

<i>ident, x, y, y_p, y_f, -, abbrev, r</i>	subscripts: p for pointers, f for functions
<i>n, i, j</i>	index variables
<i>impl_const</i>	implementation-defined constant
<i>mem_int</i>	memory integer value
<i>member</i>	C struct/union member name
	Ott-hack, ignore (annotations)
<i>nat</i>	OCaml arbitrary-width natural number
<i>mem_ptr</i>	abstract pointer value
<i>mem_val</i>	abstract memory value
	Ott-hack, ignore (locations)
<i>mem_iv_c</i>	OCaml type for memory constraints on integer values
<i>UB_name</i>	undefined behaviour
<i>string</i>	OCaml string
	Ott-hack, ignore (OCaml type variable TY)
	Ott-hack, ignore (OCaml Symbol.prefix)
<i>mem_order, _</i>	OCaml type for memory order
<i>linux_mem_order</i>	OCaml type for Linux memory order
<i>logical_val</i>	logical values (to be specified)
	Ott-hack, ignore (OCaml type variable bt)

$Stypes_t, \tau$	$::=$	C type
	$\tau*$	pointer to type τ
tag	$::=$	OCaml type for struct/union tag
	$ident$	
$\beta, -$	$::=$	base types
	unit	unit
	bool	boolean
	integer	integer
	real	rational numbers?
	loc	location
	array β	array
	list β	list
	$\overline{\beta_i}^i$	tuple
	struct tag	struct
	set β	set
	opt (β)	option
	$\beta \rightarrow \beta'$	parameter types
	β_τ M	of a C type
$binop$	$::=$	binary operators
	+	addition
	-	subtraction
	*	multiplication
	/	division
	rem_t	modulus
	rem_f	remainder
	^	exponentiation
	=	equality, defined both for integer and C types

		>	greater than
		<	less than
		>=	greater than or equal to
		<=	less than or equal to
		&\	conjunction
		\	disjunction
<i>binop_{arith}</i>	::=		arithmetic binary operators
		+	
		-	
		*	
		/	
		rem_t	
		rem_f	
		^	
<i>binop_{rel}</i>	::=		relational binary operators
		=	
		>	
		<	
		>=	
		<=	
<i>binop_{bool}</i>	::=		boolean binary operators
		&\	
		\	
<i>object_value</i>	::=		C object values (inhabitants of object types), which can be read/stored
		<i>mem_int</i>	integer value
		<i>mem_ptr</i>	pointer value

		<code>array</code> ($\overline{loaded_value_i}^i$)	C array value
		<code>(struct ident)</code> { $\overline{.member_i:\tau_i = mem_val_i}^i$ }	C struct value
		<code>(union ident)</code> { $.member = mem_val$ }	C union value
<i>loaded_value</i>	<code>::=</code>		potentially unspecified C object values
		<code>specified object_value</code>	specified loaded value
<i>value</i>	<code>::=</code>		Core values
		<i>object_value</i>	C object value
		<i>loaded_value</i>	loaded C object value
		<code>Unit</code>	unit
		<code>True</code>	boolean true
		<code>False</code>	boolean false
		$\beta[\overline{value_i}^i]$	list
		$(\overline{value_i}^i)$	tuple
<i>ctor_val</i>	<code>::=</code>		data constructors
		<code>Nil</code> β	empty list
		<code>Cons</code>	list cons
		<code>Tuple</code>	tuple
		<code>Array</code>	C array
		<code>Specified</code>	non-unspecified loaded value
<i>ctor_expr</i>	<code>::=</code>		data constructors
		<code>Ivmax</code>	max integer value
		<code>Ivmin</code>	min integer value
		<code>Ivsizeof</code>	sizeof value
		<code>Ivalignof</code>	alignof value
		<code>IvCOMPL</code>	bitwise complement
		<code>IvAND</code>	bitwise AND

		IvOR	bitwise OR
		IvXOR	bitwise XOR
		Fvfromint	cast integer to floating value
		Ivfromfloat	cast floating to integer value
<i>name</i>	::=		
		<i>ident</i>	Core identifier
		<i>impl_const</i>	implementation-defined constant
<i>pval</i>	::=		pure values
		<i>ident</i>	Core identifier
		<i>impl_const</i>	implementation-defined constant
		<i>value</i>	Core values
		constrained ($\overline{mem_iv_c_i}, pval_i^i$)	constrained value
		error (<i>string</i> , <i>pval</i>)	impl-defined static error
		<i>ctor_val</i> ($\overline{pval_i^i}$)	data constructor application
		(struct <i>ident</i>){ $\overline{.member_i = pval_i^i}$ }	C struct expression
		(union <i>ident</i>){ $\overline{.member = pval}$ }	C union expression
<i>pexpr</i>	::=		pure expressions
		<i>pval</i>	pure values
		<i>ctor_expr</i> ($\overline{pval_i^i}$)	data constructor application
		array_shift (<i>pval</i> ₁ , τ , <i>pval</i> ₂)	pointer array shift
		member_shift (<i>pval</i> , <i>ident</i> , <i>member</i>)	pointer struct/union member shift
		not (<i>pval</i>)	boolean not
		<i>pval</i> ₁ <i>binop</i> <i>pval</i> ₂	binary operations
		memberof (<i>ident</i> , <i>member</i> , <i>pval</i>)	C struct/union member access
		<i>name</i> ($\overline{pval_i^i}$)	pure function call
		assert_undef (<i>pval</i> , <i>UB_name</i>)	
		bool_to_integer (<i>pval</i>)	

	<code>conv_int</code> $(\tau, pval)$ <code>wrapI</code> $(\tau, pval)$	
<i>tpval</i>	<code>::=</code> <code>undef</code> <i>UB_name</i> <code>done</code> <i>pval</i>	top-level pure values undefined behaviour pure done
<i>ident_opt_β</i>	<code>::=</code> <code>_:β</code> <i>ident</i> : <i>β</i>	type annotated optional identifier
<i>pattern</i>	<code>::=</code> <i>ident_opt_β</i> <i>ctor_val</i> ($\overline{pattern_i}^i$)	
<i>ident_or_pattern</i>	<code>::=</code> <i>ident</i> <i>pattern</i>	
<i>tpexpr</i>	<code>::=</code> <i>tpval</i> <code>case</code> <i>pval</i> <code>of</code> $\overline{pattern_i \Rightarrow tpexpr_i}^i$ <code>end</code> <code>let</code> <i>ident_or_pattern</i> = <i>pexpr</i> <code>in</code> <i>tpexpr</i> <code>if</code> <i>pval</i> <code>then</code> <i>tpexpr</i> ₁ <code>else</code> <i>tpexpr</i> ₂ $[C/C']tpexpr$	top-level pure expressions top-level pure values pattern matching pure let pure if M simul-sub all vars in <i>C</i> for all vars in <i>C'</i> in <i>tpexpr</i>
<i>m_kill_kind</i>	<code>::=</code> <code>dynamic</code> <code>static</code> <i>τ</i>	

