

→ we ~~get~~ get all values of \bar{n}_1 also by \bar{n}_1' but with different (y_1, Δ_1) pairs, if we want to fulfill the constraint $y_i \in \mathbb{N}$!

(I already showed (in other notes) that this is fulfilled.)

I will not repeat it here, but you can also easily check ~~this~~ this by yourself)

Assume ~~we~~ we have given:

$$(*) \quad \bar{n}_1 = (2x_1 + 1)y_1 - \Delta_1 \quad \Delta_1 \in \{1, \dots, 2x_1\}$$

→ Have, for example, a look at $(x_1 = 1)$:

$$\bar{n}_1 = 3y_1 - \Delta_1 \quad \Delta_1 \in \{1, 2\}$$

$$y_1 = 1: \quad \bar{n}_1 = \begin{cases} \Delta_1 = 1: 2 \\ \Delta_1 = 2: 1 \end{cases}$$

$$y_1 = 2:$$

$$\bar{n}_1 = \begin{cases} \Delta_1 = 1: 5 \\ \Delta_1 = 2: 4 \end{cases}$$

← We see: The number u_3^* is missing!

$$y_1 = 3:$$

$$\bar{n}_1 = \begin{cases} \Delta_1 = 1: 8 \\ \Delta_1 = 2: 7 \end{cases}$$

→ That's not what we want, since we want to find all prime numbers.

→ With this we will not get u_3^*

⇒ Our equation (*) is not usable (gives us not a valid range) for values ≤ 3 .

⇒ So it's just valid for $y_1 \geq 2$!

→ But... we already have to know u_3^* to generate this (*) equation, so the given number u_3^* comes from an earlier calculation step.

Now let's switch to (only odd solutions)

$$(**) \quad \bar{n}_1^o = (2x_1 + 1)(2y_1 + 1) - 2\Delta_1^o \quad \Delta_1^o \in \{1, \dots, 2x_1\}$$

$$u_1 \in \mathbb{N}$$