

VI

$$\bar{n}_1 = (2x_1 + 1)y_1 - \Delta_1$$

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→ We only need odd \bar{n} . $1, m \in \mathbb{N}$ (Eq. 14)

$$\Rightarrow \boxed{2m+1 = \bar{n}_1 = (2x_1+1)y_1 - \Delta_1} \text{ with } \Delta_1 \in \{1, \dots, 2x_1\}$$

We have different possibilities to rewrite the right side, to get the necessary numbers. We will choose the following:

$$2m+1 = \bar{n}_1 = (2x_1+1)(2k_1+1) - \Delta_1$$

$$= (y_1)$$

$$k_1 \in \mathbb{N}$$

→ we only have odd y_1 now.

$$\Rightarrow \Delta_1 \text{ has to be } 2l, l \in \mathbb{N}$$

⇒ So, be $\Delta_1^0 \in \{1, \dots, x_1\}$ but now (with only odd numbers) we have a doubled interval, so we have in real $\Delta_1^0 \in \{1, \dots, 2x_1\}$ again

It follows:

$$\boxed{2m+1 = \bar{n}_1^0 = (2x_1+1)(2k_1+1) - 2\Delta_1^0} \text{ with } \Delta_1^0 \in \{1, \dots, 2x_1\}$$

$$= (y_1^0) \quad (\text{Eq. 15})$$

$$\Rightarrow \bar{n}_1^0 = (2x_1+1)(2k_1+1) - 2\Delta_1^0 \cdot \Delta x_{112}$$

$$\bar{n}_2^0 = (2x_2+1)(2k_2+1) - 2\Delta_2^0 \cdot \Delta x_{112}$$

$$= (y_2^0)$$

$$\Rightarrow y_1^0 = (2k_1+1) = x_2 \cdot (-\Delta_2 + \Delta_1) + (2x_2+1)z_{112}$$

$$k_1 = \frac{1}{2} \left(x_2 (-\Delta_2 + \Delta_1) + (2x_2+1)z_{112} - 1 \right)$$

$$(2x_1+1)(2k_1+1) - 2\Delta_1^0 \cdot \Delta x_{112} = (2x_2+1)(2k_2+1) - 2\Delta_2^0 \cdot \Delta x_{112}$$

$$x_2 = x_1 + \Delta x_{112}$$

~~Now we can write~~

$$0 = (2(x_1 + \Delta x_{112}) + 1)(2k_2 + 1) - (2x_1 + 1)(2k_1 + 1) - 2\Delta_2^0 \cdot \Delta x_{112} + 2\Delta_1^0 \cdot \Delta x_{112}$$

$$\frac{1}{2} = (2x_1 + 1)(2k_2 + 1 - 2k_1 + 1) + 2\Delta x_{112}(2k_2 + 1) - (2\Delta_2^0 \Delta x_{112} + 2\Delta_1^0 \Delta x_{112})$$

$$= (2x_1 + 1)(k_2 - k_1 + 1) + \Delta x_{112}(2k_2 + 1) + \Delta x_{112}(-\Delta_2 + \Delta_1)$$