<i>bool</i> , <i>_</i>	$::=$ true false	OCaml booleans
<i>int</i> , <i>_</i>	$::=$ <i>i</i>	OCaml fixed-width integer literal integer
<i>mem_action</i>	$::=$ create (<i>pval</i> , τ) create_readonly (<i>pval</i> ₁ , τ , <i>pval</i> ₂) alloc (<i>pval</i> ₁ , <i>pval</i> ₂) kill (<i>m_kill_kind</i> , <i>pval</i>) store (<i>bool</i> , τ , <i>pval</i> ₁ , <i>pval</i> ₂ , <i>mem_order</i>) load (τ , <i>pval</i> , <i>mem_order</i>) rmw (τ , <i>pval</i> ₁ , <i>pval</i> ₂ , <i>pval</i> ₃ , <i>mem_order</i> ₁ , <i>mem_order</i> ₂) fence (<i>mem_order</i>) cmp_exch_strong (τ , <i>pval</i> ₁ , <i>pval</i> ₂ , <i>pval</i> ₃ , <i>mem_order</i> ₁ , <i>mem_order</i> ₂) cmp_exch_weak (τ , <i>pval</i> ₁ , <i>pval</i> ₂ , <i>pval</i> ₃ , <i>mem_order</i> ₁ , <i>mem_order</i> ₂) linux_fence (<i>linux_mem_order</i>) linux_load (τ , <i>pval</i> , <i>linux_mem_order</i>) linux_store (τ , <i>pval</i> ₁ , <i>pval</i> ₂ , <i>linux_mem_order</i>) linux_rmw (τ , <i>pval</i> ₁ , <i>pval</i> ₂ , <i>linux_mem_order</i>)	memory actions true means store is locking
<i>polarity</i>	$::=$ Pos Neg	polarities for memory actions sequenced by let weak and let strong only sequenced by let strong
<i>pol_mem_action</i>	$::=$ <i>polarity mem_action</i>	memory actions with polarity

<i>mem_op</i>	$::=$ $pval_1 \equiv pval_2$ $pval_1 \neq pval_2$ $pval_1 < pval_2$ $pval_1 > pval_2$ $pval_1 \leq pval_2$ $pval_1 \geq pval_2$ $pval_1 -_{\tau} pval_2$ $\text{intFromPtr}(\tau_1, \tau_2, pval)$ $\text{ptrFromInt}(\tau_1, \tau_2, pval)$ $\text{ptrValidForDeref}(\tau, pval)$ $\text{ptrWellAligned}(\tau, pval)$ $\text{ptrArrayShift}(pval_1, \tau, pval_2)$ $\text{memcpy}(pval_1, pval_2, pval_3)$ $\text{memcmp}(pval_1, pval_2, pval_3)$ $\text{realloc}(pval_1, pval_2, pval_3)$ $\text{va_start}(pval_1, pval_2)$ $\text{va_copy}(pval)$ $\text{va_arg}(pval, \tau)$ $\text{va_end}(pval)$	operations involving the memory state pointer equality comparison pointer inequality comparison pointer less-than comparison pointer greater-than comparison pointer less-than comparison pointer greater-than comparison pointer subtraction cast of pointer value to integer value cast of integer value to pointer value dereferencing validity predicate
<i>res_term</i>	$::=$ emp pt <i>ident</i> $\langle res_term_1, res_term_2 \rangle$ pack (<i>pval</i> , <i>res_term</i> ₂)	resource terms empty heap single-cell heap variable seperating-conjunction pair packing for existentials
<i>spine_elem</i>	$::=$ <i>pval</i>	spine element pure value

		<i>logical_val</i>	logical variable
		<i>res_term</i>	resource value
<i>tval</i>	::=		(effectful) top-level values
		done $\overline{spine_elem_i}^i$	end of top-level expression
		undef <i>UB_name</i>	undefined behaviour
<i>res_pattern</i>	::=		resource terms
		emp	empty heap
		pt	single-cell heap
		<i>ident</i>	variable
		$\langle res_pattern_1, res_pattern_2 \rangle$	seperating-conjunction pair
		pack (<i>ident</i> , <i>res_pattern</i>)	packing for existentials
<i>ret_pattern</i>	::=		return pattern
		comp <i>ident_or_pattern</i>	computational variable
		log <i>ident</i>	logical variable
		res <i>res_pattern</i>	resource variable
<i>bool_op</i>	::=		
		$\neg term$	
		$term_1 = term_2$	
		$\bigwedge(\overline{term_i}^i)$	
		$\bigvee(\overline{term_i}^i)$	
		$term_1 \text{ binop}_{bool} term_2$	M
		if $term_1$ then $term_2$ else $term_3$	
<i>arith_op</i>	::=		
		$term_1 + term_2$	
		$term_1 - term_2$	

	$ \begin{array}{l} \quad term_1 \times term_2 \\ \quad term_1 / term_2 \\ \quad term_1 \mathbf{rem_t} term_2 \\ \quad term_1 \mathbf{rem_f} term_2 \\ \quad term_1 \wedge term_2 \\ \quad term_1 \mathit{binop}_{arith} term_2 \quad \mathbf{M} \end{array} $	
cmp_op	$ \begin{array}{l} ::= \\ \quad term_1 < term_2 \quad \text{less than} \\ \quad term_1 \leq term_2 \quad \text{less than or equal} \\ \quad term_1 \mathit{binop}_{rel} term_2 \quad \mathbf{M} \end{array} $	
$list_op$	$ \begin{array}{l} ::= \\ \quad \mathbf{nil} \\ \quad \mathbf{tl} \, term \\ \quad term^{(int)} \end{array} $	
$tuple_op$	$ \begin{array}{l} ::= \\ \quad (\overline{term_i})^i \\ \quad term^{(int)} \end{array} $	
$pointer_op$	$ \begin{array}{l} ::= \\ \quad mem_ptr \\ \quad term_1 +_{ptr} term_2 \end{array} $	
$option_op$	$ \begin{array}{l} ::= \\ \quad \mathbf{none} \, \beta \\ \quad \mathbf{some} \, term \end{array} $	
$array_op$	$::=$	

		$term_1[term_2]$		
$param_op$	$::=$	$ident:\beta.term$ $term(term_1, .., term_n)$		
$struct_op$	$::=$	$term.member$		
ct_pred	$::=$	representable ($\tau, term$) alignedI ($term_1, term_2$)		
$term, _$	$::=$	lit $arith_op$ $bool_op$ cmp_op $tuple_op$ $struct_op$ $pointer_op$ $list_op$ $array_op$ ct_pred $option_op$ $param_op$ $(term)$ $[term_1/ident]term_2$ $pval$	S M M	parentheses substitute $term_1$ for $ident$ in $term_2$ only the ones which can be embeded into the SMT value grammar, so no array literals

