

<i>ident, x, y, y_p, y_f, -, abbrev, r</i>	subscripts: p for pointers, f for functions
<i>n, i, j</i>	index variables
<i>impl_const</i>	implementation-defined constant
<i>member</i>	C struct/union member name
	Ott-hack, ignore (annotations)
<i>nat</i>	OCaml arbitrary-width natural number
<i>mem_ptr</i>	abstract pointer value
<i>mem_val</i>	abstract memory value
	Ott-hack, ignore (locations)
<i>mem_iv_c</i>	OCaml type for memory constraints on integer values
<i>UB_name</i>	undefined behaviour
<i>string</i>	OCaml string
	Ott-hack, ignore (OCaml type variable TY)
	Ott-hack, ignore (OCaml Symbol.prefix)
<i>mem_order, _</i>	OCaml type for memory order
<i>linux_mem_order</i>	OCaml type for Linux memory order
	Ott-hack, ignore (OCaml type variable bt)

$Stypes_t, \tau$	$::=$	C type
	$\tau*$	pointer to type τ
tag	$::=$	OCaml type for struct/union tag
	$ident$	
$\beta, -$	$::=$	base types
	unit	unit
	bool	boolean
	integer	integer
	real	rational numbers?
	loc	location
	array β	array
	list β	list
	$\overline{\beta_i}^i$	tuple
	struct tag	struct
	set β	set
	opt (β)	option
	$\beta \rightarrow \beta'$	parameter types
	β_τ M	of a C type
$binop$	$::=$	binary operators
	+	addition
	-	subtraction
	*	multiplication
	/	division
	rem_t	modulus
	rem_f	remainder
	^	exponentiation
	=	equality, defined both for integer and C types

		>	greater than
		<	less than
		>=	greater than or equal to
		<=	less than or equal to
		/\	conjuction
		\/	disjunction
<i>binop_{arith}</i>	::=		arithhmentic binary operators
		+	
		-	
		*	
		/	
		rem_t	
		rem_f	
		^	
<i>binop_{rel}</i>	::=		relational binary operators
		=	
		>	
		<	
		>=	
		<=	
<i>binop_{bool}</i>	::=		boolean binary operators
		/\	
		\/	
<i>mem_int</i>	::=		memory integer value
		1	M
		0	M

<i>object_value</i>	$::=$ <i>mem_int</i> <i>mem_ptr</i> array ($\overline{loaded_value_i}^i$) (struct <i>ident</i>) { $\overline{member_i:\tau_i = mem_val_i}^i$ } (union <i>ident</i>) { <i>.member</i> = <i>mem_val</i> }	C object values (inhabitants of object types), which can be read/stored integer value pointer value C array value C struct value C union value
<i>loaded_value</i>	$::=$ specified <i>object_value</i>	potentially unspecified C object values specified loaded value
<i>value</i>	$::=$ <i>object_value</i> <i>loaded_value</i> Unit True False $\beta[\overline{value_i}^i]$ ($\overline{value_i}^i$)	Core values C object value loaded C object value unit boolean true boolean false list tuple
<i>bool_value</i>	$::=$ True False	Core booleans boolean true boolean false
<i>ctor_val</i>	$::=$ Nil β Cons Tuple Array Specified	data constructors empty list list cons tuple C array non-unspecified loaded value

<i>ctor_expr</i>	::= <ul style="list-style-type: none"> <i>Ivmax</i> <i>Ivmin</i> <i>Ivsizeof</i> <i>Ivalignof</i> <i>IvCOMPL</i> <i>IvAND</i> <i>IvOR</i> <i>IvXOR</i> <i>Fvfromint</i> <i>Ivfromfloat</i> 	data constructors <ul style="list-style-type: none"> max integer value min integer value sizeof value alignof value bitwise complement bitwise AND bitwise OR bitwise XOR cast integer to floating value cast floating to integer value
<i>name</i>	::= <ul style="list-style-type: none"> <i>ident</i> <i>impl_const</i> 	<ul style="list-style-type: none"> Core identifier implementation-defined constant
<i>pval</i>	::= <ul style="list-style-type: none"> <i>ident</i> <i>impl_const</i> <i>value</i> constrained($\overline{mem_iv_c_i, pval_i}^i$) error(<i>string</i>, <i>pval</i>) <i>ctor_val</i>($\overline{pval_i}^i$) (struct <i>ident</i>){$\overline{.member_i = pval_i}^i$} (union <i>ident</i>){<i>.member</i> = <i>pval</i>} 	pure values <ul style="list-style-type: none"> Core identifier implementation-defined constant Core values constrained value impl-defined static error data constructor application C struct expression C union expression
<i>tpval</i>	::= <ul style="list-style-type: none"> undef <i>UB_name</i> done <i>pval</i> 	top-level pure values <ul style="list-style-type: none"> undefined behaviour pure done

$ident_opt_β$	$::=$ $ \quad _ : β$ $ \quad ident : β$	$binders = \{\}$ $binders = ident$	type annotated optional identifier
$pattern$	$::=$ $ \quad ident_opt_β$ $ \quad ctor_val(\overline{pattern_i}^i)$	$binders = binders(ident_opt_β)$ $binders = binders(\overline{pattern_i}^i)$	
z	$::=$ $ \quad i$ $ \quad mem_int$ $ \quad size_of(τ)$ $ \quad offset_of_{tag}(member)$ $ \quad ptr_size$ $ \quad max_int_τ$ $ \quad min_int_τ$	M M M M M M M	OCaml arbitrary-width integer literal integer size of a C type offset of a struct member size of a pointer maximum value of int of type $τ$ minimum value of int of type $τ$
$ℚ, q, -$	$::=$ $ \quad \frac{int_1}{int_2}$		OCaml type for rational numbers
lit	$::=$ $ \quad ident$ $ \quad unit$ $ \quad bool$ $ \quad z$ $ \quad ℚ$		
$ident_or_pattern$	$::=$ $ \quad ident$ $ \quad pattern$	$binders = ident$ $binders = binders(pattern)$	

$bool_op$	$::=$ $ \neg term$ $ term_1 = term_2$ $ \bigwedge (\overline{term_i})^i$ $ \bigvee (\overline{term_i})^i$ $ term_1 binop_{bool} term_2$ $ \text{if } term_1 \text{ then } term_2 \text{ else } term_3$	M	
$arith_op$	$::=$ $ term_1 + term_2$ $ term_1 - term_2$ $ term_1 \times term_2$ $ term_1 / term_2$ $ term_1 \text{rem}_t term_2$ $ term_1 \text{rem}_f term_2$ $ term_1 \wedge term_2$ $ term_1 binop_{arith} term_2$	M	
cmp_op	$::=$ $ term_1 < term_2$ $ term_1 \leq term_2$ $ term_1 binop_{rel} term_2$	M	less than less than or equal
$list_op$	$::=$ $ \text{nil}$ $ \text{tl } term$ $ term^{(int)}$		
$tuple_op$	$::=$ $ (\overline{term_i})^i$		

		$term^{(int)}$
$pointer_op$::=	
		mem_ptr
		$term_1 +_{ptr} term_2$
		$cast_int_to_ptr\ term$
		$cast_ptr_to_int\ term$
$array_op$::=	
		$term_1[term_2]$
$param_op$::=	
		$ident:\beta. term$
		$term(term_1, .., term_n)$
$struct_op$::=	
		$term.member$
ct_pred	::=	
		$\mathbf{representable}(\tau, term)$
		$\mathbf{aligned}(\tau, term)$
		$\mathbf{alignedI}(term_1, term_2)$
$term, _$::=	
		lit
		$arith_op$
		$bool_op$
		cmp_op
		$tuple_op$
		$struct_op$

		<i>pointer_op</i>		
		<i>list_op</i>		
		<i>array_op</i>		
		<i>ct_pred</i>		
		option_op		
		<i>param_op</i>		
		(<i>term</i>)	S	parentheses
		$\sigma(\textit{term})$	M	
		[<i>term</i> ₁ / <i>ident</i>] <i>term</i> ₂	M	substitute <i>term</i> ₁ for <i>ident</i> in <i>term</i> ₂
		<i>pval</i>	M	
<i>pexpr</i>	::=			pure expressions
		<i>pval</i>		pure values
		<i>ctor_expr</i> ($\overline{pval_i}^i$)		data constructor application
		array_shift (<i>pval</i> ₁ , τ , <i>pval</i> ₂)		pointer array shift
		member_shift (<i>pval</i> , <i>ident</i> , <i>member</i>)		pointer struct/union member shift
		not (<i>pval</i>)		boolean not
		<i>pval</i> ₁ <i>binop</i> <i>pval</i> ₂		binary operations
		memberof (<i>ident</i> , <i>member</i> , <i>pval</i>)		C struct/union member access
		<i>name</i> ($\overline{pval_i}^i$)		pure function call
		assert_undef (<i>pval</i> , <i>UB_name</i>)		
		bool_to_integer (<i>pval</i>)		
		conv_int (τ , <i>pval</i>)		
		wrapI (τ , <i>pval</i>)		
<i>tpexpr</i>	::=			top-level pure expressions
		<i>tpval</i>		top-level pure values
		case <i>pval</i> of $\overline{tpexpr_case_branch_i}^i$ end		pattern matching
		let <i>ident_or_pattern</i> = <i>pexpr</i> in <i>tpexpr</i>	bind binders(<i>ident_or_pattern</i>) in <i>tpexpr</i>	pure let
		let <i>ident_or_pattern</i> :($y_1:\beta_1. term_1$) = <i>tpexpr</i> ₁ in <i>tpexpr</i> ₂	bind binders(<i>ident_or_pattern</i>) in <i>tpexpr</i> ₂	pure let

