An Instruction Scratchpad Memory Allocation for the Precision Timed Architecture

Aayush Prakash, *Student Member, IEEE*, and Hiren D. Patel, *Member, IEEE*

Abstract—This paper presents a static instruction scratchpad memory allocation scheme for the precision timed architecture (PRET). Since PRET provides timing instructions to control the temporal execution of programs, the objective of the allocation scheme is to ensure that the explicitly specified temporal requirements are met. Furthermore, this allocation incorporates the timing requirements from the multiple hardware threads of the PRET architecture. We formulate the allocation problem as an integer-linear programming problem, and we implement a tool that takes compiled ARMv4 binaries, constructs a timingrequirements-aware control-flow graph, performs a WCET analysis and SPM allocation, and rewrites the binaries with the allocation. We evaluate our approach using a modified version of the Malardalen benchmarks to show the benefits of the proposed approach. We also present a UAV benchmark derived from the PapaBench benchmark.

Index Terms—Precision timed architecture, predictability, realtime embedded systems, scratchpad memory allocation.

I. Introduction

The precision timed architecture (PRET) is a hard realtime embedded processor architecture [1] that has predictable timing behaviors. PRET achieves predictability by making instruction execution repeatable. This simplifies the complexity of determining worst-case execution time (WCET) estimates of programs executing on PRET. WCET estimates are necessary to guarantee that temporal requirements of time-sensitive applications, such as those in avionics, automotive and other safety-critical systems are always met. PRET also introduces timing instructions that explicitly state timing requirements in the program. These timing instructions allow the designer to control the temporal behaviors of the program. PRET's memory hierarchy favors a shared scratchpad memory (SPM) for instruction and data. Caches are not used because obtaining tight WCET estimates with caches is complex [2]. SPMs, on the other hand, use software-controlled techniques to move instructions on and off the SPM, thereby allowing the designer to have control over the transfers on and off the SPM. This makes SPMs an attractive alternative over caches for predictability.

Although SPMs are predictable, manually performing the allocation of instruction and data is tedious and error-prone. Consequently, there are works that automatically allocate instructions and/or data onto the SPM [3], [4]. SPM allocation

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The authors are with the Department of Electrical and Computer Engineering, University of Waterloo, Waterloo, ON N2L 3G1, Canada (e-mail: a7prakash@uwaterloo.ca; hdpatel@uwaterloo.ca).

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techniques that are WCET-centric [3], [4] perform automatic allocation with the objective of reducing the worst-case execution path of the program. These works present innovative allocation techniques, but mainly for reducing the WCET of a single task. Another work [5] addresses this limitation by performing allocations with the goal of minimizing worst-case response time for concurrent embedded programs. Note, however, PRET programs have explicitly defined timing requirements, which means that reducing the execution time on the worst-case path may not be sufficient to meet the timing requirements because there may be timing requirements not on the worst-case path.

Current PRET programming practices require entire programs to fit on the SPM [1]. This limits PRET's practical use since programs are typically larger than the SPM, and manual allocation is inefficient. This brings us to the focus of our paper: a static instruction SPM allocation scheme for PRET that is aware of timing requirements explicitly specified in the program. In particular, we identify the basic blocks enclosed within PRET's timing instructions (called a timed block), and schedule the basic blocks within this timed block such that it just meets its timing requirement. By allocating just enough instructions to meet the timing requirements, we conserve space on the shared SPM. This is important because it enables other instructions from other timed blocks in the same program, and from other threads, to utilize the space for meeting requirements specified in their timed blocks. The main contributions of this paper are as follows: 1) a structured method to specify timing requirements using timing constructs; 2) a timing-requirements-aware control-flow graph (TRACFG) of the program as an intermediate representation to capture timing requirements; 3) a static instruction SPM allocation method specifically designed to meet the timing requirements for PRET programs; 4) a static WCET analysis for PRET; and 5) a tool automating the analysis and allocation. We compare the proposed approach with an average-case execution time (ACET), a WCET allocation scheme along with a hybrid of the two schemes using altered versions of the Malardalen benchmarks, and a PapaBench [6] UAV benchmark. The Malardalen benchmarks consist of small programs used for WCET analysis, and the PapaBench models core tasks for a UAV application.

