Package 'bfpwr'

October 18, 2024

Version 0.1

Date 2024-10-18
Author Samuel Pawel [aut, cre] (https://orcid.org/0000-0003-2779-320X)
Maintainer Samuel Pawel <samuel.pawel@uzh.ch></samuel.pawel@uzh.ch>
Title Power and Sample Size Calculations for Bayes Factor Analysis
Description Implements z-test, t-test, and normal moment prior Bayes factors based on summary statistics, along with functionality to perform corresponding power and sample size calculations (Pawel and Held, 2024) <doi:10.48550 arxiv.2406.19940="">.</doi:10.48550>
License GPL-3
Encoding UTF-8
Imports lamW
Suggests roxygen2, tinytest, knitr
VignetteBuilder knitr
NeedsCompilation no
RoxygenNote 7.3.1
<pre>URL https://github.com/SamCH93/bfpwr</pre>
<pre>BugReports https://github.com/SamCH93/bfpwr/issues</pre>
Contents
bf01 nbf01 nmbf01 nnmbf01 ntbf01 pbf01 plot.power.bftest pnmbf01 powerbf01 powernmbf01
1

bf01

powertbf01	
ptbf01	
tbf01	20
Index	23

bf01 z-test Bayes factor

Description

This function computes the Bayes factor that quantifies the evidence that the data (in the form of an asymptotically normally distributed parameter estimate with standard error) provide for a point null hypothesis with a normal prior assigned to the parameter under the alternative. The standard error is assumed to be known.

Usage

```
bf01(estimate, se, null = 0, pm, psd, log = FALSE)
```

Arguments

estimate	Parameter estimate
se	Standard error of the parameter estimate
null	Parameter value under the point null hypothesis. Defaults to 0
pm	Mean of the normal prior assigned to the parameter under the alternative
psd	Standard deviation of the normal prior assigned to the parameter under the alternative. Set to \emptyset to obtain a point prior at the prior mean
log	Logical indicating whether the natural logarithm of the Bayes factor should be returned. Defaults to FALSE

Value

Bayes factor in favor of the null hypothesis over the alternative (BF > 1 indicates evidence for the null hypothesis, whereas BF < 1 indicates evidence for the alternative)

Author(s)

Samuel Pawel

```
bf01(estimate = 0.2, se = 0.05, null = 0, pm = 0, psd = 2)
```

nbf01 3

nbf01

Sample size determination for z-test Bayes factor

Description

This function computes the required sample size to obtain a Bayes factor (bf01) more extreme than a threshold k with a specified target power.

Usage

```
nbf01(
    k,
    power,
    usd,
    null = 0,
    pm,
    psd,
    dpm = pm,
    dpsd = psd,
    nrange = c(1, 10^5),
    lower.tail = TRUE,
    integer = TRUE,
    analytical = TRUE,
    ...
)
```

k	Bayes factor threshold
power	Target power
usd	Unit standard deviation, the standard error of the parameter estimate based on $n=1,$ see details
null	Parameter value under the point null hypothesis. Defaults to 0
pm	Mean of the normal prior assigned to the parameter under the alternative in the analysis
psd	Standard deviation of the normal prior assigned to the parameter under the alternative in the analysis. Set to \emptyset to obtain a point prior at the prior mean
dpm	Mean of the normal design prior assigned to the parameter. Defaults to the same value as the analysis prior pm
dpsd	Standard deviation of the normal design prior assigned to the parameter. Defaults to the same value as the analysis prior psd
nrange	Sample size search range over which numerical search is performed. Defaults to $c(1, 10^5)$
lower.tail	Logical indicating whether $Pr(BF \le k)$ (TRUE) or $Pr(BF > k)$ (FALSE) should be computed. Defaults to TRUE

4 nbf01

integer	Logical indicating whether only integer valued sample sizes should be returned. If TRUE the required sample size is rounded to the next larger integer. Defaults to TRUE
analytical	Logical indicating whether analytical (if available) or numerical method should be used. Defaults to \ensuremath{TRUE}
	Other arguments passed to stats::uniroot

Details

It is assumed that the standard error of the future parameter estimate is of the form $se = usd/\sqrt{n}$. For example, for normally distributed data with known standard deviation sd and two equally sized groups of size n, the standard error of an estimated standardized mean difference is $se = sd\sqrt{2/n}$, so the corresponding unit standard deviation is $usd = sd\sqrt{2}$. See the vignette for more information.

