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Assignment 1

EE3900 - Linear Systems and Signal Processing IIT Hyderabad

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Z-transform Oppenheim and Schafer

Problem 3.12(a) Sketch the pole-zero plot for

$$X_1(n) = \frac{1 - 1/2z^{-1}}{1 + 2z^{-1}} \tag{1}$$

and shade the region of convergence:

Solution: Given that,

$$X_1(n) = \frac{1 - 1/2z^{-1}}{1 + 2z^{-1}} \tag{2}$$

As we know that, the numerator gives us the zeros and denominator gives the poles of a Z-transform.

$$1 - 1/2z^{-1} = 0 (3)$$

On solving, we get the zero 1/2. Similarly,

$$1 + 2z^{-1} = 0 (4)$$

On solving, we get the pole -2.

Since the $x_3(n)$ is absolutely summable, the ROC must include the unit circle: $\frac{2}{3} < |x| < \frac{3}{2}$

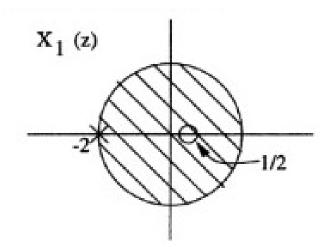


Fig. 0. Plot of Pole-zero