tag OCaml type for struct/union tag $impl_const$ implementation-defined constant x, y, v, ident OCaml type variable for symbols

mem_int memory integer value

member C struct/union member name

annots annotations

nat OCaml arbitrary-width natural number

n, i index variables

loc OCaml type for C source

mem_iv_c OCaml type for memory constraints on integer values

UB_name undefined behaviour

string OCaml string

 $tyvar_{-}TY$ OCaml type variable for types

OCaml type for symbol prefix

mem_order OCaml type for memory order

linux_mem_order OCaml type for Linux memory order

k OCaml fixed-width integer

```
C type
Sctypes_{-}t, \tau
                   ::=
                                                OCaml type for an annotated C type
	au
                   ::=
β
                                                base types
                   ::=
                         unit
                                                   unit
                                                   boolean
                         bool
                         integer
                                                   integer
                                                   rational numbers?
                         real
                         loc
                                                   location
                         \operatorname{array} \beta
                                                   array
                         [\beta]
                                                   list
                         (\beta_1, \ldots, \beta_n)
                                                   tuple
                         \mathtt{struct}\,tag
                                                   struct
                         \{\beta\}
                                                   set
                         opt(\beta)
                                                   option
                         \beta_1, \ldots, \beta_n \to \beta
                                                   parameter types
                         of\_ctype(\tau)
                                                   of a C type
binop
                                                binary operators
                   ::=
                                                   addition
                                                   subtraction
                                                   multiplication
                                                   division
                                                   modulus
                         rem_t
                                                   remainder
                         rem_f
                                                   exponentiation
                                                   equality, defined both for integer and C types
                                                   greater than
                         >
                                                   less than
                         <
```

	>= <= /\ \/	greater than or equal to less than or equal to conjuction disjunction
polarity	::= Pos Neg	memory action polarities sequenced by let weak and let strong only sequenced by let strong
ident	::=	Ott-hack, ignore
name	$::= \ \mid ident \ \mid impl_const$	Core identifier implementation-defined constant
au	::=	Ott-hack, ignore
mem_ptr	<pre>::= nullptr funcptr ident concptr nat</pre>	pointer values null pointer function pointer concrete pointer
mem_val		memory value
$object_value$::=	C object values (inhabitants of object types), which can be read/stored

		mem_int	integer value
		mem_ptr	pointer value
		$\mathtt{array}\left(\overline{loaded_value_i}^i ight)$	C array value
	ĺ	$(\mathtt{struct} ident) \{ \overline{.member_i : au_i = mem_val_i}^{i} \}$	C struct value
	i	$(union ident)\{.member = mem_val\}$	C union value
	'		
$loaded_value$::=		potentially unspecified C object values
		$\verb specified object_value $	specified loaded value
β	::=		Ott-hack, ignore
value	::=		Core values
	ļ	object_value	C object value
		$loaded_value$	loaded C object value
		Unit	unit
		True	boolean true
		False	boolean false
		$\beta[value_1,, value_i]$	list
		$(value_1,, value_i)$	tuple
ctor	::=		data constructors
		$\mathtt{Nil}\beta$	empty list
		Cons	list cons
		Tuple	tuple
		Array	C array
		Ivmax	max integer value
		Ivmin	min integer value
	İ	Ivsizeof	sizeof value
	į	Ivalignof	alignof value
	j	IvCOMPL	bitwise complement

		IvAND IvOR IvXOR Specified Fvfromint Ivfromfloat	bitwise AND bitwise OR bitwise XOR non-unspecified loaded value cast integer to floating value cast floating to integer value
$ident_opt_eta$::= 	$_{-}:eta \ ident:eta$	type annotated optional identifier
$pattern_aux$::= 	$ident_opt_eta \ ctor(\overline{pattern_i}^i)$	
pattern	::=	$loc\ annots\ pattern_aux$	
$ident_or_pattern$::= 	$ident \\ pattern$	
ident	::=		Ott-hack, ignore
$pexpr_aux$::=	ident	pure expressions
		$impl_const$ $value$	implementation-defined constant
		$ ext{constrained}(\overline{mem_iv_c_i,ident_i}^i) \ ext{error}(string,ident)$	constrained value impl-defined static error

