

Name: Swara Desai

ID: 202311005

IT549: Deep Learning

1<sup>st</sup> In-Semester Exam (7<sup>th</sup> FEB 2024)

DA-IICT, Gandhinagar

Time Duration: 60 Minutes

Total Marks: 23

20.75

Q.1 (3 points)

Answer True or False. 0.5 points for the correct answer and, -0.25 for the wrong answer, 0 points if you do not attempt it.

- (a) Output from the "ReLU" activation function is bounded between 0 to 1. False
- (b) Logistic regression is a non linear regression model. True
- (c) Gradient descent optimization always find the global minima in non-linear ANN model. False
- (d) Softmax activation function take the vector as input and output the same size vector. True
- (e) Minimum gradient value of Tanh activation function is -1. True
- (f) Multiple polynomial regression (without regularization) have a close form solution. True

Q.2 (4 points)

The confusion matrix for the testing outcome of the ANN based binary classification model for fault detection is given below. Compute accuracy, precision, sensitivity and specificity for fault detection. You need to write the formula and place the value

		Prediction	
		fault(+ve)	Normal(-ve)
Actual	fault(+ve)	100	300
	Normal(-ve)	200	1000

$$\text{Precision} = \frac{TP}{TP + FP} = \frac{100}{100 + 200} = \frac{100}{300}$$

$$\text{Recall} = \frac{TP}{TP + FN} = \frac{100}{100 + 300} = \frac{100}{400}$$

$$\begin{aligned}\text{Sensitivity} &= \frac{\cancel{TP}}{\cancel{TP} + \cancel{FP}} \quad \frac{\cancel{TP}}{\cancel{TP} + \cancel{FN}} \quad \frac{\cancel{TP}}{\cancel{TP} + \cancel{FP}} \quad \frac{TN}{TN + FP} \\ &= \frac{\cancel{TP}}{\cancel{TP} + \cancel{FN}} \quad \frac{1000}{1000 + 200} = \frac{1000}{1200} \\ &= \end{aligned}$$

$$\text{Accuracy} = \frac{TP + TN}{P + N} = \frac{100 + 1000}{100 + 300} = \frac{1100}{400}$$

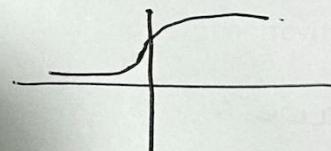
Q.3 (7 points)

Write the formulas and denote the each term.

(a) Sigmoid function and Draw function input output plot

$$f(z) = \frac{1}{1 + e^{-z}}$$

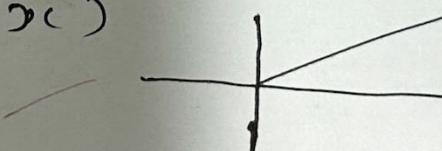
range (0, 1)



(b) Relu function and Draw function input output plot

$$f(z) = \max(0, z)$$

range (0, ∞)



(c) Multiple linear regression

$$y = w_0 + \sum_{m=1}^M w_m x_m \quad \text{where } y \text{ is output variable}$$

$x_m$  = input features

$w_0$  = bias term

$w_m$  = weight

(d) Logistic regression

$$y(z) = \frac{1}{1 + e^{-(w_0 + \sum_{m=1}^M w_m x_m)}} \quad \begin{matrix} w_m \text{ weight} \\ w_0 \text{ bias term} \\ x_m \text{ input features} \end{matrix}$$

where  $z$  = sigmoid activation function

(e) Mean square error

$$\frac{1}{n} \sum (y - \bar{y})^2$$

$y$  = target variable

$n$  = no. of input variables

$\bar{y}$  = Predicted variable

(f) Binary cross entropy

$$H(y, \hat{y}) = -(y_n \log(\hat{y}_n) + (1 - \hat{y}_n) \log(1 - \hat{y}_n))$$

$y_n$  = target variable

$\hat{y}_n$  = Predicted output variable

(g) Close-form solution for multiple linear regression

$$\omega^* = (X \cdot X^T)^{-1} X^T \cdot Y$$

where  $\omega$  = weight  $Y$  = Output  
 $X$  = features

Q.4 (3 points)

Fill the blank; MLP network with following scenario (you can specify some pre-processing of output data if you think so...)

a. Classification problem with ten classes; One hot encoding of output;

Preferable activation function at output layer: Softmax

Preferable cost function: Cross entropy

b. Classification problem with two classes

Preferable Activation function at output layer: Sigmoid

Preferable cost function: Binary cross entropy

c. Regression problem with three output variable, output ranges unbounded.

