc</code> (<i>ident</i> ₁ , <i>ident</i> ₂) <code>kill</code> (<i>m_kill_kind</i> , <i>ident</i>) <code>store</code> (<i>bool</i> , τ , <i>ident</i> ₁ , <i>ident</i> ₂ , <i>mem_order</i>) <code>load</code> (τ , <i>ident</i> , <i>mem_order</i>) <code>rmw</code> (τ , <i>ident</i> ₁ , <i>ident</i> ₂ , <i>ident</i> ₃ , <i>mem_order</i> ₁ , <i>mem_order</i> ₂) <code>fence</code> (<i>mem_order</i>) <code>cmp_exch_strong</code> (τ , <i>ident</i> ₁ , <i>ident</i> ₂ , <i>ident</i> ₃ , <i>mem_order</i> ₁ , <i>mem_order</i> ₂) <code>cmp_exch_weak</code> (τ , <i>ident</i> ₁ , <i>ident</i> ₂ , <i>ident</i> ₃ , <i>mem_order</i> ₁ , <i>mem_order</i> ₂) <code>linux_fence</code> (<i>linux_mem_order</i>) <code>linux_load</code> (τ , <i>ident</i> , <i>linux_mem_order</i>) <code>linux_store</code> (τ , <i>ident</i> ₁ , <i>ident</i> ₂ , <i>linux_mem_order</i>) <code>linux_rmw</code> (τ , <i>ident</i> ₁ , <i>ident</i> ₂ , <i>linux_mem_order</i>)	memory actions true means store is locking
<i>action</i>	$::=$ <code>loc</code> <i>action_aux</i>	
<i>memop</i>	$::=$ <i>ident</i> ₁ == <i>ident</i> ₂ <i>ident</i> ₁ ≠ <i>ident</i> ₂ <i>ident</i> ₁ < <i>ident</i> ₂ <i>ident</i> ₁ > <i>ident</i> ₂ <i>ident</i> ₁ ≤ <i>ident</i> ₂ <i>ident</i> ₁ ≥ <i>ident</i> ₂ <i>ident</i> ₁ − _τ <i>ident</i> ₂ <code>intFromPtr</code> (τ_1 , τ_2 , <i>ident</i>) <code>ptrFromInt</code> (τ_1 , τ_2 , <i>ident</i>) <code>ptrValidForDeref</code> (τ , <i>ident</i>)	operations involving the memory state pointer equality comparison pointer inequality comparison pointer less-than comparison pointer greater-than comparison pointer less-than comparison pointer greater-than comparison pointer subtraction cast of pointer value to integer value cast of integer value to pointer value dereferencing validity predicate

		<code>ptrWellAligned</code> ($\tau, ident$)	
		<code>ptrArrayShift</code> ($ident_1, \tau, ident_2$)	
		<code>memcpy</code> ($ident_1, ident_2, ident_3$)	
		<code>memcmp</code> ($ident_1, ident_2, ident_3$)	
		<code>realloc</code> ($ident_1, ident_2, ident_3$)	
		<code>va_start</code> ($ident_1, ident_2$)	
		<code>va_copy</code> ($ident$)	
		<code>va_arg</code> ($ident, \tau$)	
		<code>va_end</code> ($ident$)	
<i>paction</i>	::=		memory actions with polarity
		<i>action</i>	M positive, sequenced by both let weak and let strong
		$\neg (action)$	M negative, only sequenced by let strong
<i>expr_aux</i>	::=		(effectful) expressions
		<code>pure</code> (<i>pexpr</i>)	[V] pure expression
		<code>memop</code> (<i>memop</i>)	pointer op involving memory
		<i>paction</i>	memory action
		<code>skip</code>	[V] skip
		<code>ccall</code> ($\tau, ident, \overline{ident_i^i}$)	C function call
		<code>pcall</code> (<i>name</i> , $\overline{ident_i^i}$)	procedure call
<i>expr</i>	::=		(effectful) expressions with location and annotations
		<i>loc annots expr_aux</i>	[V]
<i>texpr_aux</i>	::=		top-level expressions
		<code>let</code> <i>ident_or_pattern</i> = <i>pexpr</i> in <i>texpr</i>	
		<code>let weak</code> <i>pattern</i> = <i>expr</i> in <i>texpr</i>	weak sequencing
		<code>let strong</code> <i>ident_or_pattern</i> = <i>expr</i> in <i>texpr</i>	strong sequencing
		<code>case</code> <i>ident</i> with $\overline{pattern_i \Rightarrow texpr_i^i}$ end	pattern matching