		$ctor(\overline{ident_i}^i) \\ array_shift (ident_1, \tau, ident_2) \\ member_shift (ident, ident, member) \\ not (ident) \\ ident_1 \ binop \ ident_2 \\ (struct \ ident) \{ \overline{.member_i = ident_i}^i \} \\ (union \ ident) \{ \overline{.member} = ident \} \\ member of (ident, member, ident) \\ name(ident_1, \dots, ident_n) \\ assert_undef (ident, loc, UB_name) \\ bool_to_integer (ident) \\ conv_int (\tau, ident) \\ wrapI (\tau, ident)$		data constructor application pointer array shift pointer struct/union member shift boolean not binary operations C struct expression C union expression C struct/union member access pure function call
pexpr	::=	$loc\ annots\ tyvar_TY\ pexpr_aux$		pure expressions with location and annotations
$tpexpr_aux$::= 	undef $loc\ UB_name$ case $ident$ of $\boxed{pattern_i\Rightarrow tpexpr_i}^i$ end let $ident_or_pattern=pexpr$ in $tpexpr$ if $ident$ then $tpexpr_1$ else $tpexpr_2$ done $ident$		top-level pure expressions undefined behaviour pattern matching pure let pure if pure done
tpexpr	::= 	$loc\ annots\ tyvar_TY\ tpexpr_aux$ $[\mathcal{C}/\mathcal{C}']tpexpr$	М	pure top-level pure expressions with location and annotations
m_kill_kind	::=	dynamic		

		$\mathtt{static}\tau$	
bool	::= 	true false	OCaml booleans
$action_aux$::=	$\label{eq:create} \begin{split} & \texttt{create} \cdot (ident, \tau) \\ & \texttt{create_readonly} \cdot (ident_1, \tau, ident_2) \\ & \texttt{alloc} \cdot (ident_1, ident_2) \\ & \texttt{kill} \cdot (m_kill_kind, ident) \\ & \texttt{store} \cdot (bool, \tau, ident_1, ident_2, mem_order) \\ & \texttt{load} \cdot (\tau, ident, mem_order) \\ & \texttt{rmw} \cdot (\tau, ident_1, ident_2, ident_3, mem_order_1, mem_order_2) \\ & \texttt{fence} \cdot (mem_order) \\ & \texttt{cmp_exch_strong} \cdot (\tau, ident_1, ident_2, ident_3, mem_order_1, mem_order_2) \\ & \texttt{cmp_exch_weak} \cdot (\tau, ident_1, ident_2, ident_3, mem_order_1, mem_order_2) \\ & \texttt{linux_fence} \cdot (linux_mem_order) \\ & \texttt{linux_store} \cdot (\tau, ident_1, ident_2, linux_mem_order) \\ & \texttt{linux_rmw} \cdot (\tau, ident_1, ident_2, linux_mem_order) \\ \\ & \texttt{linux_rmw} \cdot (\tau, ident_1, ident_2, linux_mem_order) \\ \\ & \texttt{linux_rmw} \cdot (\tau, ident_1, ident_2, linux_mem_order) \\ \\ & \texttt{linux_rmw} \cdot (\tau, ident_1, ident_2, linux_mem_order) \\ \\ & \texttt{linux_rmw} \cdot (\tau, ident_1, ide$	the boolean indicates whether the action is dynamic (i.e. free()) the boolean indicates whether the store is locking
action	::= 	$loc\ action_aux$	
memop	::= 	$ident_1 == ident_2$ $ident_1 \neq ident_2$ $ident_1 < ident_2$ $ident_1 > ident_2$	operations involving the memory state pointer equality comparison pointer inequality comparison pointer less-than comparison pointer greater-than comparison

```
ident_1 \leq ident_2
                                                                   pointer less-than comparison
                     ident_1 \geq ident_2
                                                                   pointer greater-than comparison
                     ident_1 -_{\tau} ident_2
                                                                   pointer subtraction
                     intFromPtr(\tau_1, \tau_2, ident)
                                                                   cast of pointer value to integer value
                     ptrFromInt (\tau_1, \tau_2, ident)
                                                                   cast of integer value to pointer value
                     ptrValidForDeref(\tau, ident)
                                                                   dereferencing validity predicate
                     ptrWellAligned(\tau, ident)
                     ptrArrayShift(ident_1, \tau, ident_2)
                     memcpy(ident_1, ident_2, ident_3)
                     memcmp(ident_1, ident_2, ident_3)
                     realloc(ident_1, ident_2, ident_3)
                     va\_start(ident_1, ident_2)
                     va\_copy(ident)
                     va\_arg(ident, \tau)
                     va\_end(ident)
paction
                                                                memory actions with polarity
                     action
                                                           Μ
                                                                   positive, sequenced by both let weak and let strong
                     \neg (action)
                                                           M
                                                                   negative, only sequenced by let strong
                                                                (effectful) expressions
expr\_aux
                     pure(pexpr)
                                                                   pure expression
                     memop(memop)
                                                                   pointer op involving memory
                     paction
                                                                   memory action
                     skip
                                                                   skip
                     ccall(\tau, ident, \overline{ident_i}^i)
                                                                   C function call
                     pcall (name, \overline{ident_i}^i)
                                                                   procedure call
                                                                (effectful) expressions with location and annotations
expr
               ::=
                     loc\ annots\ expr\_aux
```

```
texpr\_aux
                             \mathtt{let}\, ident\_or\_pattern = pexpr\, \mathtt{in}\, texpr
                             \mathtt{let}\,\mathtt{weak}\,pattern = expr\,\mathtt{in}\,texpr
                             \verb|let strong| ident\_or\_pattern = expr \verb|in| texpr
                             \verb|case| ident \verb|with| | \overline{|| pattern_i \Rightarrow texpr_i|}^i \verb|end|
                             if ident then texpr_1 else texpr_2
                             bound [k](texpr)
                             unseq(expr_1, .., expr_n)
                             nd(texpr_1, .., texpr_n)
                             {\tt done}\, ident
                             undef loc\ UB\_name
                             run ident ident_1, ..., ident_n
texpr
                     ::=
                             loc\ annots\ texpr\_aux
terminals
                             \in
                             П
                             \forall
                             \supset
                             \Sigma
```

