

<i>ident, x, y, y_p, y_f, -, abbrev</i>	subscripts: p for pointers, f for functions
<i>n, i, j</i>	index variables
<i>impl_const</i>	implementation-defined constant
<i>mem_int</i>	memory integer value
<i>member</i>	C struct/union member name
	Ott-hack, ignore (annotations)
<i>nat</i>	OCaml arbitrary-width natural number
<i>mem_ptr</i>	abstract pointer value
<i>mem_val</i>	abstract memory value
	Ott-hack, ignore (locations)
<i>mem_iv_c</i>	OCaml type for memory constraints on integer values
<i>UB_name</i>	undefined behaviour
<i>string</i>	OCaml string
	Ott-hack, ignore (OCaml type variable TY)
	Ott-hack, ignore (Symbol.prefix)
<i>mem_order, _</i>	OCaml type for memory order
<i>linux_mem_order</i>	OCaml type for Linux memory order
	Ott-hack, ignore (OCaml type variable bt)
<i>logical_val</i>	logical values (to be specified)

$Stypes_t, \tau$	$::=$	C type
	τ^*	pointer to type τ
tag	$::=$	OCaml type for struct/union tag
	$ident$	
$\beta, -$	$::=$	base types
	unit	unit
	bool	boolean
	integer	integer
	real	rational numbers?
	loc	location
	array β	array
	$[\beta]$	list
	$\overline{\beta_i}^i$	tuple
	struct tag	struct
	$\{\beta\}$	set
	opt (β)	option
	$\beta \rightarrow \beta'$	parameter types
	β_τ M	of a C type
$binop$	$::=$	binary operators
	+	addition
	-	subtraction
	*	multiplication
	/	division
	rem_t	modulus
	rem_f	remainder
	^	exponentiation
	=	equality, defined both for integer and C types

		>	greater than
		<	less than
		>=	greater than or equal to
		<=	less than or equal to
		&\	conjunction
		\	disjunction
<i>binop_{arith}</i>	::=		arithmetic binary operators
		+	
		-	
		*	
		/	
		rem_t	
		rem_f	
		^	
<i>binop_{rel}</i>	::=		relational binary operators
		=	
		>	
		<	
		>=	
		<=	
<i>binop_{bool}</i>	::=		boolean binary operators
		&\	
		\	
<i>object_value</i>	::=		C object values (inhabitants of object types), which can be read/stored
		<i>mem_int</i>	integer value
		<i>mem_ptr</i>	pointer value

		<code>array</code> ($\overline{loaded_value_i}^i$)	C array value
		<code>(struct ident)</code> { $\overline{.member_i:\tau_i = mem_val_i}^i$ }	C struct value
		<code>(union ident)</code> { $.member = mem_val$ }	C union value
<i>loaded_value</i>	::=		potentially unspecified C object values
		<code>specified object_value</code>	specified loaded value
<i>value</i>	::=		Core values
		<i>object_value</i>	C object value
		<i>loaded_value</i>	loaded C object value
		<code>Unit</code>	unit
		<code>True</code>	boolean true
		<code>False</code>	boolean false
		$\beta[\overline{value_i}^i]$	list
		$(\overline{value_i}^i)$	tuple
<i>ctor_val</i>	::=		data constructors
		<code>Nil</code> β	empty list
		<code>Cons</code>	list cons
		<code>Tuple</code>	tuple
		<code>Array</code>	C array
		<code>Specified</code>	non-unspecified loaded value
<i>ctor_expr</i>	::=		data constructors
		<code>Ivmax</code>	max integer value
		<code>Ivmin</code>	min integer value
		<code>Ivsizeof</code>	sizeof value
		<code>Ivalignof</code>	alignof value
		<code>IvCOMPL</code>	bitwise complement
		<code>IvAND</code>	bitwise AND

		IvOR	bitwise OR
		IvXOR	bitwise XOR
		Fvfromint	cast integer to floating value
		Ivfromfloat	cast floating to integer value
<i>name</i>	::=		
		<i>ident</i>	Core identifier
		<i>impl_const</i>	implementation-defined constant
<i>pval</i>	::=		pure values
		<i>ident</i>	Core identifier
		<i>impl_const</i>	implementation-defined constant
		<i>value</i>	Core values
		constrained ($\overline{mem_iv_c_i}, pval_i^i$)	constrained value
		error (<i>string</i> , <i>pval</i>)	impl-defined static error
		<i>ctor_val</i> ($\overline{pval_i^i}$)	data constructor application
		(struct <i>ident</i>){ $\overline{.member_i = pval_i^i}$ }	C struct expression
		(union <i>ident</i>){ $\overline{.member = pval}$ }	C union expression
<i>pexpr</i>	::=		pure expressions
		<i>pval</i>	pure values
		<i>ctor_expr</i> ($\overline{pval_i^i}$)	data constructor application
		array_shift (<i>pval</i> ₁ , τ , <i>pval</i> ₂)	pointer array shift
		member_shift (<i>pval</i> , <i>ident</i> , <i>member</i>)	pointer struct/union member shift
		not (<i>pval</i>)	boolean not
		<i>pval</i> ₁ <i>binop</i> <i>pval</i> ₂	binary operations
		memberof (<i>ident</i> , <i>member</i> , <i>pval</i>)	C struct/union member access
		<i>name</i> ($\overline{pval_i^i}$)	pure function call
		assert_undef (<i>pval</i> , <i>UB_name</i>)	
		bool_to_integer (<i>pval</i>)	

