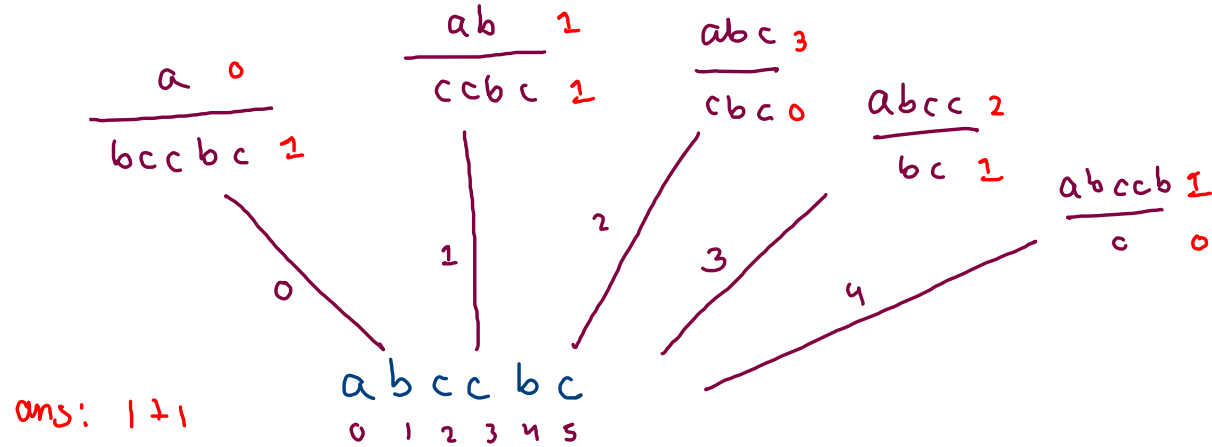


Minimum Palindromic Cut

a | b | c | c | b | c

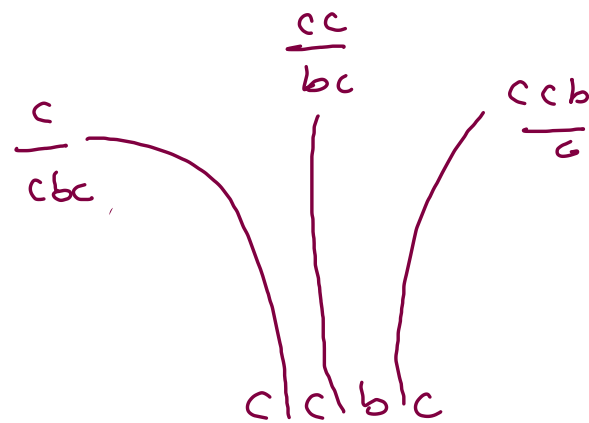
a | b | c c | b | c

a | b c c b | c

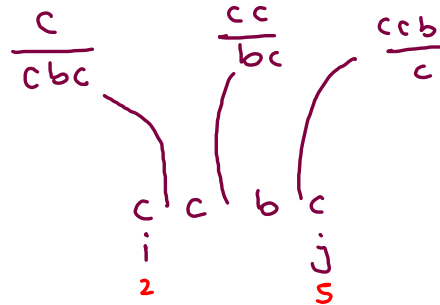


left-right
strategy

	a	b	c	c	b	c
a	0	1	2	2	1	2
b	α	0	1	1	0	1
c	α	α	0	0	1	1
c	α	α	α	0	1	0
b	α	α	α	α	0	1
c	α	α	α	α	α	0



	a_0	b_1	c_2	c_3	b_4	c_5
a_0	0	1	2	2	1	2
b_1	∞	0	1	1	0	2
c_2	∞	∞	0	0	1	2
c_3	∞	∞	∞	0	2	0
b_4	∞	∞	∞	∞	0	2
c_5	∞	∞	∞	∞	∞	0



