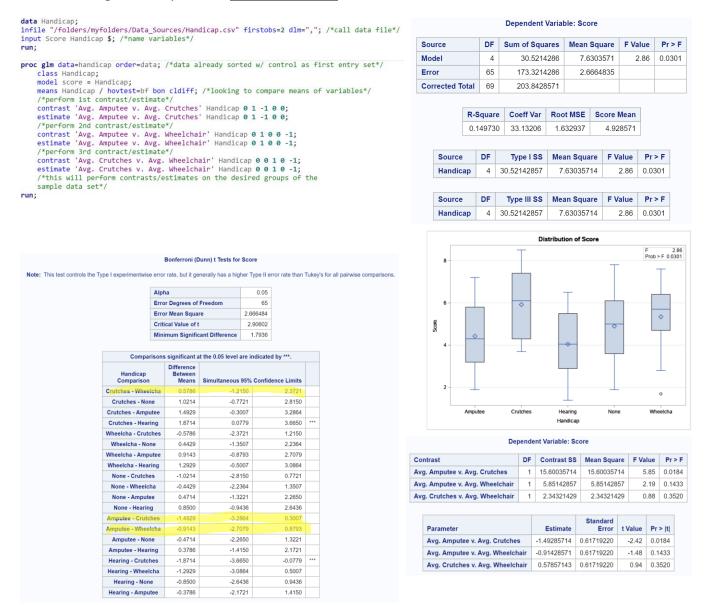
# **UNIT 6 HW**

1. **Handicap Study.** Use the Bonferroni method to construct simultaneous confidence intervals for  $\mu_2 - \mu_3$ ,  $\mu_2 - \mu_5$ , and  $\mu_3 - \mu_5$  (to see whether there are differences in attitude toward the mobility type of handicaps).

 $\mu_1$ ,  $\mu_2$ ,  $\mu_3$ ,  $\mu_4$ , and  $\mu_5$ , are the mean scores in the none, amputee, crutches, hearing, and wheelchair groups respectively. Be careful when identifying 'k' here. This study is mentioned throughout Chapter 6 of <u>Statistical Sleuth</u>.



# Handicap Study.

 See what multiple comparison procedures are available within the one-way analysis of variance procedure. Verify the 95% confidence interval half-widths in Display 6.6.

	nary of 95% cor andicap study	nfidence interval	procedures for di	fferences betwe	een treatment m
		Difference with			
Group	Average	Hearing	Amputee	Control	Wheelchair
Crutches	5.921	1.871	1.492	1.021	0.578
Wheelchair	5.343	1.293	0.914	0.443	
Control	4.900	0.850	0.471	-	
Amputee	4.429	0.379			
Hearing Procedure	4.050	95% inte	rval half-width	is centered with half-	lence interval d at a difference width given by the procedures.
LSD		1	1.233		
Dunnett			1.545 (for compar	risons with cont	rol only)
Tukey-Krame	er	1	1.735		
Bonferroni		1	1.794		
Scheffé		122116	1.957		