		if <i>ident</i> then <i>texpr</i> ₁ else <i>texpr</i> ₂	conditional
		unseq (<i>expr</i> ₁ , .., <i>expr</i> _{<i>n</i>})	[V] unsequenced expressions
		nd (<i>texpr</i> ₁ , .., <i>texpr</i> _{<i>n</i>})	nondeterministic sequencing
		done <i>ident</i>	[V] end of top-level expression
		undef <i>loc UB_name</i>	[V] undefined behaviour
		run <i>ident ident</i> ₁ , .., <i>ident</i> _{<i>n</i>}	run from label
<i>texpr</i>	::=		top-level expressions with location and annotations
		<i>loc annots texpr_aux</i>	[V]
<i>terminals</i>	::=		
		λ	
		→	
		→	
		↗	
		⇒	
		⇐	
		⊢	
		∈	
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		+ _{ptr}	
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		*	
z	::=		OCaml arbitrary-width integer
		of_mem_int(<i>mem_int</i>)	M
		of_nat(<i>nat</i>)	M
		of_ctype(τ)	M size of a C type
		ptr_size	M size of a pointer
\mathbb{Q}	::=		OCaml type for rational numbers
		$\frac{k_1}{k_2}$	
<i>lit</i>	::=		
		<i>ident</i>	
		()	
		<i>bool</i>	
		int <i>z</i>	
		\mathbb{Q}	
		ptr <i>z</i>	
<i>bool_op</i>	::=		
		\neg <i>term</i>	

		$term_1 = term_2$
		$\bigwedge(\overline{term_i}^i)$
$arith_op$	$::=$	
		$term_1 \times term_2$
$list_op$	$::=$	
		nil
		$term_1 :: term_2$
		$[term_1, .., term_n]$
		$term^{(k)}$
$tuple_op$	$::=$	
		$(term_1, .., term_n)$
		$term^{(k)}$
$pointer_op$	$::=$	
		nullop
		$term_1 +_{\text{ptr}} term_2$
$option_op$	$::=$	
		none BT_t
		some $term$
$array_op$	$::=$	
		$term[\text{int } z]$
$param_op$	$::=$	
		$term(term_1, .., term_n)$

<i>struct_op</i>	::=		<i>term.member</i>	
<i>ct_pred</i>	::=		representable ($\tau, term$)	
			alignedI ($term_1, term_2$)	
<i>term_aux</i>	::=		<i>arith_op</i>	
			<i>bool_op</i>	
			<i>tuple_op</i>	
			<i>struct_op</i>	
			<i>pointer_op</i>	
			<i>list_op</i>	
			<i>array_op</i>	
			<i>ct_pred</i>	
			<i>option_op</i>	
			<i>param_op</i>	
<i>term</i>	::=		<i>lit</i>	
			<i>term_aux</i> <i>bt</i>	
			(<i>term</i>)	S parentheses
			[<i>term</i> ₁ / <i>ident</i>] <i>term</i> ₂	M
<i>point</i>	::=			points-to predicate
			$IT_t_1 \mapsto_{z, IT_t_2} IT_t_3$	
<i>predicate_name</i>	::=			names of predicates
			<i>Sctypes_t</i>	

