

Relation  
 $|c| = |a| \cos \theta$

$$\therefore \cos \theta = \frac{|c|}{|a|}$$

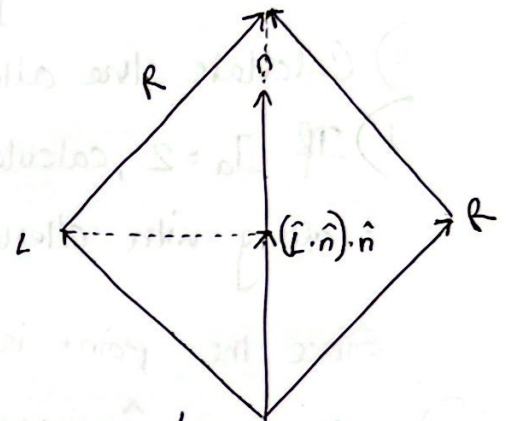
$$\vec{a} \cdot \vec{b} = |a||b| \cos \theta = |a||b| \cdot \frac{|c|}{|a|}$$

$$\Rightarrow \vec{a} \cdot \vec{b} = |b| \cdot |c|$$

$$\Rightarrow |c| = \frac{\vec{a} \cdot \vec{b}}{|b|}$$

$$\Rightarrow |c| = \vec{a} \cdot \hat{b}$$

and  $\Rightarrow \hat{c} = (\hat{a} \cdot \hat{b}) \cdot \hat{b}$



$$\hat{L} + \hat{R} = 2(\hat{L} \cdot \hat{n}) \cdot \hat{n}$$

$$\Rightarrow \hat{R} = 2(\hat{L} \cdot \hat{n}) \cdot \hat{n} - \hat{L}$$

$$f_{alt} = \max \left[ 1 - \left( \frac{d}{r} \right)^2, 0 \right]$$

where  $d$  = distance between source light and point.

$r$  = radius of influence

1) A light source with intensity 5 & radius of influence 50 is located at point  $(2, 3, 4)$  from which you are called to calculate the illumination of a point on the  $xy$  plane. The camera is set at a point  $(5, 6, 3)$  and the light is reflected back from point  $(4, 4)$ .  $K_a = 0.2$ ,  $K_d = 0.5$ ,  $K_s = 0.4$

a) Calculate  $\hat{R}$

b) Calculate Intensity of specular reflection for  $(n=10)$

c) Calculate the attenuation factor.

d) If  $I_a = 2$ , calculate the total reflected light intensity along with attenuation factor.

Since the point is on the  $xy$  plane,

a)  $\hat{n} = 0i + 0j + 1k$

$\vec{L} = (2, 3, 4) - (4, 4, 0) = -2i + (-1j) + 4k$   
 $\hat{L} = \frac{-2i - 1j + 4k}{\sqrt{21}}$

We know,

$\hat{R} = 2(\hat{L} \cdot \hat{n})\hat{n} - \hat{L}$

$\hat{L} \cdot \hat{n} = (0i + 0j + 1k) \cdot \left( \frac{-2i - 1j + 4k}{\sqrt{21}} \right)$   
 $= \frac{4}{\sqrt{21}}$

$2(\hat{L} \cdot \hat{n}) = \frac{8}{\sqrt{21}}$   $\rightarrow 2(\hat{L} \cdot \hat{n})\hat{n} = \frac{8}{\sqrt{21}} \hat{k}$

$\hat{R} = 2(\hat{L} \cdot \hat{n})\hat{n} - \hat{L} = \frac{8}{\sqrt{21}} \hat{k} - \frac{(-2i - 1j + 4k)}{\sqrt{21}}$   
 $= \frac{+2i + 1j + 4k}{\sqrt{21}}$  Ans

$$\textcircled{b} \quad \vec{V} = (5, 6, 3) - (4, 4, 0) \\ = (1, 2, 3)$$

$$\hat{V} = \frac{i + 2j + 3k}{\sqrt{14}}$$

$$\hat{R} \cdot \hat{V} = \left( \frac{2i + j + 4k}{\sqrt{21}} \right) \cdot \left( \frac{i + 2j + 3k}{\sqrt{14}} \right)$$

$$= \frac{16}{\sqrt{294}}$$

$$I = I_s K_s (\hat{R} \cdot \hat{V})^n \\ = 5 \times 0.4 \times \left( \frac{16}{\sqrt{294}} \right)^{10} \\ = 1.0011 \text{ units}$$

$$\textcircled{c} \quad f_{att} = 1 - \left( \frac{d}{r} \right)^2 \quad \begin{matrix} L & & P \\ (2, 3, 4) & \xleftrightarrow{d} & (4, 4, 0) \end{matrix}$$

$$d = \sqrt{(2-4)^2 + (3-4)^2 + (4-0)^2} \\ = \sqrt{21}$$

$$f_{att} = 1 - \frac{21}{(50)^2} \\ = 0.9916 \text{ units}$$

$$\textcircled{d} \quad I = I_a K_a + I_s f_{att} \left( K_d \cdot \max(\hat{L} \cdot \hat{n}, 0) + K_s \cdot \max(\hat{V} \cdot \hat{R}, 0)^n \right)$$