Show your work for this problem by simply copying the code and relevant output for each comparison. (Cut and paste your code and relevant output.) The half-width might be found directly from your output. If so, note where it is found. Do this for both R and SAS.

```
data Handicap;
infile "/folders/myfolders/Data_Sources/Handicap.csv" firstobs=2 dlm=","; /*call data file*/
input Score Handicap $; /*name variables*/
run;
proc glm data=handicap order=data;
                                                        Alpha
                                                                                 0.05
    class Handicap;
                                                        Error Degrees of Freedom
                                                                                   65
    model score = Handicap;
                                                        Error Mean Square
                                                                              2.666484
    means Handicap / hovtest=bf lsd cldiff;
                                                        Critical Value of t
                                                                               1.99714
run;
                                                        Least Significant Difference
proc glm data=handicap order=data;
                                                                                                 0.05
                                                                       Alpha
    class Handicap;
                                                                       Error Degrees of Freedom
    model score = Handicap;
                                                                       Error Mean Square
                                                                                              2.666484
    means Handicap / hovtest=bf dunnett('None') cldiff;
                                                                                               2 50316
                                                                       Critical Value of Dunnett's t
run;
                                                                       Minimum Significant Difference
proc glm data=handicap order=data;
                                                          Alpha
                                                                                       0.05
    class Handicap;
                                                          Error Degrees of Freedom
                                                                                         65
    model score = Handicap;
                                                          Error Mean Square
                                                                                    2.666484
    means Handicap / hovtest=bf tukey cldiff;
                                                          Critical Value of Studentized Range
                                                                                     3.96804
run;
                                                          Minimum Significant Difference
proc glm data=handicap order=data;
                                                                                   0.05
    class Handicap;
                                                        Error Degrees of Freedom
                                                                                    65
    model score = Handicap;
                                                        Error Mean Square
                                                                                2.666484
    means Handicap / hovtest=bf bon cldiff;
                                                        Critical Value of t
                                                                                 2.90602
run;
                                                        Minimum Significant Difference
proc glm data=handicap order=data;
                                                                                      0.05
                                                             Alpha
    class Handicap;
                                                             Error Degrees of Freedom
                                                                                        65
    model score = Handicap:
                                                             Error Mean Square
                                                                                   2.666484
    means Handicap / hovtest=bf scheffe cldiff;
                                                            Critical Value of F
                                                                                    2.51304
                                                             Minimum Significant Difference
run;
```

```
Javier Saldana
library(agricolae)
library(multcomp)
Handicap <- read.csv(file.choose())</pre>
#Least Significant Difference
LSD.test(aov(lm(Score ~ Handicap, data=Handicap)), "Handicap")
$`statistics`
  MSerror Df
                 Mean
                            CV t.value
                                             LSD
  2.666484 65 4.928571 33.13206 1.997138 1.232618
$parameters
       test p.ajusted name.t ntr alpha
  Fisher-LSD
               none Handicap
                                 5 0.05
$means
                                             UCL Min Max Q25 Q50
             Score
                        std r
                                    LCL
          4.428571 1.585719 14 3.556979 5.300164 1.9 7.2 3.300 4.30 5.725
Amputee
          5.921429 1.481776 14 5.049836 6.793021 3.7 8.5 4.500 6.10 7.150
Crutches
Hearing 4.050000 1.532595 14 3.178407 4.921593 1.4 6.5 3.025 4.05 5.300
          4.900000 1.793578 14 4.028407 5.771593 1.9 7.8 3.725 5.00 6.050
Wheelchair 5.342857 1.748280 14 4.471265 6.214450 1.7 7.6 4.725 5.70 6.350
$comparison
NULL
$groups
             Score groups
Crutches
         5.921429
                       a
Wheelchair 5.342857
                       ab
None
         4.900000
                      abc
Amputee
          4.428571
                       bc
        4.050000
Hearing
                        С
attr(,"class")
[1] "group"
#Dunnett
Handicap$Handicap = relevel(Handicap$Handicap, ref = "None")
fit = aov(Score ~ Handicap, data = Handicap)
gfit = glht(fit, linfct = mcp(Handicap = "Dunnett")
summary(gfit)
confint(gfit)
```

HSD.test(aov(lm(Score ~ Handicap, data=Handicap)), "Handicap")