Value

The required sample size to achieve the specified power

Author(s)

Samuel Pawel

See Also

```
pbf01, powerbf01, bf01
```

nmbf01 5

Timble1 Ivormai moment prior Bayes jactor	nmbf01	Normal moment prior Bayes factor	
---	--------	----------------------------------	--

Description

This function computes the Bayes factor that quantifies the evidence that the data (in the form of an asymptotically normally distributed parameter estimate with standard error) provide for a point null hypothesis with a normal moment prior assigned to the parameter under the alternative.

Usage

```
nmbf01(estimate, se, null = 0, psd, log = FALSE)
```

Arguments

estimate	Parameter estimate
se	Standard error of the parameter estimate
null	Parameter value under the point null hypothesis. Defaults to 0
psd	Spread of the normal moment prior assigned to the parameter under the alternative. The modes of the prior are located at $\pm\sqrt{2}\rm psd$
log	Logical indicating whether the natural logarithm of the Bayes factor should be returned. Defaults to FALSE

Details

A normal moment prior has density $f(x \mid \text{null}, \text{psd}) = N(x \mid \text{null}, \text{psd}^2) \times (x - \text{null})/\text{psd}^2$ with $N(x \mid m, v)$ the normal density with mean m and variance v evaluated at x.

Value

Bayes factor in favor of the null hypothesis over the alternative (BF > 1 indicates evidence for the null hypothesis, whereas BF < 1 indicates evidence for the alternative)

Author(s)

Samuel Pawel

References

Johnson, V. E. and Rossell, D. (2010). On the use of non-local prior densities in Bayesian hypothesis tests. Journal of the Royal Statistical Society: Series B (Statistical Methodology), 72(2):143–170. doi:10.1111/j.14679868.2009.00730.x

Pramanik, S. and Johnson, V. E. (2024). Efficient alternatives for Bayesian hypothesis tests in psychology. Psychological Methods, 29(2):243–261. doi:10.1037/met0000482

6 nnmbf01

See Also

```
nmbf01, pnmbf01, nnmbf01, powernmbf01
```

Examples

```
nmbf01(estimate = 0.25, se = 0.05, null = 0, psd = 0.5/sqrt(2)) # mode at 0.5
```

nnmbf01

Sample size determination for normal moment prior Bayes factor

Description

This function computes the required sample size to obtain a normal moment prior Bayes factor (nbf01) more extreme than a threshold k with a specified target power.

Usage

```
nnmbf01(
    k,
    power,
    usd,
    null = 0,
    psd,
    dpm,
    dpsd,
    nrange = c(1, 10^5),
    lower.tail = TRUE,
    integer = TRUE,
    ...
)
```

k	Bayes factor threshold
power	Target power
usd	Unit standard deviation, the standard error of the parameter estimate based on $n=1,$ see details
null	Parameter value under the point null hypothesis. Defaults to 0
psd	Spread of the normal moment prior assigned to the parameter under the alternative in the analysis. The modes of the prior are located at $\pm\sqrt{2}\rm psd$
dpm	Mean of the normal design prior assigned to the parameter
dpsd	Standard deviation of the normal design prior assigned to the parameter. Set to 0 to obtain a point prior at the design prior mean

ntbf01 7

nrange	Sample size search range over which numerical search is performed. Defaults to $c(1, 10^5)$
lower.tail	Logical indicating whether $Pr(BF \le k)$ (TRUE) or $Pr(BF > k)$ (FALSE) should be computed. Defaults to TRUE
integer	Logical indicating whether only integer valued sample sizes should be returned. If TRUE the required sample size is rounded to the next larger integer. Defaults to TRUE
	Other arguments passed to stats::uniroot

Details

It is assumed that the standard error of the future parameter estimate is of the form $se = usd/\sqrt{n}$. For example, for normally distributed data with known standard deviation sd and two equally sized groups of size n, the standard error of an estimated standardized mean difference is $se = sd\sqrt{2/n}$, so the corresponding unit standard deviation is $usd = sd\sqrt{2}$. See the vignette for more information.

