

<i>tag</i>	OCaml type for struct/union tag
<i>impl_const</i>	implementation-defined constant
<i>x, y, ident</i>	OCaml type variable for symbols
<i>ty_mem_int</i>	memory integer value
<i>mem_val</i>	memory value
<i>member</i>	C struct/union member name
$\tau$	C type
<i>annots</i>	annotations
<i>nat</i>	OCaml arbitrary-width natural number
<i>n, i</i>	index variables
<i>loc</i>	OCaml type for C source
<i>mem_iv_c</i>	OCaml type for memory constraints on integer values
<i>UB_name</i>	undefined behaviour
<i>string</i>	OCaml string
<i>tyvar_TY</i>	OCaml type variable for types
$\tau$	OCaml type for an annotated C type
<i>sym_prefix</i>	OCaml type for symbol prefix
<i>mem_order</i>	OCaml type for memory order
<i>linux_mem_order</i>	OCaml type for Linux memory order
<i>k</i>	OCaml fixed-width integer

$\beta$	::=	Core base types
	<b>unit</b>	unit
	<b>bool</b>	boolean
	<b>integer</b>	integer
	<b>real</b>	rational numbers?
	<b>loc</b>	location
	<b>array</b> $\beta$	array
	$[\beta]$	list
	$(\beta_1, \dots, \beta_n)$	tuple
	<b>struct</b> $tag$	struct
	$\{\beta\}$	set
	<b>opt</b> $(\beta)$	option
	$\beta_1, \dots, \beta_n \rightarrow \beta$	parameter types
$binop$	::=	binary operators
	<b>+</b>	addition
	<b>-</b>	subtraction
	<b>*</b>	multiplication
	<b>/</b>	division
	<b>rem_t</b>	modulus
	<b>rem_f</b>	remainder
	<b>^</b>	exponentiation
	<b>=</b>	equality, defined both for integer and C types
	<b>&gt;</b>	greater than
	<b>&lt;</b>	less than
	<b>&gt;=</b>	greater than or equal to
	<b>&lt;=</b>	less than or equal to
	<b>/\</b>	conjunction
	<b>\/</b>	disjunction

<i>polarity</i>	$::=$   <b>Pos</b>   <b>Neg</b>	memory action polarities sequenced by <b>let weak</b> and <b>let strong</b> only sequenced by <b>let strong</b>
<i>ident</i>	$::=$	Ott-hack, ignore
<i>name</i>	$::=$   <i>ident</i>   <i>impl_const</i>	Core identifier implementation-defined constant
<i>ptrval</i>	$::=$   <b>nullptr</b>   <b>funcptr</b> <i>ident</i>   <b>concptr</b> <i>nat</i>	pointer values null pointer function pointer concrete pointer
<i>object_value</i>	$::=$   <i>ty_mem_int</i>   <i>ptrval</i>   <b>array</b> ( <i>loaded_value</i> <sub>1</sub> , .., <i>loaded_value</i> <sub><i>n</i></sub> )   ( <b>struct</b> <i>ident</i> ) { $\overline{member_i : \tau_i = mem\_val_i}^i$ }   ( <b>union</b> <i>ident</i> ) { <i>member = mem_val</i> }	C object values integer value pointer value C array value C struct value C union value
<i>loaded_value</i>	$::=$   <b>specified</b> ( <i>object_value</i> )	potentially unspecified C object values specified loaded value
$\beta$	$::=$	Ott-hack, ignore
<i>value</i>	$::=$   <i>object_value</i>   <i>loaded_value</i>	Core values C object value loaded C object value

		<b>Unit</b>	unit
		<b>True</b>	boolean true
		<b>False</b>	boolean false
		$\beta[value_1, \dots, value_i]$	list
		$(value_1, \dots, value_i)$	tuple
<i>ctor</i>	::=		data constructors
		<b>Nil</b> $\beta$	empty list
		<b>Cons</b>	list cons
		<b>Tuple</b>	tuple
		<b>Array</b>	C array
		<b>Ivmax</b>	max integer value
		<b>Ivmin</b>	min integer value
		<b>Ivsizeof</b>	sizeof value
		<b>Ivalignof</b>	alignof value
		<b>IvCOMPL</b>	bitwise complement
		<b>IvAND</b>	bitwise AND
		<b>IvOR</b>	bitwise OR
		<b>IvXOR</b>	bitwise XOR
		<b>Specified</b>	non-unspecified loaded value
		<b>Unspecified</b>	unspecified loaded value
		<b>Fvfromint</b>	cast integer to floating value
		<b>Ivfromfloat</b>	cast floating to integer value
<i>ident_opt_β</i>	::=		type annotated optional identifier
		$\_ : \beta$	
		<i>ident</i> : $\beta$	
<i>pattern_aux</i>	::=		
		<i>ident_opt_β</i>	

