

## 03: Exploring Data Structures

*Aug 23, 2023.*

The R programming language includes a number of data structures that are frequently employed in data analysis and statistical modeling. These are some of the most popular data structures in R:

1. **Vector:** A vector is a one-dimensional array that stores identical data types, such as numeric, character, or logical. The `c()` function can be used to create vectors, and indexing can be used to access individual vector elements.
2. **Factor:** A factor is a vector representing **categorical** data, with each distinct value or category represented as a level. Using indexing, individual levels of a factor can be accessed using the `factor()` function.
3. **Dataframe:** A data frame is a two-dimensional table-like structure similar to a spreadsheet, that can store various types of data in columns. The `data.frame()` function can be used to construct data frames, and individual elements can be accessed using row and column indexing.
4. **Matrix:** A matrix is a two-dimensional array of data with identical rows and columns. The `matrix()` function can be used to construct matrices, and individual elements can be accessed using row and column indexing.
5. **Array:** An array is a multidimensional data structure that can contain data of the same data type in user-specified dimensions. Arrays can be constructed using the `array()` function, and elements can be accessed using multiple indexing.
6. **List:** A list is an object that may comprise elements of various data types, including vectors, matrices, data frames, and even other lists. The `list()` function can be used to construct lists, while indexing can be used to access individual elements.

These data structures are helpful for storing and manipulating data in R, and they can be utilized in numerous applications, such as statistical analysis and data visualization. We will focus our attention on Vectors, Factors and Dataframes, since we believe that these are the three most useful data structures. [1]

## Vectors

1. A vector is a fundamental data structure in R that can hold a sequence of values of the same data type, such as integers, numeric, character, or logical values.
2. A vector can be created using the `c()` function.
3. R supports two forms of vectors: atomic vectors and lists. Atomic vectors are limited to containing elements of a single data type, such as numeric or character. Lists, on the other hand, can contain elements of various data types and structures. [1]

## Vectors in R

1. The following R code creates a numeric vector, a character vector and a logical vector respectively.

```
# Read data into vectors
names <- c("Ashok", "Bullu", "Charu", "Divya")
ages <- c(72, 49, 46, 42)
weights <- c(65, 62, 54, 51)
income <- c(-2, 8, 19, 60)
females <- c(FALSE, TRUE, TRUE, TRUE)
```

2. The `c()` function is employed to combine the four character elements into a single vector.
3. Commas separate the elements of the vector within the parentheses.
4. Individual elements of the vector can be accessed via indexing, which utilizes square brackets `[]`. For instance, `names[1]` returns `Ashok`, while `names[3]` returns `Charu`.
5. We can also perform operations such as categorizing and filtering on the entire vector. For instance, `sort(names)` returns a vector of sorted names, whereas `names[names != "Bullu"]` returns a vector of names excluding `Bullu`.

## Vector Operations

Vectors can be used to perform the following vector operations:

1. **Accessing Elements:** We can use indexing with square brackets to access individual elements of a vector. To access the second element of the `names` vector, for instance, we can use:

```
names[2]
```

```
[1] "Bullu"
```

- This returns Bullu, the second element of the `people` vector.
2. **Concatenation:** The `c()` function can be used to combine multiple vectors into a single vector. For instance, to combine the `names` and `ages` vectors into the “people” vector, we can use:

```
persons <- c(names, ages)
persons
```

```
[1] "Ashok" "Bullu" "Charu" "Divya" "72"    "49"    "46"    "42"
```

- This generates an eight-element vector containing the names and ages of the four people.
3. **Subsetting:** We can use indexing with a logical condition to construct a new vector that contains a subset of elements from an existing vector. For instance, to construct a new vector named `female_names` containing only the female names, we can use:

```
female_names <- names[females == TRUE]
female_names
```

```
[1] "Bullu" "Charu" "Divya"
```