Value

The required sample size to achieve the specified power

Author(s)

Samuel Pawel

See Also

```
nmbf01, pnmbf01, powernmbf01
```

Examples

```
nnmbf01(k = 1/10, power = 0.9, usd = 1, null = 0, psd = 0.5/sqrt(2), dpm = 0.5, dpsd = 0)
```

ntbf01	Sample size calculations for t-test Bayes factor	

Description

This function computes the required sample size to obtain a t-test Bayes factor (tbf01) more extreme than a threshold k with a specified target power.

8 ntbf01

Usage

```
ntbf01(
    k,
    power,
    null = 0,
    plocation = 0,
    pscale = 1/sqrt(2),
    pdf = 1,
    type = c("two.sample", "one.sample", "paired"),
    alternative = c("two.sided", "less", "greater"),
    dpm = plocation,
    dpsd = pscale,
    lower.tail = TRUE,
    integer = TRUE,
    nrange = c(2, 10^4),
    ...
)
```

Arguments

k	Raves	factor	threshold
Γ\	Dayes	ractor	unconoid

power Target power

null Standardized mean difference under the point null hypothesis. Defaults to 0

plocation t prior location. Defaults to 0

pscale t prior scale. Defaults to 1/sqrt(2)

pdf t prior degrees of freedom. Defaults to 1 (a Cauchy prior)

type Type of t-test. Can be "two.sample" (default), "one.sample", or "paired"

alternative Direction of the test. Can be either "two.sided" (default), "less", or "greater".

The latter two truncate the analysis prior to negative and positive effects, respectively. If set to "less" or "greater", the power is only computed based on data

with effect estimates in the direction of the alternative

dpm Mean of the normal design prior assigned to the standardized mean difference.

Defaults to the analysis prior location

dpsd Standard deviation of the normal design prior assigned to the standardized mean

difference. Set to 0 to obtain a point prior at the design prior mean. Defaults to

the analysis prior scale

lower.tail Logical indicating whether $Pr(BF \le k)$ (TRUE) or Pr(BF > k) (FALSE) should be

computed. Defaults to TRUE

integer Logical indicating whether only integer valued sample sizes should be returned.

If TRUE the required sample size is rounded to the next larger integer. Defaults

to TRUE

nrange Sample size search range over which numerical search is performed. Defaults

to c(2, 10⁴)

... Other arguments passed to stats::uniroot

pbf01

Value

The required sample size to achieve the specified power

Author(s)

Samuel Pawel

See Also

```
ptbf01, powertbf01, tbf01
```

Examples

```
## example from Schönbrodt and Wagenmakers (2018, p.135)  
ntbf01(k = 1/6, power = 0.95, dpm = 0.5, dpsd = 0, alternative = "greater")  
ntbf01(k = 1/6, power = 0.95, dpm = 0.5, dpsd = 0.1, alternative = "greater")  
ntbf01(k = 6, power = 0.95, dpm = 0, dpsd = 0, alternative = "greater",  
lower.tail = FALSE, nrange = <math>c(2, 10000))
```

pbf01

Cumulative distribution function of the z-test Bayes factor

Description

This function computes the probability of obtaining a Bayes factor (bf01) more extreme than a threshold k with a specified sample size.

Usage

```
pbf01(k, n, usd, null = 0, pm, psd, dpm = pm, dpsd = psd, lower.tail = TRUE)
```

k	Bayes factor threshold
n	Sample size
usd	Unit standard deviation, the standard error of the parameter estimate based on $n=1,$ see details
null	Parameter value under the point null hypothesis. Defaults to 0
pm	Mean of the normal prior assigned to the parameter under the alternative in the analysis
psd	Standard deviation of the normal prior assigned to the parameter under the alternative in the analysis. Set to \emptyset to obtain a point prior at the prior mean
dpm	Mean of the normal design prior assigned to the parameter. Defaults to the same value as the analysis prior pm

10 pbf01

Details

It is assumed that the standard error of the future parameter estimate is of the form $se = usd/\sqrt{n}$. For example, for normally distributed data with known standard deviation sd and two equally sized groups of size n, the standard error of an estimated standardized mean difference is $se = sd\sqrt{2/n}$, so the corresponding unit standard deviation is $usd = sd\sqrt{2}$. See the vignette for more information.

