

<i>ident, x, y, y<sub>p</sub>, -</i>	subscript p is for pointers
<i>n, i, j</i>	index variables
<i>impl_const</i>	implementation-defined constant
<i>mem_int</i>	memory integer value
<i>member</i>	C struct/union member name
	Ott-hack, ignore (annotations)
<i>nat</i>	OCaml arbitrary-width natural number
<i>mem_ptr</i>	abstract pointer value
<i>mem_val</i>	abstract memory value
	Ott-hack, ignore (locations)
<i>mem_iv_c</i>	OCaml type for memory constraints on integer values
<i>UB_name</i>	undefined behaviour
<i>string</i>	OCaml string
	Ott-hack, ignore (OCaml type variable TY)
	Ott-hack, ignore (Symbol.prefix)
<i>mem_order, -</i>	OCaml type for memory order
<i>linux_mem_order</i>	OCaml type for Linux memory order
	Ott-hack, ignore (OCaml type variable bt)
<i>logical_val</i>	logical values (to be specified)

$Sctypes\_t, \tau$	$::=$ $  \quad \tau^*$	C type pointer to type $\tau$
$tag$	$::=$ $  \quad ident$	OCaml type for struct/union tag
$\beta, -$	$::=$ $  \quad \mathbf{unit}$ $  \quad \mathbf{bool}$ $  \quad \mathbf{integer}$ $  \quad \mathbf{real}$ $  \quad \mathbf{loc}$ $  \quad \mathbf{array} \beta$ $  \quad [\beta]$ $  \quad \overline{\beta_i}^i$ $  \quad \mathbf{struct} \, tag$ $  \quad \{\beta\}$ $  \quad \mathbf{opt} \, (\beta)$ $  \quad \beta_1, \dots, \beta_n \rightarrow \beta$ $  \quad \beta_\tau$	base types unit boolean integer rational numbers? location array list tuple struct set option parameter types of a C type
$binop$	$::=$ $  \quad +$ $  \quad -$ $  \quad *$ $  \quad /$ $  \quad \mathbf{rem\_t}$ $  \quad \mathbf{rem\_f}$ $  \quad \wedge$ $  \quad =$	binary operators addition subtraction multiplication division modulus remainder exponentiation equality, defined both for integer and C types

		>	greater than
		<	less than
		>=	greater than or equal to
		<=	less than or equal to
		&\	conjunction
		\	disjunction
<i>binop<sub>arith</sub></i>	::=		arithmetic binary operators
		+	
		-	
		*	
		/	
		rem_t	
		rem_f	
		^	
<i>binop<sub>rel</sub></i>	::=		relational binary operators
		=	
		>	
		<	
		>=	
		<=	
<i>binop<sub>bool</sub></i>	::=		boolean binary operators
		&\	
		\	
<i>object_value</i>	::=		C object values (inhabitants of object types), which can be read/stored
		<i>mem_int</i>	integer value
		<i>mem_ptr</i>	pointer value

		<code>array</code> ( $\overline{loaded\_value_i}^i$ )	C array value
		<code>(struct ident)</code> { $\overline{.member_i:\tau_i = mem\_val_i}^i$ }	C struct value
		<code>(union ident)</code> { $.member = mem\_val$ }	C union value
<i>loaded_value</i>	::=		potentially unspecified C object values
		<code>specified object_value</code>	specified loaded value
<i>value</i>	::=		Core values
		<i>object_value</i>	C object value
		<i>loaded_value</i>	loaded C object value
		<code>Unit</code>	unit
		<code>True</code>	boolean true
		<code>False</code>	boolean false
		$\beta[\overline{value_i}^i]$	list
		$(\overline{value_i}^i)$	tuple
<i>ctor_val</i>	::=		data constructors
		<code>Nil</code> $\beta$	empty list
		<code>Cons</code>	list cons
		<code>Tuple</code>	tuple
		<code>Array</code>	C array
		<code>Specified</code>	non-unspecified loaded value
<i>ctor_expr</i>	::=		data constructors
		<code>Ivmax</code>	max integer value
		<code>Ivmin</code>	min integer value
		<code>Ivsizeof</code>	sizeof value
		<code>Ivalignof</code>	alignof value
		<code>IvCOMPL</code>	bitwise complement
		<code>IvAND</code>	bitwise AND