Preferable Activation function at output layer: Linear

Preferable cost function: MSE

Q.5 (3 points)

Fill in the gap.

(a) A logistic regression model with 10-dimensional input features has 11 number of learnable

parameters, and multiple linear regression has 11 number of learnable parameters.

(b) How many parameter in ANN model that contains five neuron in input layers, five neuron in

hidden layer and three neuron in output layer.  $(5 \times 5 + 5) + (5 \times 3 + 3)$

$$= 30 + 18$$

$$= \underline{48}$$

- (c) Gradient value of ReLU activation function for positive input is 1 and for negative input value is 0.

Q.6 (3 points)

Given a following matrix; compute the performance measures e.g. precision, recall, and specificity for 'Neutral' class from following confusion matrix.

		Predicted		
		Like	Neutral	Dislike
Actual	Like	210	25	25
	Neutral	50	400	50
	Dislike	40	50	150

$$\text{Precision} = \frac{TP}{TP + FP} = \frac{400}{400 + (25 + 50)} \\ = \frac{400}{475}$$

$$\text{Recall} = \frac{TP}{TP + FN} = \frac{400}{400 + (50 + 50)} \\ = \frac{400}{500}$$

~~$$\text{Specificity} = \frac{FP}{FP + TN} = \frac{(25 + 50)}{(25 + 50) + (210 + 40)} \\ + 25 + 150$$~~

$$\text{Specificity} = \frac{TN}{TN + FP} = \frac{(210 + 40 + 25 + 150)}{(210 + 40 + 25 + 150) + (25 + 50)} \\ = \frac{425}{500}$$

Q.1 (3 points)

Answer True or False. 0.5 points for the correct answer and, -0.25 for the wrong answer, 0 points if you do not attempt it.

- (a) Output from the "ReLU" activation function is bounded between 0 to 1. F
- (b) Logistic regression is a non linear regression model. T
- (c) Gradient descent optimization always find the global minima in non-linear ANN model. F
- (d) Softmax activation function take the vector as input and output the same size vector. F
- (e) Minimum gradient value of Tanh activation function is -1. T
- (f) Multiple polynomial regression (without regularization) have a close form solution. T

Q.2 (4 points)

The confusion matrix for the testing outcome of the ANN based binary classification model for fault detection is given below. Compute accuracy, precision, sensitivity and specificity for fault detection. You need to write the formula and place the value

		Prediction	
		Classes	fault(+v)
		fault(+v)	Normal(-ve)
Actual	fault(+v)	100	300
	Normal(-ve)	200	1000

300

~~300~~  
1300

1600

400  
~~200~~ 1200

$$\text{Accuracy} = \frac{TP + TN}{P + N} =$$

$$= \frac{1100}{1600} = 11/16$$

$$\boxed{\text{Accuracy} = 0.6875}$$

$$\text{Sensitivity} = \frac{TP}{TP + FN}$$

$$= \frac{100}{400}$$

$$\boxed{\text{Sensitivity} = 0.25}$$

$$\text{Precision} = \frac{TP}{TP + FP}$$

$$= \frac{100}{300}$$

$$\boxed{\text{Precision} = 0.333}$$

$$\text{Specificity} = \frac{TN}{TN + FP}$$

$$= \frac{1000}{1200}$$

$$\boxed{\text{Specificity} = 0.833}$$

Q.3 (7 points) B3

Write the formulas and denote the each term.

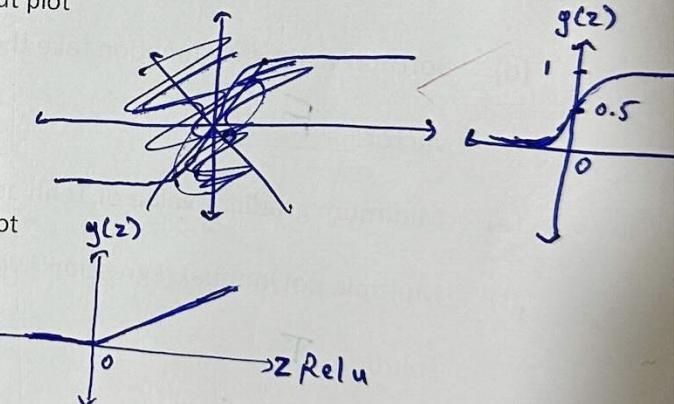
(a) Sigmoid function and Draw function input output plot