	<code>conv_int</code> $(\tau, pval)$	
	<code>wrapI</code> $(\tau, pval)$	
<i>tpval</i>	::=	top-level pure values
	<code>undef</code> <i>UB_name</i>	undefined behaviour
	<code>done</code> <i>pval</i>	pure done
<i>ident_opt_β</i>	::=	type annotated optional identifier
	<code>_:β</code>	
	<code>ident:β</code>	
<i>pattern</i>	::=	
	<code>ident_opt_β</code>	
	<code>ctor_val</code> $(\overline{pattern_i}^i)$	
<i>ident_or_pattern</i>	::=	
	<code>ident</code>	
	<code>pattern</code>	
<i>tpexpr</i>	::=	top-level pure expressions
	<code>tpval</code>	top-level pure values
	<code>case pval of</code> $\overline{pattern_i \Rightarrow tpexpr_i}^i$ <code>end</code>	pattern matching
	<code>let ident_or_pattern = pexpr in tpexpr</code>	pure let
	<code>if pval then tpexpr₁ else tpexpr₂</code>	pure if
	$[C/C']tpexpr$	M simul-sub all vars in \mathcal{C} for all vars in \mathcal{C}' in <i>tpexpr</i>
<i>m_kill_kind</i>	::=	
	<code>dynamic</code>	
	<code>static</code> τ	

<i>bool</i> , <i>_</i>	$::=$ true false	OCaml booleans
<i>int</i> , <i>_</i>	$::=$ <i>i</i>	OCaml fixed-width integer literal integer
<i>mem_action</i>	$::=$ create (<i>pval</i> , τ) create_readonly (<i>pval</i> ₁ , τ , <i>pval</i> ₂) alloc (<i>pval</i> ₁ , <i>pval</i> ₂) kill (<i>m_kill_kind</i> , <i>pval</i>) store (<i>bool</i> , τ , <i>pval</i> ₁ , <i>pval</i> ₂ , <i>mem_order</i>) load (τ , <i>pval</i> , <i>mem_order</i>) rmw (τ , <i>pval</i> ₁ , <i>pval</i> ₂ , <i>pval</i> ₃ , <i>mem_order</i> ₁ , <i>mem_order</i> ₂) fence (<i>mem_order</i>) cmp_exch_strong (τ , <i>pval</i> ₁ , <i>pval</i> ₂ , <i>pval</i> ₃ , <i>mem_order</i> ₁ , <i>mem_order</i> ₂) cmp_exch_weak (τ , <i>pval</i> ₁ , <i>pval</i> ₂ , <i>pval</i> ₃ , <i>mem_order</i> ₁ , <i>mem_order</i> ₂) linux_fence (<i>linux_mem_order</i>) linux_load (τ , <i>pval</i> , <i>linux_mem_order</i>) linux_store (τ , <i>pval</i> ₁ , <i>pval</i> ₂ , <i>linux_mem_order</i>) linux_rmw (τ , <i>pval</i> ₁ , <i>pval</i> ₂ , <i>linux_mem_order</i>)	memory actions true means store is locking
<i>polarity</i>	$::=$ Pos Neg	polarities for memory actions sequenced by let weak and let strong only sequenced by let strong
<i>pol_mem_action</i>	$::=$ <i>polarity mem_action</i>	memory actions with polarity

<i>mem_op</i>	$::=$ $pval_1 \equiv pval_2$ $pval_1 \neq pval_2$ $pval_1 < pval_2$ $pval_1 > pval_2$ $pval_1 \leq pval_2$ $pval_1 \geq pval_2$ $pval_1 -_{\tau} pval_2$ $\text{intFromPtr}(\tau_1, \tau_2, pval)$ $\text{ptrFromInt}(\tau_1, \tau_2, pval)$ $\text{ptrValidForDeref}(\tau, pval)$ $\text{ptrWellAligned}(\tau, pval)$ $\text{ptrArrayShift}(pval_1, \tau, pval_2)$ $\text{memcpy}(pval_1, pval_2, pval_3)$ $\text{memcmp}(pval_1, pval_2, pval_3)$ $\text{realloc}(pval_1, pval_2, pval_3)$ $\text{va_start}(pval_1, pval_2)$ $\text{va_copy}(pval)$ $\text{va_arg}(pval, \tau)$ $\text{va_end}(pval)$	operations involving the memory state pointer equality comparison pointer inequality comparison pointer less-than comparison pointer greater-than comparison pointer less-than comparison pointer greater-than comparison pointer subtraction cast of pointer value to integer value cast of integer value to pointer value dereferencing validity predicate
<i>tval</i>	$::=$ $\text{done } pval$ $\text{undef } UB_name$	(effectful) top-level values end of top-level expression undefined behaviour
<i>seq_expr</i>	$::=$ $pval$ $\text{ccall}(\tau, pval, \overline{pval_i}^i)$ $\text{pcall}(name, \overline{pval_i}^i)$	sequential (effectful) expressions pure values C function call procedure call