		$string$	
$predicate$	$::=$	$predicate_name(IT_t_1, IT_t_list_1 \mapsto IT_t_list_2)$	arbitrary predicate
$resource$	$::=$	$point$ $predicate$	
arg	$::=$	$\Pi ident : \beta.arg$ $\forall ident : \beta.arg$ $resource \multimap arg$ $term \supset arg$ I	argument types
$ret, -$	$::=$	$\Sigma ident : \beta. ret$ $\exists ident : \beta. ret$ $resource \star ret$ $term \wedge ret$ I	return types
\mathcal{C}	$::=$	\cdot $\mathcal{C}, ident : BT_t$ $\mathcal{C}, \mathcal{C}'$ $fresh(\mathcal{C})$	computational var env
			M identical context except with fresh variable names
\mathcal{L}	$::=$		logical var env

	$\begin{array}{ l} \cdot \\ \mathcal{L}, \text{ident} \end{array}$	
Φ	$\begin{array}{ l} ::= \\ \cdot \\ \Phi, \text{term} \\ \Phi, \text{ret} \end{array}$	<p>constraints env</p> <p>temporary hack</p>
\mathcal{R}	$\begin{array}{ l} ::= \\ \cdot \\ \mathcal{R}, \text{resource} \end{array}$	resources env
<i>formula</i>	$\begin{array}{ l} ::= \\ \text{judgement} \\ \text{smt}(\Phi \Rightarrow \text{ret}) \\ \text{ident} : \beta \in \mathcal{C} \\ \text{ident} : \text{struct tag} \ \& \ \overline{\text{member}_i : \tau_i}^i \in \text{Globals} \\ \overline{\mathcal{C}_i; \mathcal{L}_i; \Phi_i \vdash \text{mem_val}_i \Rightarrow \text{mem } y_i, \beta_i, \text{term}_i}^i \\ \overline{\mathcal{C}_i; \mathcal{L}_i; \Phi_i \vdash \text{value}_i \Rightarrow y_i, \beta_i, \text{term}_i}^i \\ \overline{\mathcal{C}_i; \mathcal{L}_i; \Phi_i \vdash \text{pexpr_aux}_i \Rightarrow \text{ret}_i}^i \\ \overline{\text{pattern}_i : \beta_i \rightsquigarrow \mathcal{C}_i}^i \\ \overline{\mathcal{C}_i; \mathcal{L}_i; \Phi_i \vdash \text{tpexpr}_i \Leftarrow \text{ret}_i}^i \end{array}$	<p>theorem to be proved: <i>ret</i> only consists of logical constraints</p>
<i>mem_value_jtype</i>	$\begin{array}{ l} ::= \\ \mathcal{C}; \mathcal{L}; \Phi \vdash \text{mem_val} \Rightarrow \text{mem } y, \beta, \text{term} \end{array}$	
<i>value_jtype</i>	$\begin{array}{ l} ::= \\ \mathcal{C}; \mathcal{L}; \Phi \vdash \text{object_value} \Rightarrow \text{obj ident}, \beta, \text{term} \\ \mathcal{C}; \mathcal{L}; \Phi \vdash \text{value} \Rightarrow \text{ident}, \beta, \text{term} \end{array}$	

$pexpr_jtype$	$::=$ $ \quad \mathcal{C}; \mathcal{L}; \Phi \vdash pexpr_aux \Rightarrow ret$
$pattern_jtype$	$::=$ $ \quad pattern : \beta \rightsquigarrow \mathcal{C}$ $ \quad ident_or_pattern : \beta \rightsquigarrow \mathcal{C}$
$texpr_jtype$	$::=$ $ \quad \mathcal{C}; \mathcal{L}; \Phi \vdash pexpr \Rightarrow ret$ $ \quad \mathcal{C}; \mathcal{L}; \Phi \vdash texpr \Leftarrow ret$ $ \quad \mathcal{C}; \mathcal{L}; \Phi \vdash texpr_aux \Leftarrow ret$
$expr_jtype$	$::=$ $ \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash action_aux \Rightarrow ret$ $ \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash expr_aux \Rightarrow ret$
$judgement$	$::=$ $ \quad mem_value_jtype$ $ \quad value_jtype$ $ \quad pexpr_jtype$ $ \quad pattern_jtype$ $ \quad texpr_jtype$ $ \quad expr_jtype$
$user_syntax$	$::=$ $ \quad ident$ $ \quad impl_const$ $ \quad mem_int$ $ \quad member$ $ \quad annots$