		<b>IvOR</b>	bitwise OR
		<b>IvXOR</b>	bitwise XOR
		<b>Fvfromint</b>	cast integer to floating value
		<b>Ivfromfloat</b>	cast floating to integer value
<i>name</i>	::=		
		<i>ident</i>	Core identifier
		<i>impl_const</i>	implementation-defined constant
<i>pval</i>	::=		pure values
		<i>ident</i>	Core identifier
		<i>impl_const</i>	implementation-defined constant
		<i>value</i>	Core values
		<b>constrained</b> ( $\overline{mem\_iv\_c_i}, pval_i^i$ )	constrained value
		<b>error</b> ( <i>string</i> , <i>pval</i> )	impl-defined static error
		<i>ctor_val</i> ( $\overline{pval_i^i}$ )	data constructor application
		( <b>struct</b> <i>ident</i> ){ $\overline{.member_i = pval_i^i}$ }	C struct expression
		( <b>union</b> <i>ident</i> ){ $\overline{.member = pval}$ }	C union expression
<i>pexpr</i>	::=		pure expressions
		<i>pval</i>	pure values
		<i>ctor_expr</i> ( $\overline{pval_i^i}$ )	data constructor application
		<b>array_shift</b> ( <i>pval</i> <sub>1</sub> , $\tau$ , <i>pval</i> <sub>2</sub> )	pointer array shift
		<b>member_shift</b> ( <i>pval</i> , <i>ident</i> , <i>member</i> )	pointer struct/union member shift
		<b>not</b> ( <i>pval</i> )	boolean not
		<i>pval</i> <sub>1</sub> <i>binop</i> <i>pval</i> <sub>2</sub>	binary operations
		<b>memberof</b> ( <i>ident</i> , <i>member</i> , <i>pval</i> )	C struct/union member access
		<b>name</b> ( <i>pval</i> <sub>1</sub> , ..., <i>pval</i> <sub><i>n</i></sub> )	pure function call
		<b>assert_undef</b> ( <i>pval</i> , <i>UB_name</i> )	
		<b>bool_to_integer</b> ( <i>pval</i> )	

	<code>conv_int</code> $(\tau, pval)$   <code>wrapI</code> $(\tau, pval)$	
<i>tpval</i>	<code>::=</code>   <code>undef</code> <i>UB_name</i>   <code>done</code> <i>pval</i>	top-level pure values undefined behaviour pure done
<i>ident_opt_β</i>	<code>::=</code>   <code>_:β</code>   <i>ident</i> : <i>β</i>	type annotated optional identifier
<i>pattern</i>	<code>::=</code>   <i>ident_opt_β</i>   <i>ctor_val</i> ( $\overline{pattern_i}^i$ )	
<i>ident_or_pattern</i>	<code>::=</code>   <i>ident</i>   <i>pattern</i>	
<i>tpexpr</i>	<code>::=</code>   <i>tpval</i>   <code>case</code> <i>pval</i> <code>of</code> $\overline{pattern_i \Rightarrow tpexpr_i}^i$ <code>end</code>   <code>let</code> <i>ident_or_pattern</i> = <i>pexpr</i> <code>in</code> <i>tpexpr</i>   <code>if</code> <i>pval</i> <code>then</code> <i>tpexpr</i> <sub>1</sub> <code>else</code> <i>tpexpr</i> <sub>2</sub>   $[C/C']tpexpr$	top-level pure expressions top-level pure values pattern matching pure let pure if M simul-sub all vars in <i>C</i> for all vars in <i>C'</i> in <i>tpexpr</i>
<i>m_kill_kind</i>	<code>::=</code>   <code>dynamic</code>   <code>static</code> <i>τ</i>	

<i>bool</i> , <i>_</i>	$::=$   <b>true</b>   <b>false</b>	OCaml booleans
<i>int</i> , <i>_</i>	$::=$   <i>i</i>	OCaml fixed-width integer literal integer
<i>mem_action</i>	$::=$   <b>create</b> ( <i>pval</i> , $\tau$ )   <b>create_readonly</b> ( <i>pval</i> <sub>1</sub> , $\tau$ , <i>pval</i> <sub>2</sub> )   <b>alloc</b> ( <i>pval</i> <sub>1</sub> , <i>pval</i> <sub>2</sub> )   <b>kill</b> ( <i>m_kill_kind</i> , <i>pval</i> )   <b>store</b> ( <i>bool</i> , $\tau$ , <i>pval</i> <sub>1</sub> , <i>pval</i> <sub>2</sub> , <i>mem_order</i> )   <b>load</b> ( $\tau$ , <i>pval</i> , <i>mem_order</i> )   <b>rmw</b> ( $\tau$ , <i>pval</i> <sub>1</sub> , <i>pval</i> <sub>2</sub> , <i>pval</i> <sub>3</sub> , <i>mem_order</i> <sub>1</sub> , <i>mem_order</i> <sub>2</sub> )   <b>fence</b> ( <i>mem_order</i> )   <b>cmp_exch_strong</b> ( $\tau$ , <i>pval</i> <sub>1</sub> , <i>pval</i> <sub>2</sub> , <i>pval</i> <sub>3</sub> , <i>mem_order</i> <sub>1</sub> , <i>mem_order</i> <sub>2</sub> )   <b>cmp_exch_weak</b> ( $\tau$ , <i>pval</i> <sub>1</sub> , <i>pval</i> <sub>2</sub> , <i>pval</i> <sub>3</sub> , <i>mem_order</i> <sub>1</sub> , <i>mem_order</i> <sub>2</sub> )   <b>linux_fence</b> ( <i>linux_mem_order</i> )   <b>linux_load</b> ( $\tau$ , <i>pval</i> , <i>linux_mem_order</i> )   <b>linux_store</b> ( $\tau$ , <i>pval</i> <sub>1</sub> , <i>pval</i> <sub>2</sub> , <i>linux_mem_order</i> )   <b>linux_rmw</b> ( $\tau$ , <i>pval</i> <sub>1</sub> , <i>pval</i> <sub>2</sub> , <i>linux_mem_order</i> )	memory actions  true means store is locking
<i>polarity</i>	$::=$   <b>Pos</b>   <b>Neg</b>	polarities for memory actions sequenced by <b>let weak</b> and <b>let strong</b> only sequenced by <b>let strong</b>
<i>pol_mem_action</i>	$::=$   <i>polarity mem_action</i>	memory actions with polarity