<i>seq_expr</i>	$::=$ <i>tval</i> run <i>ident</i> <i>pval</i> ₁ , .., <i>pval</i> _{<i>n</i>} nd (<i>pval</i> ₁ , .., <i>pval</i> _{<i>n</i>}) let <i>ident_or_pattern</i> = <i>seq_expr</i> in <i>texpr</i> case <i>pval</i> with $\overline{\text{pattern}_i \Rightarrow \text{texpr}_i}^i$ end if <i>pval</i> then <i>texpr</i> ₁ else <i>texpr</i> ₂ bound [<i>int</i>] (<i>is_expr</i>)	sequential top-level (effectful) expressions (effectful) top-level values run from label nondeterministic choice pure sequencing pattern matching conditional limit scope of indet seq behaviour, absent at runtime
<i>is_expr</i>	$::=$ memop (<i>mem_op</i>) <i>pol_mem_action</i> unseq (<i>texpr</i> ₁ , .., <i>texpr</i> _{<i>n</i>})	indet seq (effectful) expressions pointer op involving memory memory action unsequenced expressions
<i>is_texpr</i>	$::=$ let weak <i>pattern</i> = <i>is_expr</i> in <i>mu_texpr_aux</i> let strong <i>ident_or_pattern</i> = <i>is_expr</i> in <i>mu_texpr_aux</i>	indet seq top-level (effectful) expressions weak sequencing strong sequencing
<i>texpr</i>	$::=$ <i>seq_expr</i> <i>is_expr</i>	top-level (effectful) expressions sequential (effectful) expressions indet seq (effectful) expressions
<i>terminals</i>	$::=$ λ \longrightarrow \rightarrow \rightsquigarrow \Rightarrow \Leftarrow \vdash	

	\in
	Π
	\forall
	$\neg \circ$
	\cup
	Σ
	\exists
	\star
	\times
	\wedge
	\bigwedge
	\neg
	$=$
	\neq
	\leq
	\geq
	$\&$
	\cdot
	$ $
	$+_{\text{ptr}}$
	\mapsto
	$*$
	$::$
	\checkmark
	$:$
	\cdot
	\cdot
	\gg
	$::$

		\wedge	
		\vee	
		\equiv	
z	$::=$		OCaml arbitrary-width integer
		1	M
		0	M
		i	M literal integer
		$\text{to_int}(\text{mem_int})$	M
		$\text{size_of}(\tau)$	M size of a C type
		$\text{offset_of}_{\text{tag}}(\text{member})$	M offset of a struct member
		ptr_size	M size of a pointer
		max_int_{τ}	M maximum value of int of type τ
		min_int_{τ}	M minimum value of int of type τ
\mathbb{Q}	$::=$		OCaml type for rational numbers
		$\frac{\text{int}_1}{\text{int}_2}$	
lit	$::=$		
		ident	
		unit	
		bool	
		z	
		\mathbb{Q}	
bool_op	$::=$		
		$\neg \text{term}$	
		$\text{term}_1 = \text{term}_2$	
		$\bigwedge(\overline{\text{term}_i}^i)$	
		$\bigvee(\overline{\text{term}_i}^i)$	

		$term_1 \text{ binop}_{bool} term_2$	M	
		$\text{if } term_1 \text{ then } term_2 \text{ else } term_3$		
$arith_op$::=			
		$term_1 + term_2$		
		$term_1 - term_2$		
		$term_1 \times term_2$		
		$term_1 / term_2$		
		$term_1 \text{ rem_t } term_2$		
		$term_1 \text{ rem_f } term_2$		
		$term_1 ^ term_2$		
		$term_1 \text{ binop}_{arith} term_2$	M	
cmp_op	::=			
		$term_1 < term_2$		less than
		$term_1 \leq term_2$		less than or equal
		$term_1 \text{ binop}_{rel} term_2$	M	
$list_op$::=			
		nil		
		$\text{tl } term$		
		$term^{(int)}$		
$tuple_op$::=			
		$(\overline{term_i}^i)$		
		$term^{(int)}$		
$pointer_op$::=			
		$\text{of_mem_ptr } mem_ptr$		
		$term_1 +_{ptr} term_2$		