top-level expressions

weak sequencing strong sequencing pattern matching conditional ??, doesn't exist at runtime unsequenced expressions nondeterministic sequencing end of top-level expression undefined behaviour run from label

top-level expressions with location and annotations

```
OCaml arbitrary-width integer
z
       ::=
             of_mem_int(mem_int)
                                      Μ
             of_nat(nat)
                                      Μ
             of_ctype(\tau)
                                      Μ
                                             size of a C type
                                      Μ
             ptr_size
                                             size of a pointer
                                           Ott-hack, ignore
\mathbb{Q}
             \frac{k_1}{k_2}
lit
       ::=
             ident
             bool
```

```
\mathtt{int}\,z
                               \mathbb{Q}
                               \operatorname{\mathtt{ptr}} z
bool\_op
                               \neg term
                               term_1 = term_2
                               \bigwedge(\overline{term_i}^i)
arith\_op
                       ::=
                               term_1 \times term_2
list\_op
                       ::=
                               nil
                               term_1 :: term_2
                              [term_1, ..., term_n]
term^{(k)}
tuple\_op
                       ::=
                               (term_1, ..., term_n)
term^{(k)}
pointer\_op
                       ::=
                               nullop
                               term_1 +_{ptr} term_2
option\_op
                               \mathtt{none}\,BT_-t
                               \verb"some"\,term"
```

```
array\_op
                ::=
                       term[\, \mathtt{int}\, z]
param\_op
                ::=
                       term(term_1, ..., term_n)
struct\_op
                ::=
                       term.member \\
ct\_pred
                ::=
                      \texttt{representable}\left(\tau, term\right)
                       alignedI(term_1, term_2)
term\_aux
                ::=
                       arith\_op
                       bool\_op
                       tuple\_op
                       struct\_op
                      pointer\_op
                      list\_op
                       array\_op
                       ct\_pred
                       option\_op
                       param\_op
bt
                                                        Ott-hack, ignore
                ::=
BT_-t
                                                        Ott-hack, ignore
                ::=
term
                ::=
```

```
lit
                             term\_aux\ bt
                                                                                    S
                                                                                            parentheses
                             (term)
                             [term_1/ident]term_2
                                                                                    Μ
IT_{-}t
                                                                                         Ott-hack, ignore
                       ::=
IT\_t\_list
                                                                                         Ott-hack, ignore
                       ::=
point
                                                                                         points-to predicate
                       ::=
                             IT_{-}t_1 \mapsto_{z,IT_{-}t_2} IT_{-}t_3
predicate\_name
                                                                                         names of predicates
                             Sctypes\_t
                             string
predicate
                                                                                         arbitrary predicate
                       ::=
                             predicate\_name(IT\_t_1, IT\_t\_list_1 \mapsto IT\_t\_list_2)
resource
                       ::=
                             point
                             predicate
                                                                                         argument types
arg
                             \Pi ident: \beta.arg
                             \forall ident: \beta.arg
                             resource \multimap arg
                             term \supset arg
                             Ι
```

```
ret
                                                                 return types