		$ctor(\overline{pattern_i}^i)$	
$pattern$	$::=$	$loc\ annots\ pattern\_aux$	
$ident\_or\_pattern$	$::=$	$ident$	
		$pattern$	
$ident$	$::=$		Ott-hack, ignore
$pexpr\_aux$	$::=$		pure expressions
		$ident$	
		$impl\_const$	implementation-defined constant
		$value$	
		$constrained(\overline{mem\_iv\_c_i}, \overline{ident_i}^i)$	constrained value
		$error(string, ident)$	impl-defined static error
		$ctor(\overline{ident_i}^i)$	data constructor application
		$array\_shift(ident_1, \tau, ident_2)$	pointer array shift
		$member\_shift(ident, ident, member)$	pointer struct/union member shift
		$not(ident)$	boolean not
		$ident_1\ binop\ ident_2$	binary operations
		$(\mathbf{struct}\ ident)\{\overline{.member_i = ident_i}^i\}$	C struct expression
		$(\mathbf{union}\ ident)\{.member = ident\}$	C union expression
		$memberof(ident, member, ident)$	C struct/union member access
		$name(ident_1, \dots, ident_n)$	pure function call
		$\mathbf{assert\_undef}(ident, loc, UB\_name)$	
		$\mathbf{bool\_to\_integer}(ident)$	
		$\mathbf{conv\_int}(\tau, ident)$	
		$\mathbf{wrapI}(\tau, ident)$	

<i>pexpr</i>	$::=$   <i>loc annots tyvar_TY pexpr_aux</i>	pure expressions with location and annotations
<i>tpexpr_aux</i>	$::=$   <b>undef</b> <i>loc UB_name</i>   <b>case</b> <i>ident</i> <b>of</b> $\overline{\text{pattern}_i \Rightarrow \text{tpexpr}_i}^i$ <b>end</b>   <b>let</b> <i>ident_or_pattern</i> = <i>tpexpr<sub>1</sub></i> <b>in</b> <i>tpexpr<sub>2</sub></i>   <b>if</b> <i>ident</i> <b>then</b> <i>tpexpr<sub>1</sub></i> <b>else</b> <i>tpexpr<sub>2</sub></i>   <b>done</b> <i>ident</i>	top-level pure expressions undefined behaviour pattern matching pure let pure if pure done
<i>tpexpr</i>	$::=$   <i>loc annots tyvar_TY tpexpr_aux</i>	pure top-level pure expressions with location and annotations
<i>m_kill_kind</i>	$::=$   <b>dynamic</b>   <b>static</b> $\tau$	
<i>bool</i>	$::=$   <b>true</b>   <b>false</b>	OCaml booleans
<i>action_aux</i>	$::=$   <b>create</b> ( <i>ident</i> , $\tau$ ) <i>sym_prefix</i>   <b>create_readonly</b> ( <i>ident<sub>1</sub></i> , $\tau$ , <i>ident<sub>2</sub></i> ) <i>sym_prefix</i>   <b>alloc</b> ( <i>ident<sub>1</sub></i> , <i>ident<sub>2</sub></i> ) <i>sym_prefix</i>   <b>kill</b> ( <i>m_kill_kind</i> , <i>ident</i> )   <b>store</b> ( <i>bool</i> , $\tau$ , <i>ident<sub>1</sub></i> , <i>ident<sub>2</sub></i> , <i>mem_order</i> )   <b>load</b> ( $\tau$ , <i>ident</i> , <i>mem_order</i> )   <b>rmw</b> ( $\tau$ , <i>ident<sub>1</sub></i> , <i>ident<sub>2</sub></i> , <i>ident<sub>3</sub></i> , <i>mem_order<sub>1</sub></i> , <i>mem_order<sub>2</sub></i> )   <b>fence</b> ( <i>mem_order</i> )	memory actions  the boolean indicates whether the action is dynamic (i.e. free()) the boolean indicates whether the store is locking