<i>mem_op</i>	$::=$   $pval_1 == pval_2$   $pval_1 \neq pval_2$   $pval_1 < pval_2$   $pval_1 > pval_2$   $pval_1 \leq pval_2$   $pval_1 \geq pval_2$   $pval_1 -_{\tau} pval_2$   $\text{intFromPtr}(\tau_1, \tau_2, pval)$   $\text{ptrFromInt}(\tau_1, \tau_2, pval)$   $\text{ptrValidForDeref}(\tau, pval)$   $\text{ptrWellAligned}(\tau, pval)$   $\text{ptrArrayShift}(pval_1, \tau, pval_2)$   $\text{memcpy}(pval_1, pval_2, pval_3)$   $\text{memcmp}(pval_1, pval_2, pval_3)$   $\text{realloc}(pval_1, pval_2, pval_3)$   $\text{va\_start}(pval_1, pval_2)$   $\text{va\_copy}(pval)$   $\text{va\_arg}(pval, \tau)$   $\text{va\_end}(pval)$	operations involving the memory state pointer equality comparison pointer inequality comparison pointer less-than comparison pointer greater-than comparison pointer less-than comparison pointer greater-than comparison pointer subtraction cast of pointer value to integer value cast of integer value to pointer value dereferencing validity predicate
<i>tval</i>	$::=$   $\text{done } pval$   $\text{undef } UB\_name$	(effectful) top-level values end of top-level expression undefined behaviour
<i>seq_expr</i>	$::=$   $pval$   $\text{ccall}(\tau, pval, \overline{pval_i}^i)$   $\text{pcall}(name, \overline{pval_i}^i)$	sequential (effectful) expressions pure values C function call procedure call



<i>seq_expr</i>	$::=$   <i>tval</i>   <b>run</b> <i>ident</i> <i>pval</i> <sub>1</sub> , .., <i>pval</i> <sub><i>n</i></sub>   <b>nd</b> ( <i>pval</i> <sub>1</sub> , .., <i>pval</i> <sub><i>n</i></sub> )   <b>let</b> <i>ident_or_pattern</i> = <i>seq_expr</i> <b>in</b> <i>texpr</i>   <b>case</b> <i>pval</i> <b>with</b> $\overline{\text{pattern}_i \Rightarrow \text{texpr}_i}^i$ <b>end</b>   <b>if</b> <i>pval</i> <b>then</b> <i>texpr</i> <sub>1</sub> <b>else</b> <i>texpr</i> <sub>2</sub>   <b>bound</b> [ <i>int</i> ] ( <i>is_expr</i> )	sequential top-level (effectful) expressions (effectful) top-level values run from label nondeterministic choice pure sequencing pattern matching conditional limit scope of indet seq behaviour, absent at runtime
<i>is_expr</i>	$::=$   <b>memop</b> ( <i>mem_op</i> )   <i>pol_mem_action</i>   <b>unseq</b> ( <i>texpr</i> <sub>1</sub> , .., <i>texpr</i> <sub><i>n</i></sub> )	indet seq (effectful) expressions pointer op involving memory memory action unsequenced expressions
<i>is_texpr</i>	$::=$   <b>let weak</b> <i>pattern</i> = <i>is_expr</i> <b>in</b> <i>mu_texpr_aux</i>   <b>let strong</b> <i>ident_or_pattern</i> = <i>is_expr</i> <b>in</b> <i>mu_texpr_aux</i>	indet seq top-level (effectful) expressions weak sequencing strong sequencing
<i>texpr</i>	$::=$   <i>seq_expr</i>   <i>is_expr</i>	top-level (effectful) expressions sequential (effectful) expressions indet seq (effectful) expressions
<i>terminals</i>	$::=$   $\lambda$   $\longrightarrow$   $\rightarrow$   $\rightsquigarrow$   $\Rightarrow$   $\Leftarrow$   $\vdash$	