                            \Sigma ident: \beta.ret
                             \exists ident: \beta.ret
                            resource \star ret
                             term \wedge ret
                             Ι
\mathcal{C}
                                                                 computational var env
                            C, ident: BT_-t
                            \mathcal{C},\mathcal{C}'
                            \operatorname{fresh}(\mathcal{C})
                                                          M
                                                                     identical context except with fresh variable names
\mathcal{L}
                                                                 logical var env
                             \mathcal{L}, ident
Φ
                                                                 constraints env
                             \Phi, term
                                                                     Ott-hack, ignore
                             \Phi, ret
\mathcal{R}
                                                                 resources env
                             \mathcal{R}, resource
formula
                    egin{array}{ll} judgement \ | & smt \left(\Phi \Rightarrow ret
ight) \ | & ident_i: eta_i \in \mathcal{C}_i^{\ i} \end{array}
                                                                     theorem to be proved: ret only consists of logical constraints
```

```
ident: \mathtt{struct} \ tag \ \& \ \overline{member_i: 	au_i}^i \in \mathtt{Globals}

\frac{\overline{C_i; \mathcal{L}_i; \Phi_i \vdash mem\_val_i} \Rightarrow mem y_i, \beta_i, term_i}{\overline{C_i; \mathcal{L}_i; \Phi_i \vdash value_i} \Rightarrow y_i, \beta_i, term_i}^{i}} \\
\frac{\overline{C_i; \mathcal{L}_i; \Phi_i \vdash value_i} \Rightarrow y_i, \beta_i, term_i}^{i}}{\overline{pattern_i} : \beta_i \leadsto \overline{C_i}^{i}} \\
\frac{\overline{C_i; \mathcal{L}_i; \Phi_i \vdash tpexpr_i} \Leftarrow ret_i}^{i}}{\overline{C_i; \mathcal{L}_i; \Phi_i \vdash tpexpr_i} \Leftarrow ret_i}^{i}}

mem\_value\_jtype
                                                                         C; \mathcal{L}; \Phi \vdash mem\_val \Rightarrow mem y, \beta, term
value\_jtype
                                                                        C; \mathcal{L}; \Phi \vdash object\_value \Rightarrow obj ident, \beta, term
                                                                        C; \mathcal{L}; \Phi \vdash value \Rightarrow ident, \beta, term
pexpr\_jtype
                                                                        C; \mathcal{L}; \Phi \vdash pexpr\_aux \Rightarrow ret
pattern\_jtype
                                                                        pattern: \beta \leadsto \mathcal{C}
                                                                        ident\_or\_pattern: \beta \leadsto \mathcal{C}
 tpexpr\_jtype
                                                                        C; \mathcal{L}; \Phi \vdash pexpr \Rightarrow ret
                                                                        C; \mathcal{L}; \Phi \vdash tpexpr \Leftarrow ret
                                                                        C; \mathcal{L}; \Phi \vdash tpexpr\_aux \Leftarrow ret
 expr_{-}jtype
                                                                        C; \mathcal{L}; \Phi; \mathcal{R} \vdash action\_aux \Rightarrow ret
                                                                         C; \mathcal{L}; \Phi; \mathcal{R} \vdash expr\_aux \Rightarrow ret
judgement
```

```
mem\_value\_jtype
                      value\_jtype
                      pexpr\_jtype
                      pattern\_jtype
                      tpexpr\_jtype
                      expr\_jtype
user\_syntax
                      tag
                      impl\_const
                      \boldsymbol{x}
                      mem\_int
                      member
                      annots
                      nat
                      n
                      loc
                      mem\_iv\_c
                      UB\_name
                      string
                      tyvar\_TY
                      mem\_order
                      linux\_mem\_order
                      Sctypes\_t
                      binop
                      polarity
```

identnameau mem_ptr mem_val $object_value$ $loaded_value$ β valuector $ident_opt_\beta$ $pattern_aux$ pattern $ident_or_pattern$ ident $pexpr_aux$ pexpr $tpexpr_aux$ tpexpr m_kill_kind bool $action_aux$ actionmemoppaction $expr_aux$ expr $texpr_aux$

