MA shapbias analysis

Samah

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Contents

| Preliminaries and data reading | |
|--------------------------------|----|
| Tremmaries and dava reading | 1 |
| Initial exploration | 2 |
| Basic meta-analysis | 8 |
| metagen approach | 8 |
| metafor approach | 9 |
| Revised forest plot | 11 |
| Forest plot with solidity: | 13 |
| Publication bias | 17 |
| Eggers regresstion test | 21 |
| Confirmatory analysis | 24 |
| Polynomial age models | 33 |
| Discussion | 35 |
| References | 35 |
| Preliminaries and data reading | |
| # 11·1· 7 1·2 | |

```
# additional libraries
library("knitr")
library("janitor")
library("broom.mixed")
library("lme4")
library("emmeans")
library("tidyverse")
library("kableExtra")
```

```
## Warning in !is.null(rmarkdown::metadata$output) && rmarkdown::metadata$output
## %in% : 'length(x) = 2 > 1' in coercion to 'logical(1)'
```

```
library("modelr")
library("broom")
library("nlme")
library(wesanderson)
library("meta")
library("metafor")
# library("dmetar")
library(jtools) # Load jtools
theme_set(theme_bw())
# reading the data file
pilot1_data = read_csv("252.csv")
df_shape= filter(pilot1_data, !is.na(d))
# pilot1_data = pilot1_data %>%
   select(ID, Title, d, d_var, Author)
# df_shape_summary = df_shape %>%
   group_by(ID, Title, Author) %>%
#
   summarize(mean = mean(d),
              mean\_se = mean(d\_var))
df_shape_summary <- df_shape %>%
  group_by(language) %>%
  summarize( count = n())
df_shape$englishgrp <- fct_relevel(as.factor(df_shape$language %in%
                                                  c("english")),
                                      "TRUE")
```

Initial exploration

df_shape_indo <- df_shape %>%
 filter(indoeuropean == TRUE)

df_shape_nonendo <- df_shape %>%
filter(indoeuropean == FALSE)

First, Visualizing the data to have an initial idea of how it looks.

df_shape\$mean_age_months_centered36 <- df_shape\$mean_age_months - 36

df_shape\$indoeuropean <- fct_relevel(as.factor(df_shape\$language %in%

"TRUE")

df_shape\$log_mean_age_months <- log(df_shape\$mean_age_months)

First dividing the language group into two groups: the first one is the indo-european group which includes the English and the Spanish languages. The second group includes the rest of the languages: Japanese, Chinese, Tsimane.

c("english", "spanish", "german")),

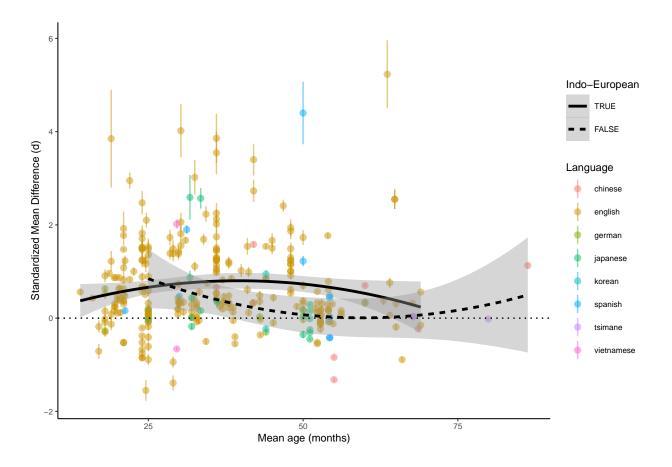
```
# creating a plot that shows the effects sizes colored per language group as well as the polynomial reg
ggplot(df_shape,
       aes(x = mean_age_months, y = d, color = indoeuropean)) + geom_point(aes(ymin = d - d_var, ymax =
                                                                                alpha = .5, size = part_num)
  geom_smooth(aes(group = indoeuropean,
                   lty = indoeuropean),
              col = "black",
              method = "lm", se = TRUE,
              formula = y \sim poly(x,2)) +
  geom_hline(yintercept = 0, lty = 3) +
 ylab("Standardized Mean Difference (d)") +
  xlab("Mean age (months)") +
  scale_color_discrete(name = "Indo-Euro language") +
  scale_linetype_discrete(name = "Indo-European") +
  theme(legend.position = "bottom") +
  theme_classic(base_size = 8)
## Warning in geom_point(aes(ymin = d - d_var, ymax = d + d_var, alpha = 0.5, :
## Ignoring unknown aesthetics: ymin and ymax
## Warning: Removed 3 rows containing non-finite values ('stat_smooth()').
## Warning: Removed 3 rows containing missing values ('geom_point()').
                                                                               Indo-European
                                                                                   TRUE
                                                                                   FALSE
Standardized Mean Difference (d)
                                                                               alpha
                                                                                • 0.5
                                                                               Indo-Euro language
                                                                                   TRUE
                                                                                   FALSE
                                                                               part_num
                                 Mean age (months)
```

```
ggplot(df_shape,
       aes(x = mean_age_months, y = d, color = language))+
  geom_pointrange(aes(ymin = d - d_var, ymax = d + d_var),
                  alpha = .5, size = 0.3) +
  geom_smooth(aes(group = indoeuropean,
                  lty = indoeuropean),
              col = "black",
              method = "lm", se = TRUE,
              formula = y \sim poly(x,2)) +
  geom_hline(yintercept = 0, lty = 3) +
  ylab("Standardized Mean Difference (d)") +
 xlab("Mean age (months)") +
  scale_color_discrete(name = "Language") +
  scale_linetype_discrete(name = "Indo-European") +
  theme(legend.position = "bottom") +
  theme_classic(base_size = 8)
```

Warning: Removed 3 rows containing non-finite values ('stat_smooth()').

Warning: Removed 3 rows containing missing values ('geom_pointrange()').

Warning: Removed 1 rows containing missing values ('geom_segment()').