II. BACKGROUND ON PRET ARCHITECTURE

PRET is a hard real-time embedded processor that has predictable and repeatable temporal behaviors [1]. PRET uses a thread-interleaved pipeline with four hardware threads. It possesses instruction-set architecture (ISA) extensions to the ARMv4 ISA that allow the user to specify temporal requirements in the form of timing instructions to control the temporal behavior of the program as shown in Table I. For example, the stt instruction starts a countdown timer, and dut ensures that the instruction after the dut executes after the timer expires, hence forcing the instructions within to take at least a specified amount of cycles to execute. PRET's memory, hierarchy is shown in Fig. 1. Each thread shares the

TABLE I

ISA EXTENSIONS WITH TIMING INSTRUCTIONS FOR PRET

Instruction	Semantics	
stt %r, offset	Load the currentTime+ offset into register %r	
dut %r	Stall pipeline until currentTime >= [%r].	
bep %r, target	Conditionally branch to the target if the currentTime > [%r].	
eoe %r, id	Processor throws an exception with id when currentTime >	
	[%r].	
dee id	Disable exception handler for exception id.	

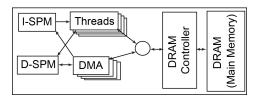


Fig. 1. PRET architecture with memory hierarchy.

instruction and data SPM. Data moves into the SPMs either through loads and stores or through explicit DMA requests. The DRAM controller implements a round-robin arbitration scheme to allow each thread access to the main memory, thereby making predictable accesses to the DRAM. For more information about the PRET memory hierarchy, we refer the readers to [7]. PRET's microarchitecture design ensures that every instruction has a known worst-case execution time.

III. INSTRUCTION SPM ALLOCATION FOR THE PRET ARCHITECTURE

We present a tool that allocates instructions for the PRET architecture [1]. The main stages of the tool are the following: 1) source-to-source translation from timing constructs to timing instructions; 2) parsing the compiled binary and generating a TRACFG to represent the program code and timing requirements; 3) a static WCET analysis for PRET; 4) an instruction SPM allocation; and 5) rewriting the binary with the SPM allocation. Stages 1–3 are executed on the four threads individually, and the combined information is provided to stage 4 to perform the allocation. The output of stage 4 provides the necessary allocations to make, which are updated in the rewriting of the four individual binaries. The PRET architecture accepts the four binaries, which are loaded into their address segments respectively.

- a) Assumptions: This paper makes the following assumptions. We make the standard assumptions for the programs that are made for WCET analysis, such as known loop bounds, and no recursions. A limitation of this analysis is that it does not support identification of target address for general register indirect jumps. However, the analysis supports partial data-flow analysis to discover certain cases. We do not focus on data allocation; thus, we assume data remains on the main memory.
- b) Source-to-Source Translation: Fig. 2 shows three timing constructs that we introduce in an example, and the timing instructions in Table I that are used to synthesize the constructs. Timing constructs provide a structured approach to encoding timing requirements in the program. They ensure

Fig. 2. Timing constructs for specifying timing requirements.

that the description of timing requirements are well formed. An example of a malformed timing requirement is one that has an stt to indicate the start of the timed block, but one that does not have a terminating dut. Notice that timing instructions by themselves do not enforce such requirements, and can be used arbitrarily. We use a front-end translator built using clang [8] to convert these timing constructs into timing instructions from Table I.

c) TRACFG Construction and Timed Blocks: We parse the binary for each thread, and construct a TRACFG that serves as an internal representation of the whole program. The TRACFG is an augmented control-flow graph where the vertices are basic blocks that have a unique identifier k, an annotation of whether the basic block is a regular, and timed block entry or exit (TENT, TEXT) type, and contains of a sequence of assembly instructions p. A basic block is a sequence of instructions that has a single entry point and exit point. Entrance to the basic block can only occur by branching to the first instruction (entry point) of the basic block. We use the TRACFG to detect timed blocks, perform static WCET analysis on the programs, and extract the necessary information for the allocation, and to rewrite the binary after implementing the allocation.

