

## ECSE 420 Assignment 2

### Group 16

Student1 : Erdong Luo  
ID: 260778475

Student2 : Sameen Mahtab  
ID: 260737048

#### Q1

- 1.1 See Filter.java
- 1.2 Yes, Filter allows some threads to overtake others an arbitrary number of times. There is concept called bounded waiting.  $r$ -bounded waiting implies that a thread cannot overtake another thread more than  $r$  times. But for filter algorithm, there is no value for " $r$ ". This means a thread can be arbitrarily overtaken.

**Answer: there is no value of " $r$ "**

- 1.3 See BakeryLock.java
- 1.4 The bakery algorithm does not allow for a thread to overtake another thread an arbitrary number of times. Bakery algorithm provides first-come-first-served for  $n$  threads. A first-come-first-served has  $r = 0$ . This means no thread can overtake another.
- 1.5 We can create a pool of threads. (the number of threads should be larger than 5). Every time, a thread enters the critical section, other threads should not be able to lock. Or mutual exclusion is failed.
- 1.6
  - Thread 10 acquire Lock
  - Thread 11 acquire Lock
  - Thread 12 acquire Lock
  - Thread 14 acquire Lock
  - Thread 13 acquire Lock
  - Thread 11 Hold Lock
  - Thread 11 Release lock
  - Thread 12 Hold Lock
  - Thread 12 Release lock
  - Thread 13 Hold Lock
  - Thread 13 Release lock
  - Thread 10 Hold Lock
  - Thread 10 Release lock
  - Thread 14 Hold Lock
  - Thread 14 Release lock

It provide mutual exclusion.

## Q2:

Yes, LockOne and LockTwo satisfy two-thread mutual exclusion when “flag” and “victim” are replaced by regular registers.

In an atomic register, read() will always return the last written value. In a regular register however, if a read overlaps a write then it may return that written value, or possibly the previous one.

```
1 class LockOne implements Lock {
2     private boolean[] flag = new boolean[2];
3     // thread-local index, 0 or 1
4     public void lock() {
5         int i = ThreadID.get();
6         int j = 1 - i;
7         flag[i] = true;
8         while (flag[j]) {} // wait
9     }
10    public void unlock() {
11        int i = ThreadID.get();
12        flag[i] = false;
13    }
14 }
```

Figure 2.4 The LockOne algorithm.

For example, let's say we have two threads (A and B). For the 'flickering' to occur, then flag[A] must be read and written in an overlapping fashion, or the same must occur for flag[B]. This means that flag[A] must be written to true by thread A and simultaneously, Thread[B] must read the value. If the old value is read, then B will enter its critical section. However, when the write is completed, then B will eventually enter its critical section. Also, since flag[B] is already set to true, thread A will not be able to enter its critical section and mutual exclusion will not be violated. If the new value of flag[A] is read, then B will not enter its critical section and for the same reason as stated above, A will not be able to e

```
1 class LockTwo implements Lock {
2     private int victim;
3     public void lock() {
4         int i = ThreadID.get();
5         victim = i; // let the other go first
6         while (victim == i) {} // wait
7     }
8     public void unlock() {}
9 }
```

Figure 2.5 The LockTwo algorithm.

If A marks itself as the victim and B reads victim, then B will not enter its critical section as it believes that it is the victim (reading old value). Once A finishes writing, in a subsequent read, B will be able to enter its critical section. A will not be able to enter its critical section as it has set itself as the victim. Therefore mutual exclusion is satisfied. If B reads the new value, then the algorithm works as expected so mutual exclusion is satisfied.

## Q3:

3.1

Suppose there are two threads, thread A and thread B. Both of them want to enter the critical section at the same time. Without the loss of generality, we assume that A arrive first. When A arrived, "busy" must have been set to true. When B arrives, turn is set to B, and since busy is true, B will be stuck in its while loop. So, if B want to enter the critical section, the busy flag must have been set to false. One of the thread A or B must have called unlock (). This is contradicting to our assumption.