#Tukey-Kramer

```
Javier Saldana
$`statistics`
   MSerror Df Mean
                     CV
                                  MSD
  2.666484 65 4.928571 33.13206 1.731733
$parameters
  test name.t ntr StudentizedRange alpha
  Tukey Handicap 5
                          3.968034 0.05
$means
             Score std r Min Max Q25 Q50 Q75
Amputee 4.428571 1.585719 14 1.9 7.2 3.300 4.30 5.725
Crutches 5.921429 1.481776 14 3.7 8.5 4.500 6.10 7.150
Hearing 4.050000 1.532595 14 1.4 6.5 3.025 4.05 5.300
         4.900000 1.793578 14 1.9 7.8 3.725 5.00 6.050
Wheelchair 5.342857 1.748280 14 1.7 7.6 4.725 5.70 6.350
$comparison
NULL
$groups
             Score groups
Crutches 5.921429
Wheelchair 5.342857
                      ab
                     ab
None 4.900000
Amputee 4.428571
                     ab
                   b
Hearing 4.050000
attr(,"class")
[1] "group"
#Bonferroni
LSD.test(aov(lm(Score ~ Handicap, data=Handicap)), "Handicap", p.adj=c("bonferroni"))
```

```
Javier Saldana
$`statistics`
   MSerror Df
                       CV t.value
                 Mean
                                           MSD
  2.666484 65 4.928571 33.13206 2.906015 1.79357
$parameters
        test p.ajusted name.t ntr alpha
  Fisher-LSD bonferroni Handicap 5 0.05
$means
                        std r
                                            UCL Min Max Q25 Q50 Q75
             Score
                                    LCL
          4.428571 1.585719 14 3.556979 5.300164 1.9 7.2 3.300 4.30 5.725
Amputee
Crutches 5.921429 1.481776 14 5.049836 6.793021 3.7 8.5 4.500 6.10 7.150
          4.050000 1.532595 14 3.178407 4.921593 1.4 6.5 3.025 4.05 5.300
Hearing
          4.900000 1.793578 14 4.028407 5.771593 1.9 7.8 3.725 5.00 6.050
None
Wheelchair 5.342857 1.748280 14 4.471265 6.214450 1.7 7.6 4.725 5.70 6.350
$comparison
NULL
$groups
             Score groups
Crutches
          5.921429
Wheelchair 5.342857
                       ab
None
          4.900000
                       ab
Amputee
          4.428571
                       ab
Hearing
          4.050000
                      b
attr(,"class")
[1] "group"
#Scheffe
scheffe.test(aov(lm(Score ~ Handicap, data=Handicap)), "Handicap"))
```

```
Javier Saldana
$`statistics`
   MSerror Df F
                                  CV Scheffe CriticalDifference
                        Mean
  2.666484 65 2.51304 4.928571 33.13206 3.170514
$parameters
    test name.t ntr alpha
  Scheffe Handicap 5 0.05
$means
             Score
                       std r Min Max
                                       Q25 Q50
Amputee 4.428571 1.585719 14 1.9 7.2 3.300 4.30 5.725
Crutches 5.921429 1.481776 14 3.7 8.5 4.500 6.10 7.150
Hearing
         4.050000 1.532595 14 1.4 6.5 3.025 4.05 5.300
          4.900000 1.793578 14 1.9 7.8 3.725 5.00 6.050
None
Wheelchair 5.342857 1.748280 14 1.7 7.6 4.725 5.70 6.350
$comparison
NULL
$groups
             Score groups
Crutches 5.921429
Wheelchair 5.342857
None 4.900000
                       a
Amputee
          4.428571
                       а
         4.050000
Hearing
attr(,"class")
[1] "group"
```

3. **Education and Future Income.** Reconsider the data problem of Exercise 5.25 concerning the distributions of annual incomes in 2005 for Americans in each of five education categories. (a) Use the Tukey–Kramer procedure to compare every group to every other group. Which pairs of means differ and by how many dollars (or by what percent)? (Use *p*-values and confidence intervals in your answer.) (b) Use the Dunnett procedure to compare every other group to the group with 12 years of education. Which group means apparently differ from the mean for those with 12 years of education and by how many dollars (or by what percent)? (Use *p*-values and confidence intervals in your answer.)

This question is obviously from the book, but assume you are starting this problem from scratch. Show all parts:

(1) Discussion of Assumptions (This could result in the inferences no longer being about the means. IF that happens, you should still compare the groups, just use the appropriate parameters when making inferences. Remember that you already did the work for addressing assumptions in prior homeworks.)

Problem: What is the strength of the evidence that at least one of the 5 group distributions of education has a different mean income than any of the others?

Assumptions: ANOVA assumptions are that the data is normally distributed and the groups have similar variances, along with being independent of each other and within. The data appears to be right skewed, this indicating there is evidence the data is not normally distributed. Considering the groups

have a large sample size, we can exact the CLT to make ANOVA robust to this assumption. However, since the data does not share equal variance; a log transformation helps address this issue. After transforming the data, there is greater evidence of similar distributions. With respect to independence, it appears they data may not be entirely independent. Since any viable members of the random sample of homes were included in the study, there is concern about cluster data being an issue. However, for the sake of the tests we will assume the data is independent among and within the groups.

```
data Edu Income 2005;
infile "/folders/myfolders/Data Sources/ex0525.csv" firstobs=2 dlm=",";
input Subj $ Ed $ Income; /*name variables*/
run;
*sort to make control group (12) first;
proc sort data=edu income 2005;
by Ed;
run;
*plot raw data by ed level;
proc sgplot data=edu_income_2005;
scatter x=Ed y=Income;
run;
*plot data to check ANOVA assumptions;
proc univariate data=edu_income_2005;
by Ed;
histogram Income;
qqplot Income;
run;
*transform raw data;
data Edu Income1; set Edu Income 2005;
logincome = log(Income);
run;
*plot logged data by education level;
proc sgplot data=edu income1;
scatter x=Ed y=logincome;
run;
*plot logged data to check ANOVA assumptions;
proc univariate data=Edu Income1;
by Ed;
Histogram logincome;
qqplot logincome;
run;
```

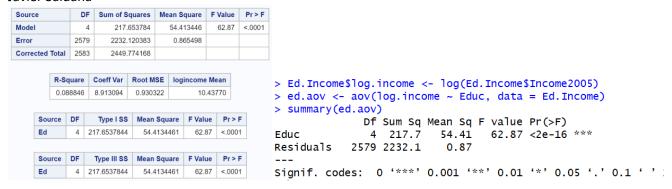
## (2) Selection and Execution of Tests

In order to ensure there is a difference among the groups, we will perform an ANOVA test.