	$\begin{array}{ l} \text{if } pval \text{ then } texpr_1 \text{ else } texpr_2 \\ \sigma(texpr) \end{array}$	$\text{bind } y_1 \text{ in } term_1$ M	pure if simul-sub environment σ in
$texpr_case_branch$	$\begin{array}{ l} ::= \\ \text{ pattern } \Rightarrow texpr \end{array}$	$\text{bind binders}(\text{pattern}) \text{ in } texpr$	pure top-level case expression top-level case expression br
m_kill_kind	$\begin{array}{ l} ::= \\ \text{ dynamic} \\ \text{ static } \tau \end{array}$		
$bool, _$	$\begin{array}{ l} ::= \\ \text{ true} \\ \text{ false} \end{array}$		OCaml booleans
$int, _$	$\begin{array}{ l} ::= \\ i \end{array}$		OCaml fixed-width integer literal integer
mem_action	$\begin{array}{ l} ::= \\ \text{ create } (pval, \tau) \\ \text{ create_readonly } (pval_1, \tau, pval_2) \\ \text{ alloc } (pval_1, pval_2) \\ \text{ kill } (m_kill_kind, pval) \\ \text{ store } (bool, \tau, pval_1, pval_2, mem_order) \\ \text{ load } (\tau, pval, mem_order) \\ \text{ rmw } (\tau, pval_1, pval_2, pval_3, mem_order_1, mem_order_2) \\ \text{ fence } (mem_order) \\ \text{ cmp_exch_strong } (\tau, pval_1, pval_2, pval_3, mem_order_1, mem_order_2) \\ \text{ cmp_exch_weak } (\tau, pval_1, pval_2, pval_3, mem_order_1, mem_order_2) \\ \text{ linux_fence } (linux_mem_order) \end{array}$		memory actions true means store is locking

		<code>linux_load($\tau, pval, linux_mem_order$)</code>	
		<code>linux_store($\tau, pval_1, pval_2, linux_mem_order$)</code>	
		<code>linux_rmw($\tau, pval_1, pval_2, linux_mem_order$)</code>	
<i>polarity</i>	::=		polarities for memory actions
			(pos) sequenced by <code>let weak</code> and <code>let strong</code>
		<code>neg</code>	only sequenced by <code>let strong</code>
<i>pol_mem_action</i>	::=		memory actions with polarity
		<code>polarity mem_action</code>	
<i>mem_op</i>	::=		operations involving the memory state
		<code>pval₁ == pval₂</code>	pointer equality comparison
		<code>pval₁ ≠ pval₂</code>	pointer inequality comparison
		<code>pval₁ < pval₂</code>	pointer less-than comparison
		<code>pval₁ > pval₂</code>	pointer greater-than comparison
		<code>pval₁ ≤ pval₂</code>	pointer less-than comparison
		<code>pval₁ ≥ pval₂</code>	pointer greater-than comparison
		<code>pval₁ −_τ pval₂</code>	pointer subtraction
		<code>intFromPtr($\tau_1, \tau_2, pval$)</code>	cast of pointer value to integer value
		<code>ptrFromInt($\tau_1, \tau_2, pval$)</code>	cast of integer value to pointer value
		<code>ptrValidForDeref($\tau, pval$)</code>	dereferencing validity predicate
		<code>ptrWellAligned($\tau, pval$)</code>	
		<code>ptrArrayShift($pval_1, \tau, pval_2$)</code>	
		<code>memcpy($pval_1, pval_2, pval_3$)</code>	
		<code>memcmp($pval_1, pval_2, pval_3$)</code>	
		<code>realloc($pval_1, pval_2, pval_3$)</code>	
		<code>va_start($pval_1, pval_2$)</code>	
		<code>va_copy($pval$)</code>	
		<code>va_arg($pval, \tau$)</code>	

		$\mathbf{va_end}(pval)$	
res_term	$::=$	<ul style="list-style-type: none"> \mathbf{emp} \mathbf{pt} $ident$ $\langle res_term_1, res_term_2 \rangle$ $\mathbf{pack}(pval, res_term)$ 	<p>resource terms</p> <ul style="list-style-type: none"> empty heap single-cell heap variable seperating-conjunction pair packing for existentials
$spine_elem$	$::=$	<ul style="list-style-type: none"> $pval$ $term$ res_term 	<p>spine element</p> <ul style="list-style-type: none"> pure value logical value resource value
$spine$	$::=$	<ul style="list-style-type: none"> $\overline{spine_elem_i}^i$ 	<p>spine</p>
$tval$	$::=$	<ul style="list-style-type: none"> $\mathbf{done\ spine}$ $\mathbf{undef\ UB_name}$ 	<p>(effectful) top-level values</p> <ul style="list-style-type: none"> end of top-level expression undefined behaviour
$res_pattern$	$::=$	<ul style="list-style-type: none"> \mathbf{emp} binders = $\{\}$ \mathbf{pt} binders = $\{\}$ $ident$ binders = $ident$ $\langle res_pattern_1, res_pattern_2 \rangle$ binders = $\text{binders}(res_pattern_1) \cup \text{binders}(res_pattern_2)$ $\mathbf{pack}(ident, res_pattern)$ binders = $ident \cup \text{binders}(res_pattern)$ 	<p>resource terms</p> <ul style="list-style-type: none"> empty heap single-cell heap variable seperating-conjunction pair packing for existentials
$ret_pattern$	$::=$	<ul style="list-style-type: none"> $\mathbf{comp\ ident_or_pattern}$ binders = $\text{binders}(ident_or_pattern)$ 	<p>return pattern</p> <ul style="list-style-type: none"> computational variable

		$\text{log } ident$	$\text{binders} = ident$	logical variable
		$res \text{ } res_pattern$	$\text{binders} = \text{binders}(res_pattern)$	resource variable
$init,$	$::=$			initialisation status
		\checkmark		initialised
		\times		uninitialised
$points_to$	$::=$			points-to separation logic predicate
		$term_1 \mathbb{Q} \stackrel{init}{\mapsto}_{\tau} term_2$		
res	$::=$			resources
		emp		empty heap
		$points_to$		points-top heap pred.
		$res_1 * res_2$		seperating conjunction
		$\exists ident:\beta. res$		existential
		$term \wedge res$		logical conjunction
		$\langle res \rangle$	S	parentheses
		$[pval/ident]res$	M	substitute $pval$ for $ident$ in res
$ret, _$	$::=$			return types
		$\Sigma ident:\beta. ret$		
		$\exists ident:\beta. ret$		
		$res \otimes ret$		
		$term \wedge ret$		
		\mathbf{I}		
		$[spine_elem/ident]ret$	M	
		$\sigma(ret)$	M	
seq_expr	$::=$			sequential (effectful) expressions
		$\text{ccall } (\tau, pval, spine)$		C function call

		pcall (<i>name</i> , <i>spine</i>)		procedure call
<i>seq_expr</i>	::=	<i>tval</i> run $\overline{ident\ pval}_i^i$ let <i>ident_or_pattern</i> = <i>pexpr</i> in <i>texpr</i> let <i>ident_or_pattern</i> :(<i>y</i> ₁ : <i>β</i> ₁ . <i>term</i> ₁) = <i>tpexpr</i> in <i>texpr</i> let $\overline{ret_pattern}_i^i = seq_expr$ in <i>texpr</i> let $\overline{ret_pattern}_i^i : ret = texpr_1$ in <i>texpr</i> ₂ case <i>pval</i> of <i>texpr_case_branch</i> _{<i>i</i>} end if <i>pval</i> then <i>texpr</i> ₁ else <i>texpr</i> ₂ bound [<i>int</i>](<i>is_expr</i>)	 bind binders(<i>ident_or_pattern</i>) in <i>texpr</i> bind binders(<i>ident_or_pattern</i>) in <i>texpr</i> bind <i>y</i> ₁ in <i>term</i> ₁ bind binders($\overline{ret_pattern}_i^i$) in <i>texpr</i> bind binders($\overline{ret_pattern}_i^i$) in <i>texpr</i> ₂	sequential top-level (effectful) expressions (effectful) top-level values run from label pure let pure let bind return patterns annotated bind return patterns pattern matching conditional limit scope of indet seq behaviour
<i>texpr_case_branch</i>	::=	<i>pattern</i> \Rightarrow <i>texpr</i>	bind binders(<i>pattern</i>) in <i>texpr</i>	top-level case expression branch top-level case expression branch
<i>is_expr</i>	::=	<i>tval</i> memop (<i>mem_op</i>) <i>pol_mem_action</i>		indet seq (effectful) expressions (effectful) top-level values pointer op involving memory memory action
<i>is_expr</i>	::=	let weak $\overline{ret_pattern}_i^i = is_expr$ in <i>texpr</i> let strong $\overline{ret_pattern}_i^i = is_expr$ in <i>texpr</i>	bind binders($\overline{ret_pattern}_i^i$) in <i>texpr</i> bind binders($\overline{ret_pattern}_i^i$) in <i>texpr</i>	indet seq top-level (effectful) expressions weak sequencing strong sequencing
<i>texpr</i>	::=	<i>seq_expr</i> <i>is_expr</i> $\sigma(texpr)$	M	top-level (effectful) expressions sequential (effectful) expressions indet seq (effectful) expressions simul-sub environment σ in <i>texpr</i>

arg	$::=$ $ \quad \Pi ident:\beta. arg$ $ \quad \forall ident:\beta. arg$ $ \quad res \multimap arg$ $ \quad term \supset arg$ $ \quad ret$ $ \quad [spine_elem/ident]arg \quad M$	argument/function types
$pure_arg$	$::=$ $ \quad \Pi ident:\beta. pure_arg$ $ \quad term \supset pure_arg$ $ \quad pure_ret$	pure argument/function types
$pure_ret$	$::=$ $ \quad \Sigma ident:\beta. pure_ret$ $ \quad term \wedge pure_ret$ $ \quad I$	pure return types
\mathcal{C}	$::=$ $ \quad \cdot$ $ \quad \mathcal{C}, ident:\beta$ $ \quad \overline{\mathcal{C}}_i^i$	computational var env
\mathcal{L}	$::=$ $ \quad \cdot$ $ \quad \overline{\mathcal{L}}_i^i$ $ \quad \mathcal{L}, ident:\beta$	logical var env
Φ	$::=$ $ \quad \cdot$	constraints env