$$g(z) = \frac{1}{1 + e^{-z}}$$

$$z = w^T x + b$$

(b) Relu function and Draw function input output plot

$$g(z) = \begin{cases} 0 & z \leq 0 \\ z & z > 0 \end{cases}$$



(c) Multiple linear regression

$$y = w^T x + b$$

$$\text{or } y = w_1 x_1 + w_2 x_2 + w_3 x_3 + \dots + w_m x_m + b$$

(d) Logistic regression

$$y = \frac{1}{1 + e^{-(w^T x + b)}}$$

(e) Mean square error

$$MSE = \frac{1}{m} \sum_{i=1}^m (y_i - \hat{y}_i)^2$$

(f) Binary cross entropy

$$E = -y \log(\hat{y}) - (1-y) \log(1-\hat{y})$$

(g) Close-form solution for multiple linear regression

$$\omega^* = (A^T A)^{-1} A^T y$$

Q.4 (3 points)-----

Fill the blank; MLP network with following scenario (you can specify some pre-processing of output data if you think so...) 3

a. Classification problem with ten classes; One hot encoding of output;

Preferable activation function at output layer: Softmax

Preferable cost function: Cross Entropy

b. Classification problem with two classes

Preferable Activation function at output layer: Sigmoid

Preferable cost function: binary cross entropy

c. Regression problem with three output variable, output ranges unbounded.

Preferable Activation function at output layer: linear

Preferable cost function: MSE

Q.5 (3 points)-----

Fill in the gap. 3

(a) A logistic regression model with 10-dimensional input features has 11 number of learnable parameters, and multiple linear regression has 11 number of learnable parameters.

(b) How many parameter in ANN model that contains five neuron in input layers, five neuron in hidden layer and three neuron in output layer. 48

$$\begin{array}{r}
 25 + 5 = 30 \\
 15 + 3 + 18 \\
 \hline
 48
 \end{array}$$

(c) Gradient value of ReLu activation function for positive input is 1 and for negative input value is 0.

Q.6 (3 points)-

Given a following matrix; compute the performance measures e.g. precision, recall, and specificity for 'Neutral' class from following confusion matrix.

		Predicted				
		classes	Like	Neutral	Dislike	
Actual	Like	210	25	25	260	
	Neutral	50	400	50	500	
	Dislike	40	50	150	240	
		300	475	225	1000	

		Predicted		Total
Actual		+ve	-ve	
		TP	FN	500
	+ve	400	100	500
	-ve	75	425	500
Total		475	525	1000

### Recall

$$R = \frac{TP}{TP+FN}$$

$$= \frac{400}{400+100} = \frac{400}{500}$$

$$\boxed{\text{Recall} = 0.8}$$

### Precision

$$P_a = \frac{TP}{TP+FP}$$

$$= \frac{400}{475}$$

$$\boxed{\text{Precision} = 0.8421}$$

### Specificity

$$S = \frac{TN}{TN+FP}$$

$$= \frac{425}{425+75} = \frac{425}{500}$$

$$\boxed{\text{Specificity} = 0.85}$$

Name: Patel Aditya

ID: 202311025

IT549: Deep Learning

1<sup>st</sup> In-Semester Exam ( 7<sup>th</sup> FEB 2024)

DA-IICT, Gandhinagar

Time Duration: 60 Minutes

Total Marks: 23

(20)

Q.1 (3 points)

Answer True or False. 0.5 points for the correct answer and, -0.25 for the wrong answer, 0 points if you do not attempt it.

- (a) Output from the "ReLU" activation function is bounded between 0 to 1. False
- (b) Logistic regression is a non linear regression model. True
- (c) Gradient descent optimization always find the global minima in non-linear ANN model. False
- (d) Softmax activation function take the vector as input and output the same size vector. True
- (e) Minimum gradient value of Tanh activation function is -1. False
- (f) Multiple polynomial regression (without regularizaiton) have a close form solution. True

Q.2 (4 points)

(4)

The confusion matrix for the testing outcome of the ANN based binary classification model for fault detection is given below. Compute accuracy, precision, sensitivity and specificity for fault detection. You need to write the formula and place the value

		Prediction	
		Classes	fault(+v)
		fault(+v)	Normal(-ve)
Actual	fault(+v)	100 TP	300 FN
	Normal(-ve)	200 FP	1000 TN

$$\text{Accuracy} = \frac{TP + TN}{TP + TN + FP + FN} = \frac{100 + 1000}{100 + 1000 + 300 + 200} = \underline{\underline{0.6875}}$$

