

BERNOULLI DISTRIBUTION

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BERNOULLI DISTRIBUTION OVERVIEW

The Bernoulli distribution is a discrete distribution for a single trial with two possible outcomes: success (1) and failure (0).

Parameters

- p : Probability of success.
- $1 - p$: Probability of failure.

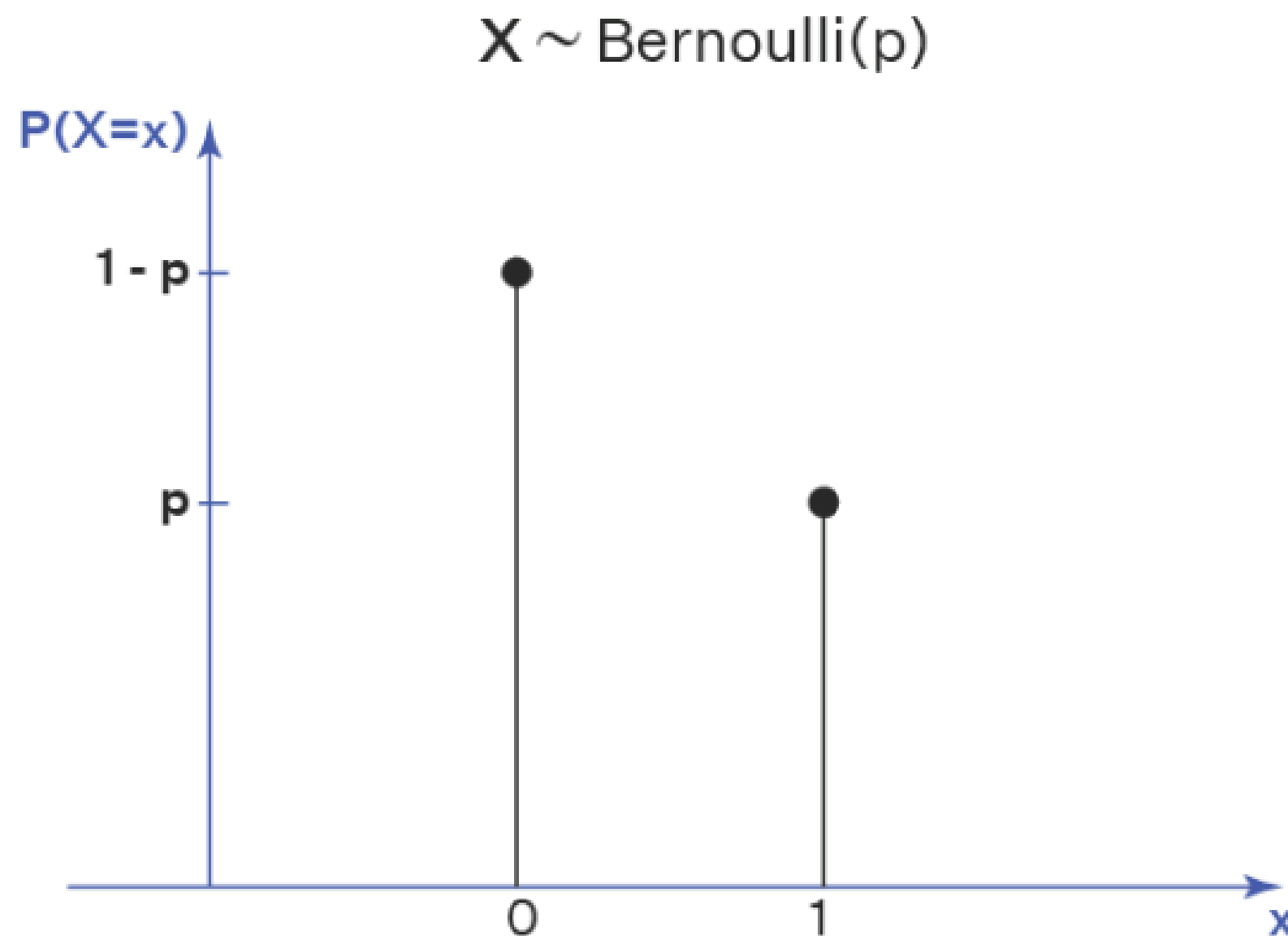
Example

- Flipping a coin once ($p = 0.5$).

Real-world Applications

- A single marketing call being successful or not.
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BERNOULLI DISTRIBUTION OVERVIEW



THE GRAPH SHOWS THAT THE
PROBABILITY
OF SUCCESS IS p
WHEN $x = 1$
AND THE PROBABILITY OF
FAILURE OF x
IS $(1 - p)$ OR q IF $x = 0$.