	$\begin{array}{ l} \Phi, term \\ \hline \Phi_i^i \end{array}$	
\mathcal{R}	$\begin{array}{ l} ::= \\ \cdot \\ \mathcal{R}, ident:res \\ \hline \mathcal{R}_i^i \end{array}$	resources env
σ	$\begin{array}{ l} ::= \\ \cdot \\ spine_elem/ident, \sigma \\ \hline \sigma_i^i \end{array}$	values env
$typing$	$\begin{array}{ l} ::= \\ \text{ \texttt{smt} } (\Phi \Rightarrow term) \\ ident:\beta \in \mathcal{C} \\ ident:\text{ \texttt{struct tag} } \& \overline{member_i:\tau_i}^i \in \text{ \texttt{Globals} } \\ \hline \mathcal{C}_i; \mathcal{L}_i; \Phi_i \vdash mem_val_i \Rightarrow \text{ \texttt{mem} } \beta_i^i \\ \mathcal{L} \vdash term:\beta \\ pval:arg \in \text{ \texttt{Globals} } \end{array}$	dependent on memory object model
$opsem$	$\begin{array}{ l} ::= \\ pval \equiv \overline{x_i}^i \mapsto texpr:(y:\beta. term) \in \text{ \texttt{Globals} } \\ pval \equiv \overline{x_i}^i \mapsto texpr:ret \in \text{ \texttt{Globals} } \\ \forall i < j. \text{ \texttt{not} } (pattern_i = pval \rightsquigarrow \sigma_i) \\ \text{ \texttt{fresh} } (mem_ptr) \end{array}$	
$formula$	$\begin{array}{ l} ::= \\ judgement \\ term \equiv term' \end{array}$	

	$\begin{array}{ l} typing \\ opsem \end{array}$	
$heap, h$	$\begin{array}{ l} ::= \\ h + \{mem_ptr \mapsto \times\} \\ h + \{mem_ptr \mapsto pval\} \end{array}$	heaps
$object_value_jtype$	$\begin{array}{ l} ::= \\ \mathcal{C}; \mathcal{L}; \Phi \vdash object_value \Rightarrow \mathbf{obj} \beta \end{array}$	
$pval_jtype$	$\begin{array}{ l} ::= \\ \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta \end{array}$	
res_jtype	$\begin{array}{ l} ::= \\ \Phi \vdash res \equiv res' \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash res_term \Leftarrow res \end{array}$	
$spine_jtype$	$\begin{array}{ l} ::= \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine_elem_i}^i :: arg \gg ret \end{array}$	
$pexpr_jtype$	$\begin{array}{ l} ::= \\ \mathcal{C}; \mathcal{L}; \Phi \vdash pexpr \Rightarrow ident:\beta. term \end{array}$	
$comp_pattern_jtype$	$\begin{array}{ l} ::= \\ term \mathbf{as} pattern:\beta \rightsquigarrow \mathcal{C}; \Phi \\ term \mathbf{as} ident_or_pattern:\beta \rightsquigarrow \mathcal{C}; \Phi \end{array}$	
$res_pattern_jtype$	$\begin{array}{ l} ::= \\ res_pattern:res \rightsquigarrow \mathcal{L}; \Phi; \mathcal{R} \end{array}$	

$ret_pattern_jtype$	$::=$ $ \quad \overline{ret_pattern_i}^i : ret \rightsquigarrow \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}$
$tpval_jtype$	$::=$ $ \quad \mathcal{C}; \mathcal{L}; \Phi \vdash tpval \Leftarrow ident:\beta. term$
$tpexpr_jtype$	$::=$ $ \quad \mathcal{C}; \mathcal{L}; \Phi \vdash tpexpr \Leftarrow ident:\beta. term$
$action_jtype$	$::=$ $ \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem_action \Rightarrow ret$
$tval_jtype$	$::=$ $ \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash tval \Leftarrow ret$
$texpr_jtype$	$::=$ $ \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash seq_expr \Rightarrow ret$ $ \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is_expr \Rightarrow ret$ $ \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash seq_texpr \Leftarrow ret$ $ \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is_texpr \Leftarrow ret$ $ \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret$
$decons_jtype$	$::=$ $ \quad pattern = pval \rightsquigarrow \sigma$ $ \quad ident_or_pattern = pval \rightsquigarrow \sigma$ $ \quad res_pattern = res_term \rightsquigarrow \sigma$ $ \quad ret_pattern = spine_elem \rightsquigarrow \sigma$
$pure_opsem_jtype$	$::=$ $ \quad \langle pexpr \rangle \longrightarrow \langle pexpr' \rangle$

$$\begin{array}{l}
| \quad \langle pexpr \rangle \longrightarrow \langle tpepr:(y:\beta. term) \rangle \\
| \quad \langle tpepr \rangle \longrightarrow \langle tpepr' \rangle
\end{array}$$

$$\begin{array}{lcl}
opsem_jtype & ::= & \\
& | & \langle seq_expr \rangle \longrightarrow \langle texpr:ret \rangle \\
& | & \langle h; seq_texpr \rangle \longrightarrow \langle h'; texpr \rangle \\
& | & \langle mem_op \rangle \longrightarrow \langle pval \rangle \\
& | & \langle h; mem_action \rangle \longrightarrow \langle h'; spine \rangle \\
& | & \langle h; is_expr \rangle \longrightarrow \langle h'; is_expr' \rangle \\
& | & \langle h; is_texpr \rangle \longrightarrow \langle h'; texpr \rangle \\
& | & \langle h; texpr \rangle \longrightarrow \langle h'; texpr' \rangle
\end{array}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash object_value \Rightarrow \text{obj } \beta}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash mem_int \Rightarrow \text{obj integer}} \quad \text{TY_PVAL_OBJ_INT}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash mem_ptr \Rightarrow \text{obj loc}} \quad \text{TY_PVAL_OBJ_PTR}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash loaded_value_i \Rightarrow \beta^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{array}(\overline{loaded_value_i^i}) \Rightarrow \text{obj array } \beta} \quad \text{TY_PVAL_OBJ_ARR}$$

$$\frac{\frac{ident: \text{struct tag} \ \& \ \overline{member_i: \tau_i^i} \in \text{Globals}}{\mathcal{C}; \mathcal{L}; \Phi \vdash mem_val_i \Rightarrow \text{mem } \beta_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash (\text{struct tag})\{\overline{member_i: \tau_i = mem_val_i^i}\} \Rightarrow \text{obj struct tag}} \quad \text{TY_PVAL_OBJ_STRUCT}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta}$$

$$\frac{x:\beta \in \mathcal{C}}{\mathcal{C}; \mathcal{L}; \Phi \vdash x \Rightarrow \beta} \quad \text{TY_PVAL_VAR}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{object_value} \Rightarrow \text{obj } \beta}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{object_value} \Rightarrow \beta} \quad \text{TY_PVAL_OBJ}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{object_value} \Rightarrow \text{obj } \beta}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{specified_object_value} \Rightarrow \beta} \quad \text{TY_PVAL_LOADED}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Unit} \Rightarrow \text{unit}} \quad \text{TY_PVAL_UNIT}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{True} \Rightarrow \text{bool}} \quad \text{TY_PVAL_TRUE}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{False} \Rightarrow \text{bool}} \quad \text{TY_PVAL_FALSE}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{value}_i \Rightarrow \beta^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \beta[\overline{\text{value}_i^i}] \Rightarrow \text{list } \beta} \quad \text{TY_PVAL_LIST}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{value}_i \Rightarrow \beta_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash (\overline{\text{value}_i^i}) \Rightarrow \overline{\beta_i^i}} \quad \text{TY_PVAL_TUPLE}$$

$$\frac{\text{smt } (\Phi \Rightarrow \text{false})}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{error } (\text{string}, \text{pval}) \Rightarrow \beta} \quad \text{TY_PVAL_ERROR}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Nil } \beta() \Rightarrow \text{list } \beta} \quad \text{TY_PVAL_CTOR_NIL}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval}_1 \Rightarrow \beta \\ \mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval}_2 \Rightarrow \text{list } \beta \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Cons}(\text{pval}_1, \text{pval}_2) \Rightarrow \text{list } \beta} \quad \text{TY_PVAL_CTOR_CONS}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_i \Rightarrow \beta_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Tuple}(\overline{pval_i^i}) \Rightarrow \overline{\beta_i^i}} \quad \text{TY_PVAL_CTOR_TUPLE}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_i \Rightarrow \beta^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Array}(\overline{pval_i^i}) \Rightarrow \text{array } \beta} \quad \text{TY_PVAL_CTOR_ARRAY}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Specified}(pval) \Rightarrow \beta} \quad \text{TY_PVAL_CTOR_SPECIFIED}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_i \Rightarrow \beta_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash (\text{struct tag})\{\overline{member_i = pval_i^i}\} \Rightarrow \text{struct tag}} \quad \text{TY_PVAL_STRUCT}$$

$$\boxed{\Phi \vdash res \equiv res'}$$

$$\frac{}{\Phi \vdash \text{emp} \equiv \text{emp}} \quad \text{TYRES_EQ_EMP}$$

$$\frac{\text{smt}(\Phi \Rightarrow (term_1 = term'_1) \wedge (term_2 = term'_2))}{\Phi \vdash term_1 \overset{init}{q \mapsto}_{\tau} term_2 \equiv term'_1 \overset{init}{q \mapsto}_{\tau} term'_2} \quad \text{TYRES_EQ_POINTSTO}$$

$$\frac{\begin{array}{l} \Phi \vdash res_1 \equiv res'_1 \\ \Phi \vdash res_2 \equiv res'_2 \end{array}}{\Phi \vdash res_1 * res_2 \equiv res'_1 * res'_2} \quad \text{TYRES_EQ_SEPCONJ}$$

