# COMP219: Artificial Intelligence

**Lecture 10: Heuristic Search** 

#### **Overview**

#### Last time

- Depth-limited, iterative deepening and bi-directional search
- Avoiding repeated states

#### Today

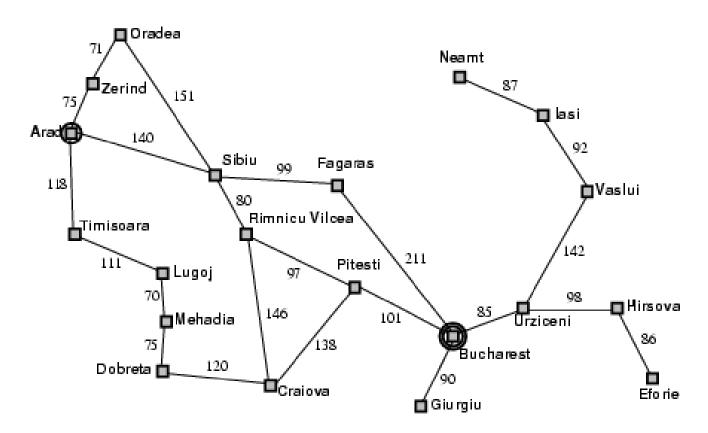
- Show how applying knowledge of the problem can help
- Introduce uniform cost search: dependent on the cost of each node
- Introduce heuristics: rules of thumb
- Introduce heuristic search
  - Greedy search
  - A\* search
- Learning outcome covered today:
   Identify, contrast and apply to simple examples the major search techniques that have been developed for problem-solving in AI

#### **Real Life Problems**

- Whatever search technique we use, we have exponential time complexity
- Tweaks to the algorithm will not reduce this to polynomial
- We need problem specific knowledge to guide the search
- Simplest form of problem specific knowledge is heuristics
- Usual implementation in search is via an evaluation function which indicates desirability of expanding a node

#### **Path Cost Function**

Recall: we have a path cost function, which gives the cost of each path. This is comprised of the step costs of each action on the path.

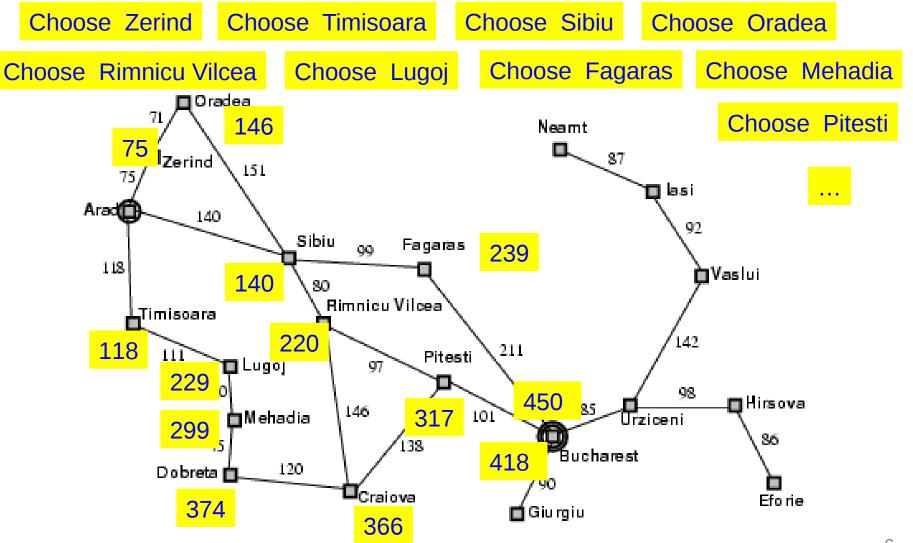


# **Finding The Best Paths**



- Why not expand the cheapest path first?
- Intuition: cheapest is likely to be best!
- Performance is like breadth-first search but we use the minimum cost path rather than the shallowest to expand
- Uniform cost search orders the agenda as a priority queue using the lowest path cost of a node

## **Cheapest First**



# General Algorithm for Uniform Cost Search

```
agenda = initial state;
while agenda not empty do
  take node from agenda such that
   g(node) = min { g(n) | n in agenda}
  if node is goal state then
    return solution;
  new nodes = apply operations to node;
  add new nodes to the agenda;
```

## **Properties of Uniform Cost Search**

- Uniform cost search guaranteed to find cheapest solution assuming path costs grow monotonically, i.e. the cost of a path never decreases as we move along it
- In other words, adding another step to the solution makes it more costly, i.e.

```
g(successor(n)) > g(n).
```

- If path costs don't grow monotonically, then exhaustive search is required
- Still requires many nodes to be examined

# **Informed Strategies**



- Use problem-specific knowledge
- More efficient than blind search
- The most promising path first!
- Rather than trying all possible search paths, you try to focus on paths that seem to be getting you nearer your target/goal state