Ho: All means are equal

Ha: At least 1 mean is different from the rest.

```
*ANOVA;
proc glm data=edu_income1;
class Ed;
model logincome = Ed;
run;
```



Based on the results of the ANOVA test, there is not sufficient evidence to support the null hypothesis that all groups have the same mean (p value <0.0001). So we will reject that ANOVA null and proceed with the Tukey and Dunnett tests.

In order to compare every group to each other, we will perform a Tukey-Kramer test.

Ho: All means are equal

```
Ha: At least one mean is different from the rest
```

```
*perform Tukey-Kramer;
proc glm data=edu_income1 order=data;
    class Ed;
    model logincome = Ed;
    means Ed / hovtest=bf tukey cldiff;
run;
```

```
> ed.tukey <- HSD.test(aov(lm(log.income ~ Educ, data=Ed.Income)), "Educ")
 ed. tuke
$`statistics`
 0.8654984 2579 10.4377 8.913094
$parameters
  test name.t ntr StudentizedRange alpha
Tukey Educ 5 3.860388 0.05
 Tukey
$means
     >16
13-15
$comparison
$groups
     log.income groups
>16
      10.89790
       10.79709
13-15
      10.39121
                   b
<12
       9.89934
attr(,"class")
[1] "aroup'
```

# Tukey's Studentized Range (HSD) Test for logincome Note: This test controls the Type I experimentwise error rate. Alpha 0.05 Error Degrees of Freedom 2579 Error Mean Square 0.865498 Critical Value of Studentized Range 3.86039

Compari	sons signific	ant at the 0.05 level a	are indicated by ***.	
Ed Comparison	Difference Between Means	Simultaneous 95%	Confidence Limits	
>16 - 16	0.10082	-0.08119	0.28283	
>16 - 13-15	0.50669	0.34178	0.67160	***
>16 - 12	0.67069	0.51717	0.82420	***
>16 - <12	0.99856	0.74427	1.25285	***
16 - >16	-0.10082	-0.28283	0.08119	
16 - 13-15	0.40588	0.24514	0.56661	***
16 - 12	0.56987	0.42085	0.71889	***
16 - <12	0.89775	0.64614	1.14935	***
13-15 - >16	-0.50669	-0.67160	-0.34178	***
13-15 - 16	-0.40588	-0.56661	-0.24514	***
13-15 - 12	0.16400	0.03642	0.29157	***
13-15 - <12	0.49187	0.25235	0.73139	***
12 - >16	-0.67069	-0.82420	-0.51717	***
12 - 16	-0.56987	-0.71889	-0.42085	***
12 - 13-15	-0.16400	-0.29157	-0.03642	***
12 - <12	0.32787	0.09605	0.55970	***
<12 ->16	-0.99856	-1.25285	-0.74427	***
<12 - 16	-0.89775	-1.14935	-0.64614	***
<12 - 13-15	-0.49187	-0.73139	-0.25235	***
<12 - 12	-0.32787	-0.55970	-0.09605	***

Based on the Tukey test results, there is sufficient evidence to support that there is a statistically significant difference in means between all the groups except >16 and 16 (-0.08119, 0.28283).

In order to compare groups to the control group (12 years of education), we will perform a Dunnett test.

Ho: Mean of 12 is equal to all other means

Ha: Mean of 12 is not equal to at least one other mean

```
> Ed.Income$Educ <- as.factor(Ed.Income$Educ)</pre>
*perform Dunnett;
                                                                      > Ed.Income$Educ = relevel(Ed.Income$Educ, ref = "12")
> fit = aov(log.income ~ Educ, data = Ed.Income)
proc glm data=edu income1 order=data;
                                                                      > gfit = glht(fit, linfct = mcp(Educ = "Dunnett"))
     class Ed;
                                                                      > summary(gfit)
     model logincome = Ed;
                                                                               Simultaneous Tests for General Linear Hypotheses
     means Ed / hovtest=bf dunnett('12') cldiff;
                                                                      Multiple Comparisons of Means: Dunnett Contrasts
run;
                                                                      Fit: aov(formula = log.income ~ Educ, data = Ed.Income)
                                                                      Linear Hypotheses:
                                                                      Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1 (Adjusted p values reported -- single-step method)
                                                                      > confint(gfit)
                                                                               Simultaneous Confidence Intervals
                                                                      Multiple Comparisons of Means: Dunnett Contrasts
                                                                      Fit: aov(formula = log.income ~ Educ, data = Ed.Income)
                                                                      95% family-wise confidence level
                                                                      Linear Hypotheses:
```