- This generates a new vector comprising three elements containing the names of the three females Bullu, Charu, and Divya.
4. **Arithmetic Operations:** We can perform element-wise arithmetic operations on vectors.

```
# Addition
addition <- ages + weights
print(addition)
```

```
[1] 137 111 100 93
```

```
# Subtraction
subtraction <- ages - weights
print(subtraction)
```

```
[1] 7 -13 -8 -9
```

```
# Multiplication
multiplication <- ages * weights
print(multiplication)
```

```
[1] 4680 3038 2484 2142
```

```
# Division
division <- ages / weights
print(division)
```

```
[1] 1.1076923 0.7903226 0.8518519 0.8235294
```

```
# Exponentiation
exponentiation <- ages^2
print(exponentiation)
```

```
[1] 5184 2401 2116 1764
```

- We perform addition, subtraction, multiplication, division, and exponentiation on these vectors using the arithmetic operators `+`, `-`, `*`, `/`, and `^` respectively.
- R also supports other arithmetic operations such as modulus, integer division, and absolute value:

```
# Modulus
modulus <- ages %% income
print(modulus)
```

```
[1] 0 1 8 42
```

```
# Integer Division
integer_division <- ages %/% income
print(integer_division)
```

```
[1] -36 6 2 0
```

```
# Absolute Value
absolute_value <- abs(ages)
print(absolute_value)
```

```
[1] 72 49 46 42
```

- R also supports additional arithmetic operations:

```
# Floor Division
floor_division <- floor(ages / income)
print(floor_division)
```

```
[1] -36 6 2 0
```

- `floor` calculates the largest integer not exceeding the quotient.

```
# Ceiling Division
ceiling_division <- ceiling(ages / income)
print(ceiling_division)
```

```
[1] -36 7 3 1
```

- `ceiling` calculates the smallest integer not less than the quotient.

```
# Logarithm
logarithm <- log(ages)
print(logarithm)
```

```
[1] 4.276666 3.891820 3.828641 3.737670
```

- `log` calculates the natural logarithm of each element.

```
# Square Root
square_root <- sqrt(ages)
print(square_root)
```

```
[1] 8.485281 7.000000 6.782330 6.480741
```

- `sqrt` calculates the square root of all the elements.

```
# Sum
sum_total <- sum(ages)
print(sum_total)
```

```
[1] 209
```

- `sum` calculates the sum of all the elements.

5. **Logical Operations:** We can perform logical operations on vectors, which are also executed element-by-element.

```
# Equality comparison
age_equal_46 <- (ages == 46)
print(age_equal_46)
```

```
[1] FALSE FALSE TRUE FALSE
```

- **Equality Comparison (`==`):** It checks if the elements of the `ages` vector are equal to 46. The resulting vector, `age_equal_46`, contains `TRUE` for elements that are equal to 46 and `FALSE` otherwise.

```
# Inequality comparison
weight_not_equal_54 <- (weights != 54)
print(weight_not_equal_54)
```

```
[1] TRUE TRUE FALSE TRUE
```

- **Inequality Comparison (`!=`):** It checks if the elements of the `weights` vector are not equal to 54. The resulting vector, `weight_not_equal_54`, contains `TRUE` for elements that are not equal to 54 and `FALSE` otherwise.

```
# Greater than Comparison
weight_greaterthan_50 <- (weights > 50)
print(weight_greaterthan_50)
```

```
[1] TRUE TRUE TRUE TRUE
```

- **Greater than Comparison (`>`):** It checks if each element of the `ages` vector is greater than 50. The resulting vector, `age_greater_50`, contains `TRUE` for elements that satisfy the condition and `FALSE` otherwise.

```
# Less than or Equal to Comparison
weight_lessthan_54 <- (weights <= 54)
print(weight_lessthan_54)
```

```
[1] FALSE FALSE TRUE TRUE
```