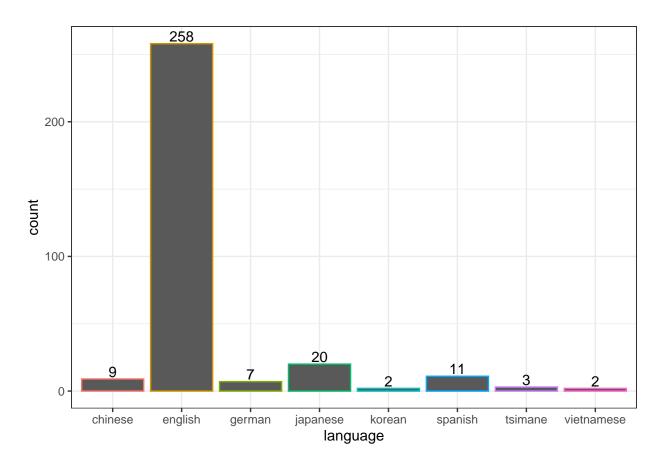
```
# ggsave("first graph.png", width = 7, height = 4)
barplot(table(df_shape$language), main = "barplot")
```



```
length(which(df_shape$language=="english"))

## [1] 258

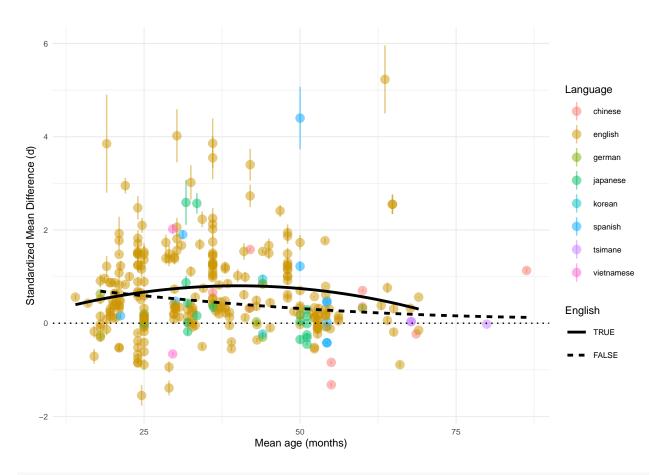
ggplot(df_shape_summary, aes(x = language, y = count)) +
    geom_col(aes(color = language), ) +
    theme(legend.position = "none") +
    geom_text(aes(label = count), vjust = -0.2)
```

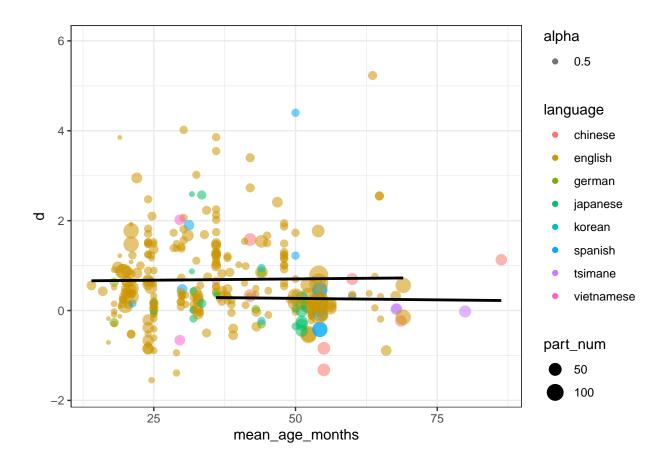


creating a plot that shows the effects sizes colored per language group as well as the polynomial reg ggplot(df_shape, aes(x = mean_age_months, y = d, color = language))+ geom_pointrange(aes(ymin = d - d_var, ymax = d + d_var), alpha = .5) +geom_smooth(aes(group = englishgrp, lty = englishgrp), col = "black", method = "lm", se = FALSE, formula = $y \sim poly(x,2)$ + geom_hline(yintercept = 0, lty = 3) + ylab("Standardized Mean Difference (d)") + xlab("Mean age (months)") + scale_color_discrete(name = "Language") + scale_linetype_discrete(name = "English") + theme(legend.position = "bottom") + theme_minimal(base_size = 8)

```
## Warning: Removed 3 rows containing missing values ('geom_pointrange()').
## Warning: Removed 1 rows containing missing values ('geom_segment()').
```

Warning: Removed 3 rows containing non-finite values ('stat_smooth()').





Basic meta-analysis

metagen approach

using the meta-analytic function meta-gen which calculates the weights for each effects and confidence interval, pooled effect size, the heterogeneity.

forest plot using the m-gen function object

```
forextobj <- forest.meta(m.gen,</pre>
                        sortvar = TE,
                        prediction = TRUE,
                        print.tau2 = FALSE,
                        leftlabs = c("Author", "g", "SE"))
                    0.3400 0.1100
                                                                     0.34
                                                                           [0.12; 0.5
                                                                     0.34
                    0.3400
                    0.3426 0.0900
                                                                     0.34
                                                                           [0.17; 0.5]
                    0.3500 0.0600
                                                                     0.35
                                                                           [0.23; 0.4]
                    0.3600 0.0900
                                                                     0.36
                                                                           [ 0.18; 0.5
                                                                     0.36
                    0.3600 0.0900
                                                                           [ 0.18; 0.5
                    0.3600 0.0800
                                                                     0.36
                                                                           [ 0.20; 0.5
                    0.3600 0.0600
                                                                     0.36
                                                                           [0.24; 0.4]
                    0.3700 0.0800
                                                                     0.37
                                                                           [ 0.21; 0.5
                    0.3800 0.1000
                                                                     0.38
                                                                           [ 0.18; 0.5
                                                                     0.38
                    0.3800 0.0500
                                                                           [ 0.28; 0.4
                    0.3800 0.0700
                                                                     0.38
                                                                           [ 0.24; 0.5
                    0.3800 0.0300
                                                                     0.38
                                                                           [ 0.32; 0.4
                    0.3937 0.0400
                                                                     0.39
                                                                           [0.32; 0.4]
                    0.4100 0.0300
                                                                     0.41
                                                                           [ 0.35; 0.4
                    0.4200 0.0700
                                                                     0.42
                                                                           [ 0.28; 0.5
                    0.4219 0.0700
                                                                     0.42
                                                                           [0.28: 0.5
                    0.4290 0.0500
                                                                     0.43
                                                                           [ 0.33; 0.5
                    0.4300 0.0700
                                                                     0.43
                                                                           [0.29; 0.5
                    0.4300 0.0700
                                                                     0.43
                                                                           [ 0.29; 0.5
                    0.4400 0.0800
                                                                     0.44
                                                                           [0.28; 0.6]
                    0.4400 0.0100
                                                                     0.44
                                                                            [0.42; 0.4]
                    0.4600 0.0800
                                                                     0.46
                                                                           10.30: 0.6
```

forest plot from the rma model

metafor approach

using rma.mv instead of m.gen

Warning: 1 row with NAs omitted from model fitting.

