

$$V=2\pi\int_0^1 x f^*(x) \, dx$$