	dp	op
$k : 2$	2, 2	3, 5
$k : 3$	2, 3	4, 5
$k : 4$	2, 4	5, 5

```

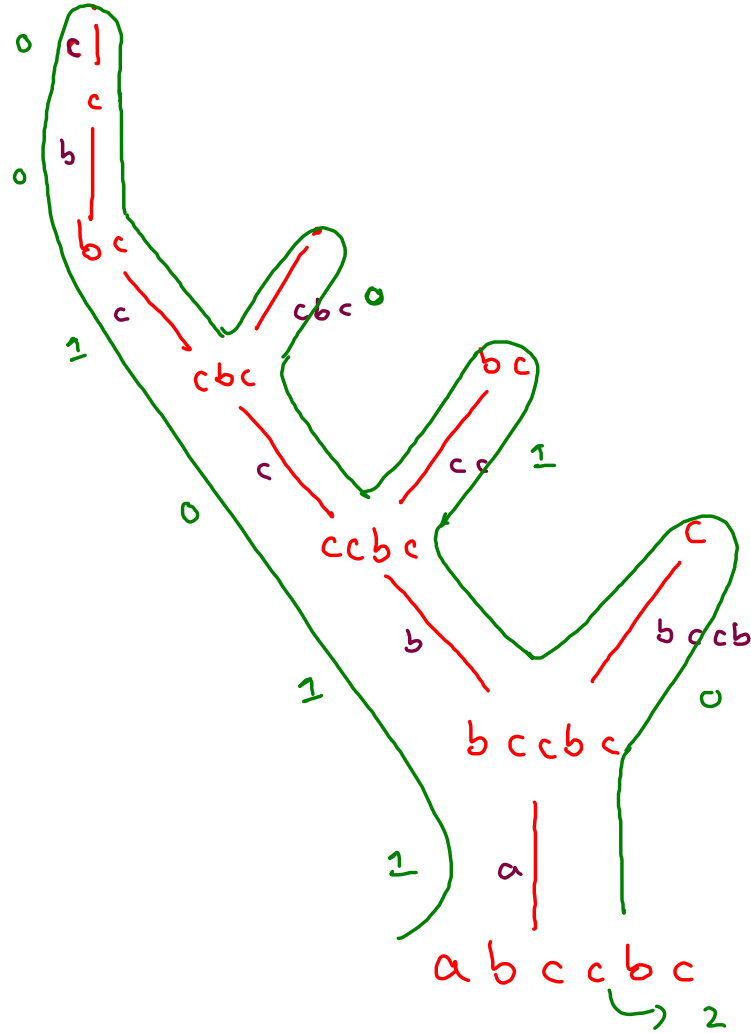
for(int d=0; d < dp.length; d++) {
    for(int i=0, j = d; j < dp[0].length; i++, j++) {
        if(d == 0) {
            dp[i][j] = 0;
        }
        else if(d == 1) {
            dp[i][j] = (s.charAt(i) == s.charAt(j)) ? 0 : 1;
        }
        else if(s.charAt(i) == s.charAt(j) && dp[i+1][j-1] == 0) {
            dp[i][j] = 0;
        }
        else {
            int min = Integer.MAX_VALUE;
            for(int k = i; k < j; k++) {
                int lans = dp[i][k];
                int rans = dp[k+1][j];

                if(lans + rans < min) {
                    min = lans + rans;
                }
            }

            dp[i][j] = min + 1;
        }
    }
}

```

optimisation



$O(n^2)$

	a_0	b_1	c_2	c_3	b_4	c_5
a_0	T	F	F	F	F	F
b_1	α	T	F	F	T	F
c_2	α	α	T	T	F	F
c_3	α	α	α	T	F	T
b_4	α	α	α	α	T	F
c_5	α	α	α	α	α	T

a	b	c	c	b	c
2	1	1	0	1	0
0	1	2	3	4	5

$bccbc$
 a
 $abccbc$
 $||$
 $||$
 $||$
 $||$

$i \rightarrow$ i to end string
 min cut to make
 each part palindromic.

	a_0	b_1	c_2	c_3	b_4	c_5
a_0	T	F	F	F	F	F
b_1	T	T	F	F	T	F
c_2	T	T	T	T	F	F
c_3	T	T	T	T	F	T
b_4	T	T	T	T	T	F
c_5	T	T	T	T	T	T