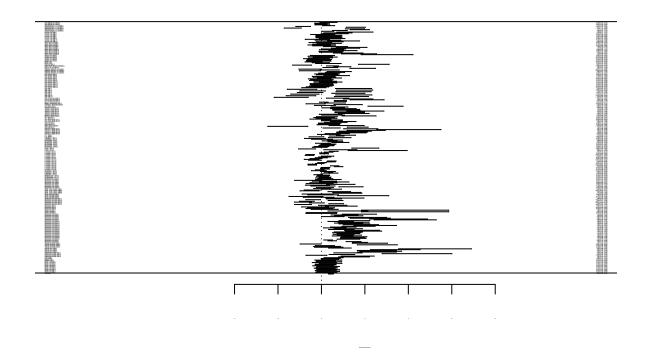
```
summary(mod)
```

```
## Multivariate Meta-Analysis Model (k = 311; method: REML)
##
     logLik Deviance
                             AIC
                                        BIC
                                                  AICc
## -797.2159 1594.4318 1598.4318 1605.9049 1598.4709
##
## Variance Components:
##
##
                       sqrt nlvls fixed factor
              estim
             0.1656 0.4069
## sigma^2
                             48
                                      no
## Test for Heterogeneity:
## Q(df = 310) = 2573.9189, p-val < .0001
## Model Results:
##
## estimate
                                   ci.lb
                se
                      zval
                              pval
                                            ci.ub
   0.4365 0.0617 7.0794 <.0001 0.3156 0.5573 ***
##
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
Nested model.
mod_nested <- rma.mv(yi = d,</pre>
                    V = d_{var}
                    random = ~ 1 | ID/exp_num,
                    slab = short_cite,
                    data = filter(df_shape, !is.na(exp_num)))
## Warning: 1 row with NAs omitted from model fitting.
summary(mod_nested)
## Multivariate Meta-Analysis Model (k = 304; method: REML)
##
##
     logLik
              Deviance
                              AIC
                                         BIC
                                                  AICc
## -743.4370 1486.8741 1492.8741 1504.0153 1492.9543
##
## Variance Components:
##
                       sqrt nlvls fixed
              estim
## sigma^2.1 0.1245 0.3528
                                48
                                      no
## sigma^2.2 0.0956 0.3093
                                75
                                      no ID/exp_num
##
## Test for Heterogeneity:
## Q(df = 303) = 2501.5515, p-val < .0001
##
## Model Results:
##
## estimate
              se zval pval ci.lb ci.ub
```

```
## 0.4530 0.0668 6.7854 <.0001 0.3221 0.5838 ***
##
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1</pre>
```

Forest plot from metafor.

```
forest(mod) +
  theme_minimal(base_size = 8)
```



NULL

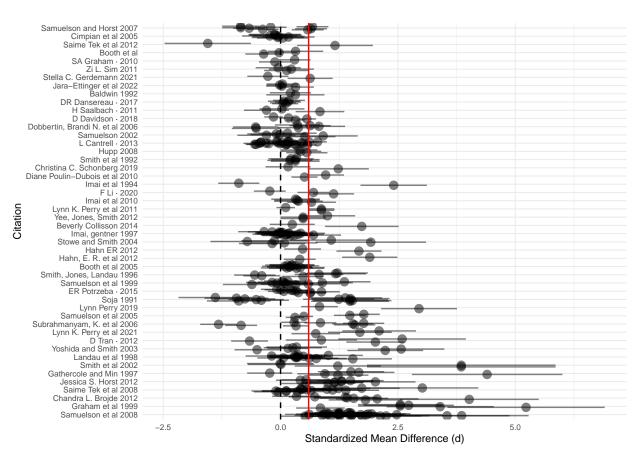
Try this using ggplot

Revised forest plot

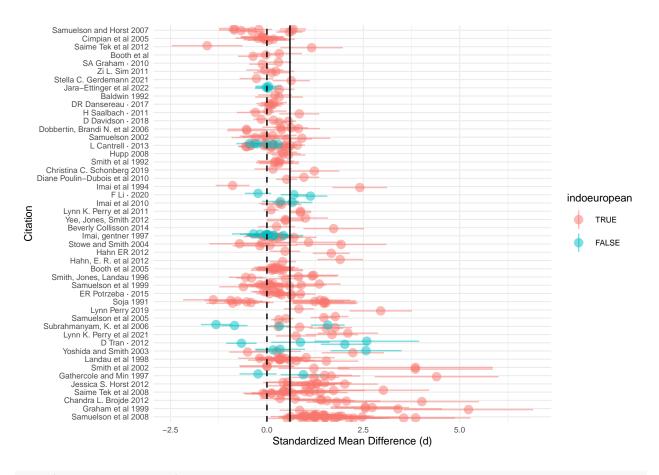
```
aes(x=reorder(short_cite,-d, sum)) +
ylab("Standardized Mean Difference (d)") +
xlab("Citation") +
theme_minimal(base_size = 8)
```

Warning: 'geom_hline()': Ignoring 'data' because 'yintercept' was provided.

Warning: Removed 1 rows containing missing values ('geom_segment()').



```
## Warning: 'geom_hline()': Ignoring 'data' because 'yintercept' was provided.
## Removed 1 rows containing missing values ('geom_segment()').
```

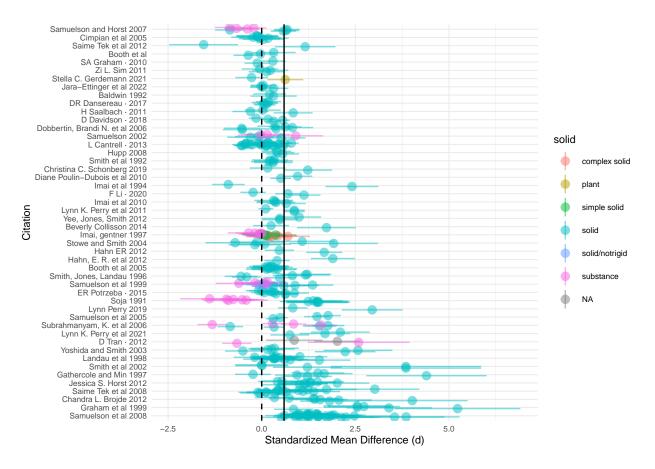


#png("secondgraph.png")

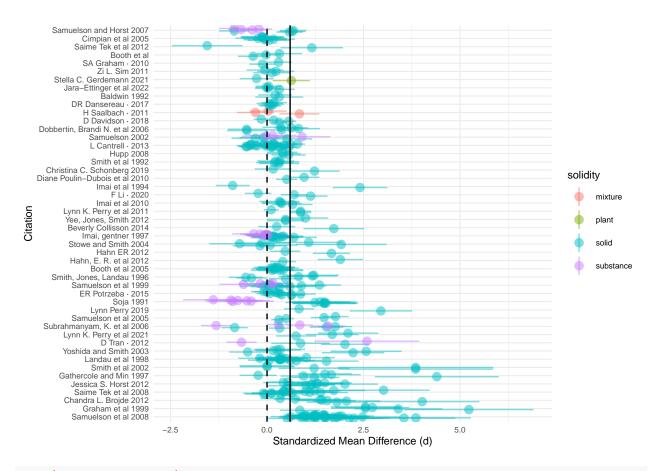
Forest plot with solidity:

```
## Warning: 'geom_hline()': Ignoring 'data' because 'yintercept' was provided.
```

Warning: Removed 1 rows containing missing values ('geom_segment()').



```
## Warning: 'geom_hline()': Ignoring 'data' because 'yintercept' was provided.
## Removed 1 rows containing missing values ('geom_segment()').
```