nat
n
loc
mem_iv_c
UB_name
string
tyvar_TY

mem_order
linux_mem_order
k
bt
Sctypes_t
tag
 β
binop
polarity
ident
ident
name
mem_ptr
mem_val
 τ
object_value
loaded_value
 β
value
ctor
ident_opt_β

- | *pattern_aux*
- | *pattern*
- | *ident_or_pattern*
- | *ident*
- | τ
- | *pexpr_aux*
- | *pexpr*
- | *tpexpr_aux*
- | *tpexpr*
- | *m_kill_kind*
- | *bool*
- | *action_aux*
- | *action*
- | *memop*
- | *paction*
- | *expr_aux*
- | *expr*
- | *texpr_aux*
- | *texpr*
- | *terminals*
- | *z*
- | \mathbb{Q}
- | *lit*
- | *bool_op*
- | *arith_op*
- | *list_op*
- | *tuple_op*
- | *pointer_op*
- | *BT_t*

$option_op$
 $array_op$
 $param_op$
 $struct_op$
 ct_pred
 $term_aux$
 $term$
 IT_t
 IT_t_list
 $point$
 $predicate_name$
 $predicate$
 $resource$
 arg
 ret
 \mathcal{C}
 \mathcal{L}
 Φ
 \mathcal{R}
 $formula$

$\mathcal{C}; \mathcal{L}; \Phi \vdash mem_val \Rightarrow \mathbf{mem}\ y, \beta, term$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathbf{int}\ mem_int \Rightarrow \mathbf{mem}\ y, \mathbf{integer}, y = \mathbf{int}\ of_mem_int(mem_int)} \quad \text{VAL_OBJ_MEM_INT}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathbf{nullptr} \Rightarrow \mathbf{mem}\ y, \mathbf{loc}, y = \mathbf{nullop}} \quad \text{VAL_OBJ_MEM_PTR_NULL}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathbf{funcptr}\ ident \Rightarrow \mathbf{mem}\ y, \mathbf{loc}, y = ident} \quad \text{VAL_OBJ_MEM_PTR_FUNC}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathbf{concptr}\ nat \Rightarrow \mathbf{mem}\ y, \mathbf{loc}, y = \mathbf{ptr}\ of_nat(nat)} \quad \text{VAL_OBJ_MEM_PTR_CONC}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{mem_val}_i \Rightarrow \text{mem } y_i, \beta, \text{term}_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{array}(\overline{\text{mem_val}_i^i}) \Rightarrow \text{mem } y, \text{array } \beta, \bigwedge(\overline{[y[\text{int } z_i] / y_i] \text{term}_i^i})} \quad \text{VAL_OBJ_MEM_ARR}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{mem_val}_i \Rightarrow \text{mem } y_i, \beta_i, \text{term}_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash (\text{struct tag})\{\overline{\text{member}_i = \text{mem_val}_i^i}\} \Rightarrow \text{mem } y, \text{struct tag}, \bigwedge(\overline{[y.\text{member}_i / y_i] \text{term}_i^i})} \quad \text{VAL_OBJ_MEM_STRUCT}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{object_value} \Rightarrow \text{obj ident}, \beta, \text{term}}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{mem_int} \Rightarrow \text{obj } y, \text{integer}, y = \text{int of_mem_int}(\text{mem_int})} \quad \text{VAL_OBJ_INT}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{nullptr} \Rightarrow \text{obj } y, \text{loc}, y = \text{nullopt}} \quad \text{VAL_OBJ_PTR_NULL}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{funcptr ident} \Rightarrow \text{obj } y, \text{loc}, y = \text{ident}} \quad \text{VAL_OBJ_PTR_FUNC}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{concptr nat} \Rightarrow \text{obj } y, \text{loc}, y = \text{ptr of_nat}(\text{nat})} \quad \text{VAL_OBJ_PTR_CONC}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{loaded_value}_i \Rightarrow y_i, \beta, \text{term}_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{array}(\overline{\text{loaded_value}_i^i}) \Rightarrow \text{obj } y, \text{array } \beta, \bigwedge(\overline{[y[\text{int } z_i] / y_i] \text{term}_i^i})} \quad \text{VAL_OBJ_ARR}$$