		<code>cmp_exch_strong</code> ( $\tau, ident_1, ident_2, ident_3, mem\_order_1, mem\_order_2$ )	
		<code>cmp_exch_weak</code> ( $\tau, ident_1, ident_2, ident_3, mem\_order_1, mem\_order_2$ )	
		<code>linux_fence</code> ( $linux\_mem\_order$ )	
		<code>linux_load</code> ( $\tau, ident, linux\_mem\_order$ )	
		<code>linux_store</code> ( $\tau, ident_1, ident_2, linux\_mem\_order$ )	
		<code>linux_rmw</code> ( $\tau, ident_1, ident_2, linux\_mem\_order$ )	
<i>action</i>	::=		
		<code>loc action_aux</code>	
<i>memop</i>	::=		operations involving the memory state
		<code>ident<sub>1</sub> == ident<sub>2</sub></code>	pointer equality comparison
		<code>ident<sub>1</sub> ≠ ident<sub>2</sub></code>	pointer inequality comparison
		<code>ident<sub>1</sub> &lt; ident<sub>2</sub></code>	pointer less-than comparison
		<code>ident<sub>1</sub> &gt; ident<sub>2</sub></code>	pointer greater-than comparison
		<code>ident<sub>1</sub> ≤ ident<sub>2</sub></code>	pointer less-than comparison
		<code>ident<sub>1</sub> ≥ ident<sub>2</sub></code>	pointer greater-than comparison
		<code>ident<sub>1</sub> −<sub>τ</sub> ident<sub>2</sub></code>	pointer subtraction
		<code>intFromPtr</code> ( $\tau_1, \tau_2, ident$ )	cast of pointer value to integer value
		<code>ptrFromInt</code> ( $\tau_1, \tau_2, ident$ )	cast of integer value to pointer value
		<code>ptrValidForDeref</code> ( $\tau, ident$ )	dereferencing validity predicate
		<code>ptrWellAligned</code> ( $\tau, ident$ )	
		<code>ptrArrayShift</code> ( $ident_1, \tau, ident_2$ )	
		<code>memcpy</code> ( $ident_1, ident_2, ident_3$ )	
		<code>memcmp</code> ( $ident_1, ident_2, ident_3$ )	
		<code>realloc</code> ( $ident_1, ident_2, ident_3$ )	
		<code>va_start</code> ( $ident_1, ident_2$ )	
		<code>va_copy</code> ( $ident$ )	
		<code>va_arg</code> ( $ident, \tau$ )	
		<code>va_end</code> ( $ident$ )	

TODO: not sure about this

<i>paction</i>	$::=$   <i>action</i>   $\neg(\textit{action})$	memory actions with polarity M    positive, sequenced by both <b>let weak</b> and <b>let strong</b> M    negative, only sequenced by <b>let strong</b>
<i>expr_aux</i>	$::=$   <b>pure</b> ( <i>pexpr</i> )   <b>memop</b> ( <i>memop</i> )   <i>paction</i>   <b>skip</b>   <b>ccall</b> ( $\tau, \textit{ident}, \overline{\textit{ident}_i}^i$ )   <b>pcall</b> ( <i>name</i> , $\overline{\textit{ident}_i}^i$ )	(effetful) expressions  pointer op involving memory memory action  C function call Core procedure call
<i>expr</i>	$::=$   <i>loc annots expr_aux</i>	(effetful) expressions with location and annotations
<i>texpr_aux</i>	$::=$   <b>let</b> <i>ident_or_pattern</i> = <i>pexpr</i> <b>in</b> <i>texpr</i>   <b>let weak</b> <i>pattern</i> = <i>expr</i> <b>in</b> <i>texpr</i>   <b>let strong</b> <i>ident_or_pattern</i> = <i>expr</i> <b>in</b> <i>texpr</i>   <b>case</b> <i>ident</i> <b>with</b> $\overline{\textit{pattern}_i \Rightarrow \textit{texpr}_i}^i$ <b>end</b>   <b>if</b> <i>ident</i> <b>then</b> <i>texpr</i> <sub>1</sub> <b>else</b> <i>texpr</i> <sub>2</sub>   <b>bound</b> [ <i>k</i> ] ( <i>texpr</i> )   <b>unseq</b> ( <i>expr</i> <sub>1</sub> , .., <i>expr</i> <sub><i>n</i></sub> )   <b>nd</b> ( <i>texpr</i> <sub>1</sub> , .., <i>texpr</i> <sub><i>n</i></sub> )   <b>done</b> <i>ident</i>   <b>undef</b> <i>loc UB_name</i>   <b>run</b> <i>ident</i> <i>ident</i> <sub>1</sub> , .., <i>ident</i> <sub><i>n</i></sub>	top-level expressions  weak sequencing strong sequencing pattern matching  ...and boundary unsequenced expressions nondeterministic sequencing  run from label
<i>texpr</i>	$::=$   <i>loc annots texpr_aux</i>	top-level expressions with location and annotations