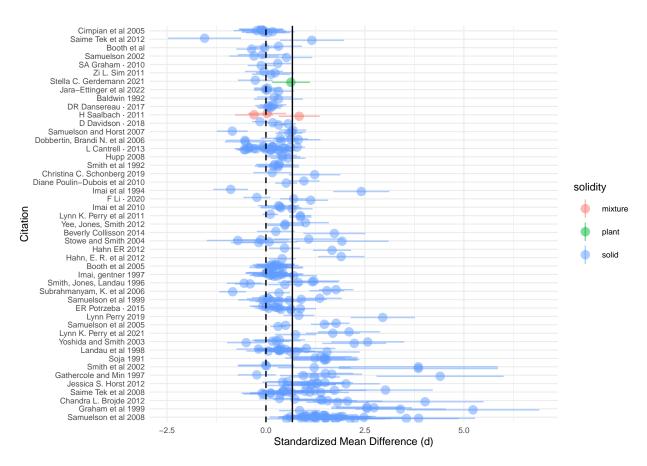
#png("secondgraph.png")

```
## data with only solidity:
df_shape_solid <- df_shape %>% filter(solid != "substance")
m.gen_solid <- metagen( TE= d,
                  seTE = d_var,
                  studlab = ID,
                  data = df_shape_solid,
                  sm = "SMD",
                  fixed = FALSE,
                  random = TRUE,
                  method.tau = "REML",
                  hakn = TRUE,
                  title = "pilot shape bias meta-analysis")
ggplot(df_shape_solid, aes(x = short_cite, y = d,
                     ymin=d-sqrt(d var)*1.96,
                     ymax=d+sqrt(d_var)*1.96)) +
  geom_pointrange(aes(color=solidity), alpha = .5, position=position_dodge2(width=.5)) +
  coord_flip() +
  geom_hline(yintercept = 0, lty = 2) +
  geom_hline(data = m.gen ,yintercept = m.gen_solid$TE.random) +
  aes(x=reorder(short_cite,-d, sum)) +
  ylab("Standardized Mean Difference (d)") +
 xlab("Citation") +
```

theme_minimal(base_size = 8)

Warning: 'geom_hline()': Ignoring 'data' because 'yintercept' was provided.

Warning: Removed 1 rows containing missing values ('geom_segment()').



m.gen_solid

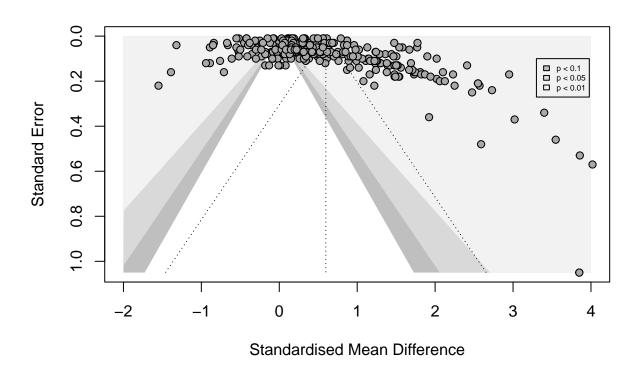
```
pilot shape bias meta-analysis
## Review:
##
## Number of studies: k = 280
##
                                 SMD
##
                                               95%-CI
                                                          t p-value
## Random effects model (HK) 0.6676 [0.5659; 0.7694] 12.92 < 0.0001
##
## Quantifying heterogeneity:
   tau^2 = 0.6554 [0.6173; 0.8995]; tau = 0.8096 [0.7857; 0.9484]
    I^2 = 99.5\% [99.5\%; 99.6\%]; H = 14.75 [14.51; 14.99]
##
##
## Test of heterogeneity:
##
           Q d.f. p-value
##
    60688.36 279
## Details on meta-analytical method:
```

```
## - Inverse variance method
## - Restricted maximum-likelihood estimator for tau^2
## - Q-Profile method for confidence interval of tau^2 and tau
## - Hartung-Knapp adjustment for random effects model (df = 279)
m.gen
              pilot shape bias meta-analysis
## Review:
## Number of studies: k = 311
##
##
                                                         t p-value
                                SMD
                                              95%-CI
## Random effects model (HK) 0.5978 [0.4980; 0.6975] 11.79 < 0.0001
##
## Quantifying heterogeneity:
## tau^2 = 0.7112 [0.6668; 0.9485]; tau = 0.8433 [0.8166; 0.9739]
## I^2 = 99.5\% [99.5%; 99.6%]; H = 14.70 [14.47; 14.93]
## Test of heterogeneity:
##
           Q d.f. p-value
  66972.27 310
##
##
## Details on meta-analytical method:
## - Inverse variance method
## - Restricted maximum-likelihood estimator for tau^2
## - Q-Profile method for confidence interval of tau^2 and tau
## - Hartung-Knapp adjustment for random effects model (df = 310)
Publication bias
col.contour = c("gray75", "gray85", "gray95")
funnel(m.gen,
       comb.random = TRUE,
      xlim = c(-2, 4),
      contour = c(0.9, 0.95, 0.99),
       col.contour = col.contour)
regtest(x = d, vi = d_var,
       data = df_shape)
## Warning: 1 study with NAs omitted from test.
## Regression Test for Funnel Plot Asymmetry
## Model:
             mixed-effects meta-regression model
## Predictor: standard error
```

Test for Funnel Plot Asymmetry: z = 14.1226, p < .0001

Limit Estimate (as sei \rightarrow 0): b = -0.7016 (CI: -0.8874, -0.5159)

```
# Add a legend
legend(x = 3.3, y = 0.1, cex = 0.5,
    legend = c("p < 0.1", "p < 0.05", "p < 0.01"),
    fill = col.contour)</pre>
```



```
#png("funnel.png")
```

funnel plots using ggplot to account for moderators:

```
x = summary(m.gen)['TE']
y = summary(m.gen)['seTE']
m.gen["TE.fixed"]

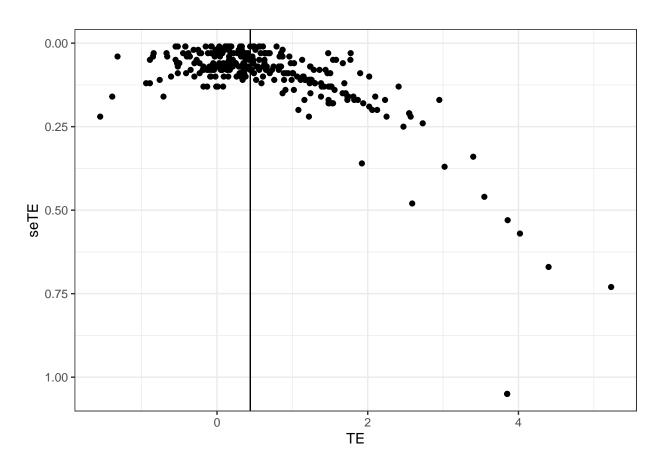
## $TE.fixed
## [1] 0.189402

ter = m.gen["TE.random"]

data.gen = data.frame(x,y,ter)

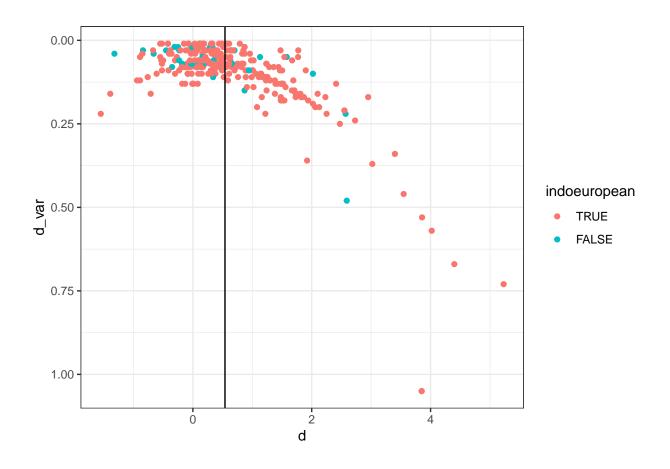
ggplot(data = data.gen, mapping = aes(x=TE, y = seTE, color= )) +
    geom_point() +
    geom_vline(xintercept = 0.4418062) +
    scale_y_reverse()
```