Value

The probability that the Bayes factor is less or greater (depending on the specified lower.tail) than the specified threshold k

Author(s)

Samuel Pawel

See Also

```
nbf01, powerbf01, bf01
```

```
## point alternative (psd = 0)
pbf01(k = 1/10, n = 200, usd = 2, null = 0, pm = 0.5, psd = 0)
## normal alternative (psd > 0)
pbf01(k = 1/10, n = 100, usd = 2, null = 0, pm = 0.5, psd = 2)
## design prior is the null hypothesis (dpm = 0, dpsd = 0)
pbf01(k = 10, n = 1000, usd = 2, null = 0, pm = 0.3, psd = 2, dpm = 0, dpsd = 0, lower.tail = FALSE)
## draw a power curve
nseq <- round(exp(seq(log(10), log(10000), length.out = 100)))
plot(nseq, pbf01(k = 1/10, n = nseq, usd = 2, null = 0, pm = 0.3, psd = 0), type = "1",
     xlab = "n", ylab = bquote("Pr(BF"["01"] <= 1/10 * ")"), ylim = c(0, 1),
     log = "x", las = 1)
## standardized mean difference (usd = sqrt(2), effective sample size = per group size)
pbf01(k = 1/10, n = n, usd = sqrt(2), null = 0, pm = 0, psd = 1)
## z-transformed correlation (usd = 1, effective sample size = n - 3)
pbf01(k = 1/10, n = n - 3, usd = 1, null = 0, pm = 0.2, psd = 0.5)
## log hazard/odds ratio (usd = 2, effective sample size = total number of events)
```

plot.power.bftest 11

```
nevents <- 100 pbf01(k = 1/10, n = nevents, usd = 2, null = 0, pm = 0, psd = sqrt(0.5))
```

plot.power.bftest

Plot method for class "power.bftest"

Description

Plot method for class "power.bftest"

Usage

```
## S3 method for class 'power.bftest'
plot(x, nlim = c(2, 500), ngrid = 100, plot = TRUE, nullplot = TRUE, ...)
```

Arguments

X	Object of class "power.bftest"
nlim	Range of sample sizes over which the power should be computed. Defaults to $c(2, 500)$
ngrid	Number of grid point for which power should be computed. Defaults to 100
plot	Logical indicating whether data should be plotted. If FALSE only the data used for plotting are returned.
nullplot	Logcal indicating whether a second plot with the power in favor of the null (using a Bayes factor threshold of 1/k) should be created. Defaults to TRUE
	Other arguments (for consistency with the generic)

Value

Plots power curves (if specified) and invisibly returns a list of data frames containing the data underlying the power curves

Author(s)

Samuel Pawel

See Also

```
powerbf01, powertbf01, powernmbf01
```

```
ssd1 \leftarrow powerbf01(k = 1/6, power = 0.95, pm = 0, psd = 1/sqrt(2), dpm = 0.5, dpsd = 0) plot(ssd1, nlim = c(1, 8000)) power1 <- powerbf01(k = 1/2, n = 120, pm = 0, psd = 1/sqrt(2), dpm = 0.5, dpsd = 0) plot(power1, nlim = c(1, 1000))
```

pnmbf01

pnmbf01	Cumulative distribution function of the normal moment prior Bayes factor

Description

This function computes the probability of obtaining a normal moment prior Bayes factor (nmbf01) more extreme than a threshold k with a specified sample size.