<i>terminals</i>	::=		
		$\lambda$	
		$\rightarrow$	
		$\rightarrow$	
		$\Rightarrow$	
		$\Leftarrow$	
		$\vdash$	
		$\in$	
		$\Pi$	
		$\forall$	
		$\neg$	
		$\cup$	
		$\Sigma$	
		$\exists$	
		$\star$	
		$\wedge$	
		$\bigwedge$	
		$\neg$	
		$=$	
		$\neq$	
		$\leq$	
		$\geq$	
		$\&$	
<i>z, Z_t</i>	::=		OCaml arbitrary-width integer
		<code>of_mem_int(<i>ty_mem_int</i>)</code>	M
		<code>of_nat(<i>nat</i>)</code>	M
<i>lit</i>	::=		
		<i>ident</i>	

		()
		<i>bool</i>
		<b>int</b> <i>Z_t</i>
		<b>ptr</b> <i>Z_t</i>
<i>bool_op</i>	::=	
		$\neg \textit{index\_term}$
		$\textit{index\_term}_1 = \textit{index\_term}_2$
		$\bigwedge(\textit{index\_term}_1, \dots, \textit{index\_term}_n)$
<i>list_op</i>	::=	
		$[\textit{index\_term}_1, \dots, \textit{index\_term}_n]$
		$\textit{index\_term}^{(k)}$
<i>tuple_op</i>	::=	
		$(\textit{index\_term}_1, \dots, \textit{index\_term}_n)$
		$\textit{index\_term}^{(k)}$
<i>pointer_op</i>	::=	
		<b>nullop</b>
<i>array_op</i>	::=	
		$\textit{index\_term}_1[\textbf{int } Z\_t]$
<i>param_op</i>	::=	
		$\textit{index\_term}(\textit{index\_term}_1, \dots, \textit{index\_term}_n)$
<i>struct_op</i>	::=	
		$\textit{index\_term}.\textit{member}$

$index\_term\_aux$	$::=$ <ul style="list-style-type: none"> <li>  <math>bool\_op</math></li> <li>  <math>list\_op</math></li> <li>  <math>pointer\_op</math></li> <li>  <math>array\_op</math></li> <li>  <math>param\_op</math></li> </ul>	
$bt$	$::=$	OCaml type variable for base types
$index\_term$	$::=$ <ul style="list-style-type: none"> <li>  <math>lit</math></li> <li>  <math>index\_term\_aux\ bt</math></li> <li>  <math>(index\_term)</math></li> <li>  <math>index\_term[index\_term_1/ident_1, \dots, index\_term_n/ident_n]</math></li> </ul>	<div style="display: flex; align-items: center; justify-content: flex-end;"> <div style="margin-right: 10px;"> <math>S</math> <math>M</math> </div> <div>             parentheses           </div> </div>
$arg$	$::=$ <ul style="list-style-type: none"> <li>  <math>\Pi ident : \beta.arg</math></li> <li>  <math>\forall ident : \mathbf{logSort}.arg</math></li> <li>  <math>\mathbf{resource} \multimap arg</math></li> <li>  <math>index\_term \supset arg</math></li> <li>  <math>I</math></li> </ul>	argument types
$ret$	$::=$ <ul style="list-style-type: none"> <li>  <math>\Sigma ident : \beta.ret</math></li> <li>  <math>\exists ident : \mathbf{logSort}.ret</math></li> <li>  <math>\mathbf{resource} \star ret</math></li> <li>  <math>index\_term \wedge ret</math></li> <li>  <math>I</math></li> </ul>	return types
$\Gamma$	$::=$	computational var env