$i \rightarrow$ i to end ss ans

a	b	c	c	b	c
2	<u>1</u>	<u>1</u>	0	<u>1</u>	0
0	1	2	3	4	5

abccbc bccbc ccbcc cbc bc c

```
int[] dp = new int[s.length()];
boolean[][] pal = longestPalSubstring(s);
```

```
//dp[i] -> i to end
dp[dp.length-1] = 0;
```

```
for(int i = dp.length-2; i >= 0; i--) {
    if(pal[i][s.length()-1] == true) {
        dp[i] = 0;
        continue;
    }

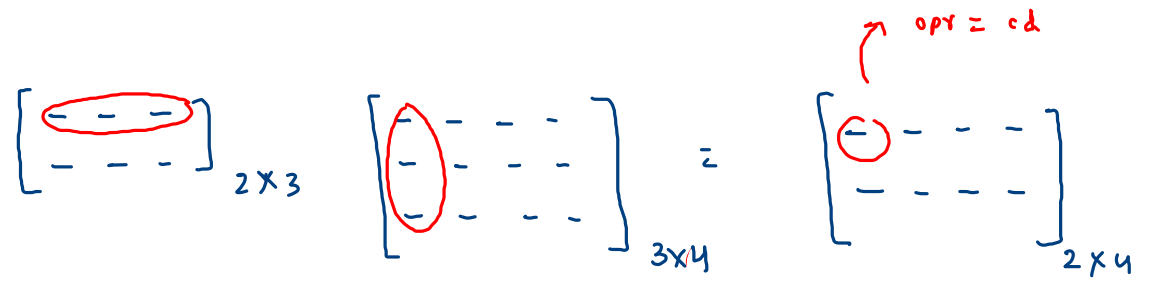
    int min = Integer.MAX_VALUE;

    //to select a valid prefix
    for(int k = i; k < dp.length-1; k++) {
        if(pal[i][k] == true) {
            min = Math.min(min, dp[k+1]);
        }
    }

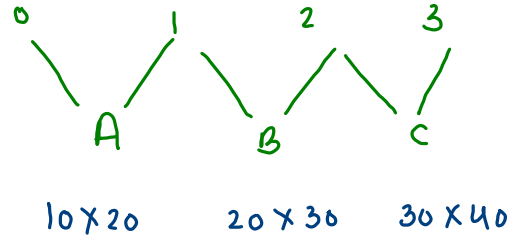
    dp[i] = min + 1;
}

return dp[0];
```

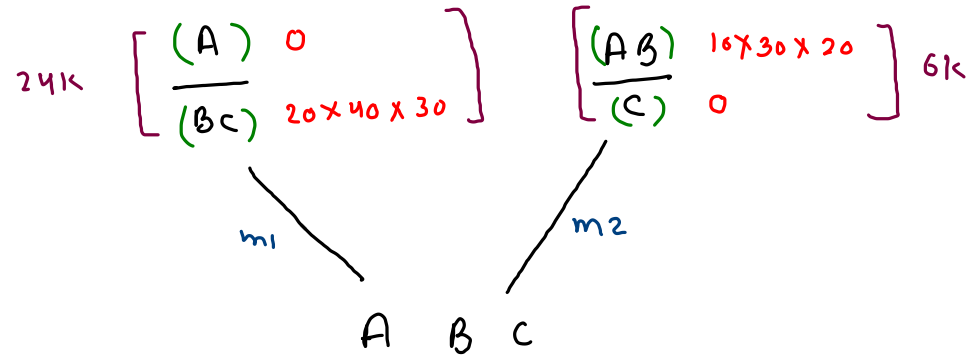
Matrix Chain Multiplication



10	20	30	40
----	----	----	----

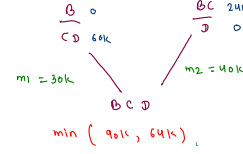
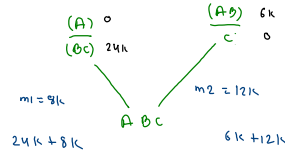
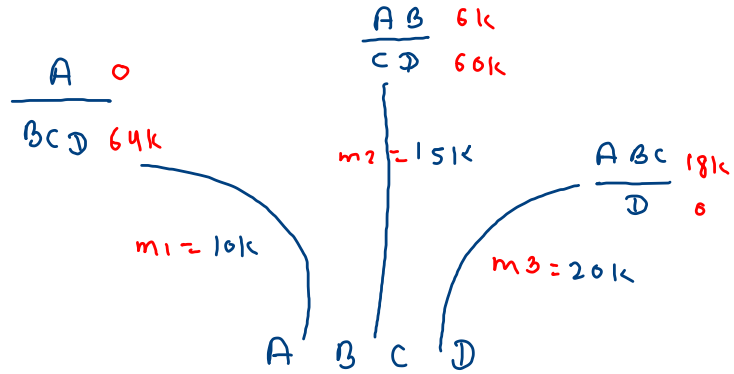
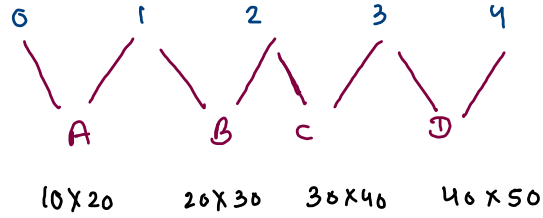