$$\frac{\overline{\text{ident} : \text{struct tag} \ \& \ \overline{\text{member}_i : \tau_i^i \in \text{Globals}}}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{mem_val}_i \Rightarrow \text{mem } y_i, \beta_i, \text{term}_i^i} \quad \text{VAL_OBJ_STRUCT}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash (\text{struct tag})\{\overline{\text{member}_i : \tau_i = \text{mem_val}_i^i}\} \Rightarrow \text{obj } y, \text{struct tag}, \bigwedge(\overline{[y.\text{member}_i / y_i] \text{term}_i^i})}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{value} \Rightarrow \text{ident}, \beta, \text{term}}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{object_value} \Rightarrow \text{obj } y, \beta, \text{term}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{object_value} \Rightarrow y, \beta, \text{term}} \quad \text{VAL_OBJ}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{object_value} \Rightarrow \text{obj } y, \beta, \text{term}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{specified_object_value} \Rightarrow y, \beta, \text{term}} \quad \text{VAL_LOADED}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Unit} \Rightarrow y, \text{unit}, y = ()} \quad \text{VAL_UNIT}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{True} \Rightarrow y, \text{bool}, y = \text{true}} \quad \text{VAL_TRUE}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{False} \Rightarrow y, \text{bool}, y = \text{false}} \quad \text{VAL_FALSE}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{value}_1 \Rightarrow y_1, \beta, \text{term}_1 \dots \mathcal{C}; \mathcal{L}; \Phi \vdash \text{value}_n \Rightarrow y_n, \beta, \text{term}_n}{\mathcal{C}; \mathcal{L}; \Phi \vdash \beta[\text{value}_1, \dots, \text{value}_n] \Rightarrow y, [\beta], \bigwedge([y^{(k_1)} / y_1] \text{term}_1, \dots, [y^{(k_n)} / y_n] \text{term}_n)} \quad \text{VAL_LIST}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{value}_1 \Rightarrow y_1, \beta_1, \text{term}_1 \dots \mathcal{C}; \mathcal{L}; \Phi \vdash \text{value}_n \Rightarrow y_n, \beta_n, \text{term}_n}{\mathcal{C}; \mathcal{L}; \Phi \vdash (\text{value}_1, \dots, \text{value}_n) \Rightarrow y, (\beta_1, \dots, \beta_n), \bigwedge([y^{(k_1)} / y_1] \text{term}_1, \dots, [y^{(k_n)} / y_n] \text{term}_n)} \quad \text{VAL_TUPLE}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pexpr_aux} \Rightarrow \text{ret}}$$

$$\frac{x : \beta \in \mathcal{C}}{\mathcal{C}; \mathcal{L}; \Phi \vdash x \Rightarrow \Sigma y : \beta. y = x \wedge \mathbf{I}} \quad \text{PEXPR_AUX_VAR}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{value} \Rightarrow y, \beta, \text{term}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{value} \Rightarrow \Sigma y : \beta. \text{term} \wedge \mathbf{I}} \quad \text{PEXPR_AUX_VAL}$$