	$\begin{array}{ l} \text{empty} \\ \Gamma, x : \beta \end{array}$	
$\Lambda$	$\begin{array}{l} ::= \\ \begin{array}{ l} \text{empty} \\ \Lambda, x \end{array} \end{array}$	logical var env
$\Xi$	$\begin{array}{l} ::= \\ \begin{array}{ l} \text{empty} \\ \Xi, \text{phi} \end{array} \end{array}$	constraints env
<i>formula</i>	$\begin{array}{l} ::= \\ \begin{array}{ l} \text{judgement} \\ \text{not } (\text{formula}) \\ \text{ident} : \beta \in \Gamma \\ \text{ident} : \text{struct } \text{tag} \& \overline{\text{member}_i : \tau_i}^i \in \Gamma \\ \text{formula}_1 \dots \text{formula}_n \end{array} \end{array}$	
<i>Jtype</i>	$\begin{array}{l} ::= \\ \begin{array}{ l} \Gamma; \Lambda; \Xi \vdash \text{value} \Rightarrow \text{ident}, \beta, \text{index\_term} \\ \Gamma; \Lambda; \Xi \vdash \text{pexpr\_aux} \Rightarrow \text{ret} \end{array} \end{array}$	
<i>judgement</i>	$\begin{array}{l} ::= \\ \begin{array}{ l} Jtype \end{array} \end{array}$	
<i>user_syntax</i>	$\begin{array}{l} ::= \\ \begin{array}{ l} \text{tag} \\ \text{impl\_const} \\ x \\ \text{ty\_mem\_int} \end{array} \end{array}$	

- | *mem\_val*
- | *member*
- |  $\tau$
- | *annots*
- | *nat*
- | *n*
- | *loc*
- | *mem\_iv\_c*
- | *UB\_name*
- | *string*
- | *tyvar\_TY*
- |  $\tau$
- | *sym\_prefix*
- | *mem\_order*
- | *linux\_mem\_order*
- | *k*
- |  $\beta$
- | *binop*
- | *polarity*
- | *ident*
- | *name*
- | *ptrval*
- | *object\_value*
- | *loaded\_value*
- |  $\beta$
- | *value*
- | *ctor*
- | *ident\_opt\_β*
- | *pattern\_aux*

| *pattern*  
| *ident\_or\_pattern*  
| *ident*  
| *pexpr\_aux*  
| *pexpr*  
| *tpexpr\_aux*  
| *tpexpr*  
| *m\_kill\_kind*  
| *bool*  
| *action\_aux*  
| *action*  
| *memop*  
| *paction*  
| *expr\_aux*  
| *expr*  
| *texpr\_aux*  
| *texpr*  
| *terminals*  
| *z*  
| *lit*  
| *bool\_op*  
| *list\_op*  
| *tuple\_op*  
| *pointer\_op*  
| *array\_op*  
| *param\_op*  
| *struct\_op*  
| *index\_term\_aux*  
| *bt*

$|$  *index\_term*  
 $|$  *arg*  
 $|$  *ret*  
 $|$   $\Gamma$   
 $|$   $\Lambda$   
 $|$   $\Xi$   
 $|$  *formula*

$\Gamma; \Lambda; \Xi \vdash \text{value} \Rightarrow \text{ident}, \beta, \text{index\_term}$