texpr

```
terminals
z
\mathbb{Q}
lit
bool\_op
arith\_op
list\_op
tuple\_op
pointer\_op
option\_op
array\_op
param\_op
struct\_op
ct\_pred
term_{-}aux
bt
BT_-t
term
IT_{-}t
IT\_t\_list
point
predicate\_name
predicate
resource
arg
ret
\mathcal{C}
\mathcal{L}
\Phi
```

```
\mathcal{R} formula
```

```
C; \mathcal{L}; \Phi \vdash mem\_val \Rightarrow mem y, \beta, term
```

$$\overline{C;\mathcal{L};\Phi\vdash \mathrm{int}\,mem_int}\Rightarrow \mathrm{mem}\,y, \mathrm{integer},y=\mathrm{intof_mem_int}(mem_int)} \quad \mathrm{Val_OBJ_MEM_INT}$$

$$\overline{C;\mathcal{L};\Phi\vdash \mathrm{nullptr}\Rightarrow \mathrm{mem}\,y, \mathrm{loc},y=\mathrm{nullop}} \quad \mathrm{Val_OBJ_MEM_PTR_NULL}$$

$$\overline{C;\mathcal{L};\Phi\vdash \mathrm{funcptr}\,ident}\Rightarrow \mathrm{mem}\,y, \mathrm{loc},y=\mathrm{ident}} \quad \mathrm{Val_OBJ_MEM_PTR_FUNC}$$

$$\overline{C;\mathcal{L};\Phi\vdash \mathrm{concptr}\,nat}\Rightarrow \mathrm{mem}\,y, \mathrm{loc},y=\mathrm{ptrof_nat}(nat) \quad \mathrm{Val_OBJ_MEM_PTR_CONC}$$

$$\overline{C;\mathcal{L};\Phi\vdash \mathrm{mem_val}_i\Rightarrow \mathrm{mem}\,y_i,\beta,term_i}^i$$

$$\overline{C;\mathcal{L};\Phi\vdash \mathrm{array}\,(\overline{mem_val}_i^i)}\Rightarrow \mathrm{mem}\,y,\mathrm{array}\,\beta,\Lambda([y[\mathrm{int}\,z_i]/y_i]term_i}^i) \quad \mathrm{Val_OBJ_MEM_ARR}$$

$$\overline{C;\mathcal{L};\Phi\vdash \mathrm{mem_val}_i\Rightarrow \mathrm{mem}\,y_i,\beta_i,term_i}^i$$

$$\overline{C;\mathcal{L};\Phi\vdash (\mathrm{struct}\,tag)\{\overline{member}_i=\overline{mem_val}_i^i\}}\Rightarrow \mathrm{mem}\,y,\mathrm{struct}\,tag,\Lambda([y.\overline{member}_i/y_i]term_i}^i)} \quad \mathrm{Val_OBJ_Mem_Struct}$$

$$\overline{C;\mathcal{L};\Phi\vdash \mathrm{object_value}}\Rightarrow \mathrm{obj}\,ident,\beta,term}$$

$$\overline{C;\mathcal{L};\Phi\vdash \mathrm{mem_int}}\Rightarrow \mathrm{obj}\,y,\mathrm{integer},y=\mathrm{intof_mem_int}(mem_int)} \quad \mathrm{Val_OBJ_INT}$$