<i>option_op</i>	::=	none <i>BT_t</i> some <i>term</i>
<i>array_op</i>	::=	<i>term</i> ₁ [<i>term</i> ₂]
<i>param_op</i>	::=	<i>ident</i> : β . <i>term</i> <i>term</i> (<i>term</i> ₁ , .., <i>term</i> _{<i>n</i>})
<i>struct_op</i>	::=	<i>term.member</i>
<i>ct_pred</i>	::=	representable (τ , <i>term</i>) alignedI (<i>term</i> ₁ , <i>term</i> ₂)
<i>term</i> , _	::=	<i>lit</i> <i>arith_op</i> <i>bool_op</i> <i>cmp_op</i> <i>tuple_op</i> <i>struct_op</i> <i>pointer_op</i> <i>list_op</i> <i>array_op</i> <i>ct_pred</i> <i>option_op</i>

		$param_op$	
		$(term)$	S parentheses
		$[term_1/ident]term_2$	M substitute $term_1$ for $ident$ in $term_2$
		$pval$	M only the ones which can be embeded into the SMT value grammar, so no array literals
		$resource$	
$terms$	$::=$		non-empty list of terms
		$[term_1, \dots, term_n]$	
$predicate_name$	$::=$		names of predicates
		$Sctypes_t$	C type
		$string$	arbitrary
$init,$	$::=$		initialisation status
		\checkmark	initialised
		\times	uninitalised
$predicate$	$::=$		arbitrary predicate
		$terms_1 \mathbb{Q} \overset{init}{\mapsto}_{predicate_name} terms_2$	
$resource$	$::=$		
		$predicate$	
$spine_elem$	$::=$		spine element
		$pval$	pure value
		$logical_val$	logical variable
		$resource$	resource
arg	$::=$		argument types
		$\Pi ident:\beta. arg$	

	$ \begin{array}{l} \quad \forall ident:\beta. arg \\ \quad resource \multimap arg \\ \quad term \supset arg \\ \quad ret \\ \quad [spine_elem/ident]arg \quad \mathbf{M} \end{array} $	
$ret, _$	$ \begin{array}{l} ::= \\ \quad \Sigma ident:\beta. ret \\ \quad \exists ident:\beta. ret \\ \quad resource \star ret \\ \quad term \wedge ret \\ \quad \mathbf{I} \end{array} $	return types
\mathcal{C}	$ \begin{array}{l} ::= \\ \quad \cdot \\ \quad \mathcal{C}, ident:BT_t \\ \quad \overline{\mathcal{C}}_i^i \\ \quad \text{fresh}(\mathcal{C}) \quad \mathbf{M} \end{array} $	computational var env identical context except with fresh variable names
\mathcal{L}	$ \begin{array}{l} ::= \\ \quad \cdot \\ \quad \mathcal{L}, ident:BT_t \end{array} $	logical var env
Φ	$ \begin{array}{l} ::= \\ \quad \cdot \\ \quad \Phi, term \end{array} $	constraints env
\mathcal{R}	$ \begin{array}{l} ::= \\ \quad \cdot \\ \quad \mathcal{R}, resource \end{array} $	resources env

<i>formula</i>	$ \begin{array}{l} ::= \\ \textit{judgement} \\ \textit{abbrev} \equiv \textit{term} \\ \textbf{smt} (\Phi \Rightarrow \textit{term}) \\ \textit{ident}:\beta \in \mathcal{C} \\ \frac{\textit{ident}:\textbf{struct tag} \ \& \ \overline{\textit{member}_i:\tau_i}^i \in \mathbf{Globals}}{\mathcal{C}_i;\mathcal{L}_i;\Phi_i \vdash \textit{mem_val}_i \Rightarrow \textbf{mem } y_i:\beta_i. \textit{term}_i^i} \\ \frac{\mathcal{C}_i;\mathcal{L}_i;\Phi_i \vdash \textit{pval}_i \Rightarrow \textit{ident}_i:\beta_i. \textit{term}_i^i}{\textit{pattern}_i:\beta_i \rightsquigarrow \mathcal{C}_i^i} \\ \frac{\mathcal{C}_i;\mathcal{L}_i;\Phi_i \vdash \textit{tpexpr}_i \Leftarrow y_i:\beta_i. \textit{term}_i^i}{\mathcal{L} \vdash \textit{logical_val}:\beta} \end{array} $	dependent on memory object model
<i>object_value_jtype</i>	$ \begin{array}{l} ::= \\ \mathcal{C};\mathcal{L};\Phi \vdash \textit{object_value} \Rightarrow \textbf{obj } \textit{ident}:\beta. \textit{term} \end{array} $	
<i>pval_jtype</i>	$ \begin{array}{l} ::= \\ \mathcal{C};\mathcal{L};\Phi \vdash \textit{pval} \Rightarrow \textit{ident}:\beta. \textit{term} \end{array} $	
<i>spine_jtype</i>	$ \begin{array}{l} ::= \\ \mathcal{C};\mathcal{L};\Phi;\mathcal{R} \vdash \overline{\textit{spine_elem}_i}^i :: \textit{arg} \gg \textit{ret} \end{array} $	
<i>pexpr_jtype</i>	$ \begin{array}{l} ::= \\ \mathcal{C};\mathcal{L};\Phi \vdash \textit{pexpr} \Rightarrow \textit{ident}:\beta. \textit{term} \end{array} $	
<i>pattern_jtype</i>	$ \begin{array}{l} ::= \\ \textit{pattern}:\beta \rightsquigarrow \mathcal{C} \\ \textit{ident_or_pattern}:\beta \rightsquigarrow \mathcal{C} \end{array} $	
<i>tpval_jtype</i>	$ \begin{array}{l} ::= \\ \mathcal{C};\mathcal{L};\Phi \vdash \textit{tpval} \Leftarrow \textit{ident}:\beta. \textit{term} \end{array} $	