	$\in$
	$\Pi$
	$\forall$
	$\neg \circ$
	$\cup$
	$\Sigma$
	$\exists$
	$\star$
	$\times$
	$\wedge$
	$\bigwedge$
	$\neg$
	$=$
	$\neq$
	$\leq$
	$\geq$
	$\&$
	$\cdot$
	$ $
	$+_{\text{ptr}}$
	$\mapsto$
	$*$
	$::$
	$\checkmark$
	$:$
	$\cdot$
	$\cdot$
	$\gg$
	$::$

		$\wedge$	
		$\vee$	
$z$	::=		OCaml arbitrary-width integer
		$i$	M literal integer
		$\text{to\_int}(\text{mem\_int})$	M
		$\text{size\_of}(\tau)$	M size of a C type
		$\text{offset\_of}_{\text{tag}}(\text{member})$	M offset of a struct member
		<b>ptr_size</b>	M size of a pointer
$\mathbb{Q}$	::=		OCaml type for rational numbers
		$\frac{\text{int}_1}{\text{int}_2}$	
$\text{lit}$	::=		
		$\text{ident}$	
		<b>unit</b>	
		$\text{bool}$	
		$z$	
		$\mathbb{Q}$	
$\text{bool\_op}$	::=		
		$\neg \text{term}$	
		$\text{term}_1 = \text{term}_2$	
		$\bigwedge (\overline{\text{term}_i})^i$	
		$\bigvee (\overline{\text{term}_i})^i$	
		$\text{term}_1 \text{ binop}_{\text{bool}} \text{term}_2$	M
$\text{arith\_op}$	::=		
		$\text{term}_1 + \text{term}_2$	
		$\text{term}_1 - \text{term}_2$	

		$term_1 \times term_2$	
		$term_1 / term_2$	
		$term_1 \text{ rem\_t } term_2$	
		$term_1 \text{ rem\_f } term_2$	
		$term_1 \wedge term_2$	
		$term_1 \text{ binop}_{arith} term_2$	M
$cmp\_op$	$::=$		
		$term_1 < term_2$	less than
		$term_1 \leq term_2$	less than or equal
		$term_1 \text{ binop}_{rel} term_2$	M
$list\_op$	$::=$		
		<b>nil</b>	
		<b>tl</b> $term$	
		$term^{(int)}$	
$tuple\_op$	$::=$		
		$(\overline{term_i})^i$	
		$term^{(int)}$	
$pointer\_op$	$::=$		
		<b>of_mem_ptr</b> $mem\_ptr$	
		$term_1 +_{ptr} term_2$	
$option\_op$	$::=$		
		<b>none</b> $BT\_t$	
		<b>some</b> $term$	
$array\_op$	$::=$		

		$term_1[term_2]$		
$param\_op$	::=		$term(term_1, .., term_n)$	
$struct\_op$	::=		$term.member$	
$ct\_pred$	::=		$\mathbf{representable}(\tau, term)$	
			$\mathbf{alignedI}(term_1, term_2)$	
$term, -$	::=		$lit$	
			$arith\_op$	
			$bool\_op$	
			$cmp\_op$	
			$tuple\_op$	
			$struct\_op$	
			$pointer\_op$	
			$list\_op$	
			$array\_op$	
			$ct\_pred$	
			$option\_op$	
			$param\_op$	
			$(term)$	S parentheses
			$[term_1/ident]term_2$	M substitute $term_1$ for $ident$ in $term_2$
			$pval$	M only the ones which can be embedded into the SMT value grammar, so no array literals
			$resource$	

<i>terms</i>	$::=$ $  \quad [term_1, \dots, term_n]$	non-empty list of terms
<i>predicate_name</i>	$::=$ $  \quad S_{types\_t}$ $  \quad string$	names of predicates C type arbitrary
<i>init,</i>	$::=$ $  \quad \checkmark$ $  \quad \times$	initialisation status initialised uninitialised
<i>predicate</i>	$::=$ $  \quad terms_1 \mathbb{Q} \overset{init}{\mapsto}_{predicate\_name} terms_2$	arbitrary predicate
<i>resource</i>	$::=$ $  \quad predicate$	
<i>spine_elem</i>	$::=$ $  \quad pval$ $  \quad logical\_val$ $  \quad resource$	spine element pure value logical variable resource
<i>arg</i>	$::=$ $  \quad \Pi ident:\beta. arg$ $  \quad \forall ident:\beta. arg$ $  \quad resource \multimap arg$ $  \quad term \supset arg$ $  \quad ret$ $  \quad [spine\_elem/ident]arg$	argument types     M

