# Double Exponential Jump Diffusion (DEJD) Validation Report - New Variation (DEX 600 & 1500)

Report Date: 28 Aug 2023

# **Squad Members**

| Area             | Person In Charge                          |
|------------------|---|
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## **Product Information**

Product Specification: https://docs.google.com/document/d/1PO6DN2w2AkK-d8faAwmFWDkJu02LLgsF/edit

Perl Code (8 Aug 2023): https://github.com/regentmarkets/perl-Feed-Index-JumpDiffusion/tree/b37fe3cf4b62104c5af82fb020bcd3f6d05f32c2

# **Background & Introduction**

There were 2 variations of Double Exponential Jump Diffusion (DEJD) indices launched on May 2023, which are DEX D900 and DEX U900.

In this time, another 4 variations are suggested to be part of the DEJD family, for the purpose of diversifying the concentration risk on a particular index, especially either on DOWN or UP.

The product description and the construction are exactly the same, except the parameters for these 4 variations are set differently.

For information about the index construction, please refer to the Double Exponential Jump Diffusion (DEJD) Index Validation Report as of 22 May 2023 (link here/Dex%20Indices%20Validation%20Report.pdf)).

The parameters are:

| New/Old | Index       | Number of Jumps per Hour $\lambda$ | Average Positive Jump Size $\eta_+$ | Average Negative Jump Size $\eta$ | Probability of Positive Jump $q_{+}$ | Probability of Negative Jump $q_{-}$ | Volatility |
|---------|-------------|------------------------------------|-------------------------------------|-----------------------------------|--------------------------------------|--------------------------------------|------------|
| Old     | DEX<br>U900 | 20, which is<br>175200 per<br>year | 0.30%                               | 0.04%                             | 20%                                  | 80%                                  | 25%        |
| Old     | DEX<br>D900 | 20, which is<br>175200 per<br>year | 0.04%                               | 0.30%                             | 80%                                  | 20%                                  | 25%        |

| New | DEX<br>U600  | 30, which is<br>262800 per<br>year | 0.20% | 0.04% | 20% | 80% | 20% |
|-----|--------------|------------------------------------|-------|-------|-----|-----|-----|
| New | DEX<br>D600  | 30, which is<br>262800 per<br>year | 0.04% | 0.20% | 80% | 20% | 20% |
| New | DEX<br>U1500 | 6, which is<br>52560 per year      | 0.20% | 0.04% | 40% | 60% | 10% |
| New | DEX<br>D1500 | 6, which is<br>52560 per year      | 0.04% | 0.20% | 60% | 40% | 10% |

# **Model Validation**

# Summary

For the validation of the new 4 variations of DEX indices, we cover the below areas and conclude the outcomes. 2 old variations are included as well for comparison.

Note that this validation covers the data from 8 August 2023 to 27 August 2023.

More details can be found in respective section.