- **Less than or Equal to Comparison ( $\leq$ ):** It checks if each element of the weights vector is less than or equal to 54. The resulting vector, `weight_less_equal_54`, contains TRUE for elements that satisfy the condition and FALSE otherwise.

```
# Logical AND
female_and_income <- females & (income > 0)
print(female_and_income)
```

```
[1] FALSE TRUE TRUE TRUE
```

- **Logical AND ( $\&$ ):** It performs a logical AND operation between the females vector and the condition (`income > 0`). The resulting vector, `female_and_income`, contains TRUE for elements that satisfy both conditions and FALSE otherwise.

```
# Logical OR
age_or_weight_greater_50 <- (ages > 50) | (weights > 50)
print(age_or_weight_greater_50)
```

```
[1] TRUE TRUE TRUE TRUE
```

- **Logical OR ( $\mid$ ):** It performs a logical OR operation between the conditions (`ages > 50`) and (`weights > 50`). The resulting vector, `age_or_weight_greater_50`, contains TRUE for elements that satisfy either condition or both.

```
# Logical NOT
not_female <- !females
print(not_female)
```

```
[1] TRUE FALSE FALSE FALSE
```

- **Logical NOT (!):** It negates the values in the females vector. The resulting vector, `not_female`, contains TRUE for elements that were originally FALSE and FALSE for elements that were originally TRUE.

```
# Negation
not_female <- !females
print(not_female)
```

```
[1] TRUE FALSE FALSE FALSE
```

- **Negation (!):** It negates the values in the females vector. The resulting vector, not\_female, contains TRUE for elements that were originally FALSE and FALSE for elements that were originally TRUE.

```
# Any True
any_age_greater_50 <- any(ages > 50)
print(any_age_greater_50)
```

```
[1] TRUE
```

- **Any True (any()):** It checks if there is at least one TRUE value in the logical vector ages > 50. The result, any\_age\_greater\_50, is TRUE if at least one element in ages is greater than 50 and FALSE otherwise.

```
# All True
all_income_positive <- all(income > 0)
print(all_income_positive)
```

```
[1] FALSE
```

- **All True (all()):** It checks if all elements in the logical vector income > 0 are TRUE. The result, all\_income\_positive, is TRUE if all values in the income vector are greater than 0 and FALSE otherwise.

```
# Subset with Logical Vector
female_names <- names[females]
print(female_names)
```

```
[1] "Bullu" "Charu" "Divya"
```

- **Subset with Logical Vector:** It uses a logical vector females to subset the names vector. The resulting vector, female\_names, contains only the names where the corresponding element in females is TRUE.



```
# Combined Logical Operation
combined_condition <- (ages > 50 & weights <= 54) | (income > 0 & females)
print(combined_condition)
```

```
[1] FALSE TRUE TRUE TRUE
```

- **Combined Logical Operation:** It combines multiple conditions using logical AND (&) and logical OR (|). The resulting vector, `combined_condition`, contains TRUE for elements that satisfy the combined condition and FALSE otherwise.

```
# Logical Function anyNA()
has_na <- anyNA(names)
print(has_na)
```

```
[1] FALSE
```

- **Logical Function anyNA():** It checks if there are any missing values (NA) in the `names` vector. The result, `has_na`, is TRUE if there is at least one NA value and FALSE otherwise.

```
# Logical Function is.na()
is_na <- is.na(ages)
print(is_na)
```

```
[1] FALSE FALSE FALSE FALSE
```

- **Logical Function is.na():** It checks if each element of the `ages` vector is NA. The resulting vector, `is_na`, contains TRUE for elements that are NA and FALSE otherwise.

```
# Finding unique values
unique(ages)
```

```
[1] 72 49 46 42
```

- **unique():** It finds the unique values in the `ages` vector
6. **Sorting:** We can sort a vector in ascending or descending order using the `sort()` function. For example, to sort the `ages` vector in descending order, we can use:

```
# Sort in ascending order
sorted_names <- sort(names)
print(sorted_names)
```

```
[1] "Ashok" "Bullu" "Charu" "Divya"
```

```
# Sort in descending order
sorted_names_desc <- sort(names, decreasing = TRUE)
print(sorted_names_desc)
```

```
[1] "Divya" "Charu" "Bullu" "Ashok"
```

In the above code, we demonstrate sorting the names vector in both ascending and descending order using the `sort()` function. By default, `sort()` sorts the vector in ascending order. To sort in descending order, we set the `decreasing` argument to `TRUE`.