$$\begin{array}{lcl} \textit{texpr_jtype} & ::= & \\ & | & \mathcal{C}; \mathcal{L}; \Phi \vdash \textit{texpr} \Leftarrow \textit{ident}; \beta. \textit{term} \end{array}$$

$$\begin{array}{lcl} \textit{action_jtype} & ::= & \\ & | & \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \textit{mem_action} \Rightarrow \textit{ret} \\ & | & \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \textit{seq_expr} \Rightarrow \textit{ret} \\ & | & \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \textit{is_expr} \Rightarrow \textit{ret} \end{array}$$

$$\begin{array}{lcl} \textit{judgement} & ::= & \\ & | & \textit{object_value_jtype} \\ & | & \textit{pval_jtype} \\ & | & \textit{spine_jtype} \\ & | & \textit{pexpr_jtype} \\ & | & \textit{pattern_jtype} \\ & | & \textit{tpval_jtype} \\ & | & \textit{texpr_jtype} \\ & | & \textit{action_jtype} \end{array}$$

$$\begin{array}{lcl} \textit{user_syntax} & ::= & \\ & | & \textit{ident} \\ & | & \textit{n} \\ & | & \textit{impl_const} \\ & | & \textit{mem_int} \\ & | & \textit{member} \\ & | & \\ & | & \textit{nat} \\ & | & \textit{mem_ptr} \\ & | & \textit{mem_val} \\ & | & \\ & | & \textit{mem_iv_c} \end{array}$$

UB_name
string

mem_order
linux_mem_order

logical_val
Sctypes_t
tag

β
binop
binop_{arith}
binop_{rel}
binop_{bool}
ident

τ
ident
object_value
loaded_value
 β

value
ctor_val
ctor_expr

τ
name
pval
pval
pexpr

- | *pexpr*
- | *tpval*
- | *tpval*
- | *ident_opt_β*
- | *pattern*
- | *pattern*
- | *ident_or_pattern*
- | *tpepr*
- | *tpepr*
- | *m_kill_kind*
- | *bool*
- | *int*
- | *mem_action*
- | *mem_action*
- | *polarity*
- | *pol_mem_action*
- | *mem_op*
- | *tval*
- | *tval*
- | *seq_expr*
- | *seq_expr*
- | *seq_texpr*
- | *seq_texpr*
- | *is_expr*
- | *is_expr*
- | *is_texpr*
- | *is_texpr*
- | *texpr*
- | *terminals*

- | z
- | \mathbb{Q}
- | lit
- | $bool_op$
- | $arith_op$
- | cmp_op
- | $list_op$
- | $tuple_op$
- | $pointer_op$
- | BT_t
- | $option_op$
- | $array_op$
- | $param_op$
- | $struct_op$
- | ct_pred
- | $term$
- | $term$
- | $term$
- | $terms$
- | $predicate_name$
- | $init$
- | $predicate$
- | $resource$
- | $spine_elem$
- | arg
- | ret
- | \mathcal{C}
- | \mathcal{L}
- | Φ

| \mathcal{R}
| *formula*

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{object_value} \Rightarrow \text{obj } \text{ident}:\beta. \text{term}}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{mem_int} \Rightarrow \text{obj } y:\text{integer}. y = \text{to_int}(\text{mem_int})} \text{PVAL_OBJ_INT}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{mem_ptr} \Rightarrow \text{obj } y:\text{loc}. y = \text{of_mem_ptr } \text{mem_ptr}} \text{PVAL_OBJ_PTR}$$

$$\frac{\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{loaded_value}_i \Rightarrow y_i:\beta. \text{term}_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{array}(\text{loaded_value}_i^i) \Rightarrow \text{obj } y:\text{array } \beta. \bigwedge ([y[i]/y_i] \text{term}_i^i)} \text{PVAL_OBJ_ARR}$$

$$\frac{\frac{\text{ident}:\text{struct tag} \ \& \ \overline{\text{member}_i:\tau_i^i} \in \text{Globals}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{mem_val}_i \Rightarrow \text{mem } y_i:\beta_i. \text{term}_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash (\text{struct tag})\{\overline{\text{member}_i:\tau_i = \text{mem_val}_i^i}\} \Rightarrow \text{obj } y:\text{struct tag}. \bigwedge ([y.\text{member}_i/y_i] \text{term}_i^i)} \text{PVAL_OBJ_STRUCT}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval} \Rightarrow \text{ident}:\beta. \text{term}}$$