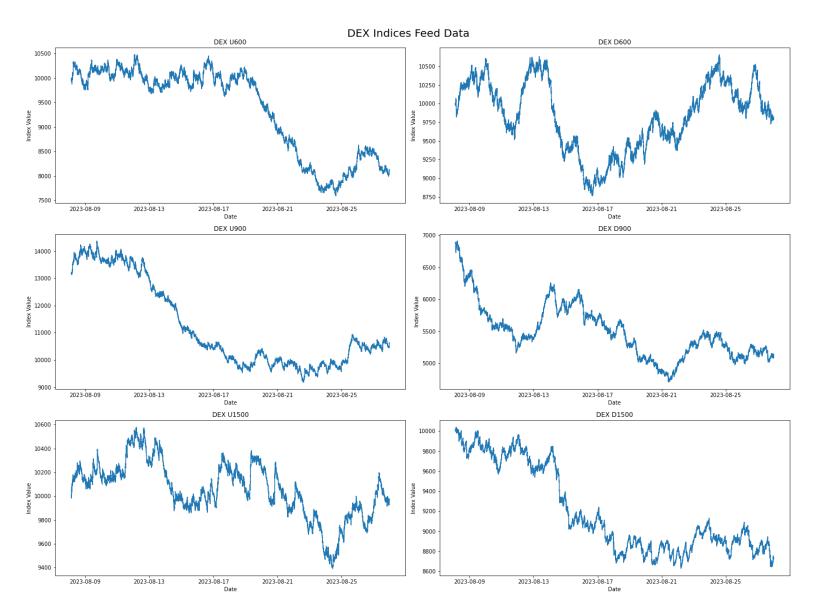
| Section | Area                                       | Validation  | Outcome   | Pass/Fail |
|---------|--|---|---|-----------|
| 1       | Check the<br>moment of the<br>feed data    | We compute the moment of the feed data, and check whether it is matching with the true distribution.  | We checked the moments of the feed data vs simulation for 3 sets of data, Dev data only, Demo data only and Dev + Demo data. The moments are matching.  | Passed    |
| 2       | Backward<br>engineering the<br>parameters. | Here we check the parameters backward engineering from the feed data moment. We do not proceed with the MLE method as the implementation is very difficult to implement | The result looks fine with the set initial condition and boundary condition.  | Passed    |
| 3       | Convergence of<br>the feed data<br>moment  | The convergence speed of the first 3 moments are checked.   | Generally the first moment and second moment converge to the true value fast, the skewness converges slower but within acceptable range. The result is fine.  | Passed    |
| 4       | Concentration<br>Risk Stress<br>Testing    | Few strategy testings on simulation data is run to ensure that there is no potential exploitation and the reasonableness of the spread.                                 | The strategy testing does not discover any potential exploitation. The strategy testing result also shows that the spread of the new 4 variations can be as low as 50% of DEX 900. While the spread of DEX 900 is set at around 0.01% of the index value, the spread of DEX 600/1500 is set at 0.0075% is reasonable. | Passed    |
| 5       | Correlation<br>between<br>variations       | This is to test the correlation between UP indices and DOWN indices, which should be almost zero  | Correlations between tickly data and hourly data do not appear high correlation.  | Passed    |

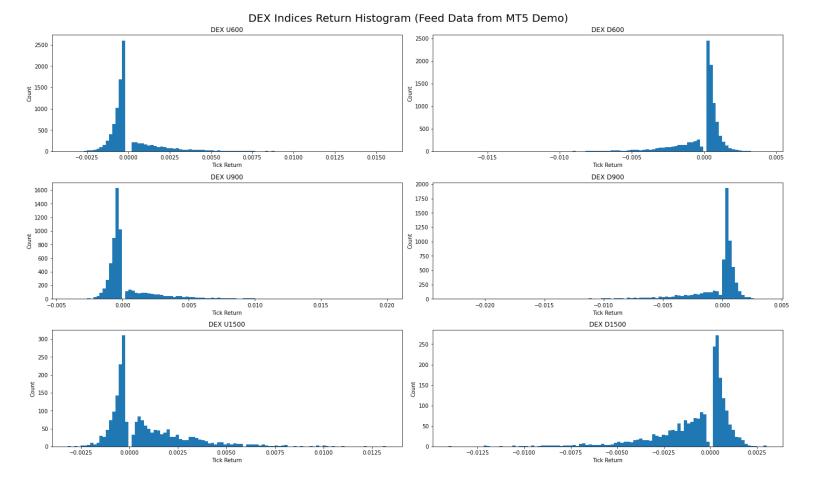
# Section 1

In here we are checking the moments of the real feed data. The validation steps are: 1) Obtain the feed data from Metabase. 2) Compute the feed data moments (Mean, Volatility, Skewness & Kurtosis). 3) Run the simulation and

compute the moments. 4) Compare (2) & (3)

Conclusion: 1) Mean - Acceptable as the abs difference is low. 2) Volatility - Acceptable as both abs and rel difference are low. 3) Skewness - Acceptable as rel difference is low. 4) Kurtosis - Acceptable.





# Moment Matching on Demo Data only

#### Feed Data Moments (Demo Data Only)

|           | Mean        | Volatility | Skewness     | Kurtosis      |
|-----------|-------------|------------|--------------|---------------|
| DEX U600  | -0.00000023 | 0.7170031  | 35.31630485  | 2274.90286739 |
| DEX U900  | -0.0        | 0.84538755 | 45.34611457  | 3078.70298327 |
| DEX U1500 | -0.0000003  | 0.41067984 | 61.2558964   | 5526.80111483 |
| DEX D600  | 0.00000009  | 0.73754885 | -37.32891679 | 2531.47848478 |
| DEX D900  | -0.00000011 | 0.88492772 | -50.08588895 | 3986.17025176 |
| DEX D1500 | -0.00000004 | 0.43067356 | -64.56591485 | 6360.34516846 |