Warning: Removed 1 rows containing missing values ('geom_point()').



```
ggplot(data = df_shape, mapping = aes(x=d, y = d_var, color= indoeuropean)) +
  geom_point() +
  geom_vline(xintercept = 0.5401759) +
  scale_y_reverse()
```

Warning: Removed 1 rows containing missing values ('geom_point()').



```
geom_point() +
geom_vline(xintercept = 0.5401759) +
scale_y_reverse() +
geom_smooth(method = "lm")

## 'geom_smooth()' using formula = 'y ~ x'

## Warning: Removed 1 rows containing non-finite values ('stat_smooth()').

## Warning in qt((1 - level)/2, df): NaNs produced

## Warning in qt((1 - level)/2, df): NaNs produced

## Warning: Removed 1 rows containing missing values ('geom_point()').

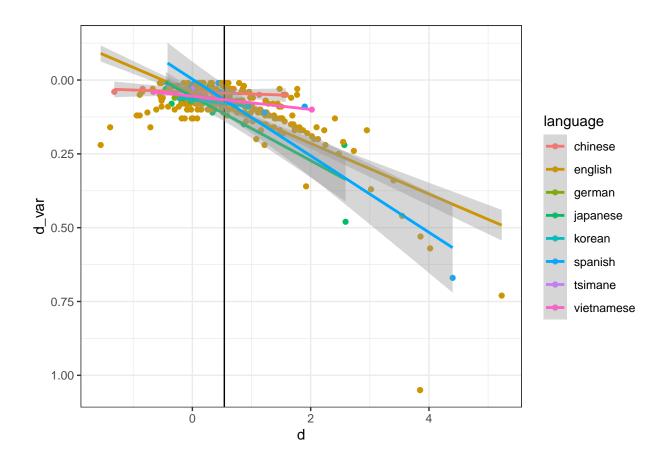
## Warning in max(ids, na.rm = TRUE): no non-missing arguments to max; returning

## -Inf

## Warning in max(ids, na.rm = TRUE): no non-missing arguments to max; returning
```

-Inf

ggplot(data = df_shape, mapping = aes(x=d, y = d_var, color= language)) +



Eggers regression test

```
m.gen$data %>%
 mutate(y = m.gen$TE/m.gen$seTE, x = 1/m.gen$seTE) %>%
 lm(y ~ x, data= .) %>%
 summary()
##
## Call:
## lm(formula = y \sim x, data = .)
##
## Residuals:
      Min
               1Q Median
                              3Q
                                      Max
## -69.191 -5.659
                   0.225
                            5.321 64.809
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 4.89851
                          1.08913
                                   4.498 9.74e-06 ***
## x
               0.09293
                          0.03203
                                    2.902 0.00398 **
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 14.26 on 309 degrees of freedom
```

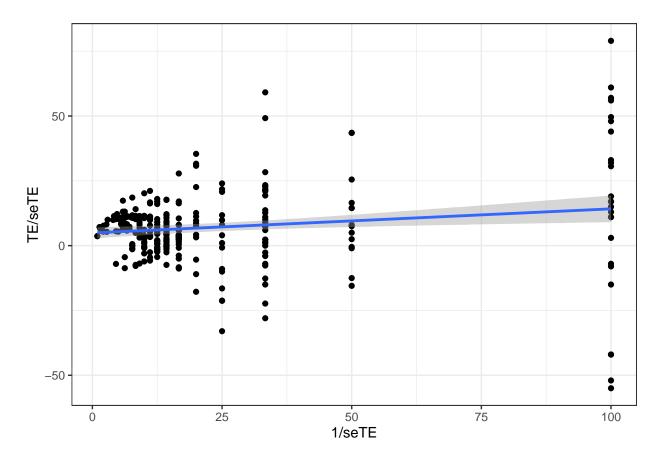
```
## (1 observation deleted due to missingness)
## Multiple R-squared: 0.02652, Adjusted R-squared: 0.02337
## F-statistic: 8.419 on 1 and 309 DF, p-value: 0.00398
```

```
#eggers regression
ggplot(data = data.gen, mapping = aes(x=1/seTE, y = TE/seTE, color= )) +
  geom_point() +
  geom_smooth(method = "lm")
```

```
## 'geom_smooth()' using formula = 'y ~ x'
```

Warning: Removed 1 rows containing non-finite values ('stat_smooth()').

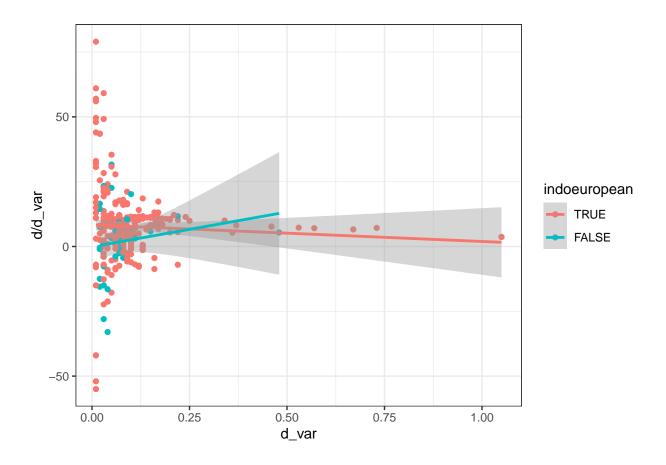
Warning: Removed 1 rows containing missing values ('geom_point()').



```
ggplot(data = df_shape, mapping = aes(x=d_var, y = d/d_var, color= indoeuropean)) +
  geom_point() +
  geom_smooth(method = "lm")
```

```
## 'geom_smooth()' using formula = 'y ~ x'
```

^{##} Warning: Removed 1 rows containing non-finite values ('stat_smooth()').
Removed 1 rows containing missing values ('geom_point()').



eggers.test(m.gen)

using rma.mv instead of m.gen

Warning: 1 row with NAs omitted from model fitting.