## Statistical Operations on Vectors

1. **Length:** The length represents the count of the number of elements in a vector.

```
length(ages)
```

```
[1] 4
```

2. **Maximum** and **Minimum:** The maximum and minimum values are the vector's greatest and smallest values, respectively.
3. **Range:** The range is a measure of the spread that represents the difference between the maximum and minimum values in a vector.

```
min(ages)
```

```
[1] 42
```

```
max(ages)
```

```
[1] 72
```

```
range(ages)
```

```
[1] 42 72
```

4. **Mean:** The mean is a central tendency measure that represents the average value of a vector's elements.
5. **Standard Deviation:** The standard deviation is a measure of dispersion that reflects the amount of variation in a vector's elements.

```
mean(ages)
```

```
[1] 52.25
```

```
sd(ages)
```

```
[1] 13.47529
```

6. **Median:** The median is a measure of central tendency that represents the middle value of a sorted vector.

```
median(ages)
```

```
[1] 47.5
```

7. **Quantiles:** The quantiles are a set of cut-off points that divide a sorted vector into equal-sized groups.

```
quantile(ages)
```

```
0%    25%    50%    75%   100%  
42.00 45.00 47.50 54.75 72.00
```

This will return a set of five values, representing the minimum, first quartile, median, third quartile, and maximum of the four ages.

8. **Standard Error of the Mean:** It calculates the standard error of the mean for the ages vector. The result is stored in `se_ages`.

```
# Standard Error of the Mean
se_ages <- sqrt(var(ages) / length(ages))
print(se_ages)
```

```
[1] 6.737643
```

9. **Cumulative Sum:** It calculates the cumulative sum of the elements in the ages vector. The cumulative sum is stored in `cumulative_sum_ages`.

```
# Cumulative Sum
cumulative_sum_ages <- cumsum(ages)
print(cumulative_sum_ages)
```

```
[1] 72 121 167 209
```

10. **Correlation Coefficient:** It calculates the correlation coefficient between the ages and females vectors using the `cor()` function. T

```
# Correlation Coefficient
correlation_ages_females <- cor(ages, females)
print(correlation_ages_females)
```

```
[1] -0.9770974
```

Thus, we note that the R programming language provides a wide range of statistical operations that can be performed on vectors for data analysis and modeling. Vectors are clearly a potent and versatile data structure that can be utilized in a variety of ways.

## Strings

Here are some common string operations that can be conducted using the provided vector examples.

1. **Substring:** The `substr()` function can be used to extract a substring from a character vector. To extract the first three characters of each name in the “names” vector, for instance, we can use:

```
substring_names <- substr(names, start = 2, stop = 4)
print(substring_names)
```

```
[1] "sho" "ull" "har" "ivy"
```

This returns a new character vector containing three letters of each name.

2. **Concatenation:** Using the `paste()` function, we can concatenate two or more character vectors into a singular vector. To create a new vector containing the names and ages of the individuals, for instance, we can use:

```
persons <- paste(names, ages)
print(persons)
```

```
[1] "Ashok 72" "Bullu 49" "Charu 46" "Divya 42"
```

```
full_names <- paste(names, "Kumar")
print(full_names)
```

```
[1] "Ashok Kumar" "Bullu Kumar" "Charu Kumar" "Divya Kumar"
```

This will generate a new eight-element character vector containing the name and age of each individual, separated by a space.

