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Algorithm Assignment

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Question: 01 Problem: 01

Boolean Distinct Week(arr, target)

2IK-3873

BSE - 5A

```
Sorted arr = mergesort (arr);  
for (i = 0; i < sortedarr.length; i++)
```

```
{  
    temp = target - sortedarr[i];  
    if binarySearch (sorted arr, i, temp)  
        return true
```

```
}  
return false
```

```
Merge Sort (arr) {  
    , e, s
```

```
    if (arr.length <= 1)
```

```
        return arr
```

```
    int mid = arr.length / 2
```

```
    left[] = mergesort (arr, 0, mid)
```

```
    right[] = mergesort (arr, mid, arr.length);
```

```
    return merge (left, right)
```

```
}
```

```

[] Merge ([left[]], [right[]])
result[] = new int [left.length + right.length];
i=0, j=0, k=0;
while (i < left.length && j < right.length)
    if (left[i] < right[j])
        result[k++] = left[i++];
    else
        result[k++] = right[j++];
}
while (i < left.length)
    result[k++] = left[i++];
while (j < right.length)
    result[k++] = right[j++];
return result;
}

```

```

backwardBinarySearch (sortedArr, temp, excludeIndex)
Low = 0, high = sorted.length - 1;
while (low <= high) {
    mid = (low + high) / 2;
    if (sortedArr[mid] == temp)
        if (mid != excludeIndex)
            return true;
        if (mid > 0 && sortedArr[mid - 1] == temp)
            return true;
        if (mid < sortedArr.length - 1 && sortedArr[mid + 1] == temp)
            return true;
    return false;
    else if (sortedArr[mid] < temp) => low = mid + 1
}

```

else

$$\text{high} = \text{mid} - 1$$

}

}

return false;

Recurrence Relation:-

$$\Rightarrow 2T\left(\frac{n}{2}\right) + n$$

$$; 2\left[\frac{n}{2}\right] + \frac{n}{2}$$

Solving by Iteration:-

$$2\left[2^0 T\left(\frac{n}{2^2}\right) + \frac{n}{2}\right] + n$$

$$; 2^2\left[\frac{n}{2^2} + \frac{n}{2}\right] + n$$

$$\Rightarrow 2^2 T\left(\frac{n}{2^2}\right) + n + n$$

$$; 2^2 \cdot 2^1 \left[\frac{n}{2^3} + \frac{n}{2^2}\right] + n + n$$

$$\Rightarrow 2^3 T\left(\frac{n}{2^3}\right) + n + n + n$$

$$; 2^k = 1$$

$$2^k T\left(\frac{n}{2^k}\right) + k \cdot n$$

$$; n = 2^k$$

$$; \log n = k$$

$$n \cdot T(1) + n \log n \quad ; T(1) = 0$$

$$\Rightarrow n + n \log n$$

\downarrow
dominating value

$$\Rightarrow O(n \log n)$$

Date: _____

Algorithm.. Step 01:-

```
Has same Pair (bakery1[], bakery2[], target) {  
    sorted Bakery1[] = mergesort(bakery1);  
    for (int i=0; i< bakery2.length; i++)  
    {  
        temp = target - bakery2[i]  
        if (binary search(sorted bakery1, temp))  
            return true;  
    }  
    return false;  
}
```

Step 02:- Merge Sort

1. Test base condition.

if beg < End

2. Calculate Midpoint

Mid = (Beg + End) / 2 \Rightarrow 3. Sort first subtable: Merge-Sort(arr, beg, mid)

4. Recursively sort the second subtable.

Merge-Sort(arr, mid+1, End)

5. Merge two ordered subtables

Merge (arr, Beg, End, Mid, End)

b. Finish

return.

Date: _____

Step 03:- Binary Search

- 1- Compare the middle element with key
 - 2- If key is not founded
 - If key < mid, iterate and search left side
 - If key > mid, iterate and search right side.
 - 3- Finish
- return.

Question : 02.

Divide -and Conquer approach.

Algorithm:-

```
Search(arr, low, high)
if (low > high)
    return -1;
if (low == high)
    return low;
mid = (low + high) / 2
```

```
if (mid % 2 != 0)
```

```
    mid --;
```

```
}
```

```
if (arr[mid] == arr[mid + 1]) {
```

```
    return search(arr, mid + 1, high);
```

```
else
```

```
    return search(arr, lowmid, mid);
```

```
}
```

Find Single Character (arr)

```
return search( arr, 0, arr.length - 1);
```

Date: _____

Recurrence Relation..

$$T(n) = T\left(\frac{n}{2}\right) + c$$

$$\Rightarrow T\left(\frac{n}{2}\right) + 2c$$

$$\Rightarrow T\left(\frac{n}{2^2}\right) + 3c$$

$$\Rightarrow T\left(\frac{n}{2^k}\right) + k \cdot c \quad \Rightarrow \frac{n}{2^k} = 1 \Rightarrow n = 2^k = \log n = k$$

$$T(1) + \log n \cdot c$$

↓
dominating value

$$\Rightarrow O(\log n)$$

Heaviest jar (arr[], start, end)

Question, 03.