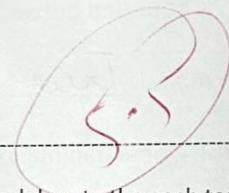
$$\text{Precision} = \frac{TP}{TP + FP} = \frac{100}{100 + 200} = \underline{\underline{0.333}}$$

$$\text{Recall} = \frac{TP}{TP + FN} = \frac{100}{100 + 300} = \underline{\underline{0.25}}$$

$$\text{Specificity} = \frac{TN}{TN + FP} = \frac{1000}{1000 + 200} = \underline{\underline{0.833}}$$

( $\because TP = 100, TN = 1000, FN = 300, FP = 200$ )

Q.3 (7 points)



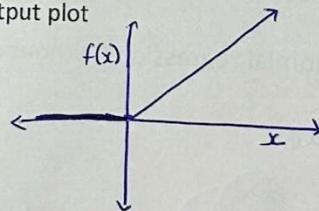
Write the formulas and denote the each term.

(a) Sigmoid function and Draw function input output plot

$$f(x) = \frac{1}{1+e^{-x}}$$

(b) Relu function and Draw function input output plot

$$f(x) = \begin{cases} 0 & ; \text{ if } x \leq 0 \\ x & ; \text{ if } x > 0 \end{cases}$$



(c) Multiple linear regression

$$f(x) = w_0 + \sum_{i=1}^m w_i x_i$$

(d) Logistic regression

$$f(x) = \begin{cases} 1 & ; \text{ if } \frac{1}{1+e^{-x}} > 0.5 \\ 0 & ; \text{ if } \frac{1}{1+e^{-x}} < 0.5 \end{cases}$$

( $\because 0.5$  is considered as boundary for classification)

$$\text{Error} = \frac{\sum_{i=1}^n (y_i - \hat{y})^2}{n}$$

where

$y_i$  is actual value  
 $\hat{y}$  predicted value

$n$  is number of data points

Specit.

(f) Binary cross entropy

$$BCE = y_i \log y_i - (1-y_i) \log (1-y_i)$$

(g) Close-form solution for multiple linear regression

$$\min \frac{1}{n} \sum_{i=1}^n \left[ y_i - \left\{ w_{0i} + \sum_{j=1}^m w_{ji} x_{ji} \right\} \right]^2$$

where  $m = \text{no. of features}$   
 $n = \text{no. of data samples}$

Q.4 (3 points)-

Fill the blank; MLP network with following scenario (you can specify some pre-processing of output data if you think so...)

- a. Classification problem with ten classes; One hot encoding of output;  
Preferable activation function at output layer: Softmax  
Preferable cost function: Cross Entropy.

- b. Classification problem with two classes

Preferable Activation function at output layer: Sigmoid  
Preferable cost function: Binary Cross Entropy

- c. Regression problem with three output variable, output ranges unbounded.  
Preferable Activation function at output layer: Linear Activation function  
Preferable cost function: Least Square Error

Q.5 (3 points)-

Fill in the gap.

- (a) A logistic regression model with 10-dimensional input features has 0 number of learnable parameters, and multiple linear regression has 11 number of learnable parameters.

- (b) How many parameter in ANN model that contains five neuron in input layers, five neuron in hidden layer and three neuron in output layer. 75

- (c) Gradient value of ReLu activation function for positive input is 1 and for negative input value is 0.

Q.6 (3 points)

Given a following matrix; compute the performance measures e.g. precision, recall, and specificity for 'Neutral' class from following confusion matrix.

		Predicted			
		classes	Like	Neutral	Dislike
Actual	Like	210	25	25	
	Neutral	50	400	50	
	Dislike	40	50	150	

Predicted.

$$\begin{array}{ccc}
 & +ve & -ve \\
 +ve & 400_{TP} & 100_{FN} \\
 \text{Actual -ve} & 75_{FP} & 425_{TN}
 \end{array}$$

$$\text{Precision} = \frac{TP}{TP + FP} = \frac{400}{400 + 75} = \underline{0.8421}$$

$$\text{Recall} = \frac{TP}{TP + FN} = \frac{400}{400 + 100} = \underline{0.8}$$

$$\text{Specificity} = \frac{TN}{TN + FP} = \frac{425}{425 + 75} = \underline{0.85}$$