

Function max

{true}

if $x > y$ then

$z := x;$

else

$z := y;$

$\{(x > y \wedge z = x) \vee (x < y \wedge z = y)\}$

{Armed conditional Rule}

2) $\{x < y \wedge P\}$

$z := y;$

$\{(x > y \wedge z = x) \vee (x < y \wedge z = y)\}$

{Assignment Axiom}

$P = ((x > y \wedge z = x) \vee (x < y \wedge z = y)) [y/z]$

$= (x > y \wedge y = x) \vee (x < y \wedge y = y)$

$= \text{False} \vee \text{True}$

$= \text{True}$

4) $\{x > y \wedge P\}$

$z := x;$

$\{(x > y \wedge z = x) \vee (x < y \wedge z = y)\}$

{Assignment Axiom}

$P = ((x > y \wedge z = x) \vee (x < y \wedge z = y)) [x/z]$

$= (x > y \wedge x = x) \vee (x < y \wedge x = y)$

$= \text{True} \vee \text{False}$

$= \text{True}$

{Precondition Strengthening}

$\{\text{True}\} \rightarrow \{\text{True}\}$

$\therefore T$

$\{Q.E.D\}$