Constructing the TRACFG from the assembly program is a non-trivial process. The crux of the challenge is in determining the target addresses for the control-transfer instructions. The two broad categories of control-transfer instructions supported by the ARM ISA are direct and indirect control-transfer instructions. Direct control-transfer instructions specify the target address as a combination of the current instruction's program counter, and an immediate field (bits of the instruction itself). Indirect control-transfer instructions specify the target address in a register. Our tool supports direct control-transfer instructions, and only a subset of indirect. We support indirect control-transfer instructions by performing partial data-flow analysis to conservatively determine the set of possible values a register can take. This allows us to determine potential target addresses for indirect control-transfer instructions. However, supporting all register indirect control-transfer instructions requires performing a complete data-flow analysis at the assembly instruction abstraction level, which we do not support.

Timing constructs synthesize to timing instructions, which form timed blocks. Timed blocks enclose program code between two timing instructions: the first is the stt and the second is typically the dut. Other variants with exception handling exist, and are explained in [9]. We identify these timed blocks in the TRACFG by transforming the vertices with timing instructions to ensure that the timing instruction resides in its own basic block. Then, we annotate that basic block with

TABLE II	
SYMBOL TABLE FOR VARIABLES	USED IN ALLOCATION

	-
Symbol	Description
$X_t(k)$	1 if basic block k , in thread t is allocated to SPM and
	0 otherwise.
g_{pjt}	Auxiliary variable that assists in reducing the dif-
	ference between the timing requirement and actual
	execution time of path p in timed block j of thread t .
g_{pjt}^{abs} $F_{jt}(k)$	The absolute value of g_{pjt} .
$F_{jt}(k)$	Frequency of execution of basic block k , with respect
	to timed block j in thread t .
$T_t^{main}(k)$	WCET of basic block k , when executed on main
	memory.
$T_t^{spm}(k)$	WCET of basic block k , when executed on SPM.
K_{pjt}	Set of all basic blocks forming path p in timed block
	j of thread t .
$S_t(k)$	The size of basic block k in thread t .
N_{pjt}	The total number of basic blocks on path p
J_t	Total number of paths for timed block j .
J_t	Total number of timed blocks in thread t .
H	Total number of threads.
N_t	Total number of basic blocks in thread t .

TENT if it is an stt and with a TEXT if the instruction in that basic block is a dut. Hence, a timed block encapsulates a subgraph of the TRACFG, and there can be multiple timed blocks in a program. We identify different timing instructions using their respective opcode and timing requirements using partial data-flow analysis.

- WCET Analysis for the PRET Architecture: We implement a WCET analysis for the PRET architecture. By design, PRET's architecture provides fixed individual instruction execution costs for both non-memory, and memory instructions. These instruction costs are defined by an implementation of PRET [9] called PTARM. Before computing the WCET, a phase of the analysis computes the execution frequencies and size of basic blocks, and the overheads in terms of instructions in potentially allocating a block to the SPM. The overhead can be in the form of added instructions to maintain correct control-flow and size by adding additional data associated with jump tables onto the SPM. We take an overly conservative approach in determining these overheads through analysis, and we do not include it in the ILP formulation. The latter would only improve the results of the allocation. The analysis iterates over all basic blocks and computes its WCET based on whether the particular block is allocated to the SPM or not. We use these basic block WCETs to compute the WCET of paths of execution within a timed block. This allows us to verify whether the timing requirement specified for a particular timed block adheres to the WCET path within the timed block.
- e) SPM Instruction Allocation: The objective of the instruction SPM allocation is to meet the timing requirements specified by the timed blocks. However, we want to allocate the minimum number of basic blocks such that we just meet our requirements. This allows us to utilize the remaining SPM space for other timed blocks from the same thread, and from other threads. Consequently, this paper differs from simply reducing the WCET path as done by others [3] where the objective is to simply reduce the WCET of the program.

We use an integer-linear programming (ILP) formulation for instruction SPM allocation. We minimize a variable A that allocates just enough instructions to meet the timing requirements. The variable g_{pjt}^{abs} is an auxiliary variable that assists in reducing the difference between the timing requirement specified by timed block j, and the WCET estimate of path p in thread t. g_{pjt}^{abs} represents an absolute value and hence, the objective function appears non-linear. However, we transform the objective function to a linear variant using known techniques, by introducing g_{pit} , a free auxiliary variable and using the constraint in (4). Therefore, (4) makes g_{nit}^{abs} non-negative or absolute value of g_{pit} . A negative value of free auxiliary variable g_{pjt} suggests a violation of the timing requirements. By minimizing the sum of the absolute value of this variable (g_{pjt}^{abs}) for all paths p in timed block j and in thread t, we reduce the difference between the timing requirements of the timed blocks and the WCETs of the enclosed paths. Table II shows the meanings of all relevant variables that we use in the formulation.