$$\frac{x:\beta \in \mathcal{C}}{\mathcal{C}; \mathcal{L}; \Phi \vdash x \Rightarrow y:\beta. y = x} \text{PVAL_VAR}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{object_value} \Rightarrow \text{obj } y:\beta. \text{term}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{object_value} \Rightarrow y:\beta. \text{term}} \text{PVAL_OBJ}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{object_value} \Rightarrow \text{obj } y:\beta. \text{term}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{specified_object_value} \Rightarrow y:\beta. \text{term}} \text{PVAL_LOADED}$$

$$\begin{array}{c}
\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Unit} \Rightarrow y:\text{unit}. y = \text{unit}} \quad \text{PVAL_UNIT} \\
\\
\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{True} \Rightarrow y:\text{bool}. y = \text{true}} \quad \text{PVAL_TRUE} \\
\\
\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{False} \Rightarrow y:\text{bool}. y = \text{false}} \quad \text{PVAL_FALSE} \\
\\
\frac{\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{value}_i \Rightarrow y_i:\beta. \text{term}_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \beta[\overline{\text{value}_i^i}] \Rightarrow y:[\beta]. \bigwedge ([y^{(i)}/y_i] \text{term}_i^i)} \quad \text{PVAL_LIST} \\
\\
\frac{\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{value}_i \Rightarrow y_i:\beta_i. \text{term}_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash (\overline{\text{value}_i^i}) \Rightarrow y:\overline{\beta_i^i}. \bigwedge ([y^{(i)}/y_i] \text{term}_i^i)} \quad \text{PVAL_TUPLE} \\
\\
\frac{\text{smt}(\Phi \Rightarrow \text{false})}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{error}(\text{string}, pval) \Rightarrow y:\beta. \text{term}} \quad \text{PVAL_ERROR} \\
\\
\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Nil } \beta() \Rightarrow y:[\beta]. y = \text{nil}} \quad \text{PVAL_CTOR_NIL} \\
\\
\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow y_1:\beta. \text{term}_1 \quad \mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow y_2:[\beta]. \text{term}_2}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Cons}(pval_1, pval_2) \Rightarrow y:[\beta]. [y^{(1)}/y_1] \text{term}_1 \wedge [\text{tl } y/y_2] \text{term}_2} \quad \text{PVAL_CTOR_CONS} \\
\\
\frac{\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_i \Rightarrow y_i:\beta_i. \text{term}_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Tuple}(\overline{pval_i^i}) \Rightarrow y:\overline{\beta_i^i}. \bigwedge ([y^{(i)}/y_i] \text{term}_i^i)} \quad \text{PVAL_CTOR_TUPLE}
\end{array}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_i \Rightarrow y_i:\beta. term_i}^i}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Array}(\overline{pval_i}^i) \Rightarrow y:\text{array } \beta. \bigwedge (\overline{[y[i]/y_i]term_i}^i)} \quad \text{PVAL_CTOR_ARRAY}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow y:\beta. term}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Specified}(pval) \Rightarrow y:\beta. term} \quad \text{PVAL_CTOR_SPECIFIED}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_i \Rightarrow y_i:\beta_i. term_i}^i}{\mathcal{C}; \mathcal{L}; \Phi \vdash (\text{struct tag})\{\overline{.member_i = pval_i}^i\} \Rightarrow y:\text{struct tag}. \bigwedge (\overline{[y.member_i/y_i]term_i}^i)} \quad \text{PVAL_STRUCT}$$

$\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine_elem_i}^i :: arg \gg ret$

$$\overline{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash :: ret \gg ret} \quad \text{SPINE_EMPTY}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow _:\beta. _ \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine_elem_i}^i :: [pval/x]arg \gg ret \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash pval, \overline{spine_elem_i}^i :: \Pi x:\beta. arg \gg ret} \quad \text{SPINE_COMPUTATIONAL}$$

$$\frac{\begin{array}{l} \mathcal{L} \vdash logical_val:\beta \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine_elem_i}^i :: [logical_val/x]arg \gg ret \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash logical_val, \overline{spine_elem_i}^i :: \forall x:\beta. arg \gg ret} \quad \text{SPINE_LOGICAL}$$

$$\frac{\begin{array}{l} \text{smt}(\Phi \Rightarrow resource = resource') \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine_elem_i}^i :: arg \gg ret \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}, resource \vdash resource', \overline{spine_elem_i}^i :: resource' \multimap arg \gg ret} \quad \text{SPINE_RESOURCE}$$