$$\frac{\Phi \vdash res \equiv res'}{\Phi \vdash \exists ident:\beta. res \equiv \exists ident:\beta. res'} \quad \text{TYRES_EQ_EXISTS}$$

$$\frac{\begin{array}{l} \text{smt}(\Phi, term \Rightarrow term') \\ \text{smt}(\Phi, term' \Rightarrow term) \\ \Phi \vdash res \equiv res' \end{array}}{\Phi \vdash term \wedge res \equiv term' \wedge res'} \quad \text{TYRES_EQ_TERM}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash res_term \Leftarrow res}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \text{emp} \Leftarrow \text{emp}} \quad \text{TYRES_EMP}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \text{pt} \Leftarrow points_to} \quad \text{TYRES_POINTSTO}$$

$$\frac{\Phi \vdash res \equiv res'}{\mathcal{C}; \mathcal{L}; \Phi; \cdot, r:res \vdash r \Leftarrow res'} \quad \text{TYRES_VAR}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_1 \vdash res_term_1 \Leftarrow res_1 \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_2 \vdash res_term_2 \Leftarrow res_2 \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_1, \mathcal{R}_2 \vdash \langle res_term_1, res_term_2 \rangle \Leftarrow res_1 * res_2} \quad \text{TYRES_SEPCONJ}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash res_term_2 \Leftarrow [pval/y]res \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{pack}(pval, res_term_2) \Leftarrow \exists y:\beta. res} \quad \text{TYRES_PACK}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine_elem_i}^i :: arg \gg ret}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash ::ret \gg ret} \quad \text{TY_SPINE_EMPTY}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine_elem_i}^i :: [pval/x]arg \gg ret \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash pval, \overline{spine_elem_i}^i :: \Pi x:\beta. arg \gg ret} \quad \text{TY_SPINE_COMP}$$

$$\frac{\begin{array}{l} \mathcal{L} \vdash term:\beta \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine_elem_i}^i :: [term/x]arg \gg ret \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash term, \overline{spine_elem_i}^i :: \forall x:\beta. arg \gg ret} \quad \text{TY_SPINE_LOG}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_1 \vdash res_term \Leftarrow res \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_2 \vdash \overline{spine_elem_i}^i :: arg \gg ret \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_1, \mathcal{R}_2 \vdash res_term, \overline{spine_elem_i}^i :: res \multimap arg \gg ret} \quad \text{TY_SPINE_RES}$$

$$\frac{\begin{array}{l} \text{smt}(\Phi \Rightarrow term) \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine_elem_i}^i :: arg \gg ret \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine_elem_i}^i :: term \supset arg \gg ret} \quad \text{TY_SPINE_CONS}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash pexpr \Rightarrow ident:\beta. term}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta}{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow y:\beta. y = pval} \quad \text{TY_PE_VAL}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \text{loc} \\ \mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \text{integer} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{array_shift}(pval_1, \tau, pval_2) \Rightarrow y:\text{loc}. y = pval_1 +_{\text{ptr}} (pval_2 \times \text{size_of}(\tau))} \quad \text{TY_PE_ARRAY_SHIFT}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \text{loc} \\ \vdots \text{struct tag} \& \overline{member_i;\tau_i}^i \in \text{Globals} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{member_shift}(pval, tag, member_j) \Rightarrow y:\text{loc}. y = pval +_{\text{ptr}} \text{offset_of}_{tag}(member_j)} \quad \text{TY_PE_MEMBER_SHIFT}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \text{bool}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{not}(pval) \Rightarrow y:\text{bool}. y = \neg pval} \quad \text{TY_PE_NOT}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \text{integer} \\ \mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \text{integer} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \text{ binop}_{arith} pval_2 \Rightarrow y:\text{integer}. y = (pval_1 \text{ binop}_{arith} pval_2)} \quad \text{TY_PE_ARITH_BINOP}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \text{integer} \\ \mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \text{integer} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \text{ binop}_{rel} pval_2 \Rightarrow y:\text{bool}. y = (pval_1 \text{ binop}_{rel} pval_2)} \quad \text{TY_PE_REL_BINOP}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \text{bool} \\ \mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \text{bool} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \text{ binop}_{bool} pval_2 \Rightarrow y:\text{bool}. y = (pval_1 \text{ binop}_{bool} pval_2)} \quad \text{TY_PE_BOOL_BINOP}$$

$$\frac{\begin{array}{c} name: pure_arg \in \text{Globals} \\ \mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \overline{pval_i}^i :: pure_arg \gg \Sigma y':\beta'. term' \wedge \mathbf{I} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash name(\overline{pval_i}^i) \Rightarrow y':\beta'. term'} \quad \text{TY_PE_CALL}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \text{bool} \\ \text{smt}(\Phi \Rightarrow pval) \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{assert_undef}(pval, UB_name) \Rightarrow y:\text{unit}. y = \text{unit}} \quad \text{TY_PE_ASSERT_UNDEF}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \text{bool}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{bool_to_integer}(pval) \Rightarrow y:\text{integer}. y = \text{if } pval \text{ then } 1 \text{ else } 0} \quad \text{TY_PE_BOOL_TO_INTEGER}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \text{integer} \\ abbrev_1 \equiv \text{max_int}_\tau - \text{min_int}_\tau + 1 \\ abbrev_2 \equiv pval \text{ rem_f } abbrev_1 \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{wrapI}(\tau, pval) \Rightarrow y:\beta. y = \text{if } abbrev_2 \leq \text{max_int}_\tau \text{ then } abbrev_2 \text{ else } abbrev_2 - abbrev_1} \quad \text{TY_PE_WRAP I}$$

$term \text{ as } pattern:\beta \rightsquigarrow \mathcal{C}; \Phi$

$$\frac{}{term \text{ as } \cdot:\beta:\beta \rightsquigarrow \cdot;\cdot} \quad \text{TY_PAT_COMP_NO_SYM_ANNOT}$$

$$\frac{}{term \text{ as } x:\beta:\beta \rightsquigarrow \cdot, x:\beta;\cdot, x = term} \quad \text{TY_PAT_COMP_SYM_ANNOT}$$

$$\frac{}{term \text{ as Nil } \beta():\text{list } \beta \rightsquigarrow \cdot;\cdot} \quad \text{TY_PAT_COMP_NIL}$$

$$\frac{\begin{array}{l} term^{(1)} \text{ as } pattern_1:\beta \rightsquigarrow \mathcal{C}_1; \Phi_1 \\ \text{tl } term \text{ as } pattern_2:\text{list } \beta \rightsquigarrow \mathcal{C}_2; \Phi_1 \end{array}}{term \text{ as Cons}(pattern_1, pattern_2):\text{list } \beta \rightsquigarrow \mathcal{C}_1, \mathcal{C}_2; \Phi_1, \Phi_2} \quad \text{TY_PAT_COMP_CONS}$$

$$\frac{\overline{term^{(i)} \text{ as } pattern_i:\beta_i \rightsquigarrow \mathcal{C}_i; \Phi_i}^i}{term \text{ as Tuple}(\overline{pattern_i}^i):\overline{\beta_i}^i \rightsquigarrow \overline{\mathcal{C}_i}^i; \overline{\Phi_i}^i} \quad \text{TY_PAT_COMP_TUPLE}$$

$$\frac{\overline{term[i] \text{ as } pattern_i:\beta \rightsquigarrow \mathcal{C}_i; \Phi_i}^i}{term \text{ as Array}(\overline{pattern_i}^i):\text{array } \beta \rightsquigarrow \overline{\mathcal{C}_i}^i; \overline{\Phi_i}^i} \quad \text{TY_PAT_COMP_ARRAY}$$

$$\frac{term \text{ as } pattern:\beta \rightsquigarrow \mathcal{C}; \Phi}{term \text{ as Specified}(pattern):\beta \rightsquigarrow \mathcal{C}; \Phi} \quad \text{TY_PAT_COMP_SPECIFIED}$$

$term \text{ as ident_or_pattern}:\beta \rightsquigarrow \mathcal{C}; \Phi$

$$\frac{}{term \text{ as } x:\beta \rightsquigarrow \cdot, x:\beta;\cdot, x = term} \quad \text{TY_PAT_SYM_OR_PATTERN_SYM}$$

$$\frac{term \text{ as pattern} : \beta \rightsquigarrow \mathcal{C}; \Phi}{term \text{ as pattern} : \beta \rightsquigarrow \mathcal{C}; \Phi} \quad \text{TY_PAT_SYM_OR_PATTERN_PATTERN}$$

$$\boxed{res_pattern : res \rightsquigarrow \mathcal{L}; \Phi; \mathcal{R}}$$

$$\frac{}{emp : emp \rightsquigarrow \cdot; \cdot; \cdot} \quad \text{TY_PAT_RES_EMPTY}$$

$$\frac{}{pt : points_to \rightsquigarrow \cdot; \cdot; \cdot, r : points_to} \quad \text{TY_PAT_RES_POINTSTO}$$

$$\frac{}{r : res \rightsquigarrow \cdot; \cdot; \cdot, r : res} \quad \text{TY_PAT_RES_VAR}$$

$$\frac{\begin{array}{l} res_pattern_1 : res_1 \rightsquigarrow \mathcal{L}_1; \Phi_1; \mathcal{R}_1 \\ res_pattern_2 : res_2 \rightsquigarrow \mathcal{L}_2; \Phi_2; \mathcal{R}_2 \end{array}}{\langle res_pattern_1, res_pattern_2 \rangle : res_1 * res_2 \rightsquigarrow \mathcal{L}_1, \mathcal{L}_2; \Phi_1, \Phi_2; \mathcal{R}_1, \mathcal{R}_2} \quad \text{TY_PAT_RES_SEP_CONJ}$$