$$\overline{C;\mathcal{L};\Phi\vdash \mathrm{mem_int}}\Rightarrow \mathrm{obj}\,y,\mathrm{loc},y=\mathrm{nullop}} \quad \mathrm{Val_OBJ_Ptr_Null}$$

```
\overline{\mathcal{C};\mathcal{L};\Phi \vdash \mathtt{funcptr}\, ident} \Rightarrow \mathtt{obj}\, y, \mathtt{loc}, y = ident} \quad \text{Val\_Obj\_Ptr\_Func}
                                                                                       \overline{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathsf{concptr}\, nat \Rightarrow \, \mathsf{obj}\, y, \mathsf{loc}, y = \mathsf{ptr}\, \mathsf{of}\_\mathsf{nat}(nat)} \quad \mathsf{Val\_Obj\_Ptr\_Conc}
                                                                                                                       \overline{C}; \mathcal{L}; \Phi \vdash loaded\_value_i \Rightarrow y_i, \beta, term_i^i
                                                                     \frac{\mathcal{C}; \mathcal{L}; \Phi \vdash loaded\_value_i \Rightarrow y_i, \beta, term_i \ \ }{\mathcal{C}; \mathcal{L}; \Phi \vdash \operatorname{array}(\overline{loaded\_value_i}^i) \Rightarrow \operatorname{obj} y, \operatorname{array} \beta, \bigwedge(\overline{[y[\operatorname{int} z_i]/y_i]term_i}^i)} \quad \operatorname{Val\_Obj\_Arr}
                                                                                                        ident: \mathtt{struct} \, tag \ \& \ \overline{member_i : \tau_i}^i \in \mathtt{Globals}
                                                                                                        \overline{C}; \mathcal{L}; \Phi \vdash mem\_val_i \Rightarrow mem y_i, \beta_i, term_i
                               \frac{\mathcal{C},\mathcal{L},* \vdash mem\_val_i \neq mem}{\mathcal{C};\mathcal{L};\Phi \vdash (\mathsf{struct}\,tag)\{\overline{.member_i : \tau_i = mem\_val_i}^i\} \Rightarrow \mathsf{obj}\,y,\mathsf{struct}\,tag,\bigwedge(\overline{[y.member_i/y_i]term_i}^i)} \quad \mathsf{VAL\_OBJ\_STRUCT}
C; \mathcal{L}; \Phi \vdash value \Rightarrow ident, \beta, term
                                                                                                                            \frac{\mathcal{C}; \mathcal{L}; \Phi \vdash object\_value \Rightarrow \mathsf{obj} \ y, \beta, term}{\mathcal{C}; \mathcal{L}; \Phi \vdash object\_value \Rightarrow y, \beta, term} \quad \text{Val\_Obj}
                                                                                                               \frac{\mathcal{C}; \mathcal{L}; \Phi \vdash object\_value \Rightarrow \mathtt{obj} \ y, \beta, term}{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathtt{specified} \ object\_value \Rightarrow y, \beta, term} \quad \text{Val\_Loaded}
                                                                                                                                    C; \mathcal{L}; \Phi \vdash \text{Unit} \Rightarrow y, \text{unit}, y = () VAL_UNIT
                                                                                                                                 \overline{\mathcal{C};\mathcal{L};\Phi \vdash \mathtt{True} \Rightarrow y,\mathtt{bool},y=\mathtt{true}} \quad \mathsf{Val\_True}
                                                                                                                             \overline{\mathcal{C};\mathcal{L};\Phi \vdash \mathtt{False} \Rightarrow y,\mathtt{bool},y=\mathtt{false}} \quad \text{Val\_False}
```

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash value_1 \Rightarrow y_1, \beta, term_1 ... \mathcal{C}; \mathcal{L}; \Phi \vdash value_n \Rightarrow y_n, \beta, term_n}{\mathcal{C}; \mathcal{L}; \Phi \vdash \beta[value_1, ..., value_n] \Rightarrow y, [\beta], \bigwedge([y^{(k_1)}/y_1]term_1, ..., [y^{(k_n)}/y_n]term_n)} \quad \text{Val_List}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash value_1 \Rightarrow y_1, \beta_1, term_1 ... \mathcal{C}; \mathcal{L}; \Phi \vdash value_n \Rightarrow y_n, \beta_n, term_n}{\mathcal{C}; \mathcal{L}; \Phi \vdash (value_1, ..., value_n) \Rightarrow y, (\beta_1, ..., \beta_n), \bigwedge([y^{(k_1)}/y_1]term_1, ..., [y^{(k_n)}/y_n]term_n)} \quad \text{Val_Tuple}$$

 $C; \mathcal{L}; \Phi \vdash pexpr_aux \Rightarrow ret$

$$\frac{x: \beta \in \mathcal{C}}{\mathcal{C}; \mathcal{L}; \Phi \vdash x \Rightarrow \Sigma \, y: \beta. y = x \, \land \, \mathsf{I}} \quad \mathsf{PEXPR_AUX_VAR}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash value \Rightarrow y, \beta, term}{\mathcal{C}; \mathcal{L}; \Phi \vdash value \Rightarrow \Sigma \ y: \beta. term \land \mathtt{I}} \quad \mathsf{PEXPR_AUX_VAL}$$