$init,$	$::=$		initialisation status
		\checkmark	initialised
		\times	uninitialised
$points_to$	$::=$		arbitrary predicate
		$term_1 \mathbb{Q} \stackrel{init}{\mapsto}_{\tau} term_2$	
$resource$	$::=$		resources
		\mathbf{emp}	empty heap
		$points_to$	points-top heap pred.
		$resource_1 \star resource_2$	seperating conjunction
		$\exists ident:\beta. resource$	existential
		$term \wedge resource$	logical conjunction
		$\langle resource \rangle$	S parentheses
		$[pval/ident]resource$	M substitute $pval$ for $ident$ in $resource$
$ret, _$	$::=$		return types
		$\Sigma ident:\beta. ret$	
		$\exists ident:\beta. ret$	
		$resource \star ret$	
		$term \wedge ret$	
		\mathbf{I}	
		$[spine_elem/ident]ret$	M
seq_expr	$::=$		sequential (effectful) expressions
		$pexpr$	pure expressions
		$\mathbf{ccall}(\tau, pval, \overline{spine_elem_i}^i)$	C function call
		$\mathbf{pcall}(name, \overline{spine_elem_i}^i)$	procedure call
seq_texpr	$::=$		sequential top-level (effectful) expressions

	$tval$ $\text{run } ident \ pval_1, \dots, pval_n$ $\text{nd } (pval_1, \dots, pval_n)$ $\text{let } \overline{ret_pattern_i}^i = seq_expr \text{ in } texpr$ $\text{let } \overline{ret_pattern_i}^i : ret = texpr_1 \text{ in } texpr_2$ $\text{case } pval \text{ of } \mid pattern_i \Rightarrow texpr_i^i \text{ end}$ $\text{if } pval \text{ then } texpr_1 \text{ else } texpr_2$ $\text{bound } [int](is_texpr)$	(effectful) top-level values run from label nondeterministic choice bind return patterns annotated bind return patterns pattern matching conditional limit scope of indet seq behaviour, absent at runtime
is_expr	$::=$ $\mid \text{memop } (mem_op)$ $\mid \text{pol_mem_action}$ $\mid \text{unseq } (texpr_1, \dots, texpr_n)$	indet seq (effectful) expressions pointer op involving memory memory action unsequenced expressions
is_texpr	$::=$ $\mid \text{let weak } pattern = is_expr \text{ in } \mu_texpr_aux$ $\mid \text{let strong } ident_or_pattern = is_expr \text{ in } \mu_texpr_aux$	indet seq top-level (effectful) expressions weak sequencing strong sequencing
$texpr$	$::=$ $\mid seq_texpr$ $\mid is_texpr$ $\mid [C/C']texpr$	top-level (effectful) expressions sequential (effectful) expressions indet seq (effectful) expressions M simul-sub all vars in C for all vars in C' in $texpr$
$terminals$	$::=$ $\mid \lambda$ $\mid \longrightarrow$ $\mid \rightarrow$ $\mid \rightsquigarrow$ $\mid \Rightarrow$ $\mid \Leftarrow$	

	\vdash
	\in
	Π
	\forall
	$\neg \circ$
	\supset
	Σ
	\exists
	\star
	\times
	\wedge
	\bigwedge
	\neg
	$=$
	\neq
	\leq
	\geq
	$\&$
	\cdot
	$ $
	\vdash_{ptr}
	\mapsto
	$*$
	$::$
	\checkmark
	$:$
	\cdot
	\cdot
	\gg

		::	
		\wedge	
		\vee	
		\equiv	
		\langle	
		\rangle	
z	::=		OCaml arbitrary-width integer
		i	M literal integer
		$\text{to_int}(\text{mem_int})$	M
		$\text{size_of}(\tau)$	M size of a C type
		$\text{offset_of}_{\text{tag}}(\text{member})$	M offset of a struct member
		ptr_size	M size of a pointer
		max_int_τ	M maximum value of int of type τ
		min_int_τ	M minimum value of int of type τ
\mathbb{Q}	::=		OCaml type for rational numbers
		$\frac{\text{int}_1}{\text{int}_2}$	
lit	::=		
		ident	
		unit	
		bool	
		z	
		\mathbb{Q}	
arg	::=		argument/function types
		$\Pi \text{ident}:\beta. \text{arg}$	
		$\forall \text{ident}:\beta. \text{arg}$	
		$\text{resource} \multimap \text{arg}$	

	$ \begin{array}{l} \quad term \supset arg \\ \quad ret \\ \quad [spine_elem/ident]arg \quad \mathbf{M} \end{array} $	
$pure_arg$	$ \begin{array}{l} ::= \\ \quad \Pi ident:\beta. pure_arg \\ \quad term \supset pure_arg \\ \quad pure_ret \end{array} $	pure argument/function types
$pure_ret$	$ \begin{array}{l} ::= \\ \quad \Sigma ident:\beta. pure_ret \\ \quad term \wedge pure_ret \\ \quad \mathbf{I} \end{array} $	pure return types
\mathcal{C}	$ \begin{array}{l} ::= \\ \quad . \\ \quad \mathcal{C}, ident:\beta \\ \quad \overline{\mathcal{C}_i}^i \\ \quad fresh(\mathcal{C}) \quad \mathbf{M} \end{array} $	computational var env identical context except with fresh variable names
\mathcal{L}	$ \begin{array}{l} ::= \\ \quad . \\ \quad \overline{\mathcal{L}_i}^i \\ \quad \mathcal{L}, ident:\beta \\ \quad [\mathcal{C}/\mathcal{C}']\mathcal{L} \quad \mathbf{M} \end{array} $	logical var env
Φ	$ \begin{array}{l} ::= \\ \quad . \\ \quad \Phi, term \\ \quad \overline{\Phi_i}^i \end{array} $	constraints env

