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ASSIGNMENT-1

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Question: Suppose the equation of AB,BC and CA are respectively given by

$$\mathbf{n}_i^{\mathsf{T}} \mathbf{x} = c_i \qquad i = 1, 2, 3. \tag{1}$$

The equation of respective angle bisector are then given by

$$\frac{\mathbf{n}_{i}^{\mathsf{T}}\mathbf{x} - c_{i}}{\|\mathbf{n}_{i}\|} = \pm \frac{\mathbf{n}_{j}^{\mathsf{T}}\mathbf{x} - c_{j}}{\|\mathbf{n}_{j}\|} \qquad i \neq j$$
 (2)

Substitute numerical values and find the equations of the angle bisectors of A, B and C.

Solution: Using the equation (1) to calculate the normal equations of AB,BC and CA:

$$AB : \mathbf{n}_1^{\mathsf{T}} \mathbf{x} - c_1 = (7.5) \mathbf{x} - 2 = 0,$$
 (3)

$$BC : \mathbf{n}_2^{\mathsf{T}} \mathbf{x} - c_2 = (11\ 1)\mathbf{x} + 38 = 0, \quad (4)$$

$$CA: \mathbf{n}_3^{\mathsf{T}} \mathbf{x} - c_3 = (1 - 1)\mathbf{x} - 2 \qquad = 0, \quad (5)$$

Using the equation (2)to calculate the angle bisector of angle C:-

$$\frac{\mathbf{n}_{i}^{\mathsf{T}}\mathbf{x} - c_{i}}{\|\mathbf{n}_{i}\|} = \pm \frac{\mathbf{n}_{j}^{\mathsf{T}}\mathbf{x} - c_{j}}{\|\mathbf{n}_{j}\|}$$
(6)

Internal angular bisector can be evaluated by taking '+' sign in the above equation. Taking i=2 and j=3:-

$$\frac{\mathbf{n}_2^{\mathsf{T}}\mathbf{x} - c_2}{\|\mathbf{n}_2\|} = \frac{\mathbf{n}_3^{\mathsf{T}}\mathbf{x} - c_3}{\|\mathbf{n}_3\|}$$
(7)

$$\frac{\left(11\ 1\right)\mathbf{x} + 38}{\sqrt{\mathbf{n}_{2}^{\mathsf{T}}\mathbf{n}_{2}}} = \frac{\left(1\ - 1\right)\mathbf{x} - 2}{\sqrt{\mathbf{n}_{3}^{\mathsf{T}}\mathbf{n}_{3}}} \tag{8}$$

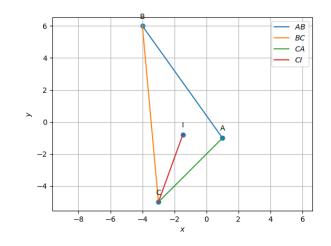


Fig. 0. Triangle generated using python

$$\implies \frac{\left(11\ 1\right)\mathbf{x} + 38}{\sqrt{\left(11\ 1\right)\left(\frac{11}{1}\right)}} = \frac{\left(1\ - 1\right)\mathbf{x} - 2}{\sqrt{\left(1\ - 1\right)\left(\frac{1}{-1}\right)}}$$

$$\implies \frac{(11\ 1)\mathbf{x}}{\sqrt{122}} - \frac{(1\ -1)\mathbf{x}}{\sqrt{2}} = \frac{-2}{\sqrt{2}} - \frac{38}{\sqrt{122}}$$
 (10)

$$\implies \left(\frac{11 - \sqrt{61}}{\sqrt{122}} \frac{1 + \sqrt{61}}{\sqrt{122}}\right) \mathbf{x} = -\frac{2\sqrt{61} + 38}{\sqrt{122}} \tag{11}$$

Hence, the equation (11) is the equation of internal angular bisector of angle C.