**True Moments** 

|                  | Mean        | Volatility | Skewness     | Kurtosis      |
|------------------|-------------|------------|--------------|---------------|
| DEX U600         | -0.00000001 | 0.72646872 | 35.77045777  | 2299.83214784 |
| DEX U900         | -0.00000001 | 0.8591107  | 49.79636322  | 3948.38173166 |
| <b>DEX U1500</b> | -0.0        | 0.43391649 | 68.53278328  | 7198.95765976 |
| DEX D600         | -0.00000001 | 0.72646872 | -35.77045777 | 2299.83214784 |
| <b>DEX D900</b>  | -0.00000001 | 0.8591107  | -49.79636322 | 3948.38173166 |
| <b>DEX D1500</b> | -0.0        | 0.43391649 | -68.53278328 | 7198.95765976 |

## Difference (abs)

|                  | Mean        | Volatility  | Skewness    | Kurtosis       |
|------------------|-------------|-------------|-------------|----------------|
| <b>DEX U600</b>  | -0.00000023 | -0.00946562 | -0.45415292 | -24.92928045   |
| DEX U900         | 0.00000001  | -0.01372315 | -4.45024866 | -869.6787484   |
| DEX U1500        | -0.0000003  | -0.02323665 | -7.27688687 | -1672.15654493 |
| <b>DEX D600</b>  | 0.0000001   | 0.01108013  | -1.55845902 | 231.64633694   |
| DEX D900         | -0.0000001  | 0.02581702  | -0.28952573 | 37.78852009    |
| <b>DEX D1500</b> | -0.00000004 | -0.00324293 | 3.96686843  | -838.6124913   |

## Difference (rel)

|           | Mean         | Volatility  | Skewness    | Kurtosis    |
|-----------|--------------|-------------|-------------|-------------|
| DEX U600  | 26.94998289  | -0.01302964 | -0.01269631 | -0.01083961 |
| DEX U900  | -0.96290162  | -0.01597367 | -0.08936895 | -0.22026207 |
| DEX U1500 | 9.27296403   | -0.05355097 | -0.10618111 | -0.23227759 |
| DEX D600  | -12.06696549 | 0.01525204  | 0.04356833  | 0.10072315  |
| DEX D900  | 8.30539816   | 0.03005086  | 0.00581419  | 0.00957063  |
| DEX D1500 | 11.82964329  | -0.00747364 | -0.05788279 | -0.11649082 |

# Moment Matching on Dev Data only

## Feed Data Moments (Dev Data Only)

|           | Mean        | Volatility | Skewness     | Kurtosis      |
|-----------|-------------|------------|--------------|---------------|
| DEX U600  | 0.00000001  | 0.71840268 | 33.49477552  | 1965.20294821 |
| DEX U900  | -0.00000027 | 0.82993469 | 50.84547655  | 4102.38097316 |
| DEX U1500 | 0.00000003  | 0.44320585 | 63.75175625  | 5996.42428316 |
| DEX D600  | -0.00000013 | 0.72896899 | -33.43859023 | 1870.90422005 |
| DEX D900  | -0.00000025 | 0.88905901 | -47.03864814 | 3373.85873422 |
| DEX D1500 | -0.00000013 | 0.47867262 | -66.22513957 | 5992.897288   |

#### **True Moments**

|                 | Mean        | Volatility | Skewness     | Kurtosis      |
|-----------------|-------------|------------|--------------|---------------|
| DEX U600        | -0.00000001 | 0.72646872 | 35.77045777  | 2299.83214784 |
| DEX U900        | -0.00000001 | 0.8591107  | 49.79636322  | 3948.38173166 |
| DEX U1500       | -0.0        | 0.43391649 | 68.53278328  | 7198.95765976 |
| <b>DEX D600</b> | -0.00000001 | 0.72646872 | -35.77045777 | 2299.83214784 |
| DEX D900        | -0.00000001 | 0.8591107  | -49.79636322 | 3948.38173166 |
| DEX D1500       | -0.0        | 0.43391649 | -68.53278328 | 7198.95765976 |