		$[\mathcal{C}/\mathcal{C}']\Phi$	M
\mathcal{R}	::=		resources env
		.	
		$\mathcal{R}, \text{ident}:\text{resource}$	
		$\mathcal{R}_1, \mathcal{R}_2$	
		$[\mathcal{C}/\mathcal{C}']\mathcal{R}$	M
<i>formula</i>	::=		
		<i>judgement</i>	
		<i>abbrev</i> \equiv <i>term</i>	
		smt ($\Phi \Rightarrow \text{term}$)	
		<i>ident</i> : $\beta \in \mathcal{C}$	
		<i>ident</i> : struct tag & $\overline{\text{member}_i:\tau_i}^i \in \mathbf{Globals}$	
		$\overline{\mathcal{C}_i;\mathcal{L}_i;\Phi_i \vdash \text{mem_val}_i \Rightarrow \text{mem } \beta_i}^i$	dependent on memory object model
		$\overline{\mathcal{C}_i;\mathcal{L}_i;\Phi_i \vdash \text{pval}_i \Rightarrow \beta_i}^i$	
		<i>name</i> : <i>arg</i> $\in \mathbf{Globals}$	
		$\overline{\text{term}_i \text{ as pattern}_i:\beta_i \rightsquigarrow \mathcal{C}_i;\Phi_i}^i$	
		$\overline{\mathcal{C}_i;\mathcal{L}_i;\Phi_i \vdash \text{texpr}_i \Leftarrow y_i:\beta_i. \text{term}_i}^i$	
		$\overline{\mathcal{C}_i;\mathcal{L}_i;\Phi_i;\mathcal{R}_i \vdash \text{texpr}_i \Leftarrow \text{ret}_i}^i$	
		$\mathcal{L} \vdash \text{logical_val}:\beta$	
		<i>pval</i> : <i>arg</i> $\in \mathbf{Globals}$	
<i>object_value_jtype</i>	::=		
		$\mathcal{C};\mathcal{L};\Phi \vdash \text{object_value} \Rightarrow \mathbf{obj } \beta$	
<i>pval_jtype</i>	::=		
		$\mathcal{C};\mathcal{L};\Phi \vdash \text{pval} \Rightarrow \beta$	
<i>resource_jtype</i>	::=		

		$resource \equiv resource'$
		$\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash res_term \Leftarrow resource$
$spine_jtype$	$::=$	
		$\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine_elem_i}^i :: arg \gg ret$
$pexpr_jtype$	$::=$	
		$\mathcal{C}; \mathcal{L}; \Phi \vdash pexpr \Rightarrow ident:\beta. term$
$pattern_jtype$	$::=$	
		$term \text{ as } pattern:\beta \rightsquigarrow \mathcal{C}; \Phi$
		$term \text{ as } ident_or_pattern:\beta \rightsquigarrow \mathcal{C}; \Phi$
		$\overline{ret_pattern_i}^i : ret \rightsquigarrow \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}$
		$res_pattern:resource \rightsquigarrow \mathcal{L}; \Phi; \mathcal{R}$
$tpval_jtype$	$::=$	
		$\mathcal{C}; \mathcal{L}; \Phi \vdash tpval \Leftarrow ident:\beta. term$
$tpexpr_jtype$	$::=$	
		$\mathcal{C}; \mathcal{L}; \Phi \vdash tpexpr \Leftarrow ident:\beta. term$
$action_jtype$	$::=$	
		$\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem_action \Rightarrow ret$
$tval_jtype$	$::=$	
		$\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash tval \Leftarrow ret$
$texpr_jtype$	$::=$	
		$\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash seq_expr \Rightarrow ret$
		$\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is_expr \Rightarrow ret$

		$\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash seq_texpr \Leftarrow ret$
		$\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is_texpr \Leftarrow ret$
		$\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash texpr \Leftarrow ret$
<i>judgement</i>	$::=$	
		<i>object_value_jtype</i>
		<i>pval_jtype</i>
		<i>resource_jtype</i>
		<i>spine_jtype</i>
		<i>pexpr_jtype</i>
		<i>pattern_jtype</i>
		<i>tpval_jtype</i>
		<i>tpexpr_jtype</i>
		<i>action_jtype</i>
		<i>tval_jtype</i>
		<i>texpr_jtype</i>
<i>user_syntax</i>	$::=$	
		<i>ident</i>
		<i>n</i>
		<i>impl_const</i>
		<i>mem_int</i>
		<i>member</i>
		<i>nat</i>
		<i>mem_ptr</i>
		<i>mem_val</i>
		<i>mem_iv_c</i>
		<i>UB_name</i>

| *string*

| *mem_order*

| *linux_mem_order*

| *logical_val*

| *Sctypes_t*

| *tag*

| β

| *binop*

| *binop_{arith}*

| *binop_{rel}*

| *binop_{bool}*

| *ident*

| τ

| *ident*

| *object_value*

| *loaded_value*

| β

| *value*

| *ctor_val*

| *ctor_expr*

| τ

| *name*

| *pval*

| *pval*

| *pexpr*

| *pexpr*

$tpval$
 $tpval$
 $ident_opt_β$
 $pattern$
 $pattern$
 $ident_or_pattern$
 $tpepr$
 $tpepr$
 m_kill_kind
 $bool$
 int
 mem_action
 mem_action
 $polarity$
 pol_mem_action
 mem_op
 res_term
 $spine_elem$
 $tval$
 $tval$
 $res_pattern$
 $ret_pattern$
 $bool_op$
 $arith_op$
 cmp_op
 $list_op$
 $tuple_op$
 $pointer_op$
 $β$

- | *option_op*
- | *array_op*
- | *param_op*
- | *struct_op*
- | *ct_pred*
- | *term*
- | *term*
- | *init*
- | *points_to*
- | *resource*
- | *ret*
- | *seq_expr*
- | *seq_expr*
- | *seq_texpr*
- | *seq_texpr*
- | *is_expr*
- | *is_expr*
- | *is_texpr*
- | *is_texpr*
- | *texpr*
- | *terminals*
- | *z*
- | \mathbb{Q}
- | *lit*
- | *arg*
- | *pure_arg*
- | *pure_ret*
- | \mathcal{C}
- | \mathcal{L}

Φ
 \mathcal{R}
formula

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{object_value} \Rightarrow \text{obj } \beta}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{mem_int} \Rightarrow \text{obj integer}} \text{PVAL_OBJ_INT}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{mem_ptr} \Rightarrow \text{obj loc}} \text{PVAL_OBJ_PTR}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{loaded_value}_i \Rightarrow \beta^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{array}(\text{loaded_value}_i^i) \Rightarrow \text{obj array } \beta} \text{PVAL_OBJ_ARR}$$

$$\frac{\begin{array}{c} \text{ident: struct tag} \ \& \ \overline{\text{member}_i: \tau_i^i} \in \text{Globals} \\ \mathcal{C}; \mathcal{L}; \Phi \vdash \text{mem_val}_i \Rightarrow \text{mem } \beta_i^i \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash (\text{struct tag})\{ \overline{\text{member}_i: \tau_i = \text{mem_val}_i^i} \} \Rightarrow \text{obj struct tag}} \text{PVAL_OBJ_STRUCT}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval} \Rightarrow \beta}$$

$$\frac{x: \beta \in \mathcal{C}}{\mathcal{C}; \mathcal{L}; \Phi \vdash x \Rightarrow \beta} \text{PVAL_VAR}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{object_value} \Rightarrow \text{obj } \beta}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{object_value} \Rightarrow \beta} \text{PVAL_OBJ}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{object_value} \Rightarrow \text{obj } \beta}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{specified_object_value} \Rightarrow \beta} \text{PVAL_LOADED}$$