# **Greedy Search**



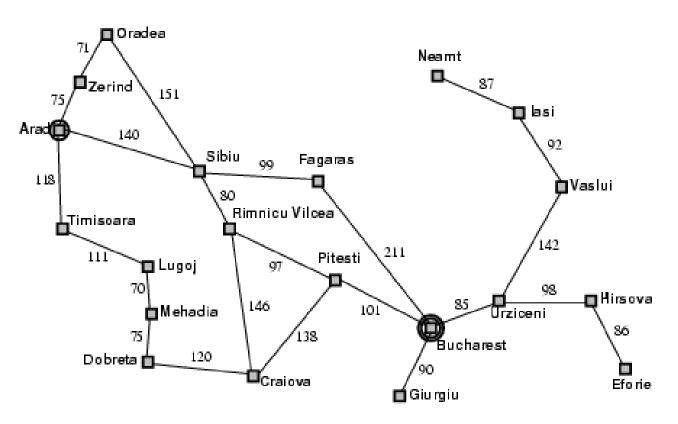
- Most heuristics estimate cost of cheapest path from node to solution
- We have a heuristic function,

 $h : Nodes \rightarrow R$ 

which estimates the distance from the node to the goal

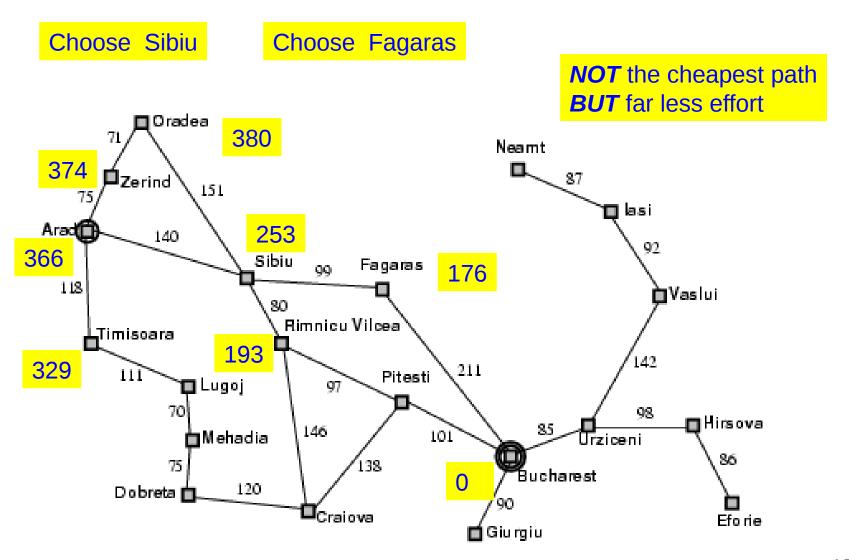
- h can be any function but should have h(n) = 0 if n is a goal
- Example: In route finding, heuristic might be straight line distance from node to destination
- Greedy search expands the node that appears to be closest to goal

## Romania Example

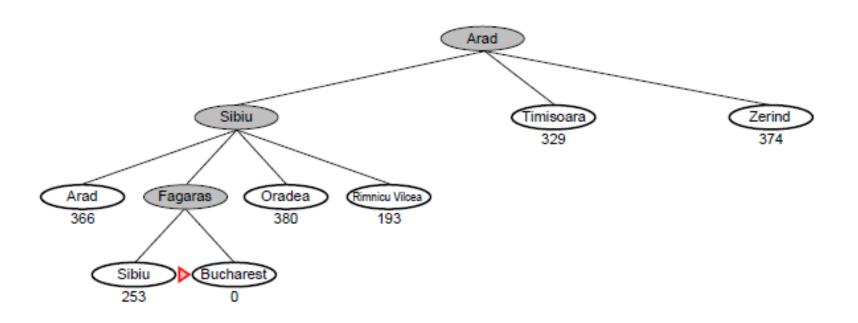


Straight-line di	<u>stance</u>
to Bucharest	
Arad	366
Bucharest	0
Craiova	160
Dobreta	242
Eforie	161
Fagaras	<b>176</b>
Giurgiu	77
Hirsova	<b>151</b>
lasi	226
Lugoj	244
Mehadia	241
Neamt	234
Oradea	380
Pitesti	98
Rimnicu Vilcea	193
Sibiu	253
Timisoara	329
Urziceni	80
Vaslui	199
Zerind	374

## **Greedy Search Example**



#### **Search Tree**



# **Exercise**

#### **General Algorithm for Greedy Search**

```
agenda = initial state;
while agenda not empty do
  take node from agenda such that
   h(node) = min { h(n) | n in agenda}
  if node is goal state then
    return solution;
  new nodes = apply operations to node;
  add new nodes to the agenda;
```

### **Properties of Greedy Search**

- Greedy search finds solutions quickly
- Doesn't always find the best
- May not find a solution if there is one (incomplete)
- Susceptible to false starts
- Only looking at current node. Ignores past!
- Short sighted