Minimize

$$A = \sum_{t=1}^{H} \sum_{i=1}^{J_t} g_{jt} \tag{1}$$

such that

$$\sum_{t=1}^{H} \sum_{k=1}^{N_t} X_t(k) S_t(k) \le S^{spm}$$
 (2)

and

$$\forall p \in [1, P_{jt}], \forall j \in [1, J_t], \forall t \in [1, H]$$

$$R_{jt} - T_{pjt} \ge g_{pjt}$$

$$g_{pit}^{abs} \ge \pm g_{pjt}$$

$$(4)$$

where

$$g_{jt} = \sum_{p=1}^{P_{jt}} g_{pjt}^{abs}$$

$$T_{pjt} = \sum_{k \in K_{pjt}} [X_t(k)F_{jt}(k)T_t^{spm}(k) + (1 - X_t(k))F_{jt}(k)T_t^{main}(k)].$$

The first constraint (2) states that the sum of the size of all basic blocks allocated to the SPM must not exceed the maximum size of the SPM (S^{spm}). The second constraint (3) indicates that the difference between the requirement and the execution time is greater or equal to the auxiliary variable. By minimizing g_{pjt} , we reduce the WCET of path p by allocating basic blocks from path p to the SPM. R_{jt} denotes the timing requirement for timed block j in thread t, and T_{pjt} is the computed WCET of path p within timed block j in thread t. There are a total of $\sum_{t=1}^{H} \sum_{j=1}^{J_t} P_{jt}$ such constraints. Note that a phase in the WCET analysis stage conservatively incorporates the overhead costs of branch instruction needed if a block is to be allocated on the SPM in $T_t^{spm}(k)$ and $T_t^{main}(k)$.

Algorithm 1: Implement the allocation in the binary.

```
Input: V_{TRA}, S
   Let S be the set of basic blocks to be allocated.
   Let M be a map structure.
   Let V_L be the ordered set of vertices according to entry point addresses.
   foreach instruction ci = (pc, i) in basic block v_c \in S to be allocated do
        Insert in map M the mapping pc to the next available SPM address npc.
         Replace the pc for ci with npc.
   end
8
   foreach basic block v_o \in S to be allocated do
        Insert a nop instruction at the end of basic block v_c.
9
10 end
foreach instruction ci = (pc, i) in basic block v_c in V_L in program V_L do
        if ci's opcode is of a control-transfer instruction then
12
              Update ci with replacement instructions to maintain control-flow
13
              semantics.
14
        end
15 end
16 foreach basic block v_i, v_{j+1} in program in V_L that are consecutive blocks do
        if v_i allocated to SPM and not v_{i+1} or v_{i+1} allocated to SPM and not v_i
17
              Update nop instruction with new target address.
18
19
        end
20 end
21 Write out the new binary with the allocation from V_L
```

Rewriting: The last stage rewrites each thread's TRACFG with the selected blocks for SPM allocation. Algorithm 1 uses the vertices of the TRACFG, and the basic blocks selected for allocation S as input. There are three key steps in the algorithm. The first step generates SPM addresses for the instructions, and preserves the mapping between the original address, and the new SPM address (lines 5-8). It also inserts a no-operation instruction at the end of the basic block to replace it later with a control-transfer instruction to honor the original control-flow semantics (lines 9–11). We define an instruction ci = (pc, i) as a pair consisting of program counter, and the instruction bit-encoding. This step is important because any control-transfer instruction whose target address points to an allocated instruction would need to update its target address to reflect the SPM address. The map M allows us to do this. The second step (lines 12-16) updates the target address for every control-transfer instruction in each block, whose target address instruction is to be allocated to the SPM. Thus, we modify branch, pc-relative load/store and jump table instructions. The third step (lines 17–21) discovers points in the program where the control-flow semantics are violated due to SPM allocation. That is, a basic block is allocated to the SPM, but the next basic block to execute after it remains on the main memory. For this, we update the no-operation instruction with a control-transfer whose target instruction points to the first instruction of the next basic block in the main memory. This allows us to preserve the original control-flow semantics of the program for each thread. We can then create the binary with the updated vertices. The memory map of PRET [9] allows us to jump into any thread's address space from the SPM address space with a single branch instructions, and the reverse is also done through a single branch instruction.