$ret, \_$	$::=$ $  \quad \Sigma ident:\beta. ret$ $  \quad \exists ident:\beta. ret$ $  \quad resource \star ret$ $  \quad term \wedge ret$ $  \quad \mathbf{I}$	return types
$\mathcal{C}$	$::=$ $  \quad \cdot$ $  \quad \mathcal{C}, ident:BT\_t$ $  \quad \mathcal{C}, \mathcal{C}'$ $  \quad \text{fresh}(\mathcal{C})$	computational var env  $\mathbf{M}$ identical context except with fresh variable names
$\mathcal{L}$	$::=$ $  \quad \cdot$ $  \quad \mathcal{L}, ident$	logical var env
$\Phi$	$::=$ $  \quad \cdot$ $  \quad \Phi, term$	constraints env
$\mathcal{R}$	$::=$ $  \quad \cdot$ $  \quad \mathcal{R}, resource$	resources env
$formula$	$::=$ $  \quad judgement$ $  \quad \mathbf{smt}(\Phi \Rightarrow term)$ $  \quad ident:\beta \in \mathcal{C}$ $  \quad ident:\mathbf{struct\ tag} \ \& \ \overline{member_i:\tau_i}^i \in \mathbf{Globals}$	

	$\begin{array}{ l} \hline \mathcal{C}_i; \mathcal{L}_i; \Phi_i \vdash \overline{mem\_val_i \Rightarrow \mathbf{mem} \, y_i:\beta_i. term_i}^i \\ \hline \mathcal{C}_i; \mathcal{L}_i; \Phi_i \vdash \overline{pval_i \Rightarrow ident_i:\beta_i. term_i}^i \\ \hline pattern_i:\beta_i \rightsquigarrow \mathcal{C}_i^i \\ \hline \mathcal{C}_i; \mathcal{L}_i; \Phi_i \vdash \overline{tpexpr_i \Leftarrow y_i:\beta_i. term_i}^i \\ \hline \mathcal{L} \vdash logical\_val:\beta \end{array}$	dependent on memory object model
<i>object_value_jtype</i>	$\begin{array}{ l} ::= \\ \hline \mathcal{C}; \mathcal{L}; \Phi \vdash object\_value \Rightarrow \mathbf{obj} \, ident:\beta. term \end{array}$	
<i>pval_jtype</i>	$\begin{array}{ l} ::= \\ \hline \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow ident:\beta. term \end{array}$	
<i>spine_jtype</i>	$\begin{array}{ l} ::= \\ \hline \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine\_elem_i}^i :: arg \gg ret \end{array}$	
<i>pexpr_jtype</i>	$\begin{array}{ l} ::= \\ \hline \mathcal{C}; \mathcal{L}; \Phi \vdash pexpr \Rightarrow ident:\beta. term \end{array}$	
<i>pattern_jtype</i>	$\begin{array}{ l} ::= \\ \hline pattern:\beta \rightsquigarrow \mathcal{C} \\ \hline ident\_or\_pattern:\beta \rightsquigarrow \mathcal{C} \end{array}$	
<i>tpval_jtype</i>	$\begin{array}{ l} ::= \\ \hline \mathcal{C}; \mathcal{L}; \Phi \vdash tpval \Leftarrow ident:\beta. term \end{array}$	
<i>tpexpr_jtype</i>	$\begin{array}{ l} ::= \\ \hline \mathcal{C}; \mathcal{L}; \Phi \vdash tpexpr \Leftarrow ident:\beta. term \end{array}$	
<i>action_jtype</i>	$\begin{array}{ l} ::= \\ \hline \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem\_action \Rightarrow ret \end{array}$	



		$\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash seq\_expr \Rightarrow ret$
		$\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is\_expr \Rightarrow ret$
<i>judgement</i>	$::=$	
		<i>object_value_jtype</i>
		<i>pval_jtype</i>
		<i>spine_jtype</i>
		<i>pexpr_jtype</i>
		<i>pattern_jtype</i>
		<i>tpval_jtype</i>
		<i>tpexpr_jtype</i>
		<i>action_jtype</i>
<i>user_syntax</i>	$::=$	
		<i>ident</i>
		<i>n</i>
		<i>impl_const</i>
		<i>mem_int</i>
		<i>member</i>
		<i>nat</i>
		<i>mem_ptr</i>
		<i>mem_val</i>
		<i>mem_iv_c</i>
		<i>UB_name</i>
		<i>string</i>
		<i>mem_order</i>

| *linux\_mem\_order*

| *logical\_val*

| *Sctypes\_t*

| *tag*

|  $\beta$

| *binop*

| *binop<sub>arith</sub>*

| *binop<sub>rel</sub>*

| *binop<sub>bool</sub>*

| *ident*

|  $\tau$

| *ident*

| *object\_value*

| *loaded\_value*

|  $\beta$

| *value*

| *ctor\_val*

| *ctor\_expr*

|  $\tau$

| *name*

| *pval*

| *pval*

| *pexpr*

| *pexpr*

| *tpval*

| *tpval*

| *ident\_opt\_ $\beta$*

| *pattern*

- | *pattern*
- | *ident\_or\_pattern*
- | *texpr*
- | *texpr*
- | *m\_kill\_kind*
- | *bool*
- | *int*
- | *mem\_action*
- | *mem\_action*
- | *polarity*
- | *pol\_mem\_action*
- | *mem\_op*
- | *tval*
- | *tval*
- | *seq\_expr*
- | *seq\_expr*
- | *seq\_texpr*
- | *seq\_texpr*
- | *is\_expr*
- | *is\_expr*
- | *is\_texpr*
- | *is\_texpr*
- | *texpr*
- | *terminals*
- | *z*
- |  $\mathbb{Q}$
- | *lit*
- | *bool\_op*
- | *arith\_op*