#### A\* Search



- A\* is a very efficient search strategy
- Basic idea is to combine uniform cost search and greedy search
- We look at the cost so far and the estimated cost to goal
- Gives heuristic f:

$$f(n) = g(n) + h(n)$$

where

g(n) is path cost of n

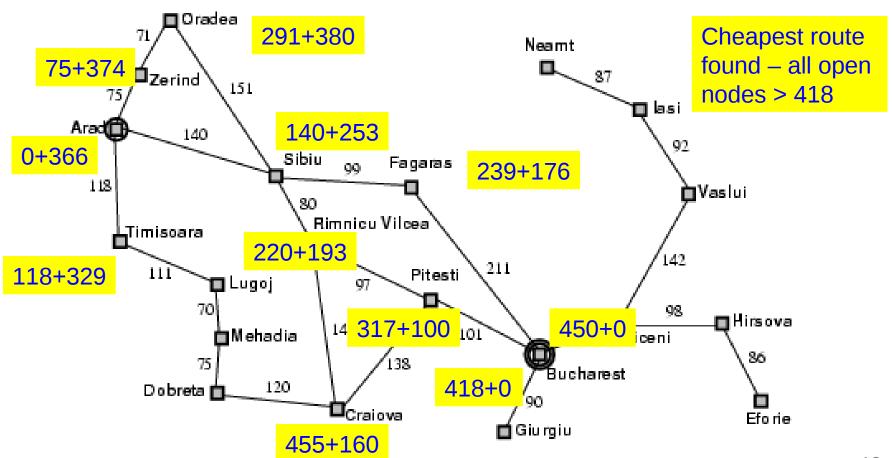
h(n) is expected cost of cheapest solution from n

Aims to minimise overall cost

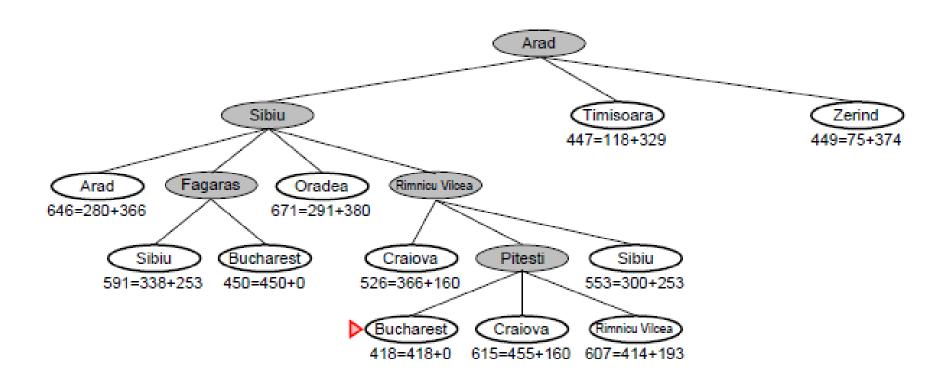
# **A\*** Search Example

Choose Sibiu

Choose Rimnicu Vilcea 413 < 415 Choose Fagaras 415 < 417 Choose Pitesti 418 < 450



#### **Search Tree**



#### **General Algorithm for A\* Search**

```
agenda = initial state;
while agenda not empty do
   take node from agenda such that
     f(node) = min \{ f(n) \mid n in agenda \}
     where f(n) = g(n) + h(n)
   if node is goal state then
    return solution;
   new nodes = apply operations to node;
   add new nodes to the agenda;
```

### **Properties of A\* Search**

- Complete, provided
  - only finitely many nodes with f < f(G)
  - an admissible heuristic is used
    - Never overestimates the distance
    - i.e., h(n) < true(n)</li>where true(n) is the true cost from n
    - Also require  $h(n) \ge 0$ , so h(G) = 0 for any goal G
- Exponential time
- Keeps all nodes in memory
- Optimal

#### **Admissible Heuristics**

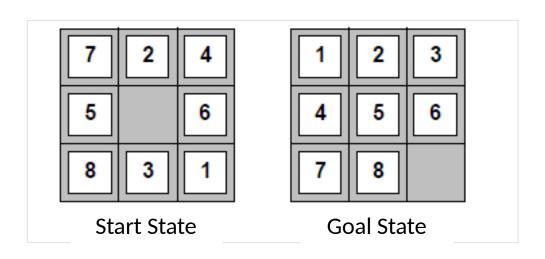


Example - for the 8-puzzle:

 $h_1(n)$  = number of misplaced tiles

 $h_2(n)$  = total Manhattan distance

• (i.e., no. of squares from desired location of each tile)



## **Exercise**

# Importance of the Heuristic Choice

Typical search costs:

$$-d = 14$$

- IDS = 3,473,941 nodes
- $A^*(h_1) = 539 \text{ nodes}$
- $A^*(h_2) = 113 \text{ nodes}$

$$-d = 24$$

- IDS ≈ 54,000,000,000 nodes
- $A^*(h_1) = 39,135 \text{ nodes}$
- $A^*(h_2) = 1,641 \text{ nodes}$

#### Summary

- Heuristic functions estimate costs of shortest paths
- Good heuristics can dramatically reduce search cost
- Greedy best-first search expands lowest h
  - incomplete and not always optimal
- A\* search expands lowest g + h
  - complete and optimal
  - also optimally efficient

#### Next week

Search in complex environments (partial observation) and in game playing