IV. EXPERIMENTAL EVALUATION

We compare the proposed approach with three extended approaches: the ACET method [10], the WCET method [4], and a WCET-H (hybrid) approach for instruction allocation to SPM. The ACET method selects basic blocks for allocation that provide the most savings in terms of execution time.

We adapt the method to support basic blocks from multiple threads by simply introducing all blocks from every thread into a 0-1 ILP formulation [10]. To estimate the execution and frequencies of the basic blocks, we profile the execution of the benchmark. Then, we use these as input into the ACET allocation. The WCET method uses a greedy algorithm [4] that allocates basic blocks that contribute most toward the execution time on the WCET path. We use our static WCET analysis for the PRET architecture to compute the execution time of the basic blocks, and produce a WCET path for the entire program. Since the WCET path is specific for one program, we perform the allocation across multiple threads in the following way. We discover the SPM size necessary to meet all timing requirements and call this the baseline SPM size. Then, we perform the allocation for one program using the WCET approach until its terminating condition (WCET does not change). Once the terminating condition is reached, we start allocation with another thread with the remaining SPM space. We continue this for all four threads. Notice that since we report the percentage of timing requirements met, the order in which the threads are selected for allocation can affect the results. Hence, we enumerate all orderings for each configuration, and we only report one that provides the highest percentage of timing requirements met.

We acknowledge that ACET and WCET methods were not designed to incorporate explicit timing requirements. Therefore, we extend the WCET method to WCET-H based on the observation that the WCET method terminates once the WCET does not change; however, SPM space may still be available. Hence, there could be timed blocks that reside outside the WCET path that miss their timing requirements. To reduce missing timing requirements, we make a simple extension: once the WCET of the program stops changing, and there exists space on the SPM, we perform an ACET on the blocks that have not been selected for allocation. This forces the WCET-H method to fill the entire SPM by selecting blocks from other paths. Note that WCET-H is also not particularly designed to explicitly incorporate timing requirements.

We use an altered subset of the Malardalen benchmarks with timing constructs around the core functions of the benchmarks. Benchmarks that use recursions are not considered. Given that each benchmark has a different SPM size requirement to meet all its timing requirements, we set the SPM size for each configuration to be the total minimum SPM size required for all the benchmarks in that configuration. We perform the allocation using the proposed tool, and the resulting programs are executed on the publicly released PRET simulator [11] to ensure functional correctness.

g) Results: Fig. 3(a) shows the percentage of timing requirements met for the three methods for dedicated (suffixed with D) and shared SPM (suffixed with S). We compute the size for the dedicated SPM by obtaining the size required to meet all the timing requirements in a configuration, and splitting it into four equal parts for each thread. The proposed method meets all timing requirements whereas other approaches do not. We attribute this to the fact that other approaches were not designed to meet timing requirements. We notice that WCET-H has a higher percentage of

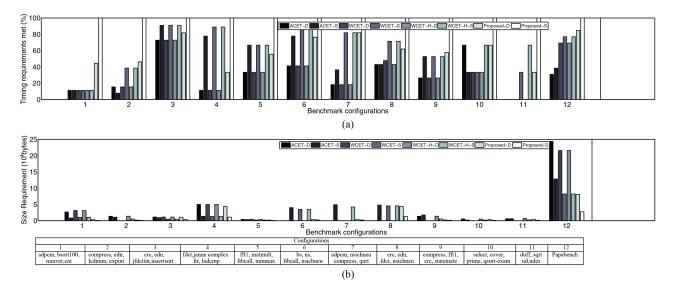


Fig. 3. Experimental results. (a) Percentage of timing requirements met for ACET, WCET, WCET-H, and the proposed methods. (b) SPM size requirements to meet all timing requirements for ACET, WCET-H, and the proposed method.

timing requirements met than WCET for configurations 10 and 11 (shared case). This is because WCET terminates while SPM space is available, but WCET-H takes advantage of the available space. For the remaining configurations, WCET-H performs the same as WCET. WCET methods outperform ACET in configurations 4, 6, 7, 8, and 12 because ACET methods allocate based on frequency and execution cost, but are agnostic to whether the basic block belongs within a timed block. We perform additional experimental evaluation using the GNU Paparazzi UAV project known as PapaBench [6] as the 12th configuration. This is a real-time benchmark with two main functional components: flybywire that manages servo/radio commands, and autopilot that controls the flight movement. Figure 3(a) also shows that having a shared SPM assists in meeting timing requirements when compared to dedicated SPM.