$$\begin{array}{c}
\frac{}{\Gamma; \Lambda; \Xi \vdash \text{ty\_mem\_int} \Rightarrow y, \text{integer}, y = \text{int of\_mem\_int}(\text{ty\_mem\_int})} \text{VAL\_OBJ\_INT} \\
\frac{}{\Gamma; \Lambda; \Xi \vdash \text{nullptr} \Rightarrow y, \text{loc}, y = \text{nullopt}} \text{VAL\_OBJ\_PTR\_NULL} \\
\frac{}{\Gamma; \Lambda; \Xi \vdash \text{funcptr ident} \Rightarrow y, \text{loc}, y = \text{ident}} \text{VAL\_OBJ\_PTR\_FUNC} \\
\frac{}{\Gamma; \Lambda; \Xi \vdash \text{concptr nat} \Rightarrow y, \text{loc}, y = \text{ptr of\_nat}(\text{nat})} \text{VAL\_OBJ\_PTR\_CONC} \\
\frac{\Gamma; \Lambda; \Xi \vdash \text{loaded\_value}_1 \Rightarrow y_1, \beta, \text{index\_term}_1 \quad \dots \quad \Gamma; \Lambda; \Xi \vdash \text{loaded\_value}_n \Rightarrow y_n, \beta, \text{index\_term}_n}{\Gamma; \Lambda; \Xi \vdash \text{array}(\text{loaded\_value}_1, \dots, \text{loaded\_value}_n) \Rightarrow y, \text{array } \beta, \bigwedge(\text{index\_term}_1, \dots, \text{index\_term}_n) [y[\text{int } z_1] / y_1, \dots, y[\text{int } z_n] / y_n]} \text{VAL\_OBJ\_ARR} \\
\frac{}{\Gamma; \Lambda; \Xi \vdash \text{Unit} \Rightarrow y, \text{unit}, y = ()} \text{VAL\_UNIT} \\
\frac{}{\Gamma; \Lambda; \Xi \vdash \text{True} \Rightarrow y, \text{bool}, y = \text{true}} \text{VAL\_TRUE} \\
\frac{}{\Gamma; \Lambda; \Xi \vdash \text{False} \Rightarrow y, \text{bool}, y = \text{false}} \text{VAL\_FALSE} \\
\frac{\Gamma; \Lambda; \Xi \vdash \text{value}_1 \Rightarrow y_1, \beta, \text{index\_term}_1 \quad \dots \quad \Gamma; \Lambda; \Xi \vdash \text{value}_n \Rightarrow y_n, \beta, \text{index\_term}_n}{\Gamma; \Lambda; \Xi \vdash \beta[\text{value}_1, \dots, \text{value}_n] \Rightarrow y, [\beta], (\bigwedge(\text{index\_term}_1, \dots, \text{index\_term}_n)) [y^{(k_1)} / y_1, \dots, y^{(k_n)} / y_n]} \text{VAL\_LIST} \\
\frac{\Gamma; \Lambda; \Xi \vdash \text{value}_1 \Rightarrow y_1, \beta_1, \text{index\_term}_1 \quad \dots \quad \Gamma; \Lambda; \Xi \vdash \text{value}_n \Rightarrow y_n, \beta_n, \text{index\_term}_n}{\Gamma; \Lambda; \Xi \vdash (\text{value}_1, \dots, \text{value}_n) \Rightarrow y, (\beta_1, \dots, \beta_n), \bigwedge(\text{index\_term}_1, \dots, \text{index\_term}_n) [y^{(k_1)} / y_1, \dots, y^{(k_n)} / y_n]} \text{VAL\_TUPLE}
\end{array}$$

$\Gamma; \Lambda; \Xi \vdash \text{pexpr\_aux} \Rightarrow \text{ret}$

$$\begin{array}{c}
\frac{x : \beta \in \Gamma}{\Gamma; \Lambda; \Xi \vdash x \Rightarrow \Sigma y : \beta. \mathbf{I}} \quad \text{PEXPR\_VAR} \\
\\
\frac{\Gamma; \Lambda; \Xi \vdash \text{value} \Rightarrow y, \beta, \text{index\_term}}{\Gamma; \Lambda; \Xi \vdash \text{value} \Rightarrow \Sigma y : \beta. \text{index\_term} \wedge \mathbf{I}} \quad \text{PEXPR\_VAL} \\
\\
\frac{x : \text{bool} \in \Gamma}{\Gamma; \Lambda; \Xi \vdash \text{not}(x) \Rightarrow \Sigma y : \text{bool}. y = (\neg x) \wedge \mathbf{I}} \quad \text{PEXPR\_NOT}
\end{array}$$

Definition rules:            13 good    0 bad  
 Definition rule clauses: 19 good    0 bad