### **Dunnett's t Tests for logincome**

est controls the Type I experimentwise error for comparisons of all treatments aga

Alpha	0.05
Error Degrees of Freedom	2579
Error Mean Square	0.865498
Critical Value of Dunnett's t	2.48068

Compari	sons signific	ant at the 0.05 level a	e 0.05 level are indicated by ***.				
Ed Comparison	Difference Between Means	Simultaneous 95%	Confidence Limits				
>16 - 12	0.67069	0.53118	0.81020	***			
16 - 12	0.56987	0.43445	0.70530	***			
13-15 - 12	0.16400	0.04806	0.27993	***			
<12 - 12	-0.32787	-0.53855	-0.11720	***			

Based on the results from the Dunnet test, there is sufficient evidence to suggest there is clearly a difference in means of income when compared against the control group.

# (3) Interpretation and Conclusion.

In short, perform a complete analysis like you usually do. Provide and interpret all the confidence intervals that suggest a significant difference in incomes; provide your SAS and R code as well. (Generate your statistics using both softwares.)

Finally, you should first test to see if any of the groups are different before you consider pairwise comparisons.

Based on the results from the Tukey test, there is evidence to suggest the mean income between all the education levels are different, except the groups 16 and >16 [confidence intervals -0.08119, 0.28283; -0.28283, 0.08119]. The contrast between 16 and >16 is the only confidence interval that contains zero, which would mean the difference in the means is not significantly different. In other words, according to these results education past 16 years didn't doesn't result in a difference than the education of those with 16 years. However, all the other confidence intervals (95%, alpha 0.05) supports that all other means are different. A 12 year education earns anywhere between 0.096 – 0.560 times more than someone with less than a 12 year education. Someone with some college earns 0.0364 - 0.291 times more than someone with a 12 year education. Someone with a college degree earns 0.245 - 0.567 times more than someone with some college. The table is below.

	<12	12	13-15	16	>16
<12	0				
12	0.096, 0.560	0			
13-15	0.492, 0.252	0.0364, 0.291	0		
16	0.646, 1.149	0.421, 0.719	0.245, 0.567	0	
>16	0.744, 1.253	0.517, 0.824	0.342, 0.672	-0.0812, 0.283*	0

With respect to the Dunnett test, it appears all of the education levels have a different mean income than that of a high school graduate only. Those with a graudate degree (>16) earned anywhere between .53 - .81 times more. A college graduate earned .43 - .71 times more. Those with some college earn .05 - 0.28 times more. Whereas, someone without a high school diploma earns 0.54 - 0.12 times less.

However, since there is concern about the cluster of the data, the results may not be applied outside of these groups. Furthermore, the study was observational and makes it difficult to establish a casual relationship between education and income (95% confidence level, alpha 0.05).

Bonus: Max 5 pts

**Equity in Group Learning.** [Continuation of Exercise 5.22.] (a) To see if the performance of low-ability students increases steadily with the ability of the best student in the group, form a linear contrast with increasing weights: -3 = Low, -1 = Low-Medium, +1 = Medium-High, and +3 = High. Estimate the contrast and construct a 95% confidence interval. (b) For the High-ability students, use multiple comparisons to determine which group composition differences are associated with different levels of test performance.

DISPLAY 5.24	Achievement test scores of Low ability students who worked in different study groups				
		Highest ability level in the study group			
		Low	Low-medium	Medium-high	High
	Average:	0.26	0.37	0.36	0.47
	St. Dev.:	0.14	0.21	0.17	0.21
	n:	17	24	25	14

(c) Give the levels of ability a quantitative representation (Low = 1, Low-Medium = 2, etc.) for the low ability students. After completing the questions above, conduct a linear regression (we haven't studied this yet!) of the **AVERAGE** performance against the level variable you just created. Be sure and address the assumptions. Defend the ones you can and assume the others are met. Include a scatterplot and residual plot. Is there evidence of linear trend? Is this inferred from the contrast? Assume the levels are equidistant in ability from each other.

Note: the data for Part b above is in Display 5.25 in your textbook.