$$\begin{array}{c}
\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathbf{Unit} \Rightarrow \mathbf{unit}} \quad \text{PVAL_UNIT} \\
\\
\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathbf{True} \Rightarrow \mathbf{bool}} \quad \text{PVAL_TRUE} \\
\\
\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathbf{False} \Rightarrow \mathbf{bool}} \quad \text{PVAL_FALSE} \\
\\
\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathit{value}_i \Rightarrow \beta^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \beta[\overline{\mathit{value}_i}^i] \Rightarrow \mathbf{list} \beta} \quad \text{PVAL_LIST} \\
\\
\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathit{value}_i \Rightarrow \beta_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash (\overline{\mathit{value}_i}^i) \Rightarrow \overline{\beta_i}^i} \quad \text{PVAL_TUPLE} \\
\\
\frac{\mathbf{smt}(\Phi \Rightarrow \mathbf{false})}{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathbf{error}(\mathit{string}, \mathit{pval}) \Rightarrow \beta} \quad \text{PVAL_ERROR} \\
\\
\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathbf{Nil} \beta() \Rightarrow \mathbf{list} \beta} \quad \text{PVAL_CTOR_NIL} \\
\\
\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathit{pval}_1 \Rightarrow \beta \quad \mathcal{C}; \mathcal{L}; \Phi \vdash \mathit{pval}_2 \Rightarrow \mathbf{list} \beta}{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathbf{Cons}(\mathit{pval}_1, \mathit{pval}_2) \Rightarrow \mathbf{list} \beta} \quad \text{PVAL_CTOR_CONS} \\
\\
\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathit{pval}_i \Rightarrow \beta_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathbf{Tuple}(\overline{\mathit{pval}_i}^i) \Rightarrow \overline{\beta_i}^i} \quad \text{PVAL_CTOR_TUPLE}
\end{array}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_i \Rightarrow \beta^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Array}(\overline{pval_i^i}) \Rightarrow \text{array } \beta} \quad \text{PVAL_CTOR_ARRAY}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Specified}(pval) \Rightarrow \beta} \quad \text{PVAL_CTOR_SPECIFIED}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_i \Rightarrow \beta_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash (\text{struct } tag)\{.member_i = pval_i^i\} \Rightarrow \text{struct } tag} \quad \text{PVAL_STRUCT}$$

$$\boxed{resource \equiv resource'}$$

$$\frac{}{\text{emp} \equiv \text{emp}} \quad \text{RESOURCE_EQ_EMP}$$

$$\frac{\text{smt}(\cdot \Rightarrow (term_1 = term'_1) \wedge (term_2 = term'_2))}{term_1 \mathbb{Q} \xrightarrow{\text{init}}_{\tau} term_2 \equiv term'_1 \mathbb{Q} \xrightarrow{\text{init}}_{\tau} term'_2} \quad \text{RESOURCE_EQ_POINTSTO}$$

$$\frac{\begin{array}{l} resource_1 \equiv resource'_1 \\ resource_2 \equiv resource'_2 \end{array}}{resource_1 \star resource_2 \equiv resource'_1 \star resource'_2} \quad \text{RESOURCE_EQ_SEPCONJ}$$

$$\frac{resource \equiv resource'}{\exists ident:\beta. resource \equiv \exists ident:\beta. resource'} \quad \text{RESOURCE_EQ_EXISTS}$$

$$\frac{\begin{array}{l} \text{smt}(\cdot, term \Rightarrow term') \\ \text{smt}(\cdot, term' \Rightarrow term) \\ resource \equiv resource' \end{array}}{term \wedge resource \equiv term' \wedge resource'} \quad \text{RESOURCE_EQ_TERM}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash res_term \Leftarrow resource}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \mathbf{emp} \Leftarrow \mathbf{emp}} \text{RESOURCE_EMP}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \mathbf{pt} \Leftarrow points_to} \text{RESOURCE_POINTSTO}$$

$$\frac{resource \equiv resource'}{\mathcal{C}; \mathcal{L}; \Phi; \cdot, r:resource \vdash r \Leftarrow resource'} \text{RESOURCE_VAR}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_1 \vdash res_term_1 \Leftarrow resource_1 \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_2 \vdash res_term_2 \Leftarrow resource_2 \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_1, \mathcal{R}_2 \vdash \langle res_term_1, res_term_2 \rangle \Leftarrow resource_1 \star resource_2} \text{RESOURCE_SEPCONJ}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash res_term_2 \Leftarrow [pval/y]resource \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \mathbf{pack}(pval, res_term_2) \Leftarrow \exists y:\beta. resource} \text{RESOURCE_PACK}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine_elem_i}^i :: arg \gg ret}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash ::ret \gg ret} \text{SPINE_EMPTY}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine_elem_i}^i :: [pval/x]arg \gg ret \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash pval, \overline{spine_elem_i}^i :: \Pi x:\beta. arg \gg ret} \text{SPINE_COMPUTATIONAL}$$

$$\frac{\begin{array}{l} \mathcal{L} \vdash logical_val:\beta \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine_elem_i}^i :: [logical_val/x]arg \gg ret \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash logical_val, \overline{spine_elem_i}^i :: \forall x:\beta. arg \gg ret} \text{SPINE_LOGICAL}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_1 \vdash \text{res_term} \Leftarrow \text{resource} \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_2 \vdash \overline{\text{spine_elem}_i}^i :: \text{arg} \gg \text{ret} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_1, \mathcal{R}_2 \vdash \text{res_term}, \overline{\text{spine_elem}_i}^i :: \text{resource} \multimap \text{arg} \gg \text{ret}} \quad \text{SPINE_RESOURCE}$$

$$\frac{\begin{array}{l} \text{smt}(\Phi \Rightarrow \text{term}) \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{\text{spine_elem}_i}^i :: \text{arg} \gg \text{ret} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{\text{spine_elem}_i}^i :: \text{term} \supset \text{arg} \gg \text{ret}} \quad \text{SPINE_CONSTRAINT}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pexpr} \Rightarrow \text{ident}:\beta. \text{term}}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval} \Rightarrow \beta}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval} \Rightarrow y:\beta. y = \text{pval}} \quad \text{PEXPR_VAL}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval}_1 \Rightarrow \text{loc} \\ \mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval}_2 \Rightarrow \text{integer} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{array_shift}(\text{pval}_1, \tau, \text{pval}_2) \Rightarrow y:\text{loc}. y = \text{pval}_1 +_{\text{ptr}} (\text{pval}_2 \times \text{size_of}(\tau))} \quad \text{PEXPR_ARRAY_SHIFT}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval} \Rightarrow \text{loc} \\ \therefore \text{struct tag} \ \& \ \overline{\text{member}_i:\tau_i}^i \in \text{Globals} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{member_shift}(\text{pval}, \text{tag}, \text{member}_j) \Rightarrow y:\text{loc}. y = \text{pval} +_{\text{ptr}} \text{offset_of}_{\text{tag}}(\text{member}_j)} \quad \text{PEXPR_MEMBER_SHIFT}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval} \Rightarrow \text{bool}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{not}(\text{pval}) \Rightarrow y:\text{bool}. y = \neg \text{pval}} \quad \text{PEXPR_NOT}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval}_1 \Rightarrow \text{integer} \\ \mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval}_2 \Rightarrow \text{integer} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval}_1 \ \text{binop}_{\text{arith}} \ \text{pval}_2 \Rightarrow y:\text{integer}. y = (\text{pval}_1 \ \text{binop}_{\text{arith}} \ \text{pval}_2)} \quad \text{PEXPR_ARITH_BINOP}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \text{integer} \\ \mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \text{integer} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \text{ binop}_{rel} pval_2 \Rightarrow y:\text{bool}. y = (pval_1 \text{ binop}_{rel} pval_2)} \quad \text{PEXPR_REL_BINOP}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \text{bool} \\ \mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \text{bool} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \text{ binop}_{bool} pval_2 \Rightarrow y:\text{bool}. y = (pval_1 \text{ binop}_{bool} pval_2)} \quad \text{PEXPR_BOOL_BINOP}$$