$$\frac{\text{smt}(\Phi \Rightarrow \text{term}) \quad \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{\text{spine_elem}_i}^i :: \text{arg} \gg \text{ret}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{\text{spine_elem}_i}^i :: \text{term} \supset \text{arg} \gg \text{ret}} \quad \text{SPINE_CONSTRAINT}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pexpr} \Rightarrow \text{ident}:\beta. \text{term}}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval} \Rightarrow y:\beta. \text{term}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval} \Rightarrow y:\beta. \text{term}} \quad \text{PEXPR_VAL}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval}_1 \Rightarrow _':\text{loc}. _ \quad \mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval}_2 \Rightarrow _':\text{integer}. _}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{array_shift}(\text{pval}_1, \tau, \text{pval}_2) \Rightarrow y:\text{loc}. y = \text{pval}_1 +_{\text{ptr}} (\text{pval}_2 \times \text{size_of}(\tau))} \quad \text{PEXPR_ARRAY_SHIFT}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval} \Rightarrow _:\text{loc}. _ \quad _':\text{struct tag} \ \& \ \overline{\text{member}_i:\tau_i}^i \in \text{Globals}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{member_shift}(\text{pval}, \text{tag}, \text{member}_j) \Rightarrow y:\text{loc}. y = \text{pval} +_{\text{ptr}} \text{offset_of}_{\text{tag}}(\text{member}_j)} \quad \text{PEXPR_MEMBER_SHIFT}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval} \Rightarrow _':\text{bool}. _}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{not}(\text{pval}) \Rightarrow y:\text{bool}. y = \neg \text{pval}} \quad \text{PEXPR_NOT}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval}_1 \Rightarrow _1:\text{integer}. _1 \quad \mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval}_2 \Rightarrow _2:\text{integer}. _2}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval}_1 \text{ binop}_{\text{arith}} \text{pval}_2 \Rightarrow y:\text{integer}. y = (\text{pval}_1 \text{ binop}_{\text{arith}} \text{pval}_2)} \quad \text{PEXPR_ARITH_BINOP}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval}_1 \Rightarrow _1:\text{integer}. _1 \quad \mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval}_2 \Rightarrow _2:\text{integer}. _2}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval}_1 \text{ binop}_{\text{rel}} \text{pval}_2 \Rightarrow y:\text{bool}. y = (\text{pval}_1 \text{ binop}_{\text{rel}} \text{pval}_2)} \quad \text{PEXPR_REL_BINOP}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow _1:\text{bool}. _1 \\ \mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow _2:\text{bool}. _2 \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \text{ binop}_{bool} pval_2 \Rightarrow y:\text{bool}. y = (pval_1 \text{ binop}_{bool} pval_2)} \quad \text{PEXPR_BOOL_BINOP}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow _:\text{bool}. _ \\ \text{smt}(\Phi \Rightarrow pval) \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{assert_undef}(pval, UB_name) \Rightarrow y:\text{unit}. y = \text{unit}} \quad \text{PEXPR_ASSERT_UNDEF}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow _:\text{bool}. _}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{bool_to_integer}(pval) \Rightarrow y:\text{integer}. y = \text{if } pval \text{ then } 1 \text{ else } 0} \quad \text{PEXPR_BOOL_TO_INTEGER}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow _:\text{integer}. _ \\ abbrev_1 \equiv \max_int_\tau - \min_int_\tau + 1 \\ abbrev_2 \equiv pval \text{ rem } f \text{ abbrev}_1 \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{wrapI}(\tau, pval) \Rightarrow y':\beta. y = \text{if } abbrev_2 \leq \max_int_\tau \text{ then } abbrev_2 \text{ else } abbrev_2 - abbrev_1} \quad \text{PEXPR_WRAP I}$$

$$\boxed{pattern:\beta \rightsquigarrow \mathcal{C}}$$

$$\frac{}{_:\beta:\beta \rightsquigarrow \cdot} \quad \text{PATTERN_NO_SYM_ANNOT}$$

$$\frac{}{x:\beta:\beta \rightsquigarrow \cdot, x:\beta} \quad \text{PATTERN_SYM_ANNOT}$$

$$\frac{}{\text{Nil } \beta():[\beta] \rightsquigarrow \cdot} \quad \text{PATTERN_NIL}$$

$$\frac{\begin{array}{c} pattern_1:\beta \rightsquigarrow \mathcal{C}_1 \\ pattern_2:[\beta] \rightsquigarrow \mathcal{C}_2 \end{array}}{\text{Cons}(pattern_1, pattern_2):[\beta] \rightsquigarrow \mathcal{C}_1, \mathcal{C}_2} \quad \text{PATTERN_CONS}$$

$$\frac{\overline{pattern_i:\beta_i \rightsquigarrow \mathcal{C}_i}^i}{\text{Tuple}(\overline{pattern_i}^i):\overline{\beta_i}^i \rightsquigarrow \overline{\mathcal{C}_i}^i} \quad \text{PATTERN_TUPLE}$$

$$\frac{\overline{pattern_i:\beta \rightsquigarrow \mathcal{C}_i}^i}{\text{Array}(\overline{pattern_i}^i):\text{array } \beta \rightsquigarrow \overline{\mathcal{C}_i}^i} \quad \text{PATTERN_ARRAY}$$

$$\frac{pattern:\beta \rightsquigarrow \mathcal{C}}{\text{Specified}(pattern):\beta \rightsquigarrow \mathcal{C}} \quad \text{PATTERN_SPECIFIED}$$