3. **Case Conversion:** The `toupper()` and `tolower()` functions can be used to convert the case of characters within a character vector. To convert the “names” vector to uppercase letters, for instance, we can use:

```
toupper(names)
```

```
[1] "ASHOK" "BULLU" "CHARU" "DIVYA"
```

This will generate a new character vector with all of the names converted to uppercase.

4. **Pattern Matching:** Using the `grep()` function, we can search for a pattern within the elements of a character vector.

- To find the names in the “names” vector that contain the letter “a”, for instance, we can write the following code, which returns a vector containing the indexes of the “names” vector elements that contain the letter “a”:

```
grep("a", names)
```

```
[1] 3 4
```

- The following code returns the text of the “names” vector elements that contain the letter “a”:

```
pattern_match <- grep("l", names, value = TRUE)
print(pattern_match)
```

```
[1] "Bullu"
```

5. **String Length::** The `nchar()` function can be used to find the length of a string.

```
# Length of Strings
name_lengths <- nchar(names)
print(name_lengths)
```

```
[1] 5 5 5 5
```

6. **%in% Operator:** It checks if each element in the names vector is present in the specified set of names.

- In this example, the resulting vector, `names_found`, contains `TRUE` for elements that are found in the set and `FALSE` otherwise.

```
# %in% Operator
names_found <- names %in% c("Ashok", "Charu")
print(names_found)
```

```
[1] TRUE FALSE TRUE FALSE
```

7. **Logical Function ifelse():** It evaluates a logical condition and returns values based on the condition.

- In this example, we use `ifelse()` to assign the value “Old” to elements in the `age_category` vector where the corresponding element in `ages` is greater than 50, and “Young” otherwise.

```
# Logical Function ifelse()
age_category <- ifelse(ages > 50, "Old", "Young")
print(age_category)
```

```
[1] "Old"    "Young" "Young" "Young"
```

## Summary of Chapter 3 – Data Structures in R

Chapter 3 navigates through the fundamental data structure in R, the vector, and elucidates various operations that can be conducted on vectors. Vectors in R, either numeric, character, or logical, hold elements of the same type and are instrumental in performing computations and managing data.

The chapter delves into creating vectors with the `c()` function and applying mathematical operations like addition, subtraction, multiplication, division, exponentiation, and modulus on numeric vectors. It further explains how character vectors can be created, inspected, and manipulated, demonstrating through examples how to alter character case, extract substrings, and concatenate strings.

A key focus of the chapter is on logical vectors and operations such as equality, inequality, greater than, less than, and logical negation. It illustrates how these can be applied to vectors to create conditions and filter data, with functions such as `any()`, `all()`, and `ifelse()`. The discussion expands on how logical vectors are used to subset data, and how the `%in%` operator and `is.na()` function operate.

The chapter presents statistical operations on vectors, describing functions to compute length, maximum and minimum values, range, mean, median, standard deviation, and quantiles. Other functionalities like standard error of the mean, cumulative sum, and correlation coefficient are also discussed.

Towards the end, the chapter discusses the usage of strings in vectors, covering operations such as substring extraction, concatenation, case conversion, and pattern matching. It finally introduces the `nchar()` function to determine the length of strings in a vector.

In essence, Chapter 3 provides a practical exploration of vectors in R, shedding light on their creation, manipulation, and utilization in various operations, from basic mathematical computations to complex statistical functions and string operations. It underscores the versatility of vectors as a vital data structure in R for data analysis and modeling. Further exploration is encouraged with a comprehensive list of references.

## References

[1] R Core Team. (2021). R: A Language and Environment for Statistical Computing. R Foundation for Statistical Computing. <https://www.R-project.org/>

R Core Team. (2022). Vectors, Lists, and Arrays. R Documentation. <https://cran.r-project.org/doc/manuals/r-release/R-intro.html#vectors-lists-and-arrays>