$$\frac{\begin{array}{c} name: pure_arg \in \text{Globals} \\ \mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \overline{pval_i}^i :: pure_arg \gg \Sigma y':\beta'. term' \wedge \mathbf{I} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash name(\overline{pval_i}^i) \Rightarrow y':\beta'. term'} \quad \text{PEXPR_CALL}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \text{bool} \\ \text{smt}(\Phi \Rightarrow pval) \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{assert_undef}(pval, UB_name) \Rightarrow y:\text{unit}. y = \text{unit}} \quad \text{PEXPR_ASSERT_UNDEF}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \text{bool}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{bool_to_integer}(pval) \Rightarrow y:\text{integer}. y = \text{if } pval \text{ then } 1 \text{ else } 0} \quad \text{PEXPR_BOOL_TO_INTEGER}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \text{integer} \\ abbrev_1 \equiv \max_int_\tau - \min_int_\tau + 1 \\ abbrev_2 \equiv pval \text{ rem } f \text{ abbrev}_1 \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{wrapI}(\tau, pval) \Rightarrow y':\beta. y = \text{if } abbrev_2 \leq \max_int_\tau \text{ then } abbrev_2 \text{ else } abbrev_2 - abbrev_1} \quad \text{PEXPR_WRAP I}$$

$term \text{ as } pattern:\beta \rightsquigarrow \mathcal{C}; \Phi$

$$\frac{}{term \text{ as } \cdot:\beta:\beta \rightsquigarrow \cdot;\cdot} \quad \text{COMP_PATTERN_NO_SYM_ANNOT}$$

$$\frac{}{term \text{ as } x:\beta:\beta \rightsquigarrow \cdot, x:\beta;\cdot, x = term} \quad \text{COMP_PATTERN_SYM_ANNOT}$$

$$\frac{}{term \text{ as Nil } \beta():\text{list } \beta \rightsquigarrow \cdot;\cdot} \quad \text{COMP_PATTERN_NIL}$$

$$\frac{\begin{array}{l} term^{(1)} \text{ as } pattern_1:\beta \rightsquigarrow \mathcal{C}_1;\Phi_1 \\ \text{tl } term \text{ as } pattern_2:\text{list } \beta \rightsquigarrow \mathcal{C}_2;\Phi_1 \end{array}}{term \text{ as Cons}(pattern_1, pattern_2):\text{list } \beta \rightsquigarrow \mathcal{C}_1, \mathcal{C}_2;\Phi_1, \Phi_2} \quad \text{COMP_PATTERN_CONS}$$

$$\frac{\overline{term^{(i)} \text{ as } pattern_i:\beta_i \rightsquigarrow \mathcal{C}_i;\Phi_i}^i}{term \text{ as Tuple}(\overline{pattern_i}^i):\overline{\beta_i}^i \rightsquigarrow \overline{\mathcal{C}_i}^i;\overline{\Phi_i}^i} \quad \text{COMP_PATTERN_TUPLE}$$

$$\frac{\overline{term[i] \text{ as } pattern_i:\beta \rightsquigarrow \mathcal{C}_i;\Phi_i}^i}{term \text{ as Array}(\overline{pattern_i}^i):\text{array } \beta \rightsquigarrow \overline{\mathcal{C}_i}^i;\overline{\Phi_i}^i} \quad \text{COMP_PATTERN_ARRAY}$$

$$\frac{term \text{ as } pattern:\beta \rightsquigarrow \mathcal{C};\Phi}{term \text{ as Specified}(pattern):\beta \rightsquigarrow \mathcal{C};\Phi} \quad \text{COMP_PATTERN_SPECIFIED}$$

$$\boxed{term \text{ as ident_or_pattern}:\beta \rightsquigarrow \mathcal{C};\Phi}$$

$$\frac{}{term \text{ as } x:\beta \rightsquigarrow \cdot, x:\beta;\cdot, x = term} \quad \text{SYM_OR_PATTERN_SYM}$$

$$\frac{term \text{ as } pattern:\beta \rightsquigarrow \mathcal{C};\Phi}{term \text{ as } pattern:\beta \rightsquigarrow \mathcal{C};\Phi} \quad \text{SYM_OR_PATTERN_PATTERN}$$

$$\boxed{\overline{ret_pattern_i}^i:ret \rightsquigarrow \mathcal{C};\mathcal{L};\Phi;\mathcal{R}}$$

$$\frac{}{\text{I} \rightsquigarrow \cdot; \cdot; \cdot} \text{RET_PATTERN_EMPTY}$$

$$\frac{\frac{y \text{ as } \text{ident_or_pattern} : \beta \rightsquigarrow \mathcal{C}_1; \Phi_1}{\overline{\text{ret_pattern}_i}^i : \text{ret} \rightsquigarrow \mathcal{C}_2; \mathcal{L}_2; \Phi_2; \mathcal{R}_2}}{\text{comp } \text{ident_or_pattern}, \overline{\text{ret_pattern}_i}^i : \Sigma y : \beta. \text{ret} \rightsquigarrow \mathcal{C}_1, \mathcal{C}_2; \mathcal{L}_2; \Phi_2; \mathcal{R}_2} \text{RET_PATTERN_COMPUTATIONAL}$$

$$\frac{\overline{\text{ret_pattern}_i}^i : \text{ret} \rightsquigarrow \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}}{\text{log } y, \overline{\text{ret_pattern}_i}^i : \exists y : \beta. \text{ret} \rightsquigarrow \mathcal{C}; \mathcal{L}; y : \beta; \Phi; \mathcal{R}} \text{RET_PATTERN_LOGICAL}$$