- | *cmp\_op*
- | *list\_op*
- | *tuple\_op*
- | *pointer\_op*
- | *BT\_t*
- | *option\_op*
- | *array\_op*
- | *param\_op*
- | *struct\_op*
- | *ct\_pred*
- | *term*
- | *term*
- | *term*
- | *terms*
- | *predicate\_name*
- | *init*
- | *predicate*
- | *resource*
- | *spine\_elem*
- | *arg*
- | *ret*
- |  $\mathcal{C}$
- |  $\mathcal{L}$
- |  $\Phi$
- |  $\mathcal{R}$
- | *formula*

$\mathcal{C}; \mathcal{L}; \Phi \vdash \text{object\_value} \Rightarrow \text{obj ident}:\beta. \text{term}$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{mem\_int} \Rightarrow \text{obj } y:\text{integer}. y = \text{to\_int}(\text{mem\_int})} \text{PVAL\_OBJ\_INT}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{mem\_ptr} \Rightarrow \text{obj } y:\text{loc}. y = \text{of\_mem\_ptr } \text{mem\_ptr}} \text{PVAL\_OBJ\_PTR}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{loaded\_value}_i \Rightarrow y_i:\beta. \text{term}_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{array}(\overline{\text{loaded\_value}_i^i}) \Rightarrow \text{obj } y:\text{array } \beta. \bigwedge(\overline{[y[i]/y_i] \text{term}_i^i})} \quad \text{PVAL\_OBJ\_ARR}$$

$$\frac{\frac{\text{ident}:\text{struct tag} \ \& \ \overline{\text{member}_i:\tau_i^i} \in \text{Globals}}{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{mem\_val}_i \Rightarrow \text{mem } y_i:\beta_i. \text{term}_i^i}}}{\mathcal{C}; \mathcal{L}; \Phi \vdash (\text{struct tag})\{.\text{member}_i:\tau_i = \text{mem\_val}_i^i\} \Rightarrow \text{obj } y:\text{struct tag}. \bigwedge(\overline{[y.\text{member}_i/y_i] \text{term}_i^i})} \quad \text{PVAL\_OBJ\_STRUCT}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{pval} \Rightarrow \text{ident}:\beta. \text{term}}$$

$$\frac{x:\beta \in \mathcal{C}}{\mathcal{C}; \mathcal{L}; \Phi \vdash x \Rightarrow y:\beta. y = x} \quad \text{PVAL\_VAR}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{object\_value} \Rightarrow \text{obj } y:\beta. \text{term}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{object\_value} \Rightarrow y:\beta. \text{term}} \quad \text{PVAL\_OBJ}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{object\_value} \Rightarrow \text{obj } y:\beta. \text{term}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{specified\_object\_value} \Rightarrow y:\beta. \text{term}} \quad \text{PVAL\_LOADED}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Unit} \Rightarrow y:\text{unit}. y = \text{unit}} \quad \text{PVAL\_UNIT}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{True} \Rightarrow y:\text{bool}. y = \text{true}} \quad \text{PVAL\_TRUE}$$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{False} \Rightarrow y:\text{bool}. y = \text{false}} \quad \text{PVAL\_FALSE}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{value}_i \Rightarrow y_i:\beta. \text{term}_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \beta[\overline{\text{value}_i^i}] \Rightarrow y:[\beta]. \bigwedge(\overline{[y^{(i)}/y_i] \text{term}_i^i})} \quad \text{PVAL\_LIST}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash value_i \Rightarrow y_i:\beta_i. term_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash (\overline{value_i^i}) \Rightarrow y:\overline{\beta_i^i}. \bigwedge ([y^{(i)}/y_i]term_i^i)} \quad \text{PVAL\_TUPLE}$$

$$\frac{\text{smt}(\Phi \Rightarrow \text{false})}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{error}(string, pval) \Rightarrow y:\beta. term} \quad \text{PVAL\_ERROR}$$

