

## Sheet 2

1- Determine which of the following systems is a linear system.

(a)  $y(n)=5x(n)+2x^2(n)$

(b)  $y(n)=x(n-1)+4x(n)$

2- Determine the causality for each of the following linear systems.

(a)  $y(n)=0.5x(n)+20x(n-2)-0.1y(n-1)$

(b)  $y(n)=x(n+2)-0.4y(n-1)$

3- Check the following systems with respect to: time invariance, linearity, causality. Also, determine if any of them is with memory.

a.  $y[n]=x^2[n-1]$

b.  $y[n]=x[-n+2]$

4-

Given the sequence

$$h(k) = \begin{cases} 2, & k=0,1,2 \\ 1, & k=3,4 \\ 0 & \text{elsewhere} \end{cases}$$

where  $k$  is the time index or sample number,

(a) sketch the sequence  $h(k)$  and the reverse sequence  $h(-k)$ ;

(b) sketch the shifted sequences  $h(-k+2)$  and  $h(-k-3)$ .

5-

Using the sequence definitions

$$h(k) = \begin{cases} 2, & k = 0, 1, 2 \\ 1, & k = 3, 4 \\ 0 & \text{elsewhere} \end{cases} \quad \text{and } x(k) = \begin{cases} 2, & k = 0 \\ 1, & k = 1, 2 \\ 0 & \text{elsewhere} \end{cases}$$

evaluate the digital convolution

$$y(n) = \sum_{k=-\infty}^{\infty} x(k)h(n-k)$$

- a.** using the graphical method;
- b.** using the table method;