CHARACTERISTICS AND FORMULA

Key Characteristics:

- Special case of the Binomial distribution with a single trial.
- Mean = p
- Variance = $p(1 - p)$

Formula

- $P(X = x) = p^x (1 - p)^{1 - x}$, where $x \in \{0, 1\}$



EXAMPLE

Consider a coin flip experiment where the probability of landing heads (success) is 0.7. Using the Bernoulli distribution formula

Probability of getting heads (success)

Success
0.7
heads $\Rightarrow x = 1$

$$P[x=1] = p^1 (1-p)^{1-1}$$

$$P[x=1] = 0,7 (1-0,7)^0$$

$$P[x=1] = 0,7$$

Failure
 \longleftrightarrow

$x = 0$

$$P[x=0] = 0,7^0 \cdot (1-0,7)^{1-0}$$

$$= 0,3$$



IMPLEMENTING BERNOULLI DISTRIBUTION IN PYTHON

```
import numpy as np
import matplotlib.pyplot as plt

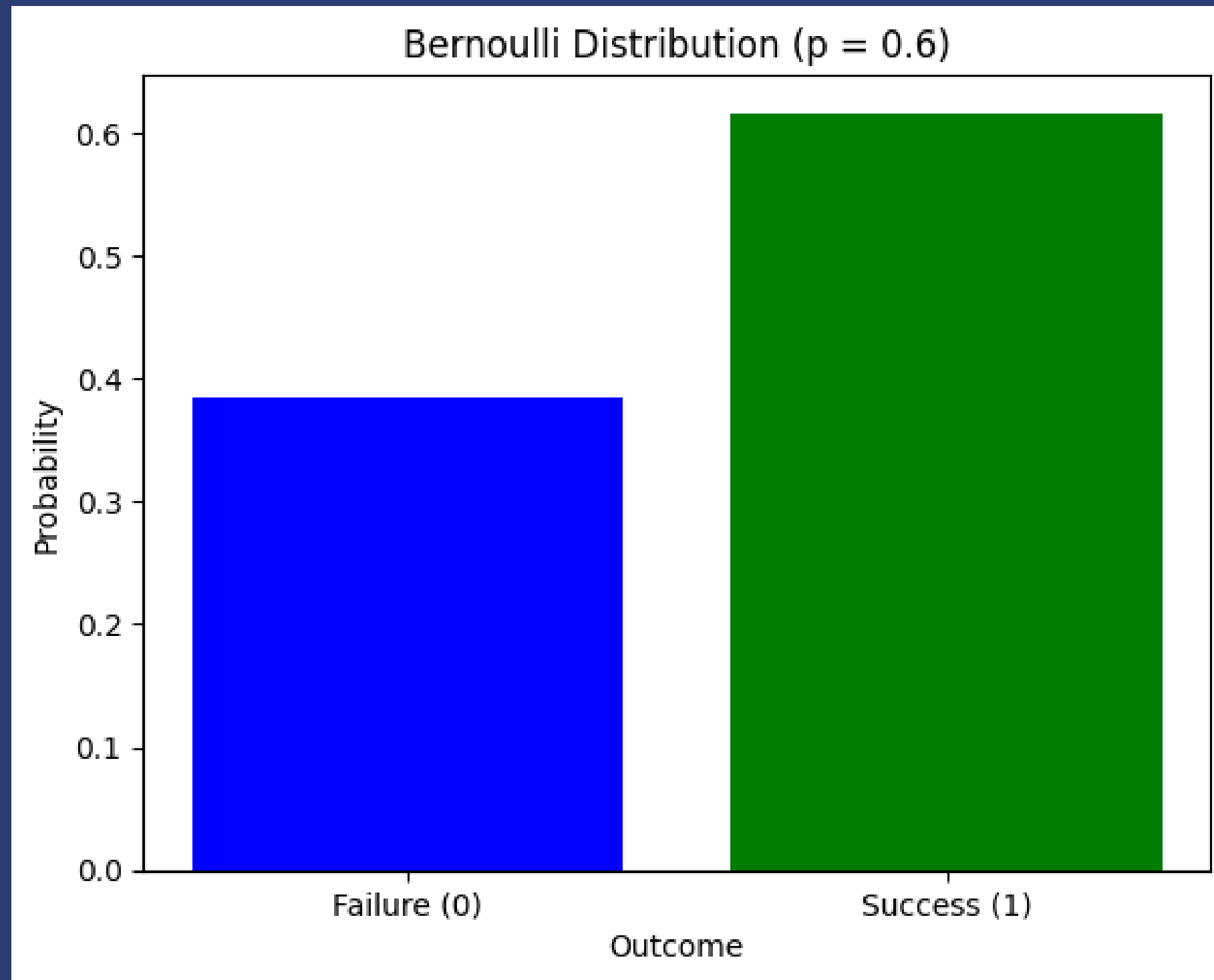
# Parameters
p = 0.6 # Probability of success

# Generate 1000 Bernoulli trials
trials = np.random.binomial(n=1, p=p, size=1000)

# Count occurrences of 0 and 1
unique, counts = np.unique(trials, return_counts=True)
probabilities = counts / sum(counts)

# Plotting
plt.bar(unique, probabilities, tick_label=["Failure (0)", "Success (1)"], color=["blue", "green"])
plt.xlabel("Outcome")
plt.ylabel("Probability")
plt.title(f"Bernoulli Distribution (p = {p})")
plt.show()
```

VISUALIZATION



The bar chart shows the probabilities for a single trial of success (1) and failure (0).

As p changes, the bar heights change, representing different probabilities.

Example:

- $p = 0.3$: Success is less likely.
- $p = 0.7$: Success is more likely.

SUMMARY

Real-world Example

- A single sales call success (1) or failure (0). The probability (p) could be based on previous sales data.

Summary

- Definition: Discrete distribution with two outcomes.
- Formula: $P(X = x) = p^x (1 - p)^{1 - x}$
- Python Code: Simulate Bernoulli trials using numpy.
- Visualization: Bar chart representation for success and failure.