$$\frac{\text{smt}(\Phi \Rightarrow \text{false} \wedge \mathbf{I})}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{error}(string, v) \Rightarrow \text{ret}} \quad \text{PEXPR_AUX_ERROR}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Nil } \beta() \Rightarrow \Sigma y: [\beta]. y = \text{nil} \wedge \mathbf{I}} \quad \text{PEXPR_AUX_CTOR_NIL}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash v_1 \Rightarrow \Sigma _ : \beta. _ \\ \mathcal{C}; \mathcal{L}; \Phi \vdash v_2 \Rightarrow \Sigma _ : [\beta]. _ \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Cons}(v_1, v_2) \Rightarrow \Sigma y: [\beta]. y = v_1 :: v_2 \wedge \mathbf{I}} \quad \text{PEXPR_AUX_CTOR_CONS}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash v_1 \Rightarrow \Sigma _ : \beta_1. \dots \mathcal{C}; \mathcal{L}; \Phi \vdash v_n \Rightarrow \Sigma _ : \beta_n. _}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Tuple}(v_1, \dots, v_n) \Rightarrow \Sigma y: (\beta_1, \dots, \beta_n). y = (v_1, \dots, v_n) \wedge \mathbf{I}} \quad \text{PEXPR_AUX_CTOR_TUPLE}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash v_1 \Rightarrow \Sigma _ : \beta. \dots \mathcal{C}; \mathcal{L}; \Phi \vdash v_n \Rightarrow \Sigma _ : \beta. _}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Array}(v_1, \dots, v_n) \Rightarrow \Sigma y: \text{array } \beta. \bigwedge (y[\text{int } z_1] = v_1, \dots, y[\text{int } z_n] = v_n) \wedge \mathbf{I}} \quad \text{PEXPR_AUX_CTOR_ARRAY}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash v \Rightarrow \Sigma _ : \beta. _}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Specified}(v) \Rightarrow \Sigma y: \beta. y = v \wedge \mathbf{I}} \quad \text{PEXPR_AUX_CTOR_SPECIFIED}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash v_1 \Rightarrow \Sigma _ : \text{loc}. _ \\ \mathcal{C}; \mathcal{L}; \Phi \vdash v_2 \Rightarrow \Sigma _ : \text{integer}. _ \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{array_shift}(v_1, \tau, v_2) \Rightarrow \Sigma y: \text{loc}. y = v_1 +_{\text{ptr}} v_2 \times \text{int of_ctype}(\tau) \wedge \mathbf{I}} \quad \text{PEXPR_AUX_ARRAY_SHIFT}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{not}(v) \Rightarrow \Sigma y: \text{bool}. y = (\neg v) \wedge \mathbf{I}} \quad \text{PEXPR_AUX_NOT}$$

$$\boxed{\text{pattern} : \beta \rightsquigarrow \mathcal{C}}$$

$$\boxed{\text{ident_or_pattern} : \beta \rightsquigarrow \mathcal{C}}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pexpr} \Rightarrow \text{ret}}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pexpr_aux \Rightarrow ret}{\mathcal{C}; \mathcal{L}; \Phi \vdash loc \text{ annots } tyvar_TY \ pexpr_aux \Rightarrow ret} \quad \text{PEXPR_AUX}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash texpr \Leftarrow ret}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash texpr_aux \Leftarrow ret}{\mathcal{C}; \mathcal{L}; \Phi \vdash loc \text{ annots } tyvar_TY \ texpr_aux \Leftarrow ret} \quad \text{TPEXPR_AUX}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash texpr_aux \Leftarrow ret}$$