$$\frac{res_pattern : res \rightsquigarrow \mathcal{L}; \Phi; \mathcal{R}}{res_pattern : term \wedge res \rightsquigarrow \mathcal{L}; \Phi, term; \mathcal{R}} \quad \text{TY_PAT_RES_CONJ}$$

$$\frac{res_pattern : [x/y]res \rightsquigarrow \mathcal{L}; \Phi; \mathcal{R}}{pack(x, res_pattern) : \exists y : \beta. res \rightsquigarrow \mathcal{L}, x : \beta; \Phi; \mathcal{R}} \quad \text{TY_PAT_RES_PACK}$$

$$\boxed{\overline{ret_pattern_i}^i : ret \rightsquigarrow \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}}$$

$$\frac{}{:I \rightsquigarrow \cdot; \cdot; \cdot; \cdot} \quad \text{TY_PAT_RET_EMPTY}$$

$$\frac{\frac{y \text{ as } \text{ident_or_pattern}:\beta \rightsquigarrow \mathcal{C}_1; \Phi_1}{\overline{\text{ret_pattern}_i}^i:\text{ret} \rightsquigarrow \mathcal{C}_2; \mathcal{L}_2; \Phi_2; \mathcal{R}_2}}{\text{comp } \text{ident_or_pattern}, \overline{\text{ret_pattern}_i}^i:\Sigma y:\beta. \text{ret} \rightsquigarrow \mathcal{C}_1, \mathcal{C}_2; \mathcal{L}_2; \Phi_2; \mathcal{R}_2} \quad \text{TY_PAT_RET_COMP}$$

$$\frac{\overline{\text{ret_pattern}_i}^i:\text{ret} \rightsquigarrow \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}}{\log y, \overline{\text{ret_pattern}_i}^i:\exists y:\beta. \text{ret} \rightsquigarrow \mathcal{C}; \mathcal{L}, y:\beta; \Phi; \mathcal{R}} \quad \text{TY_PAT_RET_LOG}$$

$$\frac{\frac{\text{res_pattern}:\text{res} \rightsquigarrow \mathcal{L}_1; \Phi_1; \mathcal{R}_1}{\overline{\text{ret_pattern}_i}^i:\text{ret} \rightsquigarrow \mathcal{C}_2; \mathcal{L}_2; \Phi_2; \mathcal{R}_2}}{\text{res } \text{res_pattern}, \overline{\text{ret_pattern}_i}^i:\text{res} \otimes \text{ret} \rightsquigarrow \mathcal{C}_2; \mathcal{L}_1, \mathcal{L}_2; \Phi_1, \Phi_2; \mathcal{R}_1, \mathcal{R}_2} \quad \text{TY_PAT_RET_RES}$$

$$\frac{\overline{\text{ret_pattern}_i}^i:\text{ret} \rightsquigarrow \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}}{\overline{\text{ret_pattern}_i}^i:\text{term} \wedge \text{ret} \rightsquigarrow \mathcal{C}; \mathcal{L}; \Phi, \text{term}; \mathcal{R}} \quad \text{TY_PAT_RET_CONS}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{tpval} \Leftarrow \text{ident}:\beta. \text{term}}$$

$$\frac{\text{smt}(\Phi \Rightarrow \text{false})}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{undef } \text{UB_name} \Leftarrow y:\beta. \text{term}} \quad \text{TY_TPVAL_UNDEF}$$

$$\frac{\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval} \Rightarrow \beta}{\text{smt}(\Phi \Rightarrow [\text{pval}/y]\text{term})}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{done pval} \Leftarrow y:\beta. \text{term}} \quad \text{TY_TPVAL_DONE}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{texpr} \Leftarrow \text{ident}:\beta. \text{term}}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval} \Rightarrow \text{bool} \\ \mathcal{C}; \mathcal{L}; \Phi, \text{pval} = \text{true} \vdash \text{texpr}_1 \Leftarrow y:\beta. \text{term} \\ \mathcal{C}; \mathcal{L}; \Phi, \text{pval} = \text{false} \vdash \text{texpr}_2 \Leftarrow y:\beta. \text{term} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{if pval then texpr}_1 \text{ else texpr}_2 \Leftarrow y:\beta. \text{term}} \quad \text{TY_TPE_IF}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pexpr \Rightarrow y_1:\beta_1. term_1 \\
y_1 \text{ as } ident_or_pattern:\beta_1 \rightsquigarrow \mathcal{C}_1; \Phi_1 \\
\mathcal{C}, \mathcal{C}_1; \mathcal{L}, y_1:\beta_1; \Phi, term_1, \Phi_1 \vdash tpepr \Leftarrow y_2:\beta_2. term_2 \\
\hline
\mathcal{C}; \mathcal{L}; \Phi \vdash \text{let } ident_or_pattern = pexpr \text{ in } tpepr \Leftarrow y_2:\beta_2. term_2
\end{array}
\quad \text{TY_TPE_LET}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash tpepr_1 \Leftarrow y_1:\beta_1. term_1 \\
y_1 \text{ as } ident_or_pattern:\beta_1 \rightsquigarrow \mathcal{C}_1; \Phi_1 \\
\mathcal{C}, \mathcal{C}_1; \mathcal{L}, y_1:\beta_1; \Phi, term_1, \Phi_1 \vdash tpepr \Leftarrow y_2:\beta_2. term_2 \\
\hline
\mathcal{C}; \mathcal{L}; \Phi \vdash \text{let } ident_or_pattern:(y_1:\beta_1. term_1) = tpepr_1 \text{ in } tpepr_2 \Leftarrow y_2:\beta_2. term_2
\end{array}
\quad \text{TY_TPE_LETT}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta_1 \\
\hline
y_1 \text{ as } pattern_i:\beta_1 \rightsquigarrow \mathcal{C}_i; \Phi_i^i \\
\hline
\mathcal{C}, \mathcal{C}_i; \mathcal{L}, y_1:\beta_1; \Phi, y_1 = pval, \Phi_i \vdash tpepr_i \Leftarrow y_2:\beta_2. term_2^i \\
\hline
\mathcal{C}; \mathcal{L}; \Phi \vdash \text{case } pval \text{ of } \mid pattern_i \Rightarrow tpepr_i \text{ end } \Leftarrow y_2:\beta_2. term_2
\end{array}
\quad \text{TY_TPE_CASE}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem_action \Rightarrow ret}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \text{integer} \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \text{create}(pval, \tau) \Rightarrow \Sigma y_p:\text{loc. representable}(\tau*, y_p) \wedge \text{alignedI}(pval, y_p) \wedge \exists y:\beta_\tau. \langle y_p \text{ } 1 \overset{\times}{\mapsto}_\tau y \rangle \otimes \text{I}
\end{array}
\quad \text{TY_ACTION_CREATE}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \text{loc} \\
\mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \beta_\tau \\
\text{smt}(\Phi \Rightarrow \text{representable}(\tau, pval_2)) \\
\text{smt}(\Phi \Rightarrow pval_0 = pval_1) \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \cdot, r:\langle pval_0 \text{ } 1 \mapsto_\tau - \rangle \vdash \text{store}(-, \tau, pval_1, pval_2, -) \Rightarrow \Sigma _:\text{unit. } pval_0 \text{ } 1 \overset{\checkmark}{\mapsto}_\tau pval_2 \otimes \text{I}
\end{array}
\quad \text{TY_ACTION_STORE}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \text{loc} \\
\text{smt}(\Phi \Rightarrow pval_0 = pval_1) \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \cdot, r:\langle pval_0 \text{ } 1 \overset{\checkmark}{\mapsto}_\tau pval_2 \rangle \vdash \text{load}(\tau, pval_1, -) \Rightarrow \Sigma y:\beta_\tau. y = pval_2 \wedge \langle pval_0 \text{ } 1 \overset{\checkmark}{\mapsto}_\tau pval_2 \rangle \otimes \text{I}
\end{array}
\quad \text{TY_ACTION_LOAD}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \text{loc} \\ \text{smt}(\Phi \Rightarrow pval_0 = pval_1) \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \cdot, r: \langle pval_0 \mapsto_{\tau} _ \rangle \vdash \text{kill}(\text{static } \tau, pval_1) \Rightarrow \Sigma \text{ :unit. I}} \quad \text{TY_ACTION_KILL_STATIC}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash tval \Leftarrow \text{ret}}$$

$$\overline{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{done}} \Leftarrow \text{I} \quad \text{TY_TVAL_I}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{done } \overline{\text{spine_elem}_i}^i \Leftarrow [pval/y]\text{ret} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{done } pval, \overline{\text{spine_elem}_i}^i \Leftarrow \Sigma y:\beta. \text{ret}} \quad \text{TY_TVAL_COMP}$$

$$\frac{\begin{array}{c} \mathcal{L} \vdash \text{term}:\beta \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{done } \overline{\text{spine_elem}_i}^i \Leftarrow [\text{term}/y]\text{ret} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{done } \text{term}, \overline{\text{spine_elem}_i}^i \Leftarrow \exists y:\beta. \text{ret}} \quad \text{TY_TVAL_LOG}$$

$$\frac{\begin{array}{c} \text{smt}(\Phi \Rightarrow \text{term}) \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{done } \text{spine} \Leftarrow \text{ret} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{done } \text{spine} \Leftarrow \text{term} \wedge \text{ret}} \quad \text{TY_TVAL_CONS}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_1 \vdash \text{res_term} \Leftarrow \text{res} \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_2 \vdash \text{done } \overline{\text{spine_elem}_i}^i \Leftarrow \text{ret} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_1, \mathcal{R}_2 \vdash \text{done } \text{res_term}, \overline{\text{spine_elem}_i}^i \Leftarrow \text{res} \otimes \text{ret}} \quad \text{TY_TVAL_RES}$$