Warning: 1 row with NAs omitted from model fitting.

```
summary(mod)
```

##

```
## Multivariate Meta-Analysis Model (k = 311; method: REML)
##
##
      logLik
              Deviance
                              AIC
                                         BIC
             1594.4318 1598.4318
  -797.2159
                                   1605.9049 1598.4709
##
##
## Variance Components:
##
##
               estim
                        sqrt nlvls
                                    fixed factor
## sigma^2
             0.1656 0.4069
                                48
                                               ID
                                       nο
##
## Test for Heterogeneity:
## Q(df = 310) = 2573.9189, p-val < .0001
## Model Results:
##
## estimate
                      zval
                              pval
                                     ci.lb
                se
                                             ci.ub
    0.4365 0.0617 7.0794 <.0001 0.3156 0.5573
##
##
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary(mod_nested)
##
## Multivariate Meta-Analysis Model (k = 304; method: REML)
##
##
      logLik
              Deviance
                              AIC
                                         BIC
  -743.4370 1486.8741
                       1492.8741 1504.0153 1492.9543
##
## Variance Components:
##
##
                        sqrt nlvls fixed
                                               factor
               estim
## sigma^2.1 0.1245
                     0.3528
                                48
                                                   ID
                                       no
## sigma^2.2 0.0956 0.3093
                                75
                                           ID/exp_num
                                       no
## Test for Heterogeneity:
## Q(df = 303) = 2501.5515, p-val < .0001
##
## Model Results:
##
                                     ci.lb
## estimate
                se
                      zval
                              pval
                                             ci.ub
##
    0.4530 0.0668 6.7854
                            <.0001 0.3221
                                            0.5838
##
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

plotting coefficients from the rmv model: assuming that those coefficients correspond to effect sizes

Confirmatory analysis

For primary analyses, i will exclude effect sizes from clinical populations and multilingual populations.

I will investigate the hypotheses via multi-level meta-regressions using the metafor package.

In all models, I will include random effects that control for non-independence between effect sizes based on grouping by paper and grouping by experiment.

I will first fit: Shape bias ~ 1 Shape bias ~ age shape bias ~ log(age) shape bias ~ poly(age,2)

intercept:

Warning: 1 row with NAs omitted from model fitting.

Warning: 1 row with NAs omitted from model fitting.

```
summary(mod_intercept_nonindo)
```

```
##
## Multivariate Meta-Analysis Model (k = 36; method: REML)
##
                                          BIC
                                                     AICc
##
      logLik
               Deviance
                               AIC
## -118.9638
               237,9276
                          243.9276
                                     248.5937
                                                 244.7018
##
## Variance Components:
##
##
                                                                          factor
               estim
                        sqrt nlvls
                                    fixed
## sigma^2.1 0.0019 0.0441
                                                                as.factor(Title)
                                  9
                                        no
                                        no as.factor(Title)/as.factor(exp_num)
## sigma^2.2 0.1019 0.3192
                                 14
## Test for Heterogeneity:
## Q(df = 35) = 308.3847, p-val < .0001
```

```
##
## Model Results:
##
## estimate
              se zval pval ci.lb ci.ub
   0.2240 0.0979 2.2874 0.0222 0.0321 0.4159 *
##
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
summary(mod_intercept_indo)
##
## Multivariate Meta-Analysis Model (k = 268; method: REML)
##
     logLik Deviance
                             AIC
                                        BIC
                                                  AICc
## -586.7531 1173.5062 1179.5062 1190.2679 1179.5975
##
## Variance Components:
##
              estim
                       sqrt nlvls fixed
                                                                      factor
                                                            as.factor(Title)
## sigma^2.1 0.1548 0.3934
                            47 no
## sigma^2.2 0.0890 0.2983
                            68 no as.factor(Title)/as.factor(exp_num)
## Test for Heterogeneity:
## Q(df = 267) = 2141.0974, p-val < .0001
## Model Results:
## estimate
              se
                   zval
                             pval
                                  ci.lb ci.ub
##
    0.4879 0.0724 6.7390 <.0001 0.3460 0.6298 ***
##
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
age
mod_age_nonindo <- rma.mv(d ~ mean_age_months_centered36,</pre>
                 V = d_{var}
                 random = ~1 | as.factor(Title) /
                   as.factor(exp_num),
                 slab = Title,
                 data = filter(df_shape_nonendo, !is.na(exp_num)))
mod_age_indo <- rma.mv(d ~ mean_age_months_centered36,</pre>
                 V = d var,
                 random = ~1 | as.factor(Title) /
                   as.factor(exp_num),
                 slab = Title,
                 data = filter(df_shape_indo, !is.na(exp_num)))
```

Warning: 4 rows with NAs omitted from model fitting.

```
summary(mod_age_nonindo)
```

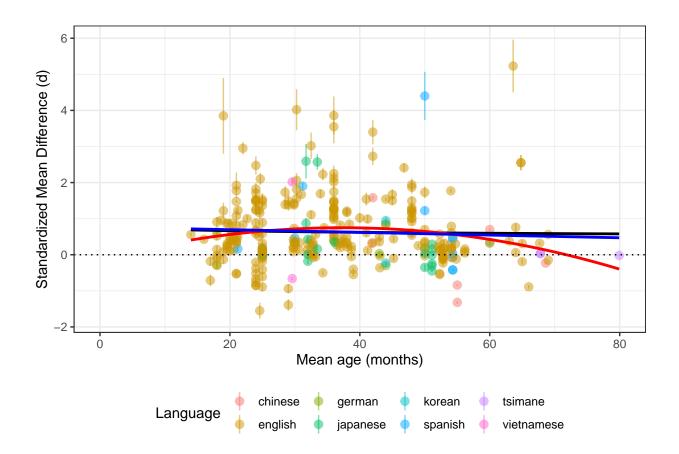
```
##
## Multivariate Meta-Analysis Model (k = 36; method: REML)
##
              Deviance
                              AIC
                                          BIC
                                                    AICc
      logLik
## -111.6430
              223.2860
                          231.2860
                                     237.3914
                                                232.6653
##
## Variance Components:
##
                                                                         factor
              estim
                        sqrt nlvls fixed
                                                               as.factor(Title)
## sigma^2.1 0.0911 0.3018
                                 9
                                       no
## sigma^2.2 0.1991 0.4462
                                14
                                       no as.factor(Title)/as.factor(exp_num)
## Test for Residual Heterogeneity:
## QE(df = 34) = 306.0195, p-val < .0001
##
## Test of Moderators (coefficient 2):
## QM(df = 1) = 17.8283, p-val < .0001
## Model Results:
##
##
                               estimate
                                             se
                                                    zval
                                                            pval
                                                                    ci.lb
                                                                             ci.ub
## intrcpt
                                0.5806 0.1868
                                                  3.1089 0.0019
                                                                   0.2146
                                                                            0.9466
                               -0.0228 0.0054 -4.2224 <.0001 -0.0334 -0.0122
## mean_age_months_centered36
## intrcpt
## mean_age_months_centered36
##
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
summary(mod_age_indo)
## Multivariate Meta-Analysis Model (k = 265; method: REML)
##
##
      logLik
              Deviance
                              AIC
                                          BIC
                                                    AICc
## -570.5792 1141.1584 1149.1584 1163.4471 1149.3135
##
## Variance Components:
##
                                                                         factor
              estim
                        sqrt nlvls fixed
                                                               as.factor(Title)
## sigma^2.1 0.1784 0.4224
                                47
                                       no
## sigma^2.2 0.0853 0.2921
                                67
                                       no as.factor(Title)/as.factor(exp_num)
##
## Test for Residual Heterogeneity:
## QE(df = 263) = 2049.0995, p-val < .0001
##
## Test of Moderators (coefficient 2):
## QM(df = 1) = 13.5952, p-val = 0.0002
##
```