### 3.2

Concurrent executions will not experience deadlock because as soon as a new thread enters, it will set *turn* to its *ThreadID*, allowing another thread to break out of the *while* loop.

However sequential executions can experience deadlock. This is because *turn* will never be changed to another *ThreadID*, hence the initial thread will stay in the while loop while the other thread is waiting for it to exit.

### 3.3

It is not starvation-free. Assume that a thread A is in the critical section and all the other threads are in the while loop (**while** ( turn = me || busy); ). When A exits the critical section and unlock, there should be another thread entering the critical section. But there isn't a way to select the next thread, thus causing starvation.

## Q4

**4.1.** History (a) is sequentially consistent in the following order of execution:

A: r.write(0)  
B: r.write(1)  
A: r.read(1)  
A: r.write(2)  
B: r.read(2)  
C: r.read(2)  
C: r.write(3)

History (a) is not linearizable. C: r.write(3) happens before B: r.read(2) and C: r.write(3) might happen before A: r.write(2) so B: r.read(2) cannot execute properly. Flattening the 3 lines will not produce a sequential execution.

History (b) is not sequentially consistent. B: r.write(1) has to occur before B: r.read(2) and C: r.write(2) has to occur after B: r.write(1) and before B: r.read(2) and C: r.read(1).

For B: r.read(2) we need the sequence:

B: r.write(1)  
C: r.write(2)  
B: r.read(2)

For C: r.read(1) we need the sequence:

C: r.write(2)  
B: r.write(1)  
C: r.read(1)

But the above two sequences are contradictory. B: r.write(1) will be overwritten by C: r.write(2) so C: r.read(1) cannot happen.

Since sequence (b) is not sequentially consistent it is also not linearizable.

#### Q5:

**5.1.** In this class, `v` is a volatile boolean. This means that the value of `v` is written to and read from main memory. If thread A changes both `v` and `x`, thread B will only be able to see the change to `v`. If thread A calls `writer()` it will set `x` to 42 and `v` to true, the change to `x` this is not visible to thread B.

After that, if thread B calls `reader()` method without calling `writer()`, it will have `v` as true but `x` will remain 0. So the reader method will divide by 0.

**5.2.** Division by 0 will not occur if both `v` and `x` are volatile. If thread A calls `writer()` and then thread B calls `reader()`, both of the updated values of `v` and `x` will be visible to thread B.

If neither are volatile, division by 0 might occur. JVM does not guarantee that the variables will be updated in sequence, as a result, `v` might be updated first by thread A and then thread A might be interrupted by thread B before setting `x` to 42. And then if thread B calls `reader()` without calling `writer()`, there will be a division by 0.

#### Q6:

**6.1.** Changing the loop at line 11 will cause the `read()` method to work incorrectly as the `write()` method will not update the lower bits. The values after `x` will be false. For instance, if we have two subsequent `write()` operations, since `read()` returns values of the lowest index, every subsequent `read()` will only return the value of the first write and will not return the second write. The construction will not remain a *regular* M-valued MRSW register.

**6.2.** Similar to 6.1, changing the loop at line 11 means that the `write()` method will not update the lower bits. The values after `x` will be set to false. As `r_bit[0]` is initialized as true, the `read()` method will keep on returning 0. The construction will not yield a *safe* M-valued MRSW register.

**7:** Supposing there exists a protocol for binary consensus using atomic registers for  $n$  threads. A two-thread binary consensus protocol can be made by having  $n=2$ ; 2 of the threads to progress, the remaining threads to hold. This brings forth the contradiction that: two-thread binary consensus is impossible. Hence, binary consensus is also impossible for  $n$ -threads.

**8:** Supposing that there exists a protocol for consensus over  $k$  values. One value could be mapped to 1 and the other to 0, the consensus protocol will be reduced to binary values and will serve as a binary consensus protocol. This brings forth the contradiction that: binary consensus is impossible. Hence, consensus over  $k$ -values is impossible.