$$\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Nil } \beta() \Rightarrow y:[\beta]. y = \text{nil}} \quad \text{PVAL\_CTOR\_NIL}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow y_1:\beta. term_1 \\ \mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow y_2:[\beta]. term_2 \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Cons}(pval_1, pval_2) \Rightarrow y:[\beta]. [y^{(1)}/y_1]term_1 \wedge [\text{tl } y/y_2]term_2} \quad \text{PVAL\_CTOR\_CONS}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_i \Rightarrow y_i:\beta_i. term_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Tuple}(\overline{pval_i^i}) \Rightarrow y:\overline{\beta_i^i}. \bigwedge ([y^{(i)}/y_i]term_i^i)} \quad \text{PVAL\_CTOR\_TUPLE}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_i \Rightarrow y_i:\beta. term_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Array}(\overline{pval_i^i}) \Rightarrow y:\text{array } \beta. \bigwedge ([y[i]/y_i]term_i^i)} \quad \text{PVAL\_CTOR\_ARRAY}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow y:\beta. term}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{Specified}(pval) \Rightarrow y:\beta. term} \quad \text{PVAL\_CTOR\_SPECIFIED}$$

$$\frac{\overline{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_i \Rightarrow y_i:\beta_i. term_i^i}}{\mathcal{C}; \mathcal{L}; \Phi \vdash (\text{struct tag})\{.member_i = pval_i^i\} \Rightarrow y:\text{struct tag}. \bigwedge ([y.member_i/y_i]term_i^i)} \quad \text{PVAL\_STRUCT}$$

$\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine\_elem_i^i} :: arg \gg ret$

$$\frac{}{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash ::ret \gg ret} \text{SPINE\_EMPTY}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \_:\beta. \_ \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine\_elem_i}^i :: [pval/x]arg \gg ret \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash pval, \overline{spine\_elem_i}^i :: \Pi x:\beta. arg \gg ret} \text{SPINE\_COMPUTATIONAL}$$

$$\frac{\begin{array}{l} \mathcal{L} \vdash logical\_val:\beta \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine\_elem_i}^i :: [logical\_val/x]arg \gg ret \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash logical\_val, \overline{spine\_elem_i}^i :: \forall x:\beta. arg \gg ret} \text{SPINE\_LOGICAL}$$

$$\frac{\begin{array}{l} \text{smt}(\Phi \Rightarrow resource = resource') \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine\_elem_i}^i :: arg \gg ret \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R}, resource \vdash resource', \overline{spine\_elem_i}^i :: resource' \multimap arg \gg ret} \text{SPINE\_RESOURCE}$$

$$\frac{\begin{array}{l} \text{smt}(\Phi \Rightarrow term) \\ \mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine\_elem_i}^i :: arg \gg ret \end{array}}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \overline{spine\_elem_i}^i :: term \supset arg \gg ret} \text{SPINE\_CONSTRAINT}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash pexpr \Rightarrow ident:\beta. term}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow y:\beta. term}{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow y:\beta. term} \text{PEXPR\_VAL}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \_':loc. \_ \\ \mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \_':integer. \_ \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{array\_shift}(pval_1, \tau, pval_2) \Rightarrow y:loc. y = pval_1 +_{\text{ptr}} (pval_2 \times \text{size\_of}(\tau))} \text{PEXPR\_ARRAY\_SHIFT}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \_:\text{loc.} \_ \\ \_': \text{struct } tag \ \& \overline{\text{member}_i:\tau_i}^i \in \text{Globals} \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{member\_shift}(pval, tag, member_j) \Rightarrow y:\text{loc. } y = pval +_{\text{ptr}} \text{offset\_of}_{tag}(member_j)} \quad \text{PEXPR\_MEMBER\_SHIFT}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \_':\text{bool.} \_'}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{not}(pval) \Rightarrow y:\text{bool. } y = \neg pval} \quad \text{PEXPR\_NOT}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \_1:\text{integer.} \_1 \\ \mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \_2:\text{integer.} \_2 \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \text{ binop}_{arith} pval_2 \Rightarrow y:\text{integer. } y = (pval_1 \text{ binop}_{arith} pval_2)} \quad \text{PEXPR\_ARITH\_BINOP}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \_1:\text{integer.} \_1 \\ \mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \_2:\text{integer.} \_2 \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \text{ binop}_{rel} pval_2 \Rightarrow y:\text{bool. } y = (pval_1 \text{ binop}_{rel} pval_2)} \quad \text{PEXPR\_REL\_BINOP}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \_1:\text{bool.} \_1 \\ \mathcal{C}; \mathcal{L}; \Phi \vdash pval_2 \Rightarrow \_2:\text{bool.} \_2 \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \text{ binop}_{bool} pval_2 \Rightarrow y:\text{bool. } y = (pval_1 \text{ binop}_{bool} pval_2)} \quad \text{PEXPR\_BOOL\_BINOP}$$

$$\frac{\begin{array}{c} \mathcal{C}; \mathcal{L}; \Phi \vdash name \Rightarrow \_:\beta_1, \dots, \beta_n \rightarrow \beta'. \_ \\ \mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \_1:\beta_1. \_1 \dots \mathcal{C}; \mathcal{L}; \Phi \vdash pval_n \Rightarrow \_n:\beta_n. \_n \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash name(pval_1, \dots, pval_n) \Rightarrow y:\beta'. term'} \quad \text{PEXPR\_CALL}$$

$$\boxed{\text{pattern}:\beta \rightsquigarrow \mathcal{C}}$$

$$\boxed{\text{ident\_or\_pattern}:\beta \rightsquigarrow \mathcal{C}}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash tpval \Leftarrow \text{ident}:\beta. term}$$

$$\frac{\text{smt}(\Phi \Rightarrow \text{false})}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{undef } UB\_name \Leftarrow y:\beta. term} \quad \text{TPVAL\_UNDEF}$$