```
## Model Results:
##
##
                               estimate
                                             se
                                                    zval
                                                             pval
                                                                     ci.lb
## intrcpt
                                                  6.5854 <.0001
                                                                    0.3505
                                                                             0.6475
                                 0.4990 0.0758
## mean_age_months_centered36
                                -0.0089 0.0024 -3.6872 0.0002 -0.0136 -0.0042
##
## intrcpt
## mean_age_months_centered36
                               ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
log age
mod_log_age_nonindo <- rma.mv(d ~ log_mean_age_months,</pre>
                      V = d_{var}
                      random = ~1 | as.factor(Title) /
                        as.factor(exp_num),
                      slab = Title,
                      data = filter(df_shape_nonendo, !is.na(log_mean_age_months) , !is.na(exp_num)))
mod_log_age_indo <- rma.mv(d ~ log_mean_age_months,</pre>
                      V = d var,
                      random = ~1 | as.factor(Title) /
                        as.factor(exp_num),
                      slab = Title,
                      data = filter(df_shape_indo, !is.na(log_mean_age_months) , !is.na(exp_num)))
## Warning: 1 row with NAs omitted from model fitting.
summary(mod_log_age_nonindo)
## Multivariate Meta-Analysis Model (k = 36; method: REML)
##
      logLik
               Deviance
                                          BIC
                                                    AICc
                               AIC
## -112.7611
               225.5223
                          233.5223
                                     239.6277
                                                234.9016
##
## Variance Components:
##
                        sqrt nlvls fixed
##
                                                                          factor
               estim
## sigma^2.1 0.0451
                     0.2123
                                  9
                                                                as.factor(Title)
## sigma^2.2 0.1386 0.3723
                                        no as.factor(Title)/as.factor(exp_num)
                                 14
## Test for Residual Heterogeneity:
## QE(df = 34) = 303.8279, p-val < .0001
## Test of Moderators (coefficient 2):
## QM(df = 1) = 13.5408, p-val = 0.0002
## Model Results:
```

```
##
##
                       estimate
                                                    pval
                                                            ci.lb
                                                                     ci.ub
                                     se
                                            zval
## intrcpt
                         3.3799 0.8674
                                          3.8966 <.0001
                                                          1.6798
                                                                   5.0799
## log_mean_age_months -0.8100 0.2201 -3.6798 0.0002 -1.2414 -0.3786 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary(mod_log_age_indo)
##
## Multivariate Meta-Analysis Model (k = 265; method: REML)
##
##
     logLik
             Deviance
                              AIC
                                         BIC
                                                   AICc
## -570.4428 1140.8855 1148.8855 1163.1742 1149.0406
##
## Variance Components:
##
##
                       sqrt nlvls fixed
                                                                        factor
              estim
                                                              as.factor(Title)
## sigma^2.1 0.1847 0.4297
                                47
                                       no
## sigma^2.2 0.0850 0.2916
                                67
                                       no as.factor(Title)/as.factor(exp_num)
##
## Test for Residual Heterogeneity:
## QE(df = 263) = 2060.5383, p-val < .0001
## Test of Moderators (coefficient 2):
## QM(df = 1) = 13.7542, p-val = 0.0002
## Model Results:
##
##
                                                    pval
                       estimate
                                                            ci.lb
                                                                     ci.ub
                                     se
                                            zval
## intrcpt
                         1.7013 0.3330
                                          5.1092 <.0001
                                                           1.0487
                                                                    2.3540
                       -0.3434 0.0926 -3.7087 0.0002 -0.5248 -0.1619 ***
## log_mean_age_months
##
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Let's look at what this means:
ggplot(df_shape,
       aes(x = mean_age_months, y = d, color = language))+
  geom_pointrange(aes(ymin = d - d_var, ymax = d + d_var),
                 alpha = .5) +
  geom_smooth(aes(group = 1),
             col = "black",
             method = "lm", se = FALSE,
             formula = y \sim log(x)) +
    geom_smooth(aes(group = 1),
             col = "red",
             method = "lm", se = FALSE,
             formula = y \sim poly(x,2) +
  geom_smooth(aes(group = 1),
```

col = "blue",

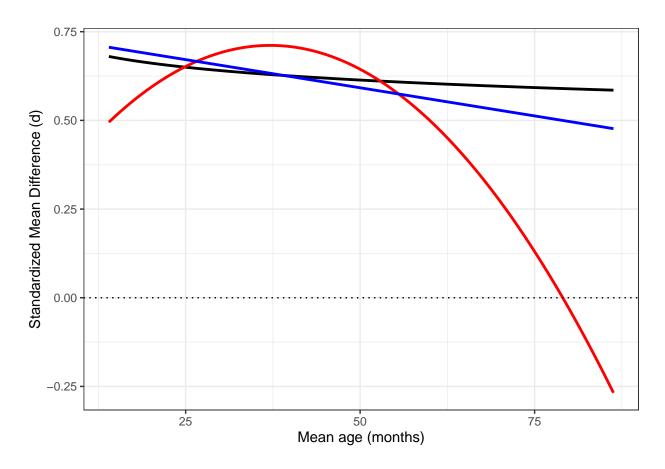
```
## Warning: Removed 4 rows containing non-finite values ('stat_smooth()').
## Removed 4 rows containing non-finite values ('stat_smooth()').
## Removed 4 rows containing non-finite values ('stat_smooth()').
## Warning: Removed 4 rows containing missing values ('geom_pointrange()').
## Warning: Removed 1 rows containing missing values ('geom_segment()').
```



```
ggplot(df_shape,
    aes(x = mean_age_months, y = d))+
geom_smooth(aes(group = 1),
    col = "black",
    method = "lm", se = FALSE,
    formula = y ~ log(x), show.legend = TRUE) +
```

Warning: Removed 3 rows containing non-finite values ('stat_smooth()').

Warning: Removed 3 rows containing non-finite values ('stat_smooth()').
Removed 3 rows containing non-finite values ('stat_smooth()').



polynomial age