$$\frac{\text{smt}(\Phi \Rightarrow \text{false})}{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \text{undef } UB_name \Leftarrow \text{ret}} \quad \text{TY_TVAL_UB}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{seq_expr} \Rightarrow \text{ret}}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \text{loc} \\
pval:arg \in \text{Globals} \\
\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine_elem_i}^i :: arg \gg ret \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{ccall}(\tau, pval, \overline{spine_elem_i}^i) \Rightarrow ret
\end{array}
\quad \text{TY_SEQ_E_CCALL}$$

$$\begin{array}{c}
name:arg \in \text{Globals} \\
\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine_elem_i}^i :: arg \gg ret \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{pcall}(name, \overline{spine_elem_i}^i) \Rightarrow ret
\end{array}
\quad \text{TY_SEQ_E_PROC}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is_expr \Rightarrow ret}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \text{loc} \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \text{memop}(\text{intFromPtr}(\tau_1, \tau_2, pval)) \Rightarrow \Sigma y:\text{integer}. y = \text{cast_ptr_to_int } pval \wedge \text{I}
\end{array}
\quad \text{TY_IS_E_MEMOP_INTFROMPTR}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \text{integer} \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \text{memop}(\text{ptrFromInt}(\tau_1, \tau_2, pval)) \Rightarrow \Sigma y:\text{loc}. y = \text{cast_int_to_ptr } pval \wedge \text{I}
\end{array}
\quad \text{TY_IS_E_MEMOP_PTRFROMINT}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \text{loc} \\
\text{smt}(\Phi \Rightarrow pval_0 = pval_1) \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \cdot, r: \langle pval_0 \xrightarrow{\checkmark} \tau _ \rangle \vdash \text{memop}(\text{ptrValidForDeref}(\tau, pval_1)) \Rightarrow \Sigma y:\text{bool}. y = \text{aligned}(\tau, pval_0) \wedge \text{I}
\end{array}
\quad \text{TY_IS_E_MEMOP_PTRVALIDFORDEREF}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \text{loc} \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \text{memop}(\text{ptrWellAligned}(\tau, pval)) \Rightarrow \Sigma y:\text{bool}. y = \text{aligned}(\tau, pval) \wedge \text{I}
\end{array}
\quad \text{TY_IS_E_MEMOP_PTRWELLALIGNED}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \text{loc} \\
\mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \text{integer} \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \text{memop}(\text{ptrArrayShift}(pval_1, \tau, pval_2)) \Rightarrow \Sigma y:\text{loc}. y = pval_1 +_{\text{ptr}} (pval_2 \times \text{size_of}(\tau)) \wedge \text{I}
\end{array}
\quad \text{TY_IS_E_MEMOP_PTRARRAYSHIFT}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{mem_action} \Rightarrow \text{ret}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{mem_action} \Rightarrow \text{ret}} \quad \text{TY_IS_E_ACTION}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{mem_action} \Rightarrow \text{ret}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{neg mem_action} \Rightarrow \text{ret}} \quad \text{TY_IS_E_NEG_ACTION}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{seq_expr} \Leftarrow \text{ret}}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{tval} \Leftarrow \text{ret}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{tval} \Leftarrow \text{ret}} \quad \text{TY_SEQ_TE_TVAL}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash \text{pexpr} \Rightarrow y:\beta. \text{term} \\ y \text{ as ident_or_pattern}:\beta \rightsquigarrow \mathcal{C}_1; \Phi_1 \\ \mathcal{C}, \mathcal{C}_1; \mathcal{L}, y:\beta; \Phi, \text{term}, \Phi_1; \mathcal{R} \vdash \text{texpr} \Leftarrow \text{ret} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{let ident_or_pattern} = \text{pexpr in texpr} \Leftarrow \text{ret}} \quad \text{TY_SEQ_TE_LETP}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash \text{tpexpr} \Leftarrow y:\beta. \text{term} \\ y \text{ as ident_or_pattern}:\beta \rightsquigarrow \mathcal{C}_1; \Phi_1 \\ \mathcal{C}, \mathcal{C}_1; \mathcal{L}, y:\beta; \Phi, \text{term}, \Phi_1; \mathcal{R} \vdash \text{texpr} \Leftarrow \text{ret} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{let ident_or_pattern}:(y:\beta. \text{term}) = \text{tpexpr in texpr} \Leftarrow \text{ret}} \quad \text{TY_SEQ_TE_LETPPT}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}' \vdash \text{seq_expr} \Rightarrow \text{ret}_1 \\ \overline{\text{ret_pattern}_i}^i : \text{ret}_1 \rightsquigarrow \mathcal{C}_1; \mathcal{L}_1; \Phi_1; \mathcal{R}_1 \\ \mathcal{C}, \mathcal{C}_1; \mathcal{L}, \mathcal{L}_1; \Phi, \Phi_1; \mathcal{R}, \mathcal{R}_1 \vdash \text{texpr} \Leftarrow \text{ret}_2 \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}', \mathcal{R} \vdash \text{let } \overline{\text{ret_pattern}_i}^i = \text{seq_expr in texpr} \Leftarrow \text{ret}_2} \quad \text{TY_SEQ_TE_LET}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}' \vdash \text{texpr}_1 \Leftarrow \text{ret}_1 \\ \overline{\text{ret_pattern}_i}^i : \text{ret}_1 \rightsquigarrow \mathcal{C}_1; \mathcal{L}_1; \Phi_1; \mathcal{R}_1 \\ \mathcal{C}, \mathcal{C}_1; \mathcal{L}, \mathcal{L}_1; \Phi, \Phi_1; \mathcal{R}, \mathcal{R}_1 \vdash \text{texpr}_2 \Leftarrow \text{ret}_2 \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}', \mathcal{R} \vdash \text{let } \overline{\text{ret_pattern}_i}^i : \text{ret}_1 = \text{texpr}_1 \text{ in texpr}_2 \Leftarrow \text{ret}_2} \quad \text{TY_SEQ_TE_LETT}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta_1 \\
\hline
y_1 \text{ as } pattern_i : \beta_1 \rightsquigarrow \mathcal{C}_i; \Phi_i^i \\
\hline
\mathcal{C}, \mathcal{C}_i; \mathcal{L}, y_1 : \beta_1; \Phi, y_1 = pval, \Phi_i; \mathcal{R} \vdash texpr_i \Leftarrow ret^i \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{case } pval \text{ of } | pattern_i \Rightarrow texpr_i^i \text{ end} \Leftarrow ret
\end{array}
\quad \text{TY_SEQ_TE_CASE}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \text{bool} \\
\mathcal{C}; \mathcal{L}; \Phi, pval = \text{true}; \mathcal{R} \vdash texpr_1 \Leftarrow ret \\
\mathcal{C}; \mathcal{L}; \Phi, pval = \text{false}; \mathcal{R} \vdash texpr_2 \Leftarrow ret \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{if } pval \text{ then } texpr_1 \text{ else } texpr_2 \Leftarrow ret
\end{array}
\quad \text{TY_SEQ_TE_IF}$$

$$\begin{array}{c}
ident : arg \in \text{Globals} \\
\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \overline{pval_i}^i :: arg \gg \text{false} \wedge \text{I} \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \text{run } ident \overline{pval_i}^i \Leftarrow \text{false} \wedge \text{I}
\end{array}
\quad \text{TY_SEQ_TE_RUN}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is_texpr \Leftarrow ret \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{bound}[int](is_texpr) \Leftarrow ret
\end{array}
\quad \text{TY_SEQ_TE_BOUND}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is_texpr \Leftarrow ret}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is_expr \Rightarrow ret_1 \\
\overline{ret_pattern_i}^i : ret_1 \rightsquigarrow \mathcal{C}_1; \mathcal{L}_1; \Phi_1; \mathcal{R}_1 \\
\mathcal{C}, \mathcal{C}_1; \mathcal{L}, \mathcal{L}_1; \Phi, \Phi_1; \mathcal{R}, \mathcal{R}_1 \vdash texpr \Leftarrow ret_2 \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{let strong } \overline{ret_pattern_i}^i = is_expr \text{ in } texpr \Leftarrow ret_2
\end{array}
\quad \text{TY_IS_TE_LETS}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is_texpr \Leftarrow ret \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is_texpr \Leftarrow ret
\end{array}
\quad \text{TY_TE_IS}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash seq_expr \Leftarrow ret}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash seq_expr \Leftarrow ret} \quad \text{TY_TE_SEQ}$$

$$\boxed{pattern = pval \rightsquigarrow \sigma}$$

$$\frac{}{\therefore = pval \rightsquigarrow \cdot} \quad \text{OP_DECONS_VALUE_NO_SYM_ANNOT}$$

$$\frac{}{x \therefore = pval \rightsquigarrow pval/x, \cdot} \quad \text{OP_DECONS_VALUE_SYM_ANNOT}$$

$$\frac{\begin{array}{l} pattern_1 = pval_1 \rightsquigarrow \sigma_1 \\ pattern_2 = pval_2 \rightsquigarrow \sigma_2 \end{array}}{\text{Cons}(pattern_1, pattern_2) = \text{Cons}(pval_1, pval_2) \rightsquigarrow \sigma_1, \sigma_2} \quad \text{OP_DECONS_VALUE_CONS}$$

$$\frac{\overline{pattern_i = pval_1 \rightsquigarrow \sigma_i^i}}{\text{Tuple}(\overline{pattern_i^i}) = \text{Tuple}(\overline{pval_i^i}) \rightsquigarrow \overline{\sigma_i^i}} \quad \text{OP_DECONS_VALUE_TUPLE}$$

$$\frac{\overline{pattern_i = pval_1 \rightsquigarrow \sigma_i^i}}{\text{Array}(\overline{pattern_i^i}) = \text{Array}(\overline{pval_i^i}) \rightsquigarrow \overline{\sigma_i^i}} \quad \text{OP_DECONS_VALUE_ARRAY}$$

$$\frac{pattern = pval \rightsquigarrow \sigma}{\text{Specified}(pattern) = pval \rightsquigarrow \sigma} \quad \text{OP_DECONS_VALUE_SPECIFIED}$$