#### Difference (abs)

|                  | Mean        | Volatility  | Skewness    | Kurtosis       |
|------------------|-------------|-------------|-------------|----------------|
| <b>DEX U600</b>  | 0.00000001  | -0.00806604 | -2.27568225 | -334.62919963  |
| DEX U900         | -0.00000026 | -0.02917602 | 1.04911332  | 153.9992415    |
| DEX U1500        | 0.00000004  | 0.00928936  | -4.78102703 | -1202.5333766  |
| <b>DEX D600</b>  | -0.00000012 | 0.00250027  | 2.33186754  | -428.92792779  |
| DEX D900         | -0.00000024 | 0.02994831  | 2.75771509  | -574.52299744  |
| <b>DEX D1500</b> | -0.00000012 | 0.04475613  | 2.30764371  | -1206.06037176 |

## Difference (rel)

|                  | Mean         | Volatility  | Skewness    | Kurtosis    |
|------------------|--------------|-------------|-------------|-------------|
| DEX U600         | -1.74963747  | -0.01110307 | -0.06361904 | -0.14550157 |
| DEX U900         | 22.38809714  | -0.03396072 | 0.02106807  | 0.03900313  |
| DEX U1500        | -11.76561656 | 0.02140817  | -0.06976263 | -0.16704271 |
| DEX D600         | 14.77945336  | 0.00344167  | -0.06518976 | -0.18650401 |
| DEX D900         | 20.44369707  | 0.03485966  | -0.05537985 | -0.14550847 |
| <b>DEX D1500</b> | 41.01740137  | 0.10314456  | -0.03367211 | -0.16753264 |

# Moment Matching on Combined Data

Feed Data Moments (Combined)

|                  | Mean        | Volatility | Skewness     | Kurtosis      |
|------------------|-------------|------------|--------------|---------------|
| DEX U600         | -0.00000012 | 0.71765247 | 34.46910274  | 2130.70946432 |
| DEX U900         | -0.00000013 | 0.83825829 | 47.82644862  | 3535.79249721 |
| <b>DEX U1500</b> | -0.0        | 0.42606943 | 62.69202013  | 5813.94411069 |
| DEX D600         | -0.00000001 | 0.73358329 | -35.5608073  | 2233.16634786 |
| DEX D900         | -0.00000017 | 0.88684544 | -48.66281382 | 3699.50689559 |
| DEX D1500        | -0.00000008 | 0.45356051 | -65.74089934 | 6220.25237644 |

#### **True Moments**

|                  | Mean        | Volatility | Skewness     | Kurtosis      |
|------------------|-------------|------------|--------------|---------------|
| <b>DEX U600</b>  | -0.00000001 | 0.72646872 | 35.77045777  | 2299.83214784 |
| DEX U900         | -0.00000001 | 0.8591107  | 49.79636322  | 3948.38173166 |
| DEX U1500        | -0.0        | 0.43391649 | 68.53278328  | 7198.95765976 |
| <b>DEX D600</b>  | -0.00000001 | 0.72646872 | -35.77045777 | 2299.83214784 |
| DEX D900         | -0.00000001 | 0.8591107  | -49.79636322 | 3948.38173166 |
| <b>DEX D1500</b> | -0.0        | 0.43391649 | -68.53278328 | 7198.95765976 |

## Difference (abs)

|                  | Mean        | Volatility  | Skewness    | Kurtosis       |
|------------------|-------------|-------------|-------------|----------------|
| DEX U600         | -0.00000011 | -0.00881625 | -1.30135503 | -169.12268352  |
| DEX U900         | -0.00000012 | -0.02085241 | -1.9699146  | -412.58923446  |
| DEX U1500        | 0.0         | -0.00784706 | -5.84076314 | -1385.01354907 |
| DEX D600         | -0.0        | 0.00711457  | 0.20965047  | -66.66579998   |
| DEX D900         | -0.00000016 | 0.02773473  | 1.1335494   | -248.87483607  |
| <b>DEX D1500</b> | -0.00000008 | 0.01964402  | 2.79188394  | -978.70528332  |

# Difference (rel)

|                  | Mean        | Volatility  | Skewness    | Kurtosis    |
|------------------|-------------|-------------|-------------|-------------|
| DEX U600         | 13.64327165 | -0.01213576 | -0.03638072 | -0.07353697 |
| DEX U900         | 9.86389657  | -0.02427209 | -0.03955941 | -0.10449578 |
| <b>DEX U1500</b> | -0.48167082 | -0.01808425 | -0.08522583 | -0.19239085 |
| DEX D600         | 0.38050033  | 0.00979336  | -0.00586099 | -0.02898725 |
| DEX D900         | 13.93337639 | 0.03228307  | -0.0227637  | -0.06303211 |
| DEX D1500        | 25.36268183 | 0.04527143  | -0.04073793 | -0.13595097 |

# Section 2

Here we check the parameters backward engineering from the feed data moments.