Divide - Conquer approach

Algorithm.

findHeaviestJar (arr[], start, end)

if (start == end)

 return start

third = (end - start) / 3

firstThird = sum (arr, start, start + third - 1)

secondThird = sum (arr, start + third, start + 2 * third - 1)

Date: _____

```
if (firstThird > secondThird)
    return findheaviestjar(arr, start, start + third - 1)
else if (firstThird < secondThird)
    return findheaviestjar(arr, start + third, start + 2 * third - 1)
else
    findheaviestjar(arr, start + 2 * third, end);
```

```
Sum (arr, start, end)
```

```
total = 0
```

```
for (i = start; i <= end; i++)
    total += arr[i]
```

```
return total
```

Recursive $\Rightarrow O(\log_3 n)$

Approach:-

- 1- Divide array into thirds
- 2- Compare weights to see which is heavier and recursively
- 3- Look there
- 3- Keep narrowing unless we find the heaviest jar.

Question : 04

Let's take an input of 10 numbers (Ternary Search)

3, 5, 7, 9, 11, 13, 15, 17, 19, 20. ∴ Key = 20

1- Divide the array in three parts. m_1, m_2

$$m_1 = l + (r-l)/3 \Rightarrow 0 + (9-0)/3 = 3.$$

$$m_2 = r + (r-l)/3 \Rightarrow 9 + (9-0)/3 = 6.$$

$$\underline{m_1 = 3}, \underline{m_2 = 15}. \text{ arr}[m_1] = 9, \text{arr}[m_2] = 15.$$

3, 5, 7, 9, 11, 13, 15, 17, 19, 20
 m_1 m_2

Since $20 > 15$, key lies in final third
 then recursively add m_2 value

$$l = m_2 + 1 = 6 + 1 = 7.$$

$\text{arr}[l] = 17 < 20 \rightarrow$ add again

$\oplus \text{arr}[l] = 19 < 20 \rightarrow$ add again

$$\text{arr}[l] = 20, \text{arr}[r] = 20.$$

Search completed.

⇒ Since we are dividing array in third we

can analyze complexity as

$$\Rightarrow O(\log_3 n).$$

Pros: - Since it is dividing array in three parts.

array in three halves, its time can only be used on ordered list

complexity is much better. 1. Not easy implementation

• Works well for large dataset 1. Requires in depth knowledge of Recursion

• Number of comparison reduced 1. Not suitable for non-contiguous

• Space efficient 1. function

Date: _____

Meta Search

Let's take an input of 10 numbers

$$A = [3, 5, 7, 9, 11, 13, 15, 17, 19, 20] \text{ search} = 15$$

Step 01:- Divide array in half and then compare mid-value.

• Here middle element is 11 (can be 13 too)

$$\text{10) } 11 < 15 \text{ so,}$$

$15 - 11 = 2$, we will skip 2 values and compare again

• after two elements we find our desired value 15.

∴ Let's take 13 as middle value.

$$\text{since } 13 < 15$$

$\frac{15 - 13}{2} = 1$ check next element and we find our desired value.

Since we are checking only half, the time it takes is $O(\log n)$.

Pros:-

fewer comparison in some cases when target element is beginning of list

Cons:-

More comparison when target element is at the end of the list.

Question : 05.

Algorithm:-

freqCount (arr, n)

{

 int max = Math. max (a, n).

 temp = new int [max + 1]

 for (i=0; i<max; i++)

 {

 temp[i] = 0

 }

 for (i=0; i<n; i++)

 {

 temp[a[i]]++;

 }

 for (i=1; i<=max; i++) {

 temp[i] += temp[i-1]

 }

 getCount (int a, int b) {

 if (a == 0) {

 return temp[b];

 }

 return temp[b] - temp[a-1]

}

}

Date: _____

Example.

$$\text{Arr} = [1, 3, 6, 5, 1, 6, 8, 9, 4] \quad \text{Range} = [4, 6]$$

num :	0	1	2	3	4	5	6	7	8	9
count :	0	1	0	1	1	1	3	0	1	1

$$\text{temp} = [0, 1, 1, 2, 3, 4, 7, 7, 8, 9] \Rightarrow \text{cumulative frequency}$$

Step 01)

Find numbers that are less than or equal to upper bound

Here $b = b$.

~~[0, 1, 2, 3, 4, 5, 6]~~ are less than or equal to, $\text{temp}[6] = 7$.

total = 7

Step 02. Find number less than lower bound, here $a = 4$ $\xrightarrow{\text{equal to } a-1}$

$\therefore a - 1 = 3$.

$\text{temp}[3] = 2 \Rightarrow$ less than or equal to 3.

Step 03.

Calculate numbers within Range [4, 6].

Numbers in [4, 6] = $\text{temp}[6] - \text{temp}[4]$

$$\Rightarrow 7 - 2 = 5$$

There 5 numbers lie in O(1)

Question : Ob

Use of Radix-Sort (LMS) left most significant.

Input.

ihab abid afif fadi adib hadi ibad.

Step 01:-

Take left most value and keep smallest at top

abid

adib

a f i f

fadi

had i

ihab

ibad

Step 02

Now separate all the letters in subarray.

abid fadi hadi ihab

adib ibad

afif

Step 03:-

Now sort second LSB of each subarray

abid fadi hadi ibad

adib

a f;f

~~now~~ Step 04:- Page all

ahid adib asif hadi ibad ihab

Since we are going through every value and check $\Rightarrow O(n)$.