VISVESVARAYA TECHNOLOGICAL UNIVERSITY

"JnanaSangama", Belgaum -590014, Karnataka.



Bio Inspired Systems (23CS5BSBIS)

Submitted by

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in partial fulfillment for the award of the degree of

BACHELOR OF ENGINEERING

in

COMPUTER SCIENCE AND ENGINEERING



B.M.S. COLLEGE OF ENGINEERING
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Department of Computer Science and Engineering



CERTIFICATE

This is to certify that the Lab work entitled "Bio Inspired Systems (23CS5BSBIS)" carried out by **SAMARTH KUMAR DUBEY(1BM22CS235)**, who is bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements of the above mentioned subject and the work prescribed for the said degree.

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Github Link:

https://github.com/Samarth512/BIS Lab

Program 1

Genetic Algorithm for Optimization Problems

Genetic Algorithms (GA) are inspired by the process of natural selection and genetics, where the fittest individuals are selected for reproduction to produce the next generation. GAs are widely used for solving optimization and search problems. Implement a Genetic Algorithm using Python to solve a basic optimization problem, such as finding the maximum value of a mathematical function.

Implementation Steps:

- 1. **Define the Problem**: Create a mathematical function to optimize.
- 2. **Initialize Parameters**: Set the population size, mutation rate, crossover rate, and number of generations.
- 3. Create Initial Population: Generate an initial population of potential solutions.
- 4. **Evaluate Fitness**: Evaluate the fitness of each individual in the population.
- 5. **Selection**: Select individuals based on their fitness to reproduce.
- 6. Crossover: Perform crossover between selected individuals to produce offspring.
- 7. **Mutation**: Apply mutation to the offspring to maintain genetic diversity.
- 8. **Iteration**: Repeat the evaluation, selection, crossover, and mutation processes for a fixed number of generations or until convergence criteria are met.
- 9. Output the Best Solution: Track and output the best solution found during the generations.

Algorithm:

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Code:

```
import numpy as np
def target function(x):
  return x^{**}2 + np.random.normal(0, 0.1)
def create population(size, bounds):
  return np.random.uniform(bounds[0], bounds[1], size)
def calculate fitness(population):
  return np.array([target function(ind) for ind in population])
def select parents(population, fitness):
  fitness sum = np.sum(fitness)
  if fitness sum == 0:
    return np.random.choice(population, size=2)
  probabilities = fitness / fitness sum
  return population[np.random.choice(range(len(population)), size=2, p=probabilities)]
def crossover(parent1, parent2, crossover rate):
  if np.random.rand() < crossover rate:
    return (parent1 + parent2) / 2
  return parent 1
def mutate(individual, mutation rate, bounds):
  if np.random.rand() < mutation rate:
    mutation = np.random.uniform(-1, 1)
    individual += mutation
    return np.clip(individual, bounds[0], bounds[1])
  return individual
def replacement(old population, new population):
  combined population = np.concatenate((old population, new population))
  combined fitness = calculate fitness(combined population)
  best indices = np.argsort(combined fitness)[-len(old population):]
  return combined population[best indices]
def genetic algorithm(pop size, bounds, generations, mutation rate, crossover rate):
  population = create population(pop size, bounds)
  for gen in range(generations):
     fitness = calculate fitness(population)
    best fitness = round(np.max(fitness), 5)
    print(f''Generation \{gen + 1\}: Best Fitness = \{best fitness\}'')
```

```
new population = []
    for in range(pop size // 2):
      parent1, parent2 = select parents(population, fitness)
      child1 = mutate(crossover(parent1, parent2, crossover rate), mutation rate, bounds)
      child2 = mutate(crossover(parent2, parent1, crossover rate), mutation rate, bounds)
      new population.extend([child1, child2])
    population = replacement(population, new population)
  final fitness = calculate fitness(population)
  best idx = np.argmax(final fitness)
  best_individual = int(round(population[best idx]))
  best fitness = round(final fitness[best idx], 5)
  print(f"Best individual: {best individual}, Fitness: {best fitness}")
POPULATION SIZE = 10
GENERATION COUNT = 50
MUTATION RATE = 0.1
CROSSOVER RATE = 0.7
BOUNDS = (0, 4)
genetic algorithm(POPULATION SIZE, BOUNDS, GENERATION COUNT,
MUTATION RATE, CROSSOVER RATE)
```

OutPut:

```
Generation 1: Best Fitness = 14.03015
Generation 2: Best Fitness = 14.25866
Generation 3: Best Fitness = 14.92493
Generation 4: Best Fitness = 16.07853
Generation 5: Best Fitness = 15.9414
Generation 6: Best Fitness = 16.0325
Generation 7: Best Fitness = 16.10904
Generation 8: Best Fitness = 16.18451
Generation 9: Best Fitness = 16.12389
Generation 10: Best Fitness = 16.11446
Generation 11: Best Fitness = 16.03909
Generation 12: Best Fitness = 16.19334
Generation 13: Best Fitness = 16.14563
Generation 14: Best Fitness = 16.13926
Generation 15: Best Fitness = 16.21125
Generation 16: Best Fitness = 16.24335
Generation 17: Best Fitness = 16.25528
Generation 18: Best Fitness = 16.17218
Generation 19: Best Fitness = 16.1357
Generation 20: Best Fitness = 16.14817
Generation 21: Best Fitness = 16.14305
Generation 22: Best Fitness = 16.0949
Generation 23: Best Fitness = 16.26894
Generation 24: Best Fitness = 16.20695
Generation 25: Best Fitness = 16.16363
Generation 26: Best Fitness = 16.21272
Generation 27: Best Fitness = 16.08122
Generation 28: Best Fitness = 16.12665
Generation 29: Best Fitness = 16.18215
Generation 30: Best Fitness = 16.10114
Generation 31: Best Fitness = 16.16454
Generation 32: Best Fitness = 16.26946
Generation 33: Best Fitness = 16.17145
Generation 34: Best Fitness = 16.12566
Generation 35: Best Fitness = 16.1072
Generation 36: Best Fitness = 16.13436
Generation 37: Best Fitness = 16.18996
Generation 38: Best Fitness = 16.22735
Generation 39: Best Fitness = 16.08516
Generation 40: Best Fitness = 16.11481
Generation 41: Best Fitness = 16.17697
Generation 42: Best Fitness = 16.1651
Generation 43: Best Fitness = 16.09014
Generation 44: Best Fitness = 16.16286
Generation 45: Best Fitness = 16.08904
Generation 46: Best Fitness = 16.18089
Generation 47: Best Fitness = 16.16205
Generation 48: Best Fitness = 16.09395
Generation 49: Best Fitness = 16.18297
Generation 50: Best Fitness = 16.07618
Best individual: 4, Fitness: 16.19651
```

Program 2

Particle Swarm Optimization for Function Optimization

Particle Swarm Optimization (PSO) is inspired by the social behavior of birds flocking or fish schooling. PSO is used to find optimal solutions by iteratively improving a candidate solution with regard to a given measure of quality. Implement the PSO algorithm using Python to optimize a mathematical function.