Usage

```
pnmbf01(k, n, usd, null = 0, psd, dpm, dpsd, lower.tail = TRUE)
```

Arguments

k	Bayes factor threshold
n	Sample size
usd	Unit standard deviation, the standard error of the parameter estimate based on $n=1,$ see details
null	Parameter value under the point null hypothesis. Defaults to 0
psd	Spread of the normal moment prior assigned to the parameter under the alternative in the analysis. The modes of the prior are located at $\pm\sqrt{2}\text{psd}$
dpm	Mean of the normal design prior assigned to the parameter
dpsd	Standard deviation of the normal design prior assigned to the parameter. Set to 0 to obtain a point prior at the design prior mean
lower.tail	Logical indicating whether $Pr(BF \le k)$ (TRUE) or $Pr(BF > k)$ (FALSE) should be computed. Defaults to TRUE

Details

It is assumed that the standard error of the future parameter estimate is of the form $se = usd/\sqrt{n}$. For example, for normally distributed data with known standard deviation sd and two equally sized groups of size n, the standard error of an estimated standardized mean difference is $se = sd\sqrt{2/n}$, so the corresponding unit standard deviation is $usd = sd\sqrt{2}$. See the vignette for more information.

Value

The probability that the Bayes factor is less or greater (depending on the specified lower.tail) than the specified threshold k

Author(s)

Samuel Pawel

powerbf01 13

See Also

```
nmbf01, nnmbf01, powernmbf01
```

Examples

```
## point desing prior (psd = 0)
pnmbf01(k = 1/10, n = 200, usd = 2, null = 0, psd = 0.5/sqrt(2), dpm = 0.5, dpsd = 0)
## normal design prior to incorporate parameter uncertainty (psd > 0)
pnmbf01(k = 1/10, n = 200, usd = 2, null = 0, psd = 0.5/sqrt(2), dpm = 0.5, dpsd = 0.25)
## design prior is the null hypothesis (dpm = 0, dpsd = 0)
pnmbf01(k = 10, n = 200, usd = 2, null = 0, psd = 0.5/sqrt(2), dpm = 0, dpsd = 0, lower.tail = FALSE)
```

powerbf01

Power and sample size calculations for z-test Bayes factor

Description

Compute probability that z-test Bayes factor is smaller than a specified threshold (the power), or determine sample size to obtain a target power

Usage

```
powerbf01(
    n = NULL,
    power = NULL,
    k = 1/10,
    sd = 1,
    null = 0,
    pm,
    psd,
    type = c("two.sample", "one.sample", "paired"),
    dpm = pm,
    dpsd = psd,
    nrange = c(1, 10^5)
)
```

dence' against the null hypothesis

Arguments

n Sample size (per group for two-sample tests). Has to be NULL if power is specified. Defaults to NULL

power Target power. Has to be NULL if n is specified. Defaults to NULL

k Bayes factor threshold. Defaults to 1/10, Jeffreys' threshold for 'strong evi-

powerbf01

sd	Standard deviation of one observation (for type = "two.sample" or type = "one.sample") or of one difference within a pair of observations (type = "paired"). Is assumed to be known. Defaults to 1
null	Mean difference under the point null hypothesis. Defaults to 0
pm	Mean of the normal prior assigned to the mean difference under the alternative in the analysis
psd	Standard deviation of the normal prior assigned to the mean difference under the alternative in the analysis. Set to 0 to obtain a point prior at the prior mean
type	The type of test. One of "two.sample", "one.sample", "paired". Defaults to "two.sample"
dpm	Mean of the normal design prior assigned to the mean difference. Defaults to the same value as the analysis prior pm
dpsd	Standard deviation of the normal design prior assigned to the mean difference. Defaults to the same value as the analysis prior psd
nrange	Sample size search range over which numerical search is performed (only taken into account when n is NULL). Defaults to c(1, 10^5)

Value

Object of class "power.bftest", a list of the arguments (including the computed one) augmented with method and note elements

Note

An error message will be displayed in case that the specified target power is not achievable under the specified analysis and design priors.