$$\frac{\mathtt{smt}\,(\Phi\Rightarrow\mathtt{false}\,\wedge\,\mathtt{I})}{\mathcal{C};\mathcal{L};\Phi\vdash\mathtt{error}\,(string,ident)\Rightarrow ret}\quad \mathtt{PEXPR_AUX_ERROR}$$

$$\overline{\mathcal{C};\mathcal{L};\Phi \vdash \mathtt{Nil}\,\beta(\,) \Rightarrow \Sigma\,y : [\beta].y = \mathtt{nil}\ \land \mathtt{I}} \quad \mathsf{PExpr_Aux_Ctor_Nil}$$

$$\begin{aligned} x_1 : \beta \in \mathcal{C} \\ x_2 : [\beta] \in \mathcal{C} \\ \overline{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathsf{Cons}(x_1, x_2) \Rightarrow \Sigma \ y : [\beta]. y = x_1 :: x_2 \ \land \mathtt{I}} \end{aligned} \quad \text{PExpr_Aux_Ctor_Cons}$$

$$\frac{x_1:\beta_1\in\mathcal{C}..x_n:\beta_n\in\mathcal{C}}{\mathcal{C};\mathcal{L};\Phi\vdash \mathtt{Tuple}(x_1,..,x_n)\Rightarrow\Sigma\,y:(\beta_1,..,\beta_n).y=(x_1,..,x_n)\,\wedge\,\mathtt{I}}\quad \mathtt{PEXPR_AUX_CTOR_TUPLE}$$

$$\frac{x_1:\beta\in\mathcal{C}..x_n:\beta\in\mathcal{C}}{\mathcal{C};\mathcal{L};\Phi\vdash\operatorname{Array}(x_1,..,x_n)\Rightarrow\Sigma\,y:\operatorname{array}\beta.\bigwedge(y[\operatorname{int}z_1]=x_1,..,y[\operatorname{int}z_n]=x_n)\,\wedge\,\mathtt{I}}\quad\operatorname{PEXPR_AUX_CTOR_ARRAY}$$

$$\frac{x:\beta\in\mathcal{C}}{\mathcal{C};\mathcal{L};\Phi\vdash \mathtt{Specified}(x)\Rightarrow \Sigma\,y:\beta.y=x\,\wedge\,\mathtt{I}}\quad \mathtt{PExpr_Aux_Ctor_Specified}$$

$$x_1: \mathtt{loc} \in \mathcal{C} \ x_2: \mathtt{integer} \in \mathcal{C}$$

PEXPR_AUX_ARRAY_SHIFT $\overline{\mathcal{C};\mathcal{L};\Phi \vdash \mathtt{array_shift}\,(x_1,\tau,x_2) \Rightarrow \Sigma\,\,y: \mathtt{loc}.y = x_1 +_{\mathtt{ptr}} x_2 \times \mathtt{int}\,\mathtt{of_ctype}(\tau) \ \land \mathtt{I}}$

$$\overline{\mathcal{C};\mathcal{L};\Phi \vdash \mathtt{not}\,(x) \Rightarrow \Sigma\,y : \mathtt{bool}.y = (\lnot\,x\,)\,\land\,\mathtt{I}} \quad \mathsf{PExpr_Aux_Not}$$

 $pattern: \beta \leadsto \mathcal{C}$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pexpr_aux \Rightarrow ret}{\mathcal{C}; \mathcal{L}; \Phi \vdash loc \ annots \ tyvar_TY \ pexpr_aux \Rightarrow ret} \quad \text{PExpr_Aux}$$

 $C; \mathcal{L}; \Phi \vdash tpexpr \Leftarrow ret$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash tpexpr_aux \Leftarrow ret}{\mathcal{C}; \mathcal{L}; \Phi \vdash loc \ annots \ tyvar_TY \ tpexpr_aux \Leftarrow ret} \quad \text{TPExpr_Aux}$$