$$\frac{\frac{\text{res_pattern} : \text{resource} \rightsquigarrow \mathcal{L}_1; \Phi_1; \mathcal{R}_1}{\overline{\text{ret_pattern}_i}^i : \text{ret} \rightsquigarrow \mathcal{C}_2; \mathcal{L}_2; \Phi_2; \mathcal{R}_2}}{\text{res } \text{res_pattern}, \overline{\text{ret_pattern}_i}^i : \text{resource} \star \text{ret} \rightsquigarrow \mathcal{C}_2; \mathcal{L}_1, \mathcal{L}_2; \Phi_1, \Phi_2; \mathcal{R}_1, \mathcal{R}_2} \text{RET_PATTERN_RESOURCE}$$

$$\frac{\overline{\text{ret_pattern}_i}^i : \text{ret} \rightsquigarrow \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}}{\overline{\text{ret_pattern}_i}^i : \text{term} \wedge \text{ret} \rightsquigarrow \mathcal{C}; \mathcal{L}; \Phi, \text{term}; \mathcal{R}} \text{RET_PATTERN_CONSTRAINT}$$

$$\boxed{\text{res_pattern} : \text{resource} \rightsquigarrow \mathcal{L}; \Phi; \mathcal{R}}$$

$$\frac{}{\text{emp} : \text{emp} \rightsquigarrow \cdot; \cdot; \cdot} \text{RES_PATTERN_EMPTY}$$

$$\frac{}{\text{pt} : \text{points_to} \rightsquigarrow \cdot; \cdot; \cdot, r : \text{points_to}} \text{RES_PATTERN_POINTSTO}$$

$$\frac{}{r : \text{resource} \rightsquigarrow \cdot; \cdot; \cdot, r : \text{resource}} \text{RES_PATTERN_VAR}$$

$$\frac{\begin{array}{c} \text{res_pattern}_1:\text{resource}_1 \rightsquigarrow \mathcal{L}_1; \Phi_1; \mathcal{R}_1 \\ \text{res_pattern}_2:\text{resource}_2 \rightsquigarrow \mathcal{L}_2; \Phi_2; \mathcal{R}_2 \end{array}}{\langle \text{res_pattern}_1, \text{res_pattern}_2 \rangle : \text{resource}_1 \star \text{resource}_2 \rightsquigarrow \mathcal{L}_1, \mathcal{L}_2; \Phi_1, \Phi_2; \mathcal{R}_1, \mathcal{R}_2} \quad \text{RES_PATTERN_SEP_CONJ}$$

$$\frac{\text{res_pattern}:\text{resource} \rightsquigarrow \mathcal{L}; \Phi; \mathcal{R}}{\text{res_pattern}:\text{term} \wedge \text{resource} \rightsquigarrow \mathcal{L}; \Phi, \text{term}; \mathcal{R}} \quad \text{RES_PATTERN_CONJ}$$

$$\frac{\text{res_pattern}:[x/y]\text{resource} \rightsquigarrow \mathcal{L}; \Phi; \mathcal{R}}{\text{pack}(x, \text{res_pattern}):\exists y:\beta. \text{resource} \rightsquigarrow \mathcal{L}, x:\beta; \Phi; \mathcal{R}} \quad \text{RES_PATTERN_PACK}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{tpval} \Leftarrow \text{ident}:\beta. \text{term}}$$

$$\frac{\text{smt}(\Phi \Rightarrow \text{false})}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{undef } UB_name \Leftarrow y:\beta. \text{term}} \quad \text{TPVAL_UNDEF}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval} \Rightarrow \beta \\ \text{smt}(\Phi \Rightarrow \text{term}) \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{done pval} \Leftarrow y:\beta. \text{term}} \quad \text{TPVAL_DONE}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{tpexpr} \Leftarrow \text{ident}:\beta. \text{term}}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval} \Rightarrow \text{bool} \\ \mathcal{C}; \mathcal{L}; \Phi, \text{pval} = \text{true} \vdash \text{tpexpr}_1 \Leftarrow y:\beta. \text{term} \\ \mathcal{C}; \mathcal{L}; \Phi, \text{pval} = \text{false} \vdash \text{tpexpr}_2 \Leftarrow y:\beta. \text{term} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{if pval then tpexpr}_1 \text{ else tpexpr}_2 \Leftarrow y:\beta. \text{term}} \quad \text{TPEXPR_IF}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash \text{pexpr} \Rightarrow y_1:\beta_1. \text{term}_1 \\ y_1 \text{ as ident_or_pattern}:\beta_1 \rightsquigarrow \mathcal{C}_1; \Phi_1 \\ \mathcal{C}, \text{fresh}(\mathcal{C}_1); \mathcal{L}, y_1:\beta_1; \Phi, \text{term}_1, [\text{fresh}(\mathcal{C}_1)/\mathcal{C}_1]\Phi_1 \vdash [\text{fresh}(\mathcal{C}_1)/\mathcal{C}_1]\text{tpexpr} \Leftarrow y_2:\beta_2. \text{term}_2 \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{let ident_or_pattern} = \text{pexpr in tpexpr} \Leftarrow y_2:\beta_2. \text{term}_2} \quad \text{TPEXPR_LET}$$

$$\frac{\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta_1}{y_1 \text{ as } pattern_i : \beta_1 \rightsquigarrow \mathcal{C}_i; \Phi_i^i} \quad \frac{\mathcal{C}, \text{fresh}(\mathcal{C}_i); \mathcal{L}, y_1 : \beta_1; \Phi, y_1 = pval, [\text{fresh}(\mathcal{C}_i)/\mathcal{C}_i] \Phi_i \vdash [\text{fresh}(\mathcal{C}_i)/\mathcal{C}_i] tpepr_i \Leftarrow y_2 : \beta_2. term_2^i}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{case } pval \text{ of } [pattern_i \Rightarrow tpepr_i^i] \text{ end} \Leftarrow y_2 : \beta_2. term_2} \quad \text{TPEXPR_CASE}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem_action \Rightarrow ret}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \text{integer}}{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \text{create}(pval, \tau) \Rightarrow \Sigma y_p : \text{loc}. \exists y : \beta_\tau. \text{representable}(\tau*, y_p) \wedge \text{alignedI}(pval, y_p) \wedge \langle y_p \rangle 1 \mapsto_\tau y \star \text{I}} \quad \text{ACTION_CREATE}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \text{loc} \\ \mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \beta_\tau \\ \text{smt}(\Phi \Rightarrow \text{representable}(\tau, pval_2)) \\ \text{smt}(\Phi \Rightarrow pval_0 = pval_1) \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \cdot, r : \langle pval_0 \rangle 1 \mapsto_\tau \cdot \vdash \text{store}(\cdot, \tau, pval_1, pval_2, \cdot) \Rightarrow \Sigma \cdot : \text{unit}. pval_0 \overset{\checkmark}{1 \mapsto_\tau} pval_2 \star \text{I}} \quad \text{ACTION_STORE}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \text{loc} \\ \text{smt}(\Phi \Rightarrow pval_0 = pval_1) \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \cdot, r : \langle pval_0 \rangle 1 \mapsto_\tau \cdot \vdash \text{kill}(\text{static } \tau, pval_1) \Rightarrow \Sigma \cdot : \text{unit}. \text{I}} \quad \text{ACTION_KILL_STATIC}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash tval \Leftarrow ret}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{done} \Leftarrow \text{I}} \quad \text{TVAL_I}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{done } \overline{spine_elem_i}^i \Leftarrow [pval/y]ret \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{done } pval, \overline{spine_elem_i}^i \Leftarrow \Sigma y : \beta. ret} \quad \text{TVAL_COMPUTATIONAL}$$