Author(s)

Samuel Pawel

See Also

```
plot.power.bftest, nbf01, pbf01, bf01
```

```
## determine power
powerbf01(n = 100, pm = 0, psd = 1, dpm = 0.5, dpsd = 0)
## determine sample size
powerbf01(power = 0.99, pm = 0, psd = 1, dpm = 0.5, dpsd = 0)
```

powernmbf01 15

powernmbf01	Power and sample size calculations for normal moment prior Bayes factor

Description

Compute probability that normal moment prior Bayes factor is smaller than a specified threshold (the power), or determine sample size to obtain a target power

Usage

```
powernmbf01(
    n = NULL,
    power = NULL,
    k = 1/10,
    sd = 1,
    null = 0,
    psd,
    type = c("two.sample", "one.sample", "paired"),
    dpm,
    dpsd,
    nrange = c(1, 10^5)
)
```

n	Sample size (per group for two-sample tests). Has to be NULL if power is specified. Defaults to NULL
power	Target power. Has to be NULL if n is specified. Defaults to NULL
k	Bayes factor threshold. Defaults to 1/10, Jeffreys' threshold for 'strong evidence' against the null hypothesis
sd	Standard deviation of one observation (for type = "two.sample" or type = "one.sample") or of one difference within a pair of observations (type = "paired"). Is assumed to be known. Defaults to 1
null	Parameter value under the point null hypothesis. Defaults to 0
psd	Spread of the normal moment prior assigned to the parameter under the alternative in the analysis. The modes of the prior are located at $\pm\sqrt{2}$ psd
type	The type of test. One of "two.sample", "one.sample", "paired". Defaults to "two.sample"
dpm	Mean of the normal design prior assigned to the parameter
dpsd	Standard deviation of the normal design prior assigned to the parameter. Set to 0 to obtain a point prior at the design prior mean
nrange	Sample size search range over which numerical search is performed (only taken into account when n is NULL). Defaults to c(1, 10^5)

powertbf01

Value

Object of class "power.bftest", a list of the arguments (including the computed one) augmented with method and note elements

Author(s)

Samuel Pawel

See Also

```
plot.power.bftest, nnmbf01, pnmbf01, nmbf01
```

Examples

```
## determine power
powernmbf01(n = 100, psd = 1, dpm = 0.5, dpsd = 0)
## determine sample size
powernmbf01(power = 0.99, psd = 1, dpm = 0.5, dpsd = 0)
```

powertbf01

Power and sample size calculations for t-test Bayes factor

Description

Compute probability that t-test Bayes factor is smaller than a specified threshold (the power), or determine sample size to obtain a target power

Usage

```
powertbf01(
  n = NULL,
  power = NULL,
  k = 1/10,
  null = 0,
  plocation = 0,
  pscale = 1/sqrt(2),
  pdf = 1,
  type = c("two.sample", "one.sample", "paired"),
  alternative = c("two.sided", "less", "greater"),
  dpm = plocation,
  dpsd = pscale,
  nrange = c(2, 10^4)
)
```

powertbf01 17

Arguments

n	Sample size	(per group)

power Target power. Has to be NULL if n is specified. Defaults to NULL

k Bayes factor threshold. Defaults to 1/10, Jeffreys' threshold for 'strong evi-

dence' against the null hypothesis

null Standardized mean difference under the point null hypothesis. Defaults to 0

plocation t prior location. Defaults to 0

pscale t prior scale. Defaults to 1/sqrt(2)

pdf t prior degrees of freedom. Defaults to 1 (a Cauchy prior)

type Type of t-test. Can be "two.sample" (default), "one.sample", or "paired"

alternative Direction of the test. Can be either "two.sided" (default), "less", or "greater".

The latter two truncate the analysis prior to negative and positive effects, respectively. If set to "less" or "greater", the power is only computed based on data

with effect estimates in the direction of the alternative

dpm Mean of the normal design prior assigned to the standardized mean difference.