 $C; \mathcal{L}; \Phi \vdash tpexpr_aux \Leftarrow ret$

$$\frac{\mathtt{smt}\,(\Phi\Rightarrow\mathtt{false}\wedge\mathtt{I})}{\mathcal{C};\mathcal{L};\Phi\vdash\mathtt{undef}\,loc\;UB_name\Leftarrow\mathit{ret}}\quad\mathsf{TPExpr_Aux_Undef}$$

$$x: \mathtt{bool} \in \mathcal{C}$$

$$\mathcal{C}; \mathcal{L}; \Phi, x = \mathtt{true} \vdash tpexpr_1 \Leftarrow ret$$

$$\mathcal{C}; \mathcal{L}; \Phi, x = \mathtt{false} \vdash tpexpr_2 \Leftarrow ret$$

$$\mathsf{TPExpr_Aux_IF}$$

 $\overline{\mathcal{C};\mathcal{L};\Phi} \vdash \text{if } x \text{ then } tpexpr_1 \text{ else } tpexpr_2 \Leftarrow ret$

$$\begin{aligned} x: \beta &\in \mathcal{C} \\ && \text{smt} \left(\Phi \Rightarrow ret \right) \\ \hline \mathcal{C}; \mathcal{L}; \Phi \vdash \text{done} \ x &\leftarrow \Sigma \ y: \beta.ret \end{aligned} \quad \text{TPExpr_Aux_Done}$$

$$\begin{split} & \mathcal{C}; \mathcal{L}; \Phi \vdash pexpr \Rightarrow \Sigma \ y : \beta.ret' \\ & ident_or_pattern : \beta \leadsto \mathcal{C}' \\ & \mathcal{C}, \mathrm{fresh}(\mathcal{C}'); \mathcal{L}; \Phi \vdash [\mathrm{fresh}(\mathcal{C}')/\mathcal{C}'] tpexpr \Leftarrow ret \\ & \overline{\mathcal{C}; \mathcal{L}; \Phi \vdash \mathtt{let} \ ident_or_pattern = pexpr \ \mathtt{in} \ tpexpr \Leftarrow ret} \end{split}$$
 TPExpr_Aux_Let

$$\frac{x: \beta \in \mathcal{C}}{pattern_i: \beta \leadsto \mathcal{C}_i}^i$$

$$\frac{\mathcal{C}, \operatorname{fresh}(\mathcal{C}_i); \mathcal{L}; \Phi \vdash [\operatorname{fresh}(\mathcal{C}_i)/\mathcal{C}_i] tpexpr_i \Leftarrow ret}^i}{\mathcal{C}; \mathcal{L}; \Phi \vdash \operatorname{case} x \text{ of } \overline{\mid pattern_i \Rightarrow tpexpr_i}^i \text{ end } \Leftarrow ret} \quad \text{TPExpr_Aux_Case}$$

 $C; \mathcal{L}; \Phi; \mathcal{R} \vdash action_aux \Rightarrow ret$

$$\frac{x: \mathtt{integer} \in \mathcal{C}}{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \mathtt{create}\,(x,\tau) \Rightarrow \Sigma\, y: \mathtt{loc}. \exists\, y': \mathtt{of_ctype}(\tau). \mathtt{representable}\,(*\tau,y) \, \wedge \, \mathtt{alignedI}\,(x,y) \, \wedge \, \tau(y,[] \mapsto [y',\mathtt{false}]) \star \mathtt{I}} \quad \text{ACTION_CREATE}$$

$$\frac{x_1 : \texttt{loc} \in \mathcal{C}}{x_2 : \texttt{of_ctype}(\tau) \in \mathcal{C}} \\ \frac{\mathcal{C}; \mathcal{L}; \Phi; \cdot, x_1 \mapsto_{\texttt{ptr_size}, 1} \textit{term} \vdash \texttt{store}\left(\textit{bool}, \tau, x_1, x_2, \textit{mem_order}\right) \Rightarrow \Sigma \, y : \texttt{unit}.x_1 \mapsto_{\texttt{ptr_size}, 1} x_2 \star \mathtt{I}} \quad \text{ACTION_STORE}$$

 $C; \mathcal{L}; \Phi; \mathcal{R} \vdash expr_aux \Rightarrow ret$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi \vdash pexpr \Rightarrow ret}{\mathcal{C}; \mathcal{L}; \Phi; \cdot \vdash \mathsf{pure}\left(pexpr\right) \Rightarrow ret} \quad \texttt{EXPR_AUX_PURE}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash action_aux \Rightarrow ret}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash loc\ action_aux \Rightarrow ret} \quad \text{Expr_Aux_Action}$$

$$\frac{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash action_aux \Rightarrow ret}{\mathcal{C}; \mathcal{L}; \Phi; \mathcal{R} \vdash \neg (loc\ action_aux) \Rightarrow ret} \quad \text{Expr_Aux_Neg_Action}$$

Definition rules: 41 good 0 bad Definition rule clauses: 80 good 0 bad