$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow y:\beta. term' \quad \text{smt}(\Phi, term' \Rightarrow term)}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{done } pval \Leftarrow y:\beta. term} \quad \text{TPVAL\_DONE}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi \vdash texpr \Leftarrow ident:\beta. term}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \text{bool}. \_ \\ \mathcal{C}; \mathcal{L}; y'; \Phi, pval = \text{true} \vdash texpr_1 \Leftarrow y:\beta. term \\ \mathcal{C}; \mathcal{L}; y'; \Phi, pval = \text{false} \vdash texpr_2 \Leftarrow y:\beta. term \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{if } pval \text{ then } texpr_1 \text{ else } texpr_2 \Leftarrow y:\beta. term} \quad \text{TPEXPR\_IF}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pexpr \Rightarrow \beta. \_ \\ ident\_or\_pattern:\beta \rightsquigarrow \mathcal{C}' \\ \mathcal{C}, \text{fresh}(\mathcal{C}'); \mathcal{L}; \Phi \vdash [\text{fresh}(\mathcal{C}')/\mathcal{C}'] texpr \Leftarrow y:\beta. term \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{let } ident\_or\_pattern = pexpr \text{ in } texpr \Leftarrow y:\beta. term} \quad \text{TPEXPR\_LET}$$

$$\frac{\begin{array}{l} \mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \beta. \_ \\ \overline{pattern_i:\beta \rightsquigarrow \mathcal{C}_i^i} \\ \mathcal{C}, \text{fresh}(\mathcal{C}_i); \mathcal{L}; \Phi \vdash [\text{fresh}(\mathcal{C}_i)/\mathcal{C}_i] texpr_i \Leftarrow y:\beta. term^i \end{array}}{\mathcal{C}; \mathcal{L}; \Phi \vdash \text{case } pval \text{ of } \overline{pattern_i \Rightarrow texpr_i^i} \text{ end} \Leftarrow y:\beta. term} \quad \text{TPEXPR\_CASE}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem\_action \Rightarrow ret}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow \text{integer}. \_}{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \text{create}(pval, \tau) \Rightarrow \Sigma y_p:\text{loc}. \exists y:\beta_\tau. \text{representable}(\tau*, y_p) \wedge \text{alignedI}(pval, y_p) \wedge [y_p] 1 \overset{\times}{\rightarrow}_\tau [y] \star \mathbf{I}} \quad \text{ACTION\_CREATE}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \text{loc. } \_ \\
\mathcal{C}; \mathcal{L}; \Phi \vdash pval' \Rightarrow y':\beta_\tau. term' \\
\text{smt}(\Phi, term' \Rightarrow \text{representable}(\tau, y')) \\
\text{smt}(\Phi \Rightarrow pval_0 = pval_1) \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \cdot, [pval_0] \vdash_{\rightarrow_\tau} [-'] \vdash \text{store}(\_, \tau, pval_1, pval', \_) \Rightarrow \Sigma \text{loc. unit. } \exists y':\beta_\tau. term' \wedge [pval_0] \vdash_{\rightarrow_\tau} [y'] \star \mathbf{I}
\end{array}
\quad \text{ACTION\_STORE}$$

$$\begin{array}{c}
\mathcal{C}; \mathcal{L}; \Phi \vdash pval_1 \Rightarrow \text{loc. } \_ \\
\text{smt}(\Phi \Rightarrow pval_0 = pval_1) \\
\hline
\mathcal{C}; \mathcal{L}; \Phi; \cdot, [pval_0] \vdash_{\rightarrow_\tau} [-'] \vdash \text{kill}(\text{static } \tau, pval_1) \Rightarrow \Sigma \text{loc. unit. } \mathbf{I}
\end{array}
\quad \text{ACTION\_KILL\_STATIC}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash seq\_expr \Rightarrow ret}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pval \Rightarrow y:\beta. term}{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash pval \Rightarrow \Sigma y:\beta. term \wedge \mathbf{I}} \quad \text{SEQ\_EXPR\_PURE}$$

$$\boxed{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash is\_expr \Rightarrow ret}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem\_action \Rightarrow ret}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{Pos } mem\_action \Rightarrow ret} \quad \text{IS\_EXPR\_ACTION}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash mem\_action \Rightarrow ret}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \text{Neg } mem\_action \Rightarrow ret} \quad \text{IS\_EXPR\_NEG\_ACTION}$$

Definition rules:            43 good    0 bad  
Definition rule clauses: 102 good    0 bad