$$\boxed{ident_or_pattern = pval \rightsquigarrow \sigma}$$

$$\frac{}{x = pval \rightsquigarrow pval/x, \cdot} \quad \text{OP_DECONS_VALUE_SYM}$$

$$\frac{pattern = pval \rightsquigarrow \sigma}{pattern = pval \rightsquigarrow \sigma} \quad \text{OP_DECONS_VALUE_PATTERN}$$

$$\boxed{res_pattern = res_term \rightsquigarrow \sigma}$$

$$\frac{}{emp = emp \rightsquigarrow \cdot} \quad \text{OP_DECONS_RES_EMP}$$

$$\frac{}{pt = pt \rightsquigarrow \cdot} \quad \text{OP_DECONS_RES_POINTS_TO}$$

$$\frac{}{ident = res_term \rightsquigarrow res_term/ident, \cdot} \quad \text{OP_DECONS_RES_VAR}$$

$$\frac{\begin{array}{l} res_pattern_1 = res_term_1 \rightsquigarrow \sigma_1 \\ res_pattern_2 = res_term_2 \rightsquigarrow \sigma_2 \end{array}}{\langle res_pattern_1, res_pattern_2 \rangle = \langle res_term_1, res_term_2 \rangle \rightsquigarrow \sigma_1, \sigma_2} \quad \text{OP_DECONS_RES_PAIR}$$

$$\frac{res_pattern = res_term \rightsquigarrow \sigma}{\mathbf{pack}(ident, res_pattern) = \mathbf{pack}(pval, res_term) \rightsquigarrow pval/ident, \sigma} \quad \text{OP_DECONS_RES_PACK}$$

$$\boxed{ret_pattern = spine_elem \rightsquigarrow \sigma}$$

$$\frac{ident_or_pattern = pval \rightsquigarrow \sigma}{\mathbf{comp} \ ident_or_pattern = pval \rightsquigarrow \sigma} \quad \text{OP_DECONS_RET_COMP}$$

$$\frac{}{\mathbf{log} \ ident = term \rightsquigarrow term/ident, \cdot} \quad \text{OP_DECONS_RET_LOG}$$

$$\frac{res_pattern = res_term \rightsquigarrow \sigma}{res \ res_pattern = res_term \rightsquigarrow \sigma} \quad \text{OP_DECONS_RET_RES}$$

$$\boxed{\langle pepr \rangle \longrightarrow \langle pepr' \rangle}$$

$$\frac{mem_ptr' \equiv mem_ptr +_{ptr} mem_int \times size_of(\tau)}{\langle array_shift(mem_ptr, \tau, mem_int) \rangle \longrightarrow \langle mem_ptr' \rangle} \quad OP_PE_PE_ARRAYSHIFT$$

$$\frac{mem_ptr' \equiv mem_ptr +_{ptr} offset_of_tag(member)}{\langle member_shift(mem_ptr, tag, member) \rangle \longrightarrow \langle mem_ptr' \rangle} \quad OP_PE_PE_MEMBERSHIFT$$

$$\overline{\langle not(True) \rangle} \longrightarrow \langle False \rangle \quad OP_PE_PE_NOTTRUE$$

$$\overline{\langle not(False) \rangle} \longrightarrow \langle True \rangle \quad OP_PE_PE_NOTFALSE$$

$$\frac{mem_int \equiv mem_int_1 binop_{arith} mem_int_2}{\langle mem_int_1 binop_{arith} mem_int_2 \rangle \longrightarrow \langle mem_int \rangle} \quad OP_PE_PE_ARITH_BINOP$$

$$\frac{bool_value \equiv mem_int_1 binop_{rel} mem_int_2}{\langle mem_int_1 binop_{rel} mem_int_2 \rangle \longrightarrow \langle bool_value \rangle} \quad OP_PE_PE_REL_BINOP$$

$$\frac{bool_value \equiv bool_value_1 binop_{bool} bool_value_2}{\langle bool_value_1 binop_{bool} bool_value_2 \rangle \longrightarrow \langle bool_value \rangle} \quad OP_PE_PE_BOOL_BINOP$$

$$\overline{\langle assert_undef(True, UB_name) \rangle} \longrightarrow \langle Unit \rangle \quad OP_PE_PE_ASSERT_UNDEF$$

$$\overline{\langle bool_to_integer(True) \rangle} \longrightarrow \langle 1 \rangle \quad OP_PE_PE_BOOL_TO_INTEGER_TRUE$$

$$\overline{\langle bool_to_integer(False) \rangle} \longrightarrow \langle 0 \rangle \quad OP_PE_PE_BOOL_TO_INTEGER_FALSE$$

$$\begin{array}{l}
abbrev_1 \equiv \max_int_\tau - \min_int_\tau + 1 \\
abbrev_2 \equiv pval \mathbf{rem_f} abbrev_1 \\
mem_int' \equiv \mathbf{if} abbrev_2 \leq \max_int_\tau \mathbf{then} abbrev_2 \mathbf{else} abbrev_2 - abbrev_1 \\
\hline
\langle \mathbf{wrapI}(\tau, mem_int) \rangle \longrightarrow \langle mem_int' \rangle \quad \text{OP_PE_PE_WRAP I}
\end{array}$$

$$\boxed{\langle pexpr \rangle \longrightarrow \langle texpr:(y:\beta. term) \rangle}$$

$$\begin{array}{l}
name \equiv \overline{x_i}^i \mapsto texpr:(y:\beta. term) \in \mathbf{Globals} \\
\hline
\langle name(\overline{pval_i}^i) \rangle \longrightarrow \langle \overline{pval_i/x_i, \cdot}^i(texpr):(y:\beta. \overline{pval_i/x_i, \cdot}^i(term)) \rangle \quad \text{OP_PE_TPE_CALL}
\end{array}$$

$$\boxed{\langle texpr \rangle \longrightarrow \langle texpr' \rangle}$$

$$\begin{array}{l}
pattern_j = pval \rightsquigarrow \sigma_j \\
\forall i < j. \mathbf{not} (pattern_i = pval \rightsquigarrow \sigma_i) \\
\hline
\langle \mathbf{case} pval \mathbf{of} \mid \overline{pattern_i \Rightarrow texpr_i}^i \mathbf{end} \rangle \longrightarrow \langle \sigma_j(texpr_j) \rangle \quad \text{OP_TPE_TPE_CASE}
\end{array}$$

$$\begin{array}{l}
ident_or_pattern = pval \rightsquigarrow \sigma \\
\hline
\langle \mathbf{let} ident_or_pattern = pval \mathbf{in} texpr \rangle \longrightarrow \langle \sigma(texpr) \rangle \quad \text{OP_TPE_TPE_LET_SUB}
\end{array}$$

$$\begin{array}{l}
\langle pexpr \rangle \longrightarrow \langle pexpr' \rangle \\
\hline
\langle \mathbf{let} ident_or_pattern = pexpr \mathbf{in} texpr \rangle \longrightarrow \langle \mathbf{let} ident_or_pattern = pexpr' \mathbf{in} texpr \rangle \quad \text{OP_TPE_TPE_LET_LET}
\end{array}$$

$$\begin{array}{l}
\langle pexpr \rangle \longrightarrow \langle texpr_1:(y:\beta. term) \rangle \\
\hline
\langle \mathbf{let} ident_or_pattern = pexpr \mathbf{in} texpr_2 \rangle \longrightarrow \langle \mathbf{let} ident_or_pattern:(y:\beta. term) = texpr_1 \mathbf{in} texpr_2 \rangle \quad \text{OP_TPE_TPE_LET_LETT}
\end{array}$$

$$\begin{array}{l}
ident_or_pattern = pval \rightsquigarrow \sigma \\
\hline
\langle \mathbf{let} ident_or_pattern:(y:\beta. term) = \mathbf{done} pval \mathbf{in} texpr \rangle \longrightarrow \langle \sigma(texpr) \rangle \quad \text{OP_TPE_TPE_LETT_SUB}
\end{array}$$

$$\frac{\langle texpr_1 \rangle \longrightarrow \langle texpr'_1 \rangle}{\langle \text{let } ident_or_pattern:(y:\beta. term) = texpr_1 \text{ in } texpr_2 \rangle \longrightarrow \langle \text{let } ident_or_pattern:(y:\beta. term) = texpr'_1 \text{ in } texpr_2 \rangle} \quad \text{OP_TPE_TPE_LETT_LETT}$$

$$\frac{}{\langle \text{if True then } texpr_1 \text{ else } texpr_2 \rangle \longrightarrow \langle texpr_1 \rangle} \quad \text{OP_TPE_TPE_IF_TRUE}$$

$$\frac{}{\langle \text{if False then } texpr_1 \text{ else } texpr_2 \rangle \longrightarrow \langle texpr_2 \rangle} \quad \text{OP_TPE_TPE_IF_FALSE}$$

$$\boxed{\langle seq_expr \rangle \longrightarrow \langle texpr:ret \rangle}$$

$$\frac{pval \equiv \overline{x_i}^i \mapsto texpr:ret \in \text{Globals}}{\langle \text{ccall } (\tau, pval, \overline{spine_elem_i}^i) \rangle \longrightarrow \langle \overline{spine_elem_i/x_i, \cdot}^i (texpr):\overline{spine_elem_i/x_i, \cdot}^i (ret) \rangle} \quad \text{OP_SE_TE_CCALL}$$

$$\frac{name \equiv \overline{x_i}^i \mapsto texpr:ret \in \text{Globals}}{\langle \text{pcall } (name, \overline{spine_elem_i}^i) \rangle \longrightarrow \langle \overline{spine_elem_i/x_i, \cdot}^i (texpr):\overline{spine_elem_i/x_i, \cdot}^i (ret) \rangle} \quad \text{OP_SE_TE_PCALL}$$