$$\boxed{ident_or_pattern:\beta \rightsquigarrow \mathcal{C}}$$

$$\frac{}{x:\beta \rightsquigarrow \cdot, x:\beta} \quad \text{SYM_OR_PATTERNSYM}$$

$$\frac{pattern:\beta \rightsquigarrow \mathcal{C}}{pattern:\beta \rightsquigarrow \mathcal{C}} \quad \text{SYM_OR_PATTERNPATTERN}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash tpval \Leftarrow ident:\beta. term}$$

$$\frac{\text{smt}(\Phi \Rightarrow \text{false})}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{undef } UB_name \Leftarrow y:\beta. term} \quad \text{TPVAL_UNDEF}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow y:\beta. term' \\ \text{smt}(\Phi, term' \Rightarrow term) \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{done } pval \Leftarrow y:\beta. term} \quad \text{TPVAL_DONE}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash tpexpr \Leftarrow ident:\beta. term}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \text{bool.} _ \\
\mathcal{C}; \mathcal{L}; \Phi, pval = \text{true} \vdash tpepr_1 \Leftarrow y:\beta. \text{term} \\
\mathcal{C}; \mathcal{L}; \Phi, pval = \text{false} \vdash tpepr_2 \Leftarrow y:\beta. \text{term} \\
\hline
\mathcal{C}; \mathcal{L}; \Phi \vdash \text{if } pval \text{ then } tpepr_1 \text{ else } tpepr_2 \Leftarrow y:\beta. \text{term}
\end{array}
\quad \text{TPEXPR_IF}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pexpr \Rightarrow \beta. _ \\
ident_or_pattern:\beta \rightsquigarrow C' \\
\mathcal{C}, \text{fresh}(C'); \mathcal{L}; \Phi \vdash [\text{fresh}(C')/C'] tpepr \Leftarrow y:\beta. \text{term} \\
\hline
\mathcal{C}; \mathcal{L}; \Phi \vdash \text{let } ident_or_pattern = pexpr \text{ in } tpepr \Leftarrow y:\beta. \text{term}
\end{array}
\quad \text{TPEXPR_LET}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta. _ \\
\overline{pattern_i:\beta \rightsquigarrow C_i^i} \\
\hline
\mathcal{C}, \text{fresh}(C_i); \mathcal{L}; \Phi \vdash [\text{fresh}(C_i)/C_i] tpepr_i \Leftarrow y:\beta. \text{term}^i \\
\hline
\mathcal{C}; \mathcal{L}; \Phi \vdash \text{case } pval \text{ of } \overline{pattern_i \Rightarrow tpepr_i^i} \text{ end} \Leftarrow y:\beta. \text{term}
\end{array}
\quad \text{TPEXPR_CASE}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem_action \Rightarrow ret}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \text{integer.} _ \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \text{create}(pval, \tau) \Rightarrow \Sigma y_p:\text{loc.} \exists y:\beta_\tau. \text{representable}(\tau*, y_p) \wedge \text{alignedI}(pval, y_p) \wedge [y_p] 1 \overset{\times}{\mapsto}_\tau [y] \star \mathbf{I}
\end{array}
\quad \text{ACTION_CREATE}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \text{loc.} _ \\
\mathcal{C}; \mathcal{L}; \Phi \vdash pval' \Rightarrow y':\beta_\tau. \text{term}' \\
\text{smt}(\Phi, \text{term}' \Rightarrow \text{representable}(\tau, y')) \\
\text{smt}(\Phi \Rightarrow pval_0 = pval_1) \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \cdot, [pval_0] 1 \mapsto_\tau [-'] \vdash \text{store}(_, \tau, pval_1, pval', _) \Rightarrow \Sigma \text{unit.} \exists y':\beta_\tau. \text{term}' \wedge [pval_0] 1 \overset{\checkmark}{\mapsto}_\tau [y'] \star \mathbf{I}
\end{array}
\quad \text{ACTION_STORE}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \text{loc.} _ \\
\text{smt}(\Phi \Rightarrow pval_0 = pval_1) \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \cdot, [pval_0] 1 \mapsto_\tau [-'] \vdash \text{kill}(\text{static } \tau, pval_1) \Rightarrow \Sigma \text{unit.} \mathbf{I}
\end{array}
\quad \text{ACTION_KILL_STATIC}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash seq_expr \Rightarrow ret}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow y:\beta. term}{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash pval \Rightarrow \Sigma y:\beta. term \wedge \mathbf{I}} \quad \text{SEQ_EXPR_PURE}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is_expr \Rightarrow ret}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem_action \Rightarrow ret}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \mathbf{Pos} mem_action \Rightarrow ret} \quad \text{IS_EXPR_ACTION}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem_action \Rightarrow ret}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \mathbf{Neg} mem_action \Rightarrow ret} \quad \text{IS_EXPR_NEG_ACTION}$$

Definition rules: 54 good 0 bad
Definition rule clauses: 123 good 0 bad