Implementation Steps:

- 1. **Define the Problem**: Create a mathematical function to optimize.
- 2. **Initialize Parameters**: Set the number of particles, inertia weight, cognitive and social coefficients.
- 3. **Initialize Particles**: Generate an initial population of particles with random positions and velocities.
- 4. Evaluate Fitness: Evaluate the fitness of each particle based on the optimization function.
- 5. **Update Velocities and Positions**: Update the velocity and position of each particle based on its own best position and the global best position.
- 6. **Iterate**: Repeat the evaluation, updating, and position adjustment for a fixed number of iterations or until convergence criteria are met.
- 7. Output the Best Solution: Track and output the best solution found during the iterations.

Algorithm:

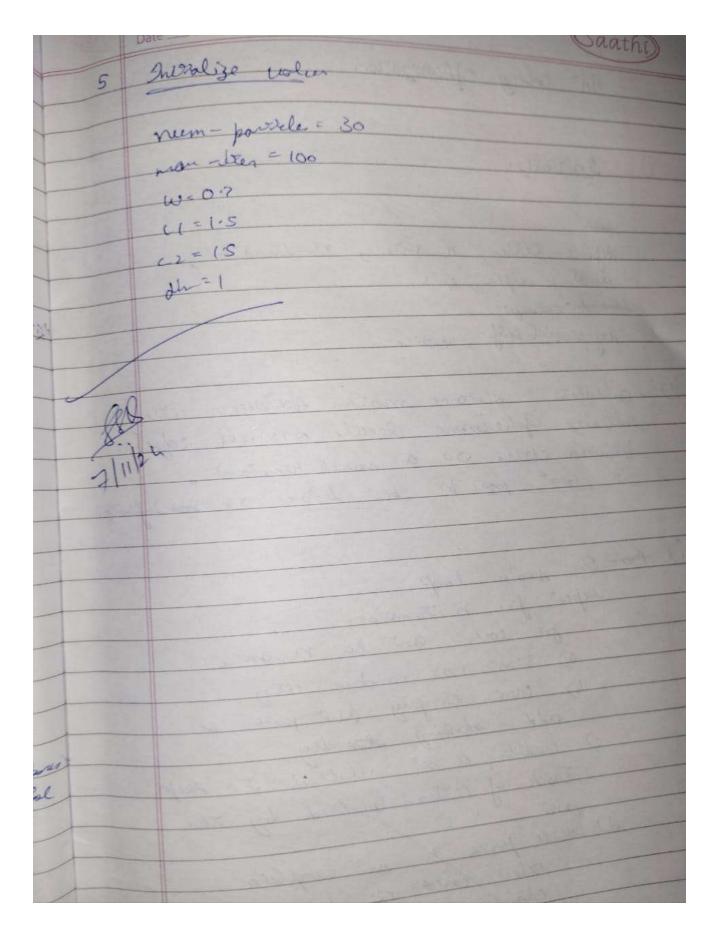
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```
Code:
import numpy as np
# Define the optimization function (Sphere function)
def sphere function(x):
  return np.sum(x^{**2})
# PSO parameters
num particles = 30
                      # Number of particles
num dimensions = 2
                         # Dimensionality of the problem
num iterations = 100
                        # Number of iterations
w = 0.5
                  # Inertia weight
c1 = 1.5
                  # Cognitive (personal) coefficient
c2 = 1.5
                  # Social (global) coefficient
# Initialize particles' positions and velocities
particles position = np.random.uniform(-10, 10, (num particles, num dimensions))
particles velocity = np.random.uniform(-1, 1, (num particles, num dimensions))
# Initialize personal best positions and global best position
personal best position = particles position.copy()
personal best value = np.array([sphere function(x) for x in particles position])
global best position = personal best position[np.argmin(personal best value)]
global best value = np.min(personal best value)
```

PSO main loop

```
for t in range(num iterations):
  for i in range(num particles):
    # Update velocity
    r1, r2 = np.random.rand(num_dimensions), np.random.rand(num_dimensions)
    cognitive velocity = c1 * r1 * (personal best position[i] - particles position[i])
    social velocity = c2 * r2 * (global best position - particles position[i])
    particles velocity[i] = w * particles velocity[i] + cognitive velocity + social velocity
    # Update position
    particles position[i] = particles position[i] + particles velocity[i]
    # Evaluate fitness
    fitness value = sphere function(particles position[i])
    # Update personal best
    if fitness value < personal best value[i]:
       personal best value[i] = fitness value
       personal best position[i] = particles position[i]
    # Update global best
    if fitness value < global best value:
       global best value = fitness value
       global best position = particles position[i]
  # Print best value in current iteration
  print(f"Iteration {t+1}/{num iterations}, Best Value: {global best value}")
```

```
# Output the best solution found
print("Best solution found:")
print("Position:",(global_best_position))
print("Value:", (global_best_value))
```

Output:

```
Iteration 46/100, Best Value: 1.8530325312352947e-11
Iteration 47/100, Best Value: 1.8530325312352947e-11
Iteration 48/100, Best Value: 1.8530325312352947e-11
Iteration 49/100, Best Value: 1.8530325312352947e-11
Iteration 59/100, Best Value: 1.8530325312352947e-11
Iteration 51/100, Best Value: 1.740053178971114e-11
Iteration 52/100, Best Value: 1.424714208530917e-11
Iteration 53/100, Best Value: 2.960973190313839e-14
Iteration 55/100, Best Value: 2.960973190313839e-14
Iteration 55/100, Best Value: 2.960973190313839e-14
Iteration 56/100, Best Value: 2.960973190313839e-14
Iteration 58/100, Best Value: 2.960973190313839e-14
Iteration 60/100, Best Value: 2.960973190313839e-14
 Iteration 60/100, Best Value: 2.960973190313889e-14
Iteration 61/100, Best Value: 2.960973190313889e-14
Iteration 62/100, Best Value: 2.960973190313889e-14
Iteration 63/100, Best Value: 2.960973190313889e-14
Iteration 64/100, Best Value: 2.960973190313889e-14
 Iteration 65/100, Best Value: 2.92075771196141e-14
Iteration 66/100, Best Value: 5.808300002181341e-16
Iteration 67/100, Best Value: 5.808300002181341e-16
Iteration 68/100, Best Value: 5.808300002181341e-16
   Iteration 69/100, Best Value: 5.808300002181341e-16
 Iteration 79/100, Best Value: 5.808300002181341e-16
Iteration 71/100, Best Value: 5.808300002181341e-16
Iteration 72/100, Best Value: 5.808300002181341e-16
Iteration 73/100, Best Value: 5.808300002181341e-16
Iteration 74/100, Best Value: 5.808300002181341e-16
Iteration 74/100, Best Value: 3.982905232835492e-16
 Iteration 75/100, Best Value: 4.0962666995010955e-17
Iteration 76/100, Best Value: 4.0962666995010955e-17
Iteration 77/100, Best Value: 4.0962666995010955e-17
Iteration 78/100, Best Value: 4.0962666995010955e-17
Iteration 79/100, Best Value: 3.366508883506532e-17
  Iteration 80/100, Best Value: 2.4601423037380456e-17
  Iteration 81/100, Best Value: 2.4601423037380456e-17
 Iteration 82/100, Best Value: 1.9404201911347848e-17
Iteration 83/100, Best Value: 2.9494226572905646e-18
Iteration 84/100, Best Value: 2.9494226572905646e-18
Iteration 85/100, Best Value: 2.9494226572905646e-18
   Iteration 86/100, Best Value: 2.9494226572905646e-18
  Iteration 87/100, Best Value: 2.9494226572905646e-18
Iteration 88/100, Best Value: 2.9494226572905646e-18
  Iteration 89/100, Best Value: 2.9494226572905646e-18
Iteration 90/100, Best Value: 2.9494226572905646e-18
  Iteration 91/100, Best Value: 2.9494226572905646e-18
 Iteration 92/100, Best Value: 2.9494226572965646e-18
Iteration 93/100, Best Value: 6.289531829382844e-19
Iteration 94/100, Best Value: 6.289531829382844e-19
Iteration 95/100, Best Value: 6.289531829382844e-19
Iteration 95/100, Best Value: 6.289531829382844e-19
Iteration 96/100, Best Value: 2.687283750634462e-19
Iteration 97/100, Best Value: 2.687283750634462e-19
Iteration 98/100, Best Value: 1.78959873922167e-19
Iteration 100/100, Best Value: 1.78959873922167e-19
Iteration 100/100, Best Value: 1.1280850297663162e-19
Best solution found:
   Position: [ 2.24611439e-10 -2.49716248e-10]
   Value: 1.1280850297663162e-19
```

Program 3:

Ant Colony Optimization for the Traveling Salesman Problem

The foraging behavior of ants has inspired the development of optimization algorithms that can solve complex problems such as the Traveling Salesman Problem (TSP). Ant Colony Optimization (ACO) simulates the way ants find the shortest path between food sources and their nest. Implement the ACO algorithm using Python to solve the TSP, where the objective is to find the shortest possible route that visits a list of cities and returns to the origin city.

Implementation Steps:

- 1. **Define the Problem**: Create a set of cities with their coordinates.
- 2. **Initialize Parameters**: Set the number of ants, the importance of pheromone (alpha), the importance of heuristic information (beta), the evaporation rate (rho), and the initial pheromone value.
- 3. **Construct Solutions**: Each ant constructs a solution by probabilistically choosing the next city based on pheromone trails and heuristic information.
- 4. **Update Pheromones**: After all ants have constructed their solutions, update the pheromone trails based on the quality of the solutions found.
- 5. **Iterate**: Repeat the construction and updating process for a fixed number of iterations or until convergence criteria are met.
- 6. **Output the Best Solution**: Keep track of and output the best solution found during the iterations.

Algorithm:

Date __ /__ /__ Ant colony optimization i) Intralize define cetter, nants, notreratter, does alpea, who class And colony: deficial (self, widele i) calculate disorce motion Noteucen cette snivalze phermone level on all edges between cetter 50 a mall constant, Se Ger por k best disone so me infinite (11) that In main loop repeat for noveration pre lock and en nonte a) Stant at random Wity 6) create empty lest pare a add stortly to dity. c) weath a set ulstiged to keep Trock of aller legated by the ant d) will park for not complica Clays using rule

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After completing pare update best path, for destance V) Pheromone Update After all polls are completed for each edge (ist) => 5 (ij) (ip). This where & is decay rate VD for each and calculate amount of pheromone to deposit on edge in ant's poth DTEISIS O T(i,i) = T(i,i) + OT(i,i) Vi) Return les poil a total distag Pseido Cade Intraliz cities, phermore matri, distance moth Invalige ber fore so empery , Ger- distance to sifnity for journallan is 1 Jo nover : & for some : & Restanly select a song way Involize antis par or Esou-city? Initialize white wite on \$5000 wy ? well anti path is not complete & calculate someth probabilities for antited was seller sent city Gosed on probability

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for each edge (i, j):

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T(ij) + = 0/L-12 tetun best pate & best-distance

Code:

```
import random
import math
import numpy as np
class AntColonyTSP:
  def init (self, cities, n ants, n iterations, alpha, beta, rho, tau 0):
     self.cities = cities
     self.n cities = len(cities)
     self.n ants = n ants
     self.n iterations = n iterations
     self.alpha = alpha # Pheromone importance
     self.beta = beta # Heuristic information importance
     self.rho = rho # Evaporation rate
     self.tau 0 = tau 0 \# Initial pheromone value
     self.dist matrix = self.calculate distances() # Calculate the distance
matrix
     self.pheromone matrix = np.full((self.n cities, self.n cities), tau 0) #
Initialize pheromone matrix
  def calculate distances(self):
     """Calculate the Euclidean distance between each pair of cities."""
     dist matrix = np.zeros((self.n cities, self.n cities))
     for i in range(self.n cities):
       for j in range(i + 1, self.n cities):
          dist = math.sqrt((self.cities[i][0] - self.cities[j][0])**2 +
                     (self.cities[i][1] - self.cities[j][1])**2)
          dist matrix[i][j] = dist matrix[j][i] = dist
     self.print distance matrix(dist matrix) # Print the distance matrix
     return dist matrix
  def print distance matrix(self, dist matrix):
     """Print the distance matrix with cities numbered starting from 1."""
     print("Distance Matrix:")
     print("
                 ", end="")
     for i in range(self.n cities):
       print(f"City \{i+1\}", end=" ") # Print cities starting from 1
     print()
     for i in range(self.n cities):
       print(f"City {i + 1}: ", end="") # Print cities starting from 1
       for i in range(self.n cities):
```