total opr = $2 \times 4 \times cd$



ans: $\min [(24k + m_1), (6k + m_2)]$

10	20	30	40	50
----	----	----	----	----



	A	B	C	D
A	0	6k	18k	38k
B	∞	0	24k	64k
C	∞	∞	0	60k
D	∞	∞	∞	0

$$A : 10 \times 20 \quad m_1 = 10 \times 20 \times 50 = 10k$$

$$BCD : 20 \times 50$$

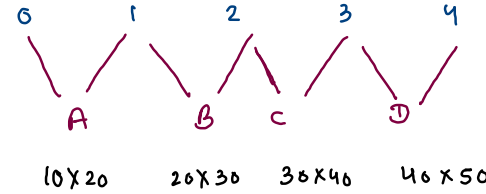
$$AB : 10 \times 30 \quad m_2 = 10 \times 30 \times 50 = 15k$$

$$CD : 30 \times 50$$

$$ABC : 10 \times 40 \quad m_3 = 10 \times 40 \times 50 = 20k$$

$$D : 40 \times 50$$

10	20	30	40	50
----	----	----	----	----



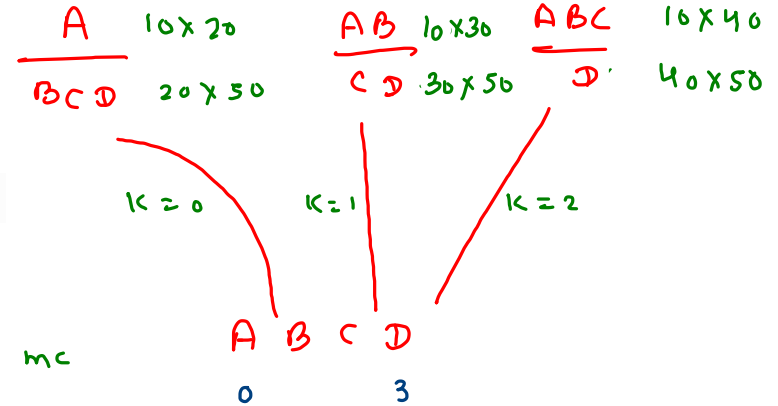
	10	20	30	40	50
	A ₀	B ₁	C ₂	D ₃	
10 A ₀	0	6k	18k	38k	
20 B ₁	×	0	24k	64k	
30 C ₂	×	×	0	60k	
40 D ₃	×	×	×	0	
50					

```

for(int k = i; k < j; k++) {
    int lans = dp[i][k];
    int rans = dp[k+1][j];

    int mc = ; //mult cost
    int cont = lans + rans + mc;
    min = Math.min(min, cont);
}

```



k = 0

lans + rans + mc
0 64k 10k

k = 1

6k 60k 15k

k = 2

18k 0 20k

Ad -> i x (k+1)

Ad -> (k+1) x (j+1)

Boolean Parenthesization

Input: $N = 7$

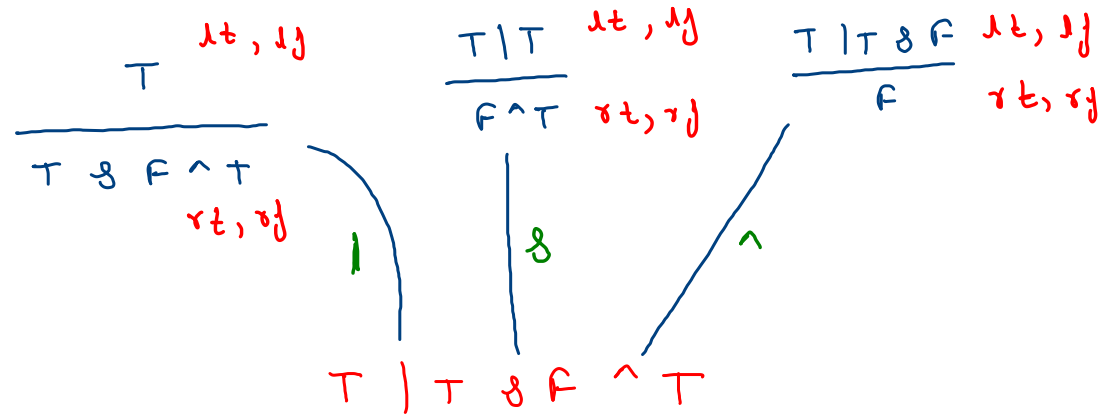
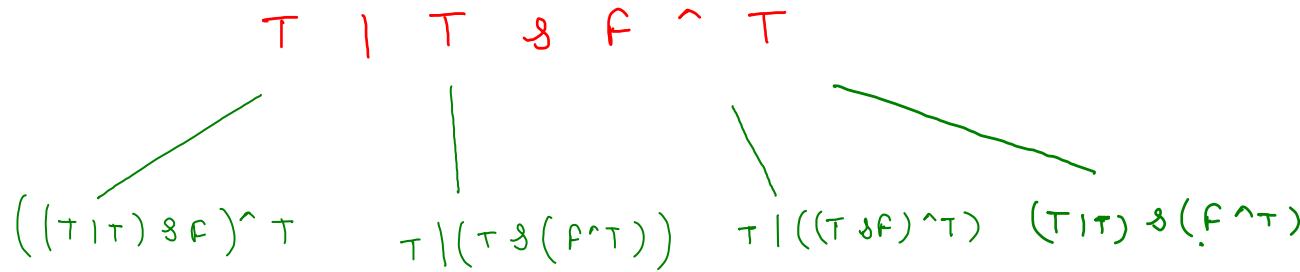
$S = T|T\&F\wedge T$