The result is highly dependable on the initial and boundary condition. The difference in the results are acceptable.

#### Feed Data Params

|                 | Vol        | Lambda         | Probability | Positive Eta | Negative Eta |
|-----------------|------------|----------------|-------------|--------------|--------------|
| <b>DEX U600</b> | 0.19885    | 261288.9       | 0.19885     | 0.0018915    | 0.0003977    |
| <b>DEX U900</b> | 0.2485625  | 174192.6       | 0.19885     | 0.00283725   | 0.0003977    |
| DEX U1500       | 0.099425   | 52257.78       | 0.3977      | 0.0018915    | 0.0003977    |
| <b>DEX D600</b> | 0.19495306 | 254922.5395474 | 0.77218777  | 0.0003783    | 0.00192919   |
| <b>DEX D900</b> | 0.24402909 | 171015.585434  | 0.77110692  | 0.00039048   | 0.00289164   |
| DEX D1500       | 0.099425   | 52257.78       | 0.56745     | 0.0003977    | 0.0018915    |

#### **True Params**

|          | Vol  | Lambda | Probability | Positive Eta | Negative Eta |
|----------|------|--------|-------------|--------------|--------------|
| DEX U60  | 0.2  | 262800 | 0.2         | 0.002        | 0.0004       |
| DEX U90  | 0.25 | 175200 | 0.2         | 0.003        | 0.0004       |
| DEX U150 | 0.1  | 52560  | 0.4         | 0.002        | 0.0004       |
| DEX D60  | 0.2  | 262800 | 0.8         | 0.0004       | 0.002        |
| DEX D90  | 0.25 | 175200 | 0.8         | 0.0004       | 0.003        |
| DEX D150 | 0.1  | 52560  | 0.6         | 0.0004       | 0.002        |

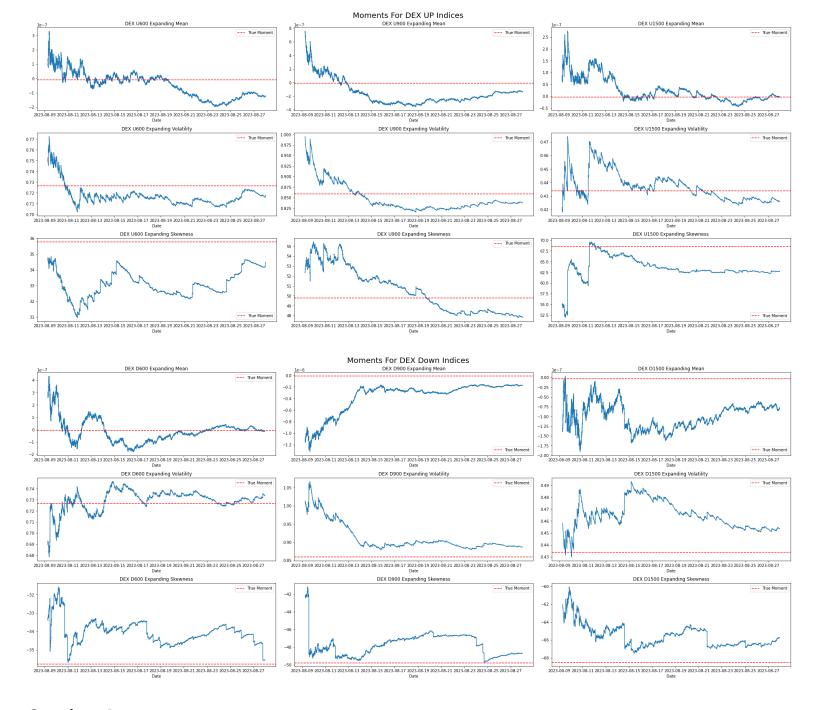
## Difference (rel)