```
print(f"{dist matrix[i][j]:.2f}", end=" ")
       print()
  def select next city(self, ant, visited):
     """Select the next city for the ant to visit based on pheromone and
distance."""
     current city = ant[-1]
     probabilities = []
     for next city in range(self.n cities):
       if next city not in visited:
          pheromone = self.pheromone matrix[current city][next city] **
self.alpha
          distance = self.dist matrix[current city][next city]
          heuristic = (1.0 / \text{distance}) ** self.beta
          probabilities.append(pheromone * heuristic)
       else:
          probabilities.append(0)
     total = sum(probabilities)
     probabilities = [prob / total for prob in probabilities]
     return random.choices(range(self.n cities), probabilities)[0]
  def construct solution(self):
     """Construct a solution for one ant."""
     visited = set()
     ant = [random.randint(0, self.n cities - 1)] # Start at a random city
     visited.add(ant[0])
     for in range(self.n cities - 1):
       next city = self.select next city(ant, visited)
       ant.append(next city)
       visited.add(next city)
     return ant
  def calculate total distance(self, solution):
     """Calculate the total distance of a solution."""
     total distance = 0
     for i in range(len(solution) - 1):
       total distance += self.dist matrix[solution[i]][solution[i + 1]]
     total distance += self.dist matrix[solution[-1]][solution[0]] # Return to
start
     return total distance
  def update pheromones(self, all solutions, all distances):
     """Update pheromones based on the solutions found by the ants."""
     # Evaporate pheromone
     self.pheromone matrix *= (1 - self.rho)
```

```
# Deposit pheromone
     for i in range(self.n ants):
       solution = all solutions[i]
       distance = all distances[i]
       pheromone deposit = 1.0 / distance
       for i in range(len(solution) - 1):
          self.pheromone matrix[solution[i]][solution[i + 1]] +=
pheromone deposit
       self.pheromone matrix[solution[-1]][solution[0]] +=
pheromone deposit # Return to start
  def run(self):
     """Run the Ant Colony Optimization algorithm."""
     best solution = None
     best distance = float('inf')
     for in range(self.n iterations):
       all solutions = []
       all distances = []
       # Each ant constructs a solution
       for in range(self.n ants):
          solution = self.construct solution()
          total distance = self.calculate total distance(solution)
          all solutions.append(solution)
          all distances.append(total distance)
          # Update best solution
          if total distance < best distance:
            best solution = solution
            best distance = total distance
       # Update pheromones
       self.update pheromones(all solutions, all distances)
     return best solution, best distance
# Example usage
# Define cities (x, y) coordinates
cities = [(0, 0), (1, 3), (4, 3), (6, 1), (5, 0), (3, 2), (2, 5), (7, 6)]
# Parameters
n ants = 10
n iterations = 100
alpha = 1.0 # Influence of pheromone
```

```
beta = 2.0  # Influence of distance heuristic
rho = 0.1  # Pheromone evaporation rate
tau_0 = 1.0  # Initial pheromone level

# Create the ACO solver
aco = AntColonyTSP(cities, n_ants, n_iterations, alpha, beta, rho, tau_0)

# Run the algorithm
best_solution, best_distance = aco.run()

# Output the results
print(f"\nBest solution (starting from City 1): {['City ' + str(i+1) for i in best_solution]}")
print(f"Best distance: {best_distance:.2f}")
```

Output:

```
Distance Matrix:
       City 1 City 2 City 3
                                  City 4
                                          City 5 City 6 City 7 City 8
City 1: 0.00
                                         3.61 5.39
              3.16 5.00 6.08
                                  5.00
                                                       9.22
City 2: 3.16
              0.00
                     3.00
                            5.39
                                   5.00
                                          2.24
                                                2.24
                                                       6.71
City 3: 5.00
              3.00
                     0.00
                            2.83
                                   3.16
                                          1.41
                                                 2.83
                                                        4.24
City 4: 6.08
City 5: 5.00
                                   1.41
              5.39
                     2.83
                            0.00
                                          3.16
                                                 5.66
                                                        5.10
              5.00
                            1.41
                     3.16
                                   0.00
                                          2.83
                                                 5.83
City 6: 3.61
              2.24
                     1.41
                            3.16
                                   2.83
                                          0.00
City 7: 5.39
              2.24
                     2.83
                            5.66
                                   5.83
                                          3.16
                                                 0.00
                                                       5.10
City 8: 9.22
              6.71
                     4.24
                           5.10
                                          5.66
                                                5.10
                                                       0.00
                                   6.32
Best solution (starting from City 1): ['City 8', 'City 4', 'City 5', 'City 3', 'City 6', 'City 1', 'City 2', 'City 7']
Best distance: 25.19
```

Program 4:

Cuckoo Search (CS) Optimization

Cuckoo Search (CS) is a nature-inspired optimization algorithm based on the brood parasitism of some cuckoo species. This behavior involves laying eggs in the nests of other birds, leading to the optimization of survival strategies. CS uses Lévy flights to generate new solutions, promoting global search capabilities and avoiding local minima. The algorithm is widely used for solving continuous optimization problems and has applications in various domains, including engineering design, machine learning, and data mining.

Implementation Steps:

- 1. **Define the Problem**: Create a mathematical function to optimize.
- 2. **Initialize Parameters**: Set the number of nests, the probability of discovery, and the number of iterations.
- 3. **Initialize Population**: Generate an initial population of nests with random positions.
- 4. Evaluate Fitness: Evaluate the fitness of each nest based on the optimization function.
- 5. **Generate New Solutions**: Create new solutions via Lévy flights.
- 6. **Abandon Worst Nests**: Abandon a fraction of the worst nests and replace them with new random positions.
- 7. **Iterate**: Repeat the evaluation, updating, and replacement process for a fixed number of iterations or until convergence criteria are met.
- 8. Output the Best Solution: Track and output the best solution found during the iterations.

Algorithm:

Cuckbo search Algorithm 2 Initalize Inevalge men of objective Junevan jan) number of our on news, number · of exercise (n-stration), very flager paramer (Lambdo), abandonnas probability (p-a), step size scaling foctor (alpha) , Dimensoralisty of searce office (dem) 2) Inivalize nevs randomly wither the search Afraco . next - randon intalgation (n-rest &m) 3) Engliste Jitnes Jitness = [evaluate Jones (new) for each next in next I D I dentify the best best bet ones = new with minimum fitness ber-jøners = moninum fitnes realier 5) Repeat for each iteration (1 To nesterolars); a) fre each new new went wing Levy fight new new new i - new tis & alpho * 15 my - fly Chambdo Im

new_ner_i = clips new new_i lower- bound, upper-bound) - Enduces joness of the new next new-nev-1) if the new new is better , replace the old nev: ef new jonen; < fornen [i]: nevatij = new_nev_1' Jenentis = new-jerness-i 6) Abondon mert nexts based on probability - For each new , if romber (0, 1) LPA DI Junen [1] he work. Replace nest i word new panem c) lipdote the best nev of necessary; best nest mest with minimum gother best finen = minimum gitnen walry 6) Return best hear.

Code:

```
import numpy as np
import math
# Objective Function (Optimization Problem)
# This is a sample function to optimize. Modify it as per your problem.
def objective function(x):
  return np.sum(x**2) # Example: Minimize the sum of squares (f(x) = sum(x^2))
# Lévy Flight Step (used to explore the solution space)
def levy flight(Lambda, size):
  sigma u = (math.gamma(1 + Lambda) * np.sin(math.pi * Lambda / 2) /
         math.gamma((1 + Lambda) / 2) * np.power(Lambda, 1 / 2))
  u = np.random.normal(0, sigma u, size)
  v = np.random.normal(0, 1, size)
  step = u / np.power(np.abs(v), 1 / Lambda)
  return step
# Cuckoo Search Algorithm
def cuckoo search(objective function, n nests=25, n iterations=1000, alpha=0.01,
p a=0.25, Lambda=1.5, dim=5):
  # Initialize nests (positions of the solutions)
  nests = np.random.uniform(-10, 10, (n nests, dim)) # Random positions in a 10x10
  fitness = np.array([objective function(nest) for nest in nests]) # Fitness of each nest
  # Find the best solution
  best nest = nests[np.argmin(fitness)]
  best fitness = np.min(fitness)
  for iteration in range(n iterations):
    # Generate new solutions via Lévy flights
    new nests = np.copy(nests)
    for i in range(n nests):
       # Generate a new solution using Lévy flights
       step = levy flight(Lambda, dim)
       new nests[i] = nests[i] + alpha * step
       # Ensure the new nest is within the boundary
       new nests[i] = np.clip(new nests[i], -10, 10)
    # Evaluate the new solutions
```

```
new fitness = np.array([objective function(nest) for nest in new nests])
     # Abandon the worst nests and replace with new random solutions
     for i in range(n nests):
       if new fitness[i] < fitness[i] or np.random.rand() < p a:
          nests[i] = new nests[i]
          fitness[i] = new fitness[i]
     # Update the best solution if a new better nest is found
     best nest = nests[np.argmin(fitness)]
     best fitness = np.min(fitness)
     # Print iteration information
     if (iteration + 1) \% 100 == 0:
       print(f"Iteration {iteration+1}: Best Fitness = {best fitness}")
  return best nest, best fitness
# Parameters for the algorithm
n nests = 25 # Number of nests (population size)
n iterations = 1000 # Number of iterations
alpha = 0.01 # Step size scaling factor
p a = 0.25 # Probability of discovering a new nest
Lambda = 1.5 # Lévy flight exponent (controls the step distribution)
dim = 5 # Dimensionality of the problem (number of variables)
# Run the Cuckoo Search
best nest, best fitness = cuckoo search(objective function, n nests, n iterations, alpha,
p a, Lambda, dim)
# Output the best solution found
print("\nBest Nest (Solution):", best nest)
print("Best Fitness:", best fitness)
```

Output:

```
Iteration 100: Best Fitness = 22.184333732744214
Iteration 200: Best Fitness = 19.25748572535071
Iteration 300: Best Fitness = 15.294817086770632
Iteration 400: Best Fitness = 8.00207803162981
Iteration 500: Best Fitness = 2.0182324333288624
Iteration 600: Best Fitness = 0.379165696672302
Iteration 700: Best Fitness = 0.05124632843442799
Iteration 800: Best Fitness = 0.39524011518223845
Iteration 900: Best Fitness = 0.011230471136135817
Iteration 1000: Best Fitness = 0.07234012599821558
Best Nest (Solution): [ 0.04672369 -0.21664565    0.0092467    0.13564409 -0.06882489]
Best Fitness: 0.07234012599821558
```

Program 5:

Grey Wolf Optimizer (GWO)

The Grey Wolf Optimizer (GWO) algorithm is a swarm intelligence algorithm inspired by the social hierarchy and hunting behavior of grey wolves. It mimics the leadership structure of alpha, beta, delta, and omega wolves and their collaborative hunting strategies. The GWO algorithm uses these social hierarchies to model the optimization process, where the alpha wolves guide the search process while beta and delta wolves assist in refining the search direction. This algorithm is effective for continuous optimization problems and has applications in engineering, data analysis, and machine learning.

Implementation Steps:

- 1. **Define the Problem**: Create a mathematical function to optimize.
- 2. **Initialize Parameters**: Set the number of wolves and the number of iterations.
- 3. **Initialize Population**: Generate an initial population of wolves with random positions.
- 4. **Evaluate Fitness**: Evaluate the fitness of each wolf based on the optimization function.
- 5. **Update Positions**: Update the positions of the wolves based on the positions of alpha, beta, and delta wolves.
- 6. **Iterate**: Repeat the evaluation and position updating process for a fixed number of iterations or until convergence criteria are met.
- 7. **Output the Best Solution**: Track and output the best solution found during the iterations.

Algorithm:

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	Algorithm
7	Inintalize parameten population vze, dimensionality, lawen a upper bound of solution, & manimum steation
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Code:

```
import numpy as np
class GreyWolfOptimizer:
  def init (self, obj function, dim, lb, ub, population size=30,
max iter=100):
    self.obj function = obj function
    self.dim = dim
    self.lb = lb
    self.ub = ub
    self.population size = population size
    self.max iter = max iter
    # Initialize the positions of the wolves
    self.positions = np.random.uniform(lb, ub, (population size, dim))
    self.alpha pos = np.zeros(dim)
    self.beta pos = np.zeros(dim)
    self.delta pos = np.zeros(dim)
    self.alpha score = float('inf')
    self.beta score = float('inf')
    self.delta score = float('inf')
  def optimize(self):
     for iteration in range(self.max iter):
       for i in range(self.population size):
          # Calculate the fitness of each wolf
          fitness = self.obj function(self.positions[i])
          # Update Alpha, Beta, and Delta wolves
          if fitness < self.alpha score:
            self.alpha score = fitness
            self.alpha pos = self.positions[i].copy()
          elif fitness < self.beta score:
            self.beta score = fitness
            self.beta pos = self.positions[i].copy()
          elif fitness < self.delta score:
            self.delta score = fitness
            self.delta pos = self.positions[i].copy()
       # Update the positions of wolves
       for i in range(self.population size):
          for d in range(self.dim):
            # Generate random numbers
            r1, r2 = np.random.rand(), np.random.rand()
            A1 = 2 * r1 - 1 \# coefficient for exploration/exploitation
            C1 = 2 * r2 # coefficient for attraction to alpha wolf
```

```
r1, r2 = np.random.rand(), np.random.rand()
            A2 = 2 * r1 - 1
            C2 = 2 * r2
            r1, r2 = np.random.rand(), np.random.rand()
            A3 = 2 * r1 - 1
            C3 = 2 * r2
            # Calculate the distances from the alpha, beta, and delta wolves
            D alpha = abs(C1 * self.alpha pos[d] - self.positions[i, d])
            D beta = abs(C2 * self.beta pos[d] - self.positions[i, d])
            D delta = abs(C3 * self.delta pos[d] - self.positions[i, d])
            # Calculate the new positions for each wolf
            X1 = self.alpha pos[d] - A1 * D alpha
            X2 = self.beta pos[d] - A2 * D beta
            X3 = self.delta pos[d] - A3 * D delta
            # Update the position by averaging the attraction from all three
wolves
            self.positions[i, d] = (X1 + X2 + X3) / 3
          # Clamp positions to stay within the bounds
          self.positions[i] = np.clip(self.positions[i], self.lb, self.ub)
       print(f"Iteration {iteration + 1}/{self.max iter}, Best Score:
{self.alpha score}")
     return self.alpha pos, self.alpha score
# Example Usage
def sphere function(x):
  return np.sum(x^{**2})
gwo = GreyWolfOptimizer(obj function=sphere function, dim=5, lb=-10, ub=10,
population size=30, max iter=50)
best position, best score = gwo.optimize()
print("Best Position:", best position)
print("Best Score:", best score)
```

Output:

```
Generation 1: Best Fitness = 14.34775
Generation 2: Best Fitness = 14.32671
Generation 3: Best Fitness = 14.49234
Generation 4: Best Fitness = 14.49828
Generation 5: Best Fitness = 14.55672
Generation 6: Best Fitness = 14.55423
Generation 7: Best Fitness = 14.48036
Generation 8: Best Fitness = 14.53179
Generation 9: Best Fitness = 16.13716
Generation 10: Best Fitness = 15.93086
Generation 11: Best Fitness = 16.09927
Generation 12: Best Fitness = 16.35004
Generation 13: Best Fitness = 16.06671
Generation 14: Best Fitness = 16.10586
Generation 15: Best Fitness = 16.03114
Generation 16: Best Fitness = 16.14713
Generation 17: Best Fitness = 16.1142
Generation 18: Best Fitness = 16.07266
Generation 19: Best Fitness = 16.0683
Generation 20: Best Fitness = 16.04721
Generation 21: Best Fitness = 16.14037
Generation 22: Best Fitness = 15.99784
Generation 23: Best Fitness = 16.11707
Generation 24: Best Fitness = 16.00427
Generation 25: Best Fitness = 16.09823
Generation 26: Best Fitness = 16.09977
Generation 27: Best Fitness = 16.18316
Generation 28: Best Fitness = 16.19172
Generation 29: Best Fitness = 16.14199
Generation 30: Best Fitness = 16.08512
Generation 31: Best Fitness = 16.12503
Generation 32: Best Fitness = 16.0563
Generation 33: Best Fitness = 16.14116
Generation 34: Best Fitness = 16.10875
Generation 35: Best Fitness = 16.07223
Generation 36: Best Fitness = 16.16
Generation 37: Best Fitness = 16.13314
Generation 38: Best Fitness = 16.12542
Generation 39: Best Fitness = 16.18574
Generation 40: Best Fitness = 16.14181
Generation 41: Best Fitness = 16.12434
Generation 42: Best Fitness = 16.05498
Generation 43: Best Fitness = 16.05837
Generation 44: Best Fitness = 16.11661
Generation 45: Best Fitness = 16.07196
Generation 46: Best Fitness = 16.15789
Generation 47: Best Fitness = 16.17652
Generation 48: Best Fitness = 16.12622
Generation 49: Best Fitness = 16.20949
Generation 50: Best Fitness = 16.17873
Best individual: 4, Fitness: 16.1344
```

Program 6:

Parallel Cellular Algorithms and Programs

Parallel Cellular Algorithms are inspired by the functioning of biological cells that operate in a highly parallel and distributed manner. These algorithms leverage the principles of cellular automata and parallel computing to solve complex optimization problems efficiently. Each cell represents a potential solution and interacts with its neighbors to update its state based on predefined rules. This interaction models the diffusion of information across the cellular grid, enabling the algorithm to explore the search space effectively. Parallel Cellular Algorithms are particularly suitable for large-scale optimization problems and can be implemented on parallel computing architectures for enhanced performance.

Implementation Steps:

- 1. **Define the Problem**: Create a mathematical function to optimize.
- 2. **Initialize Parameters**: Set the number of cells, grid size, neighborhood structure, and number of iterations.
- 3. **Initialize Population**: Generate an initial population of cells with random positions in the solution space.
- 4. **Evaluate Fitness**: Evaluate the fitness of each cell based on the optimization function.
- 5. **Update States**: Update the state of each cell based on the states of its neighboring cells and predefined update rules.
- 6. **Iterate**: Repeat the evaluation and state updating process for a fixed number of iterations or until convergence criteria are met.
- 7. **Output the Best Solution**: Track and output the best solution found during the iterations.

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Code:

```
import numpy as np
import random
# Define any optimization function to minimize (can be changed as needed)
def custom function(x):
  # Example function: x^2 to minimize
  return np.sum(x ** 2) # Ensuring the function works for multidimensional
inputs
# Initialize population of genetic sequences (each individual is a sequence of
definitialize population(population size, num genes, lower bound,
upper bound):
  # Create a population of random genetic sequences
  population = np.random.uniform(lower bound, upper bound, (population size,
num genes))
  return population
# Evaluate the fitness of each individual (genetic sequence) in the population
def evaluate fitness(population, fitness function):
  fitness = np.zeros(population.shape[0])
  for i in range(population.shape[0]):
     fitness[i] = fitness function(population[i]) # Apply the fitness function to
each individual
  return fitness
# Perform selection: Choose individuals based on their fitness (roulette wheel
selection)
def selection(population, fitness, num selected):
  # Select individuals based on their fitness (higher fitness, more likely to be
selected)
  probabilities = fitness / fitness.sum() # Normalize fitness to create selection
probabilities
  selected indices = np.random.choice(range(len(population)),
size=num selected, p=probabilities)
  selected population = population[selected indices]
  return selected population
# Perform crossover: Combine pairs of individuals to create offspring
def crossover(selected population, crossover rate):
  new population = []
  num individuals = len(selected population)
  for i in range(0, num individuals - 1, 2): # Iterate in steps of 2, skipping the
```

```
last one if odd
    parent1, parent2 = selected population[i], selected population[i + 1]
    if len(parent1) > 1 and random.random() < crossover rate: # Only perform
crossover if more than 1 gene
       crossover point = random.randint(1, len(parent1) - 1) # Choose a random
crossover point
       offspring1 = np.concatenate((parent1[:crossover point],
parent2[crossover point:]))
       offspring2 = np.concatenate((parent2[:crossover point],
parent1[crossover point:]))
       new population.extend([offspring1, offspring2]) # Create two offspring
       new population.extend([parent1, parent2]) # No crossover, retain the
parents
  # If the number of individuals is odd, carry the last individual without crossover
  if num individuals \% 2 == 1:
    new population.append(selected population[-1])
  return np.array(new population)
# Perform mutation: Introduce random changes in offspring
def mutation(population, mutation rate, lower bound, upper bound):
  for i in range(population.shape[0]):
    if random.random() < mutation rate: # Apply mutation based on the rate
       gene to mutate = random.randint(0, population.shape[1] - 1) # Choose a
random gene to mutate
       population[i, gene to mutate] = np.random.uniform(lower bound,
upper bound) # Mutate the gene
  return population
# Gene expression: In this context, it is how we decode the genetic sequence into
a solution
def gene expression(individual, fitness function):
  return fitness function(individual)
# Main function to run the Gene Expression Algorithm
def gene expression algorithm(population size, num genes, lower bound,
upper bound,
                  max generations, mutation rate, crossover rate,
fitness function):
  # Step 2: Initialize the population of genetic sequences
  population = initialize population(population size, num genes, lower bound,
upper bound)
  best solution = None
  best fitness = float('inf')
  # Step 9: Iterate for the specified number of generations
  for generation in range(max generations):
```

```
# Step 4: Evaluate fitness of the current population
     fitness = evaluate fitness(population, fitness function)
    # Track the best solution found so far
    min fitness = fitness.min()
    if min fitness < best fitness:
       best fitness = min fitness
       best solution = population[np.argmin(fitness)]
    # Step 5: Perform selection (choose individuals based on fitness)
    selected population = selection(population, fitness, population size // 2) #
Select half of the population
    # Step 6: Perform crossover to generate new individuals
    offspring population = crossover(selected population, crossover rate)
    # Step 7: Perform mutation on the offspring population
    population = mutation(offspring population, mutation rate, lower bound,
upper bound)
    # Print output every 10 generations
    if (generation + 1) \% 10 == 0:
       print(f'Generation \{generation + 1\}/\{max generations\}, Best Fitness:
{best fitness}")
  # Step 10: Output the best solution found
  return best solution, best fitness
# Parameters for the algorithm
population size = 50 # Number of individuals in the population
num genes = 1 # Number of genes (for a 1D problem, this is just 1, extendable
for higher dimensions)
lower bound = -5 # Lower bound for the solution space
upper bound = 5 # Upper bound for the solution space
max generations = 100 # Number of generations to evolve the population
mutation rate = 0.1 # Mutation rate (probability of mutation per gene)
crossover rate = 0.7 # Crossover rate (probability of crossover between two
parents)
# Run the Gene Expression Algorithm
best solution, best fitness = gene expression algorithm(
  population size, num genes, lower bound, upper bound,
  max generations, mutation rate, crossover rate, custom function)
# Output the best solution found
print("\nBest Solution Found:", best solution)
print("Best Fitness Value:", best fitness)
```

Output:

```
Generation 10/100, Best Fitness: 0.0002226428362338621
Generation 30/100, Best Fitness: 0.0002226428362338621
Generation 30/100, Best Fitness: 0.0002226428362338621
Generation 40/100, Best Fitness: 0.0002226428362338621
Generation 50/100, Best Fitness: 0.0002226428362338621
Generation 60/100, Best Fitness: 0.0002226428362338621
Generation 70/100, Best Fitness: 0.0002226428362338621
Generation 80/100, Best Fitness: 0.0002226428362338621
Generation 90/100, Best Fitness: 0.0002226428362338621
Generation 100/100, Best Fitness: 0.0002226428362338621
Best Solution Found: [0.01492122]
Best Fitness Value: 0.0002226428362338621
```

Program 7:

Optimization via Gene Expression Algorithms

Gene Expression Algorithms (GEA) are inspired by the biological process of gene expression in living organisms. This process involves the translation of genetic information encoded in DNA into functional proteins. In GEA, solutions to optimization problems are encoded in a manner similar to genetic sequences. The algorithm evolves these solutions through selection, crossover, mutation, and gene expression to find optimal or near-optimal solutions. GEA is effective for solving complex optimization problems in various domains, including engineering, data analysis, and machine learning.

Implementation Steps:

- 1. **Define the Problem**: Create a mathematical function to optimize.
- 2. **Initialize Parameters**: Set the population size, number of genes, mutation rate, crossover rate, and number of generations.
- 3. Initialize Population: Generate an initial population of random genetic sequences.
- 4. **Evaluate Fitness**: Evaluate the fitness of each genetic sequence based on the optimization function.
- 5. **Selection**: Select genetic sequences based on their fitness for reproduction.
- 6. Crossover: Perform crossover between selected sequences to produce offspring.
- 7. **Mutation**: Apply mutation to the offspring to introduce variability.
- 8. **Gene Expression**: Translate genetic sequences into functional solutions.
- 9. **Iterate**: Repeat the selection, crossover, mutation, and gene expression processes for a fixed number of generations or until convergence criteria are met.
- 10. Output the Best Solution: Track and output the best solution found during the iterations.

Algorithm:

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	Grene Expansion Algorithm
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Code:

```
import numpy as np
import random
# Step 1: Define the Problem (Optimization Function)
def fitness function(position):
  """Example fitness function: Sphere function"""
  return sum(x^{**}2 for x in position)
# Step 2: Initialize Parameters
grid size = (10, 10) # Grid size (10x10 \text{ cells})
dim = 2 # Dimensionality of each cell's position
minx, maxx = -10.0, 10.0 # Search space bounds
max iterations = 50 # Number of iterations
# Step 3: Initialize Population (Random positions)
definitialize population(grid size, dim, minx, maxx):
  population = np.zeros((grid size[0], grid size[1], dim))
  for i in range(grid size[0]):
     for j in range(grid size[1]):
       population[i, i] = [random.uniform(minx, maxx) for in range(dim)]
  return population
# Step 4: Evaluate Fitness (Calculate fitness for each cell)
def evaluate fitness(population):
  fitness grid = np.zeros((grid size[0], grid_size[1]))
  for i in range(grid size[0]):
     for j in range(grid size[1]):
       fitness grid[i, j] = fitness function(population[i, j])
  return fitness grid
# Step 5: Update States (Update each cell based on its neighbors)
def get neighbors(i, j):
  """Returns the coordinates of neighboring cells."""
  neighbors = []
  for di in [-1, 0, 1]:
     for dj in [-1, 0, 1]:
       if not (di == 0 and dj == 0): # Exclude the cell itself
          ni, nj = (i + di) \% grid size[0], (j + dj) \% grid size[1]
          neighbors.append((ni, nj))
  return neighbors
def update cell(population, fitness grid, i, i, minx, maxx):
  """Update the state of a cell based on the average state of its neighbors."""
  neighbors = get neighbors(i, j)
  best neighbor = min(neighbors, key=lambda x: fitness grid[x[0], x[1]])
```

```
# Update cell position to move towards the best neighbor's position
  new position = population[best neighbor[0], best neighbor[1]] + \
           np.random.uniform(-0.1, 0.1, dim) # Small random perturbation
  # Ensure the new position stays within bounds
  new position = np.clip(new position, minx, maxx)
  return new position
# Step 6: Iterate (Repeat for a fixed number of iterations)
population = initialize population(grid size, dim, minx, maxx)
for iteration in range(max iterations):
  fitness grid = evaluate fitness(population)
  # Update each cell in parallel (simultaneously)
  new population = np.zeros like(population)
  for i in range(grid size[0]):
     for j in range(grid size[1]):
       new population[i, i] = update cell(population, fitness grid, i, j, minx,
maxx)
  population = new population
  # Print best fitness at each iteration
  best fitness = np.min(fitness grid)
  print(f"Iteration {iteration + 1}, Best Fitness: {best fitness}")
# Step 7: Output the Best Solution
best index = np.unravel index(np.argmin(fitness grid), fitness grid.shape)
best position = population[best index[0], best index[1]]
best fitness = np.min(fitness grid)
print("Best Position Found:", best position)
print("Best Fitness Found:", best fitness)
```

Output:

```
Iteration 1, Best Fitness: 2.0826803502492166
Iteration 2, Best Fitness: 1.7744398596087352
Iteration 3, Best Fitness: 1.4883681724573383
Iteration 4, Best Fitness: 1.387002652076188
Iteration 5, Best Fitness: 1.2427437690805143
Iteration 6, Best Fitness: 1.0599616727655872
Iteration 7, Best Fitness: 0.8679138915700586
Iteration 8, Best Fitness: 0.7270295605596662
Iteration 9, Best Fitness: 0.5602986423626427
Iteration 10, Best Fitness: 0.4288173108004688
Iteration 11, Best Fitness: 0.29608524463484226
Iteration 12, Best Fitness: 0.24338248635399468
Iteration 13, Best Fitness: 0.1653629256411268
Iteration 14, Best Fitness: 0.09981682496633203
Iteration 15, Best Fitness: 0.03965954346480205
Iteration 16, Best Fitness: 0.007780710681381793
Iteration 17, Best Fitness: 0.00029849766888554087
Iteration 18, Best Fitness: 0.0004899086297133481
Iteration 19, Best Fitness: 4.251173519935761e-05
Iteration 20, Best Fitness: 6.0338848084739565e-05
Iteration 21, Best Fitness: 3.6146911539659715e-05
Iteration 22, Best Fitness: 9.196981175899878e-05
Iteration 23, Best Fitness: 1.938276328999423e-05
Iteration 24, Best Fitness: 0.00011841546744371104
Iteration 25, Best Fitness: 7.587836680690964e-05
Iteration 26, Best Fitness: 9.106396162522501e-05
Iteration 27, Best Fitness: 0.00048545538760096476
Iteration 28, Best Fitness: 2.8078803253508404e-05
Iteration 29, Best Fitness: 7.200201265540344e-05
Iteration 30, Best Fitness: 0.0001614676021904634
Iteration 31, Best Fitness: 0.0003952025944379032
Iteration 32, Best Fitness: 3.239940240533401e-05
Iteration 33, Best Fitness: 0.00019472366858021127
Iteration 34, Best Fitness: 9.766847442440533e-05
Iteration 35, Best Fitness: 2.8878862975346795e-05
Iteration 36, Best Fitness: 2.0488363026836332e-05
Iteration 37, Best Fitness: 5.6206471847444956e-05
Iteration 38, Best Fitness: 0.00010026031741971453
Iteration 39, Best Fitness: 2.351888244594138e-05
Iteration 40, Best Fitness: 6.908851328290999e-05
Iteration 41, Best Fitness: 9.091741874917746e-05
Iteration 42, Best Fitness: 0.00012684003938990727
Iteration 43, Best Fitness: 1.5983340123524183e-05
Iteration 44, Best Fitness: 0.00048724364611154735
Iteration 45, Best Fitness: 0.00029834779012142203
Iteration 46, Best Fitness: 1.0771428049026778e-05
Iteration 47, Best Fitness: 4.5911759331353676e-05
Iteration 48, Best Fitness: 4.446408549143865e-05
Iteration 49, Best Fitness: 0.00016271325878503776
Iteration 50, Best Fitness: 5.0893201170283464e-05
Best Position Found: [0.02679162 0.00329233]
Best Fitness Found: 5.0893201170283464e-05
```