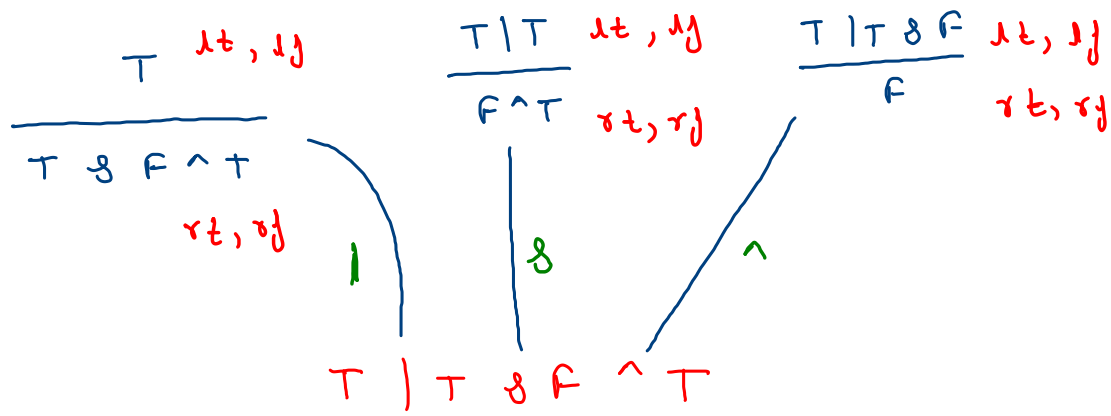
Output: 4

Explanation: The expression evaluates

to true in 4 ways $((T|T)\&(F\wedge T))$,

$(T|(T\&(F\wedge T)))$, $((T|(T\&F))\wedge T)$ and $(T|((T\&F)\wedge T))$.





interaction $\left[\begin{array}{l} (F \mid F \wedge T) \mid (F \wedge T \wedge F) \\ \wedge t = 2 \quad \wedge t = 2 \\ \wedge j = 0 \quad \wedge j = 0 \end{array} \right]$

opr	true count	false count
	$\wedge t * \wedge t + \wedge t * \wedge j + \wedge j * \wedge t$	$\wedge j * \wedge j$
\oplus	$\wedge t * \wedge t$	$\wedge t * \wedge j + \wedge j * \wedge t + \wedge j * \wedge j$
\wedge	$\wedge t * \wedge j + \wedge j * \wedge t$	$\wedge j * \wedge j + \wedge t * \wedge t$

ops	true count	false count
	$ut \times st + ut \times sj + uj \times st$	$uj \times sj$
&	$ut \times st$	$ut \times sj + uj \times st + uj \times sj$
^	$ut \times sj + uj \times st$	$uj \times sj + ut \times st$

(tc, fc)
pairs

	T	I	T	F	^	T
T	1,0	1,0	1,1	4,1		
I	α	1,0	0,1	2,0		
T	α	α	0,1	1,0		
F	α	α	α	1,0		
^	α	α	α	1,0		

T | T & F ^ T

S1 : T T F T

S2 : 1 8 ^

$\frac{T \quad ut=1, uj=0}{F \wedge T \quad st=1, sj=0} \quad \frac{T \wedge F \quad ut=0, uj=1}{T \quad st=1, sj=0}$

$t=1$
 $j=0$

$\left. \begin{array}{c} \text{)} \\ T \end{array} \right\} \text{ & } \left. \begin{array}{c} \text{)} \\ F \end{array} \right\} \text{ ^ } \left. \begin{array}{c} \text{)} \\ T \end{array} \right\} \quad t=1$
 $j=0$

$\hookrightarrow 2,0$