

$$0 = (2x_2 + 1)(2u_2 + 1) - 2\Delta x_{12}\Delta_2 \\ - (2x_1 + 1)(2u_1 + 1) + 2\Delta x_{12}\Delta_1$$

Be  $x_2 > x_1$   $x_1 = x_2 - \Delta x_{12}$  and  $(2x_2 + 1) = (2x_1 + 1)(2x'_1 + 1)$   
 ~~$(\Delta x_{12} = x_2 - x_1)$~~

or

$$(2x_1 + 1)(2u_1 + 1) = (2x_2 + 1)(2u_2 + 1) + 2\Delta x_{12}(-\Delta_2 + \Delta_1)$$

$$(2x_1 + 1)(2u_1 + 1) = (2x_1 + 1)(2x'_1 + 1)(2u_2 + 1) + 2\Delta x_{12}(-\Delta_2 + \Delta_1)$$

$$(2u_1 + 1) = (2x'_1 + 1)(2u_2 + 1) + \underbrace{2\Delta x_{12}(-\Delta_2 + \Delta_1)}_{\textcircled{1}}$$

$$\textcircled{1} = \frac{2 \cdot (x_2 - x_1)(-\Delta_2 + \Delta_1)}{2x_1 + 1}$$

$$= \frac{2 \cdot ((2x_1 + 1)(2x'_1 + 1) - 1) \frac{1}{2} - x_1(-\Delta_2 + \Delta_1)}{2x_1 + 1}$$

$$= \frac{((2x_1 + 1)(2x'_1 + 1) - 1 - 2x_1)(-\Delta_2 + \Delta_1)}{(2x_1 + 1)}$$

$$= \frac{(2x_1 + 1)(2x'_1 + 1)(-\Delta_2 + \Delta_1)}{(2x_1 + 1)} - \frac{(2x_1 + 1)(-\Delta_2 + \Delta_1)}{(2x_1 + 1)}$$

$$= (2x'_1 + 1)(-\Delta_2 + \Delta_1) - (-\Delta_2 + \Delta_1)$$

$$= (-\Delta_2 + \Delta_1)(2x'_1 + 1 - 1)$$

$$= (-\Delta_2 + \Delta_1) 2x'_1$$

$$\Rightarrow \boxed{2u_1 + 1 = (2x'_1 + 1)(2u_2 + 1) + (-\Delta_2 + \Delta_1) \cdot 2x'_1}$$

$$= 2x'_1 u_2 \cdot 2 + 2x'_1 + 2u_2 + 1 + (-\Delta_2 + \Delta_1) \cdot 2x'_1$$

$$2u_1 = 2x'_1 u_2 + 2x'_1 + 2u_2 + (-\Delta_2 + \Delta_1) \cdot 2x'_1$$

$$\boxed{u_1 = 2x'_1 u_2 + x'_1 + u_2 + (-\Delta_2 + \Delta_1)x'_1}$$

$$\boxed{u_1 = \underbrace{2x'_1 u_2 + u_2}_{(2x'_1 + 1)u_2} + (-\Delta_2 + \Delta_1 + 1)x'_1}$$