|                 | Vol         | Lambda      | Probability | Positive Eta | Negative Eta |
|-----------------|-------------|-------------|-------------|--------------|--------------|
| DEX U600        | -0.00575    | -0.00575    | -0.00575    | -0.05425     | -0.00575     |
| <b>DEX U900</b> | -0.00575    | -0.00575    | -0.00575    | -0.05425     | -0.00575     |
| DEX U1500       | -0.00575    | -0.00575    | -0.00575    | -0.05425     | -0.00575     |
| <b>DEX D600</b> | -0.02523471 | -0.02997512 | -0.03476529 | -0.05425     | -0.03540599  |
| DEX D900        | -0.02388364 | -0.02388364 | -0.03611636 | -0.02379041  | -0.03612101  |
| DEX D1500       | -0.00575    | -0.00575    | -0.05425    | -0.00575     | -0.05425     |

# Section 3

We want to check the convergence speed of the DEX feed data in term of the moments.

Overall looks fine.



## Section 4

The simulation steps of the strategy testing are:

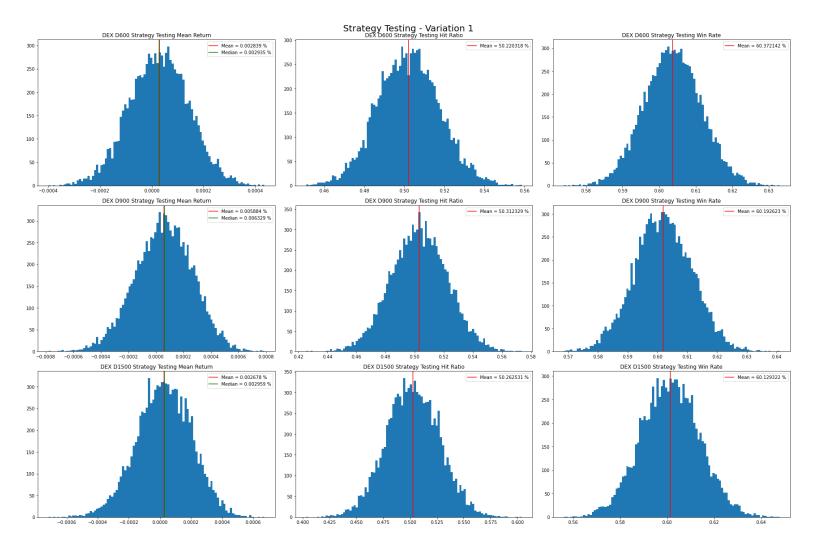
- 1. Run 3-months simulation for DEX Down 600/900/1500. Up indices is not run because it is just opposite direction.
- 2. Run the trading strategy on the simulation data.
  - A. Define the jump size same as the negative eta.
  - B. After each jump, wait for mean jump frequency (which is 600/900/1500 seconds respectively). If there is no jump, enter into a short position.
  - C. Enter into additional short position every mean jump frequency if there is no jump.
  - D. Exit all positions in next jump.
- 3. Repeat the strategy for a sufficient number of times. In here, it is 10K.
- 4. Plot the average PnL%, Hit Ratio and Win Rate.