$$\boxed{\langle h; seq_texpr \rangle \longrightarrow \langle h'; texpr \rangle}$$

$$\frac{ident \equiv \overline{x_i}^i \mapsto texpr:_ \in \text{Globals}}{\langle h; \text{run } ident \overline{pval_i}^i \rangle \longrightarrow \langle h; \overline{pval_i/x_i, \cdot}^i (texpr) \rangle} \quad \text{OP_STE_TE_RUN}$$

$$\frac{\begin{array}{l} pattern_j = pval \rightsquigarrow \sigma_j \\ \forall i < j. \text{ not } (pattern_i = pval \rightsquigarrow \sigma_i) \end{array}}{\langle h; \text{case } pval \text{ of } \overline{pattern_i \Rightarrow texpr_i}^i \text{ end} \rangle \longrightarrow \langle h; \sigma_j(texpr_j) \rangle} \quad \text{OP_STE_TE_CASE}$$

$$\frac{ident_or_pattern = pval \rightsquigarrow \sigma}{\langle h; \text{let } ident_or_pattern = pval \text{ in } texpr \rangle \longrightarrow \langle h; \sigma(texpr) \rangle} \quad \text{OP_STE_TE_LETP_SUB}$$

$$\frac{\langle pexpr \rangle \longrightarrow \langle pexpr' \rangle}{\langle h; \text{let } ident_or_pattern = pexpr \text{ in } texpr \rangle \longrightarrow \langle h; \text{let } ident_or_pattern = pexpr' \text{ in } texpr \rangle} \quad \text{OP_STE_TE_LETP_LETP}$$

$$\frac{\langle pexpr \rangle \longrightarrow \langle texpr:(y:\beta. term) \rangle}{\langle h; \text{let } ident_or_pattern = pexpr \text{ in } texpr \rangle \longrightarrow \langle h; \text{let } ident_or_pattern:(y:\beta. term) = texpr \text{ in } texpr \rangle} \quad \text{OP_STE_TE_LETP_LETP}$$

$$\frac{ident_or_pattern = pval \rightsquigarrow \sigma}{\langle h; \text{let } ident_or_pattern:(y:\beta. term) = \text{done } pval \text{ in } texpr \rangle \longrightarrow \langle h; \sigma(texpr) \rangle} \quad \text{OP_STE_TE_LETP_SUB}$$

$$\frac{\langle texpr \rangle \longrightarrow \langle texpr' \rangle}{\langle h; \text{let } ident_or_pattern:(y:\beta. term) = texpr \text{ in } texpr \rangle \longrightarrow \langle h; \text{let } ident_or_pattern:(y:\beta. term) = texpr' \text{ in } texpr \rangle} \quad \text{OP_STE_TE_LETP_LETP}$$

$$\frac{\overline{ret_pattern_i = spine_elem_i \rightsquigarrow \sigma_i^i}}{\langle h; \text{let } \overline{ret_pattern_i^i} : ret = \text{done } spine_elem_i^i \text{ in } texpr \rangle \longrightarrow \langle h; \overline{\sigma_i^i}(texpr) \rangle} \quad \text{OP_STE_TE_LETT_SUB}$$

$$\frac{\langle seq_expr \rangle \longrightarrow \langle texpr_1 : ret \rangle}{\langle h; \text{let } \overline{ret_pattern_i^i} = seq_expr \text{ in } texpr_2 \rangle \longrightarrow \langle h; \text{let } \overline{ret_pattern_i^i} : ret = texpr_1 \text{ in } texpr_2 \rangle} \quad \text{OP_STE_TE_LETT_LETT}$$

$$\frac{\langle h; texpr_1 \rangle \longrightarrow \langle h'; texpr_1' \rangle}{\langle h; \text{let } \overline{ret_pattern_i^i} : ret = texpr_1 \text{ in } texpr_2 \rangle \longrightarrow \langle h; \text{let } \overline{ret_pattern_i^i} : ret = texpr_1' \text{ in } texpr_2 \rangle} \quad \text{OP_STE_TE_LETT_LETT}$$

$$\frac{}{\langle h; \text{if True then } texpr_1 \text{ else } texpr_2 \rangle \longrightarrow \langle h; texpr_1 \rangle} \quad \text{OP_STE_TE_IF_TRUE}$$

$$\frac{}{\langle h; \text{if False then } texpr_1 \text{ else } texpr_2 \rangle \longrightarrow \langle h; texpr_2 \rangle} \quad \text{OP_STE_TE_IF_FALSE}$$

$$\frac{}{\langle h; \text{bound } [int](is_texpr) \rangle \longrightarrow \langle h; is_texpr \rangle} \quad \text{OP_STE_TE_BOUND}$$

$$\boxed{\langle mem_op \rangle \longrightarrow \langle pval \rangle}$$

$$\frac{mem_int \equiv \text{cast_ptr_to_int } pval}{\langle \text{intFromPtr } (\tau_1, \tau_2, pval) \rangle \longrightarrow \langle mem_int \rangle} \quad \text{OP_MEMOP_PVAL_INTFROMPTR}$$

$$\frac{mem_ptr \equiv \text{cast_ptr_to_int } pval}{\langle \text{ptrFromInt } (\tau_1, \tau_2, pval) \rangle \longrightarrow \langle mem_ptr \rangle} \quad \text{OP_MEMOP_PVAL_PTRFROMINT}$$

$$\frac{bool_value \equiv \text{aligned } (\tau, pval)}{\langle \text{ptrValidForDeref } (\tau, pval) \rangle \longrightarrow \langle bool_value \rangle} \quad \text{OP_MEMOP_PVAL_PTRVALIDFORDEREF}$$

$$\frac{bool_value \equiv \text{aligned } (\tau, pval)}{\langle \text{ptrWellAligned } (\tau, pval) \rangle \longrightarrow \langle bool_value \rangle} \quad \text{OP_MEMOP_PVAL_PTRWELLALIGNED}$$

$$\frac{mem_ptr \equiv pval_1 +_{\text{ptr}} (pval_2 \times \text{size_of } (\tau))}{\langle \text{ptrArrayShift } (pval_1, \tau, pval_2) \rangle \longrightarrow \langle mem_ptr \rangle} \quad \text{OP_MEMOP_PVAL_PTRARRAYSHIFT}$$

$$\boxed{\langle h; mem_action \rangle \longrightarrow \langle h'; spine \rangle}$$

$$\frac{\text{fresh } (mem_ptr)}{\langle h; \text{create } (pval, \tau) \rangle \longrightarrow \langle h + \{ mem_ptr \mapsto \times \}; mem_ptr, -, \mathbf{pt} \rangle} \quad \text{OP_ACTION_SPINE_CREATE}$$

$$\frac{}{\langle h + \{ mem_ptr \mapsto - \}; \text{store } (-, \tau, mem_ptr, pval, -) \rangle \longrightarrow \langle h + \{ mem_ptr \mapsto pval \}; \mathbf{Unit}, \mathbf{pt} \rangle} \quad \text{OP_ACTION_SPINE_STORE}$$

$$\frac{}{\langle h + \{ mem_ptr \mapsto - \}; \text{kill } (\text{static } \tau, mem_ptr) \rangle \longrightarrow \langle h; \mathbf{Unit} \rangle} \quad \text{OP_ACTION_SPINE_KILL_STATIC}$$

$$\boxed{\langle h; is_expr \rangle \longrightarrow \langle h'; is_expr' \rangle}$$

$$\frac{\langle mem_op \rangle \longrightarrow \langle pval \rangle}{\langle h; \mathbf{memop}(mem_op) \rangle \longrightarrow \langle h; \mathbf{done} \ pval \rangle} \quad \text{OP_ISE_ISE_MEMOP}$$

$$\frac{\langle h; mem_action \rangle \longrightarrow \langle h; spine \rangle}{\langle h; mem_action \rangle \longrightarrow \langle h; \mathbf{done} \ spine \rangle} \quad \text{OP_ISE_ISE_ACTION}$$

$$\frac{\langle h; mem_action \rangle \longrightarrow \langle h'; spine \rangle}{\langle h; \mathbf{neg} \ mem_action \rangle \longrightarrow \langle h'; \mathbf{done} \ spine \rangle} \quad \text{OP_ISE_ISE_NEG_ACTION}$$

$$\boxed{\langle h; is_expr \rangle \longrightarrow \langle h'; expr \rangle}$$

$$\frac{\overline{ret_pattern_i = spine_elem_i \rightsquigarrow \sigma_i^i}}{\langle h; \mathbf{let strong} \ \overline{ret_pattern_i^i} = \mathbf{done} \ \overline{spine_elem_i^i} \ \mathbf{in} \ expr \rangle \longrightarrow \langle h; \overline{\sigma_i^i}(expr) \rangle} \quad \text{OP_ISTE_ISTE_LETS_SUB}$$

$$\frac{\langle h; is_expr \rangle \longrightarrow \langle h'; is_expr' \rangle}{\langle h; \mathbf{let strong} \ \overline{ret_pattern_i^i} = is_expr \ \mathbf{in} \ expr \rangle \longrightarrow \langle h'; \mathbf{let strong} \ \overline{ret_pattern_i^i} = is_expr' \ \mathbf{in} \ expr \rangle} \quad \text{OP_ISTE_ISTE_LETS_LETS}$$

$$\boxed{\langle h; expr \rangle \longrightarrow \langle h'; expr' \rangle}$$

$$\frac{\langle h; seq_expr \rangle \longrightarrow \langle h; expr \rangle}{\langle h; seq_expr \rangle \longrightarrow \langle h; expr \rangle} \quad \text{OP_TE_TE_SEQ}$$

$$\frac{\langle h; is_expr \rangle \longrightarrow \langle h'; expr \rangle}{\langle h; is_expr \rangle \longrightarrow \langle h'; expr \rangle} \quad \text{OP_TE_TE_IS}$$

Definition rules: 168 good 0 bad
Definition rule clauses: 366 good 0 bad