Fig. 3(b) shows the total SPM size required to meet all timing requirements, if possible. For all benchmarks, the proposed method requires the least amount of SPM space in all configurations. Note that it is possible for ACET and WCET-H to meet all the timing requirements in the program. However, the worst-case space requirement for this could be the entire program. For example, configuration 7 requires 23× more SPM space for the ACET to meet all timing requirements. Similarly, for WCET-H, it is $20\times$. Notice that when using WCET, the total size requirement in configurations 2, 7, 9, 10, and 11 is zero. This is because there does not exist an allocation using WCET that will meet all timing requirements because some timing requirements are outside the path with the WCET. It is evident that shared SPM performs better than dedicated SPM. For example, in all the configurations we meet higher or equal percentage of timing requirements for shared SPM than dedicated SPM.

V. CONCLUSION

This paper presented a method to statically allocate instructions to the SPM for the PRET architecture. The PRET architecture was unique as it allowed programs to specify explicit timing requirements. The proposed allocation scheme attempted to meet these timing requirements by identifying them, and allocating the minimum number of basic blocks necessary to satisfy them. We automated the allocation process in a tool. Our experiments showed the benefit of the proposed approach for the PRET architecture.

REFERENCES

- B. Lickly, I. Liu, S. Kim, H. D. Patel, S. A. Edwards, and E. A. Lee, "Predictable programming on a precision timed architecture," in *Proc. Int. Conf. Compilers, Architectures, Synthesis Embedded Syst.*, 2008, pp. 137–146.
- [2] C. Cullmann, C. Ferdinand, G. Gebhard, D. Grund, C. Maiza, J. Reineke, B. Triquet, S. Wegener, and R. Wilhelm, "Predictability considerations in the design of multi-core embedded systems," *Ingénieurs de* l'Automobile, vol. 807, pp. 36–42, May 2010.
- [3] J.-F. Deverge and I. Puaut, "WCET-directed dynamic scratchpad memory allocation of data," in *Proc. Euromicro Conf. Real-Time Syst.*, 2007, pp. 179–190.
- [4] V. Suhendra, T. Mitra, A. Roychoudhury, and T. Chen, "WCET centric data allocation to scratchpad memory," in *Proc. IEEE Int. Real-Time* Syst. Symp., 2005, pp. 223–232.
- [5] V. Suhendra, A. Roychoudhury, and T. Mitra, "Scratchpad allocation for concurrent embedded software," in *Proc. Int. Conf. Hardware/Software Codesign Syst. Synthesis*, 2008, pp. 37–42.
- [6] F. Nemer, H. Cass, P. Sainrat, J.-P. Bahsoun, and M. D. Michiel, "PapaBench: A free real-time benchmark," in *Proc. Workshop Worst-Case Execution Time Anal.*, 2006, pp. 1–6.
- [7] J. Reineke, I. Liu, H. D. Patel, S. Kim, and E. A. Lee, "PRET DRAM controller: Bank privatization for predictability and temporal isolation," in *Proc. Int. Conf. Hardware/Software Codesign Syst. Synthesis*, 2011, pp. 99–108.
- [8] C. Lattner, "LLVM and Clang: Next generation compiler technology," in *Proc. BSD Conf.*, 2008.
- [9] I. Liu, J. Reineke, D. Broman, M. Zimmer, and E. A. Lee, "A PRET microarchitecture implementation with repeatable timing and competitive performance," in *Proc. 30th IEEE Int. Conf. Comput. Design*, Oct. 2012.
- [10] O. Avissar, R. Barua, and D. Stewart, "An optimal memory allocation scheme for scratch-pad-based embedded systems," ACM Trans. Embeded Comput. Syst., vol. 1, no. 1, pp. 6–26, 2002.
- [11] The CHESS PRET team. (2011). The PRET Simulator PTARM [Online]. Available: http://chess.eecs.berkeley.edu/pret/src/ptarm-1.0/