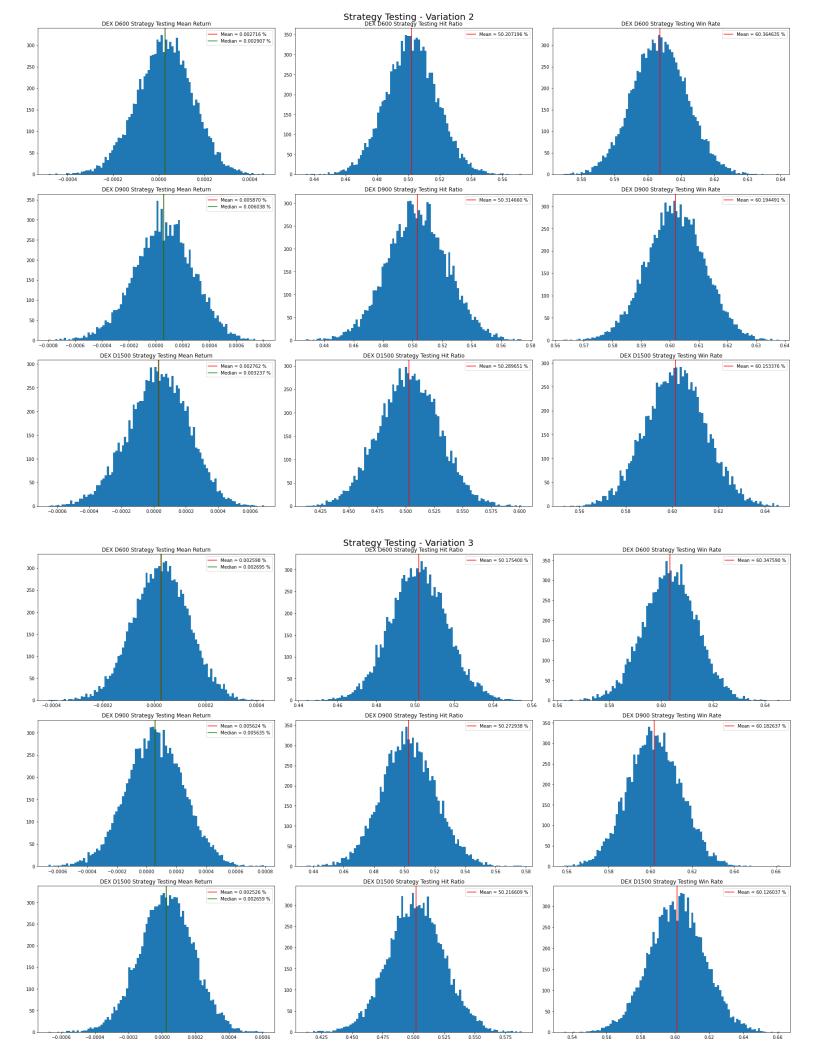
In total there are 3 variations of this strategies are run too, which is to:

- 1. Waiting time and additional position frequency same as mean jump frequency.
- 2. Waiting time same as mean jump frequency but additional position frequency at 5 mins.
- 3. Double the waiting time and enter into additional positions every 5 mins.

#### Key points to conclude the strategy testing:

- 1. Mean Hit Ratio of 50% shows that the exploitation is not possible.
- 2. Mean Win Rate of 60% is expected due to the clear pattern of the index.
- 3. Spread of 0.01% is sufficient for DEX 900 as it covers the mean and median of the strategy PnL in %.
- 4. The strategy also shows that the spread of DEX 600/1500 can be lower than DEX 900, and as low as 50%. After discussion with Antoine, 75% of DEX 900 Spread will be the go-live decision.





## Section 5

In here we check the correlations between each UP or DOWN DEX indices. The correlation is important for the concentration risk diversification.

Overall, it looks fine.

#### For DEX UP

#### Tickly

```
DEX U600 DEX U900 DEX U1500
DEX U600 1.00000000 -0.00005356 -0.00009738
DEX U900 -0.00005356 1.00000000 -0.00099314
DEX U1500 -0.00009738 -0.00099314 1.00000000
```

#### **Hourly**

|     |       | DEX U600   | DEX U900    | DEX U1500   |
|-----|-------|------------|-------------|-------------|
| DEX | U600  | 1.00000000 | 0.08863632  | 0.00939919  |
| DEX | U900  | 0.08863632 | 1.00000000  | -0.05071911 |
| DEX | U1500 | 0.00939919 | -0.05071911 | 1.00000000  |

#### For DEX DOWN

#### **Tickly**

```
DEX D600 DEX D900 DEX D1500
DEX D600 1.00000000 -0.00109056 0.00022100
DEX D900 -0.00109056 1.00000000 -0.00013249
DEX D1500 0.00022100 -0.00013249 1.00000000
```

#### **Hourly**

|     |       | DEX D600   | DEX D900   | DEX D1500  |
|-----|-------|------------|------------|------------|
| DEX | D600  | 1.00000000 | 0.02069979 | 0.01597954 |
| DEX | D900  | 0.02069979 | 1.00000000 | 0.04598549 |
| DEX | D1500 | 0.01597954 | 0.04598549 | 1.00000000 |

R&D effort needs to be in line with Deriv's vision and mission as formulated by our CEO. Therefore all R&D projects are carefully selected by our C-Level senior management represented by JY and Rakshit and resources for the projects are only allocated after review and shortlisting based on their vision and priorities.

In line with the standards and criterias set out by the CEO, the Model Validation team has validated the product/indices as documented in this report.