$$\frac{\mathcal{L} \vdash \text{logical_val}:\beta \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{done } \overline{\text{spine_elem}_i}^i \Leftarrow [\text{logical_val}/y] \text{ret}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{done } \text{logical_val}, \overline{\text{spine_elem}_i}^i \Leftarrow \exists y:\beta. \text{ret}} \text{TVAl_LOGICAL}$$

$$\frac{\text{smt}(\Phi \Rightarrow \text{term}) \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{done } \overline{\text{spine_elem}_i}^i \Leftarrow \text{ret}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{done } \overline{\text{spine_elem}_i}^i \Leftarrow \text{term} \wedge \text{ret}} \text{TVAl_CONSTRAINT}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_1 \vdash \text{res_term} \Leftarrow \text{resource} \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_2 \vdash \text{done } \overline{\text{spine_elem}_i}^i \Leftarrow \text{ret}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_1, \mathcal{R}_2 \vdash \text{done } \text{res_term}, \overline{\text{spine_elem}_i}^i \Leftarrow \text{resource} \star \text{ret}} \text{TVAl_RESOURCE}$$

$$\frac{\text{smt}(\Phi \Rightarrow \text{false})}{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \text{undef } \text{UB_name} \Leftarrow \text{ret}} \text{TVAl_UB}$$

$\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{seq_expr} \Rightarrow \text{ret}$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pexpr} \Rightarrow y:\beta. \text{term}}{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \text{pval} \Rightarrow \Sigma y:\beta. \text{term} \wedge \text{I}} \text{SEQ_EXPR_PURE}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval} \Rightarrow \text{loc} \quad \text{pval:arg} \in \text{Globals} \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{\text{spine_elem}_i}^i :: \text{arg} \gg \text{ret}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{ccall}(\tau, \text{pval}, \overline{\text{spine_elem}_i}^i) \Rightarrow \text{ret}} \text{SEQ_EXPR_CCALL}$$

$$\frac{\text{name:arg} \in \text{Globals} \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{\text{spine_elem}_i}^i :: \text{arg} \gg \text{ret}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{pcall}(\text{name}, \overline{\text{spine_elem}_i}^i) \Rightarrow \text{ret}} \text{SEQ_EXPR_PROC}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is_expr \Rightarrow ret}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem_action \Rightarrow ret}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash Pos\ mem_action \Rightarrow ret} \quad IS_EXPR_ACTION$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem_action \Rightarrow ret}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash Neg\ mem_action \Rightarrow ret} \quad IS_EXPR_NEG_ACTION$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash seq_texpr \Leftarrow ret}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash tval \Leftarrow ret}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash tval \Leftarrow ret} \quad SEQ_TEXPR_TVAL$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}' \vdash seq_expr \Rightarrow ret_1 \\ \overline{ret_pattern_i}^i : ret_1 \rightsquigarrow \mathcal{C}_1; \mathcal{L}_1; \Phi_1; \mathcal{R}_1 \\ \mathcal{C}, fresh(\mathcal{C}_1); \mathcal{L}, \mathcal{L}_1; \Phi, [fresh(\mathcal{C}_1)/\mathcal{C}_1]\Phi_1; \mathcal{R}, [fresh(\mathcal{C}_1)/\mathcal{C}_1]\mathcal{R}_1 \vdash [fresh(\mathcal{C}_1)/\mathcal{C}_1]texpr \Leftarrow ret \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}', \mathcal{R} \vdash \mathbf{let} \overline{ret_pattern_i}^i = seq_expr \mathbf{in} texpr \Leftarrow ret} \quad SEQ_TEXPR_LET$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}' \vdash texpr_1 \Leftarrow ret_1 \\ \overline{ret_pattern_i}^i : ret_1 \rightsquigarrow \mathcal{C}_1; \mathcal{L}_1; \Phi_1; \mathcal{R}_1 \\ \mathcal{C}, fresh(\mathcal{C}_1); \mathcal{L}, \mathcal{L}_1; \Phi, [fresh(\mathcal{C}_1)/\mathcal{C}_1]\Phi_1; \mathcal{R}, [fresh(\mathcal{C}_1)/\mathcal{C}_1]\mathcal{R}_1 \vdash [fresh(\mathcal{C}_1)/\mathcal{C}_1]texpr_2 \Leftarrow ret_2 \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}', \mathcal{R} \vdash \mathbf{let} \overline{ret_pattern_i}^i : ret_1 = texpr_1 \mathbf{in} texpr \Leftarrow ret_2} \quad SEQ_TEXPR_LETT$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta_1 \\ \overline{y_1 \mathbf{as} pattern_i : \beta_1}^i \rightsquigarrow \mathcal{C}_i; \Phi_i \\ \mathcal{C}, fresh(\mathcal{C}_i); \mathcal{L}, y_1 : \beta_1; \Phi, y_1 = pval, [fresh(\mathcal{C}_i)/\mathcal{C}_i]\Phi_i; \mathcal{R} \vdash [fresh(\mathcal{C}_i)/\mathcal{C}_i]texpr_i \Leftarrow ret \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \mathbf{case} pval \mathbf{of} \mid \overline{pattern_i \Rightarrow texpr_i}^i \mathbf{end} \Leftarrow ret} \quad SEQ_TEXPR_CASE$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \text{bool} \\
\mathcal{C}; \mathcal{L}; \Phi, pval = \text{true}; \mathcal{R}_1 \vdash \text{expr}_1 \Leftarrow \text{ret} \\
\mathcal{C}; \mathcal{L}; \Phi, pval = \text{false}; \mathcal{R}_2 \vdash \text{expr}_2 \Leftarrow \text{ret} \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}_1, \mathcal{R}_2 \vdash \text{if } pval \text{ then } \text{expr}_1 \text{ else } \text{expr}_2 \Leftarrow \text{ret}
\end{array}
\quad \text{SEQ_TEXPR_IF}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{is_expr} \Leftarrow \text{ret}}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{expr} \Leftarrow \text{ret}}$$

Definition rules: 89 good 0 bad
 Definition rule clauses: 209 good 0 bad