Defaults to the analysis prior location

dpsd Standard deviation of the normal design prior assigned to the standardized mean

difference. Set to 0 to obtain a point prior at the design prior mean. Defaults to

the analysis prior scale

nrange Sample size search range over which numerical search is performed (only taken

into account when n is NULL). Defaults to c(2, 10⁴)

Value

Object of class "power.bftest", a list of the arguments (including the computed one) augmented with method and note elements

Author(s)

Samuel Pawel

See Also

```
plot.power.bftest, ptbf01, ntbf01, tbf01
```

```
## determine power powertbf01(n = 146, k = 1/6, dpm = 0.5, dps = 0, alternative = "greater") ## determine sample size powertbf01(power = 0.95, k = 1/6, dpm = 0.5, dps = 0, alternative = "greater")
```

print.power.bftest

```
print.power.bftest
```

Print method for class "power.bftest"

Description

Print method for class "power.bftest"

Usage

```
## S3 method for class 'power.bftest'
print(x, digits = getOption("digits"), ...)
```

Arguments

```
x Object of class "power.bftest"digits Number of digits for formatting of numbers... Other arguments (for consistency with the generic)
```

Value

Prints text summary in the console and invisibly returns the "power.bftest" object

Note

Function adapted from stats:::print.power.htest written by Peter Dalgaard

Author(s)

Samuel Pawel

See Also

powerbf01

```
powerbf01(power = 0.95, pm = 0, psd = 1, dpm = 0.5, dpsd = 0)
powerbf01(power = 0.95, pm = 0, psd = 1, dpm = 0.5, dpsd = 0, type = "one.sample")
powerbf01(power = 0.95, pm = 0, psd = 1, dpm = 0.5, dpsd = 0, type = "paired")
powerbf01(power = 0.95, pm = 1, psd = 0, dpm = 0.8, dpsd = 0, type = "paired")
```

ptbf01

ptbf01

Cumulative distribution function of the t-test Bayes factor

Description

This function computes the probability of obtaining a t-test Bayes factor (tbf01) more extreme than a threshold k with a specified sample size.

Usage

```
ptbf01(
 k,
 n,
 n1 = n,
 n2 = n,
 null = 0,
 plocation = 0,
  pscale = 1/sqrt(2),
  pdf = 1,
  dpm = plocation,
  dpsd = pscale,
  type = c("two.sample", "one.sample", "paired"),
  alternative = c("two.sided", "less", "greater"),
  lower.tail = TRUE,
  drange = "adaptive",
)
```

k	Bayes factor threshold
n	Sample size (per group)
n1	Sample size in group 1 (only required for two-sample t -test with unequal group sizes)
n2	Sample size in group 2 (only required for two-sample t -test with unequal group sizes)
null	Standardized mean difference under the point null hypothesis. Defaults to 0
plocation	t prior location. Defaults to 0
pscale	t prior scale. Defaults to 1/sqrt(2)
pdf	t prior degrees of freedom. Defaults to 1 (a Cauchy prior)
dpm	Mean of the normal design prior assigned to the standardized mean difference. Defaults to the analysis prior location
dpsd	Standard deviation of the normal design prior assigned to the standardized mean difference. Set to \emptyset to obtain a point prior at the design prior mean. Defaults to the analysis prior scale

20 tbf01

type	Type of t-test. Can be "two.sample" (default), "one.sample", or "paired"
alternative	Direction of the test. Can be either "two.sided" (default), "less", or "greater". The latter two truncate the analysis prior to negative and positive effects, respectively. If set to "less" or "greater", the power is only computed based on data with effect estimates in the direction of the alternative
lower.tail	Logical indicating whether $Pr(BF \le k)$ (TRUE) or $Pr(BF > k)$ (FALSE) should be computed. Defaults to TRUE
drange	Standardized mean difference search range over which the critical values are searched for. Can be either set to a numerical range or to "adaptive" (default) which determines the range in an adaptive way from the other input parameters
	Other arguments passed to stats::uniroot

Value

The probability that the Bayes factor is less or greater (depending on the specified lower.tail) than the specified threshold k

Author(s)

Samuel Pawel

See Also

```
tbf01, ntbf01, powertbf01
```

tbf01 21

Description

This function computes the Bayes factor that forms the basis of the informed Bayesian *t*-test from Gronau et al. (2020). The Bayes factor quantifies the evidence that the data provide for the null hypothesis that the standardized mean difference (SMD) is zero against the alternative that the SMD is non-zero. A location-scale *t*-distribution is assumed for the SMD under the alternative hypothesis. The Jeffreys-Zellner-Siow (JZS) Bayes factor (Rouder et al., 2009) is obtained as a special case by setting the location of the prior to zero and the prior degrees of freedom to one, which is the default.