$$\frac{\text{smt}(\Phi \Rightarrow \text{false} \wedge \text{I})}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{undef } loc \ UB_name \Leftarrow ret} \quad \text{TPEXPR_AUX_UNDEF}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash v \Rightarrow \Sigma_:\text{bool}. _ \\ \mathcal{C}; \mathcal{L}; \Phi, v = \text{true} \vdash texpr_1 \Leftarrow ret \\ \mathcal{C}; \mathcal{L}; \Phi, v = \text{false} \vdash texpr_2 \Leftarrow ret \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{if } v \text{ then } texpr_1 \text{ else } texpr_2 \Leftarrow ret} \quad \text{TPEXPR_AUX_IF}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash v \Rightarrow \Sigma_:\beta. ret' \\ \text{smt}(\Phi, ret' \Rightarrow ret) \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{done } v \Leftarrow \Sigma y:\beta. ret} \quad \text{TPEXPR_AUX_DONE}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pexpr \Rightarrow \Sigma y:\beta. ret' \\ ident_or_pattern : \beta \rightsquigarrow \mathcal{C}' \\ \mathcal{C}, \text{fresh}(\mathcal{C}'); \mathcal{L}; \Phi \vdash [\text{fresh}(\mathcal{C}')/\mathcal{C}'] texpr \Leftarrow ret \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{let } ident_or_pattern = pexpr \text{ in } texpr \Leftarrow ret} \quad \text{TPEXPR_AUX_LET}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash v \Rightarrow \Sigma_{-}:\beta. _ \\
\hline
pattern_i : \beta \rightsquigarrow \mathcal{C}_i^i \\
\hline
\mathcal{C}, \text{fresh}(\mathcal{C}_i); \mathcal{L}; \Phi \vdash [\text{fresh}(\mathcal{C}_i)/\mathcal{C}_i] tpepr_i \Leftarrow ret^i \\
\hline
\mathcal{C}; \mathcal{L}; \Phi \vdash \text{case } v \text{ of } \overline{pattern_i \Rightarrow tpepr_i^i} \text{ end} \Leftarrow ret
\end{array} \quad \text{TPEXPR_AUX_CASE}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash action_aux \Rightarrow ret}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash v \Rightarrow \Sigma_{-}:\text{integer}. _ \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \text{create}(v, \tau) \Rightarrow \Sigma_{y_p}:\text{loc}. \exists v':\text{of_ctype}(\tau). \text{representable}(\tau*, y_p) \wedge \text{alignedI}(v, y_p) \wedge \tau(y_p, []) \mapsto [v', \text{false}] \star \text{I}
\end{array} \quad \text{ACTION_CREATE}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash v_p \Rightarrow \Sigma_{-}:\text{loc}. _ \\
\mathcal{C}; \mathcal{L}; \Phi \vdash v_2 \Rightarrow \Sigma_{-}:\text{of_ctype}(\tau). _ \\
\text{smt}(\Phi \Rightarrow \text{representable}(\tau, v_2) \wedge \text{I}) \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \cdot, \tau(v_p, []) \mapsto [v_1, _] \vdash \text{store}(_, \tau, v_p, v_2, _) \Rightarrow \Sigma_{-}:\text{unit}. \tau(v_p, []) \mapsto [v_2, \text{true}] \star \text{I}
\end{array} \quad \text{ACTION_STORE}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash v_p \Rightarrow \Sigma_{-}:\text{loc}. _ \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \cdot, \tau(v_p, []) \mapsto [v_1, _] \vdash \text{kill}(\text{static } \tau, v_p) \Rightarrow \Sigma_{-}:\text{unit}. \text{I}
\end{array} \quad \text{ACTION_KILL_STATIC}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash expr_aux \Rightarrow ret}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pexpr \Rightarrow ret \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \text{pure}(pexpr) \Rightarrow ret
\end{array} \quad \text{EXPR_AUX_PURE}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash action_aux \Rightarrow ret \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash loc\ action_aux \Rightarrow ret
\end{array} \quad \text{EXPR_AUX_ACTION}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash action_aux \Rightarrow ret \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \neg (loc\ action_aux) \Rightarrow ret
\end{array} \quad \text{EXPR_AUX_NEG_ACTION}$$

Definition rules: 42 good 0 bad
Definition rule clauses: 83 good 0 bad