```
as.factor(exp_num),
                   slab = Title,
                   data = filter(df_shape_nonendo, !is.na(log_mean_age_months), !is.na(exp_num)))
mod_poly_indo <- rma.mv(d ~ mean_age_months_centered36 + I(mean_age_months_centered36^2),
                   V = d var,
                   random = ~1 | as.factor(ID) /
                     as.factor(exp_num),
                   slab = Title,
                   data = filter(df_shape_indo, !is.na(log_mean_age_months), !is.na(exp_num)))
## Warning: 1 row with NAs omitted from model fitting.
summary(mod_poly_nonindo)
##
## Multivariate Meta-Analysis Model (k = 36; method: REML)
##
      logLik
              Deviance
                               AIC
                                          BIC
                                                    AICc
## -111.4396
               222.8792
                          232.8792
                                     240.3617
                                                235.1014
##
## Variance Components:
##
                        sqrt nlvls fixed
                                                                      factor
               estim
                                                               as.factor(ID)
## sigma^2.1 0.0647
                     0.2543
                                  9
                                        no
## sigma^2.2 0.1535 0.3918
                                 14
                                       no as.factor(ID)/as.factor(exp_num)
## Test for Residual Heterogeneity:
## QE(df = 33) = 286.5903, p-val < .0001
##
## Test of Moderators (coefficients 2:3):
## QM(df = 2) = 16.5974, p-val = 0.0002
## Model Results:
##
##
                                                                         ci.lb
                                    estimate
                                                  se
                                                         zval
                                                                 pval
                                                       3.0188 0.0025
## intrcpt
                                      0.5200 0.1723
                                                                        0.1824
## mean_age_months_centered36
                                     -0.0249 0.0080 -3.1284 0.0018 -0.0405
## I(mean_age_months_centered36^2)
                                     0.0002 0.0003
                                                       0.6881 0.4914 -0.0003
##
                                      ci.ub
## intrcpt
                                     0.8576
## mean_age_months_centered36
                                    -0.0093 **
## I(mean_age_months_centered36^2)
                                     0.0007
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary(mod_poly_indo)
## Multivariate Meta-Analysis Model (k = 265; method: REML)
```

```
##
                              AIC
                                          BTC
                                                    ATCc
##
      logLik
              Deviance
  -570.6134 1141.2268 1151.2268 1169.0686 1151.4612
##
## Variance Components:
##
                                                                      factor
                        sqrt nlvls fixed
              estim
                                                               as.factor(ID)
## sigma^2.1 0.1852 0.4303
                                 46
                                       no
## sigma^2.2 0.0852 0.2918
                                 67
                                       no as.factor(ID)/as.factor(exp_num)
##
## Test for Residual Heterogeneity:
## QE(df = 262) = 2039.8480, p-val < .0001
## Test of Moderators (coefficients 2:3):
## QM(df = 2) = 13.9443, p-val = 0.0009
##
## Model Results:
##
##
                                                                         ci.lb
                                    estimate
                                                  se
                                                         zval
                                                                 pval
## intrcpt
                                      0.4848 0.0806
                                                       6.0178 <.0001
                                                                        0.3269
## mean_age_months_centered36
                                     -0.0099 0.0030 -3.3254 0.0009
                                                                      -0.0158
## I(mean_age_months_centered36^2)
                                                       0.5625 0.5738 -0.0002
                                      0.0001 0.0001
##
                                      ci.ub
                                     0.6427
## intrcpt
## mean_age_months_centered36
                                    -0.0041
## I(mean_age_months_centered36^2)
                                     0.0003
##
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

model comparison and plotting AICc, what is the criteria? cutoff

Polynomial age models

Let's start with an interaction with indoeuropean with standard quadratic terms. This model is very interpretable.

```
## sigma^2.1 0.1582 0.3978
                                 48
                                                    ID
                                        no
## sigma^2.2 0.0933 0.3054
                                 74
                                            ID/exp_num
                                        nο
##
## Test for Residual Heterogeneity:
## QE(df = 295) = 2326.4383, p-val < .0001
##
## Test of Moderators (coefficients 2:6):
## QM(df = 5) = 56.0555, p-val < .0001
##
## Model Results:
##
##
                                                      estimate
                                                                    se
                                                                            zval
## intrcpt
                                                        0.4989 0.0757
                                                                          6.5873
## mean_age_months_centered36
                                                       -0.0099
                                                                0.0029
                                                                        -3.4579
## indoeuropeanFALSE
                                                                0.0737
                                                                         -1.9967
                                                       -0.1472
## I(mean_age_months_centered36^2)
                                                        0.0000
                                                                0.0001
                                                                          0.1988
## mean_age_months_centered36:indoeuropeanFALSE
                                                       -0.0143
                                                                0.0065
                                                                        -2.2109
## indoeuropeanFALSE:I(mean_age_months_centered36^2)
                                                        0.0003
                                                                0.0002
                                                                         1.1043
##
                                                                 ci.lb
                                                                          ci.ub
                                                        pval
## intrcpt
                                                      <.0001
                                                               0.3505
                                                                         0.6474
## mean_age_months_centered36
                                                      0.0005 -0.0155
                                                                       -0.0043
## indoeuropeanFALSE
                                                              -0.2917
                                                                        -0.0027
                                                      0.0459
## I(mean_age_months_centered36^2)
                                                              -0.0002
                                                                         0.0002
                                                      0.8424
                                                              -0.0270
## mean_age_months_centered36:indoeuropeanFALSE
                                                                        -0.0016
                                                      0.0270
## indoeuropeanFALSE:I(mean_age_months_centered36^2)
                                                      0.2694 - 0.0002
                                                                         0.0007
## intrcpt
## mean_age_months_centered36
## indoeuropeanFALSE
## I(mean_age_months_centered36^2)
## mean_age_months_centered36:indoeuropeanFALSE
## indoeuropeanFALSE:I(mean_age_months_centered36^2)
##
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
rma.mv(d ~ mean_age_months_centered36 * indoeuropean ,
       V = d_var,
       random = ~ 1 | ID/exp_num,
       slab = short_cite,
       data = filter(df_shape, !is.na(exp_num), !is.na(language)))
## Warning: 4 rows with NAs omitted from model fitting.
##
## Multivariate Meta-Analysis Model (k = 301; method: REML)
## Variance Components:
##
##
                                                factor
               estim
                        sqrt nlvls
                                     fixed
## sigma^2.1 0.1601
                      0.4001
                                 48
                                        no
## sigma^2.2 0.1051
                      0.3242
                                 74
                                            ID/exp_num
##
```

```
## Test for Residual Heterogeneity:
## QE(df = 297) = 2355.1191, p-val < .0001
##
## Test of Moderators (coefficients 2:4):
## QM(df = 3) = 54.7650, p-val < .0001
##
## Model Results:
##
##
                                                 estimate
                                                                       zval
                                                                               pval
                                                                se
                                                                            <.0001
## intrcpt
                                                   0.5139 0.0738
                                                                     6.9608
                                                                             <.0001
## mean_age_months_centered36
                                                  -0.0093 0.0023
                                                                   -4.0273
                                                           0.0737
## indoeuropeanFALSE
                                                  -0.1497
                                                                    -2.0327
                                                                             0.0421
## mean_age_months_centered36:indoeuropeanFALSE
                                                                    -1.9826 0.0474
                                                  -0.0093 0.0047
##
                                                   ci.lb
                                                             ci.ub
## intrcpt
                                                  0.3692
                                                           0.6586
                                                                    ***
## mean_age_months_centered36
                                                  -0.0139
                                                          -0.0048
## indoeuropeanFALSE
                                                 -0.2941
                                                          -0.0054
## mean_age_months_centered36:indoeuropeanFALSE -0.0184
                                                          -0.0001
##
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

Next try breaking down by language. Here we can see Spanish is sparse and has a huge interaction term for some reason. Probably just overfit.

With the orthogonal polynomials, it blows up completely.

here is the same model but changing the contrasts:

Discussion

References