The data are summarized by t-statistics and sample sizes. The following types of t-statistics are accepted:

- Two-sample *t*-test where the SMD represents the standardized mean difference between two group means (assuming equal variances in both groups)
- One-sample *t*-test where the SMD represents the standardized mean difference to the null value
- Paired t-test where the SMD represents the standardized mean change score

Usage

```
tbf01(
    t,
    n,
    n1 = n,
    n2 = n,
    plocation = 0,
    pscale = 1/sqrt(2),
    pdf = 1,
    type = c("two.sample", "one.sample", "paired"),
    alternative = c("two.sided", "less", "greater"),
    log = FALSE,
    ...
)
```

```
t-statistic
t
                   Sample size (per group)
n
                   Sample size in group 1 (only required for two-sample t-test with unequal group
n1
                   Sample size in group 2 (only required for two-sample t-test with unequal group
n2
                   sizes)
plocation
                   t prior location. Defaults to 0
                   t prior scale. Defaults to 1/sqrt(2)
pscale
pdf
                   t prior degrees of freedom. Defaults to 1 (a Cauchy prior)
                   Type of t-test. Can be "two.sample" (default), "one.sample", or "paired"
type
```

22 tbf01

alternative	Direction of the test. Can be either "two.sided" (default), "less", or "greater". The latter two truncate the analysis prior to negative and positive effects, respectively.
log	Logical indicating whether the natural logarithm of the Bayes factor should be returned. Defaults to FALSE
	Additional arguments passed to stats::integrate

Details

The Bayes factor is implemented as in equation (5) in Gronau et al. (2020), and using suitable truncation in case of one-sided alternatives. Integration is performed numerically with stats::integrate.

Value

Bayes factor in favor of the null hypothesis over the alternative (BF > 1 indicates evidence for the null hypothesis, whereas BF < 1 indicates evidence for the alternative)

Author(s)

Samuel Pawel

References

Rouder, J. N., Speckman, P. L., Sun, D., Morey, R. D., Iverson, G. (2009). Bayesian t tests for accepting and rejecting the null hypothesis. Psychonomic Bulletin & Review, 16(2):225-237. doi:10.3758/PBR.16.2.225

Gronau, Q. F., Ly., A., Wagenmakers, E.J. (2020). Informed Bayesian t-Tests. The American Statistician, 74(2):137-143. doi:10.1080/00031305.2018.1562983

See Also

```
powertbf01, ptbf01, ntbf01
```

```
## analyses from Rouder et al. (2009):
## values from Table 1
tbf01(t = c(0.69, 3.20), n = 100, pscale = 1, type = "one.sample")
## examples from p. 232
tbf01(t = c(2.24, 2.03), n = 80, pscale = 1, type = "one.sample")
## analyses from Gronau et al. (2020) section 3.2:
## informed prior
tbf01(t = -0.90, n1 = 53, n2 = 57, plocation = 0.350, pscale = 0.102, pdf = 3, alternative = "greater", type = "two.sample")
## default (one-sided) prior
tbf01(t = -0.90, n1 = 53, n2 = 57, plocation = 0, pscale = 1/sqrt(2), pdf = 1, alternative = "greater", type = "two.sample")
```

Index

```
bf01, 2, 3, 4, 9, 10, 14

nbf01, 3, 6, 10, 14

nmbf01, 5, 6, 7, 12, 13, 16

nnmbf01, 6, 6, 13, 16

ntbf01, 7, 17, 20, 22

pbf01, 4, 9, 14

plot.power.bftest, 11, 14, 16, 17

pnmbf01, 6, 7, 12, 16

powerbf01, 4, 10, 11, 13, 18

powernmbf01, 6, 7, 11, 13, 15

powertbf01, 9, 11, 16, 20, 22

print.power.bftest, 18

ptbf01, 9, 17, 19, 22

tbf01, 7, 9, 17, 19, 20, 20
```