

(S3S)

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$$\Rightarrow \bar{n}_{123,4}' = (2x_1+1)(2x_2+1)(2x_3+1)(2x_4+1)z_{123,4} \\ + (2x_1+1)(2x_2+1)(2x_3+1)$$

$$\cdot \left\{ -\Delta_4 - (2x_1+1)(2x_2+1) \left\{ -\Delta_3 - (2x_1+1)(-\Delta_2+\Delta_1)x_2 \right. \right. \\ \left. \left. + \Delta x_{12} \Delta_1 \right\} x_3 \right. \\ \left. + \Delta x_{12,3} \left\{ - (2x_1+1)(-\Delta_2+\Delta_1)x_2 + \Delta x_{12} \Delta_1 \right\} \right\}$$

$$\cdot x_4$$

$$- \Delta x_{123,4} \cdot \left\{ - (2x_1+1)(2x_2+1) \left\{ -\Delta_3 - (2x_1+1)(-\Delta_2+\Delta_1)x_2 \right. \right. \\ \left. \left. + \Delta x_{12} \Delta_1 \right\} x_3 \right. \\ \left. + \Delta x_{12,3} \left\{ - (2x_1+1)(-\Delta_2+\Delta_1)x_2 + \Delta x_{12} \Delta_1 \right\} \right\}$$

... and so on.

Let's try to bring this in a more general solution...

We want a general ~~set~~ form of $\bar{n}_{123\dots,n}'$, $n \geq 2$, $n \in \mathbb{N}$
for the intersection of n -equations.

Part 1:

That's easy:

$$\textcircled{1} \quad \boxed{\text{We have } \bar{n}_{123\dots,n}' = \prod_{k=1}^n (2x_k+1) z_{12\dots n-1,n} + A}$$

Part 2: A ? That's much harder.

$$\textcircled{2} \quad \begin{array}{l} \text{S1S:} \\ (\bar{n}_{1,2}') \\ (n=2) \end{array} \quad A_{12} = (2x_1+1)(-\Delta_2+\Delta_1)x_2 - \Delta x_{12} \Delta_1 \\ = \prod_{e=1}^{n-1} (2x_e+1) \cdot \left\{ -\Delta_n + \Delta_{n-1} \right\} x_n + \Delta x_{12\dots n-1,n} \Delta_{n-1}$$

$$\begin{array}{l} \text{S2S} \\ (\bar{n}_{12,3}') \\ (n=3) \end{array} \quad A_{123} = \prod_{e=1}^{n-1} (2x_e+1) \left\{ -\Delta_n - \prod_{e=1}^{n-2} (2x_e+1) (-\Delta_{n-1} + \Delta_{n-2}) x_{n-1} \right. \\ \left. + \Delta x_{1\dots n-2,n-1} \Delta_{n-2} \right\} x_n \\ - \Delta x_{1\dots n-1,n} \left\{ - \prod_{e=1}^{n-2} (2x_e+1) (-\Delta_{n-1} + \Delta_{n-2}) x_{n-1} \right. \\ \left. + \Delta x_{1\dots n-2,n-1} \Delta_{n-2} \right\}$$