

## Defining Functions

## Outline

- Introduction
  - What is a neural network?
  - Why use neural networks?
  - Types of neural networks
- Feedforward neural networks
  - Architecture
  - Training
  - Applications
- Convolutional neural networks
  - Architecture
  - Training
  - Applications
- Recurrent neural networks
  - Architecture
  - Training
  - Applications
- Deep learning
  - Overview
  - Challenges
  - Future research

## Defining Functions

# Defining Functions

## Function definition

```
def <name>(<parameter name>, <parameter name>, ...):  
    <statement>  
    <statement>  
    ...
```

# Defining Functions

## Function definition

```
def <name>(<parameter name>, <parameter name>, ...):  
    <statement>  
    <statement>  
    ...
```

## Return statement

```
return [<expression>]
```

# Defining Functions

## Function definition

```
def <name>(<parameter name>, <parameter name>, ...):  
    <statement>  
    <statement>  
    ...
```

## Return statement

```
return [<expression>]
```

## Example

```
def is_prime(n):  
    if n < 2:  
        return False  
    i = 2  
    while i <= n // i:  
        if n % i == 0:  
            return False  
        i += 1  
    return True
```

## Defining Functions

## Defining Functions

The scope of a function's local and parameter variables is limited to that function



## Defining Functions

The scope of a function's local and parameter variables is limited to that function

The scope of a variable defined in global code — known as a global variable — is limited to the `.py` file containing that variable

## Defining Functions

## Defining Functions

A function may designate an argument to be optional by specifying a default value for that argument

## Defining Functions

A function may designate an argument to be optional by specifying a default value for that argument

Example (computing  $H_{n,r} = 1 + 1/2^r + 1/3^r + \cdots + 1/n^r$ )

```
def harmonic(n, r = 1):  
    total = 0.0  
    for i in range(1, n + 1):  
        total += 1 / (i ** r)  
    return total
```

## Defining Functions

## Defining Functions

If a function parameter refers to a mutable object, changing that object's value within the function also changes the object's value in the calling code

## Defining Functions

If a function parameter refers to a mutable object, changing that object's value within the function also changes the object's value in the calling code

### Example

```
def exchange(a, i, j):  
    temp = a[i]  
    a[i] = a[j]  
    a[j] = temp  
  
a = [1, 2, 3, 4, 5]  
exchange(a, 1, 3)  
stdio.writeln(a)
```

## Defining Functions

If a function parameter refers to a mutable object, changing that object's value within the function also changes the object's value in the calling code

### Example

```
def exchange(a, i, j):  
    temp = a[i]  
    a[i] = a[j]  
    a[j] = temp  
  
a = [1, 2, 3, 4, 5]  
exchange(a, 1, 3)  
stdio.writeln(a)
```

```
[1, 4, 3, 2, 5]
```



## Defining Functions

## Defining Functions

Program: `harmonicredux.py`

## Defining Functions

Program: `harmonicredux.py`

- Command-line input:  $n$  (int)

## Defining Functions

Program: `harmonicredux.py`

- Command-line input:  $n$  (int)
- Standard output: the  $n$ th harmonic number  $H_n = 1 + \frac{1}{2} + \frac{1}{3} + \cdots + \frac{1}{n}$

## Defining Functions

Program: `harmonicredux.py`

- Command-line input:  $n$  (int)
- Standard output: the  $n$ th harmonic number  $H_n = 1 + \frac{1}{2} + \frac{1}{3} + \cdots + \frac{1}{n}$

```
> ~/workspace/ipp/programs
```

```
$ _
```

## Defining Functions

Program: `harmonicredux.py`

- Command-line input:  $n$  (int)
- Standard output: the  $n$ th harmonic number  $H_n = 1 + \frac{1}{2} + \frac{1}{3} + \cdots + \frac{1}{n}$

```
>_ ~/workspace/ipp/programs
```

```
$ python3 harmonicredux.py 10
```

## Defining Functions

Program: `harmonicredux.py`

- Command-line input:  $n$  (int)
- Standard output: the  $n$ th harmonic number  $H_n = 1 + \frac{1}{2} + \frac{1}{3} + \cdots + \frac{1}{n}$

```
>_ ~/workspace/ipp/programs
```

```
$ python3 harmonicredux.py 10  
2.9289682539682538  
$ _
```

## Defining Functions

Program: `harmonicredux.py`

- Command-line input:  $n$  (int)
- Standard output: the  $n$ th harmonic number  $H_n = 1 + \frac{1}{2} + \frac{1}{3} + \cdots + \frac{1}{n}$

```
> ~/workspace/ipp/programs
```

```
$ python3 harmonicredux.py 10
2.9289682539682538
$ python3 harmonicredux.py 1000
```



## Defining Functions

Program: `harmonicredux.py`

- Command-line input:  $n$  (int)
- Standard output: the  $n$ th harmonic number  $H_n = 1 + \frac{1}{2} + \frac{1}{3} + \cdots + \frac{1}{n}$

```
>_ ~/workspace/ipp/programs
```

```
$ python3 harmonicredux.py 10
2.9289682539682538
$ python3 harmonicredux.py 1000
7.485470860550343
$ _
```

## Defining Functions

Program: `harmonicredux.py`

- Command-line input:  $n$  (int)
- Standard output: the  $n$ th harmonic number  $H_n = 1 + \frac{1}{2} + \frac{1}{3} + \cdots + \frac{1}{n}$

```
> ~/workspace/ipp/programs
```

```
$ python3 harmonicredux.py 10
2.9289682539682538
$ python3 harmonicredux.py 1000
7.485470860550343
$ python3 harmonicredux.py 10000
```

## Defining Functions

Program: `harmonicredux.py`

- Command-line input:  $n$  (int)
- Standard output: the  $n$ th harmonic number  $H_n = 1 + \frac{1}{2} + \frac{1}{3} + \cdots + \frac{1}{n}$

```
>_ ~/workspace/ipp/programs
```

```
$ python3 harmonicredux.py 10
2.9289682539682538
$ python3 harmonicredux.py 1000
7.485470860550343
$ python3 harmonicredux.py 10000
9.787606036044348
$ _
```

## Defining Functions

## Defining Functions

harmonicredux.py

```
1 import stdio
2 import sys
3
4 def main():
5     n = int(sys.argv[1])
6     stdio.writeln(_harmonic(n))
7
8 def _harmonic(n):
9     total = 0.0
10    for i in range(1, n + 1):
11        total += 1 / i
12    return total
13
14 if __name__ == '__main__':
15     main()
```

## Defining Functions

harmonicredux.py

```
1 import stdio
2 import sys
3
4 def main():
5     n = int(sys.argv[1])
6     stdio.writeln(_harmonic(n))
7
8 def _harmonic(n):
9     total = 0.0
10    for i in range(1, n + 1):
11        total += 1 / i
12    return total
13
14 if __name__ == '__main__':
15     main()
```

When a program is imported as a library, the program's `__name__` attribute is not set to `'__main__'`

>\_ ~/workspace/ipp/programs

>>> \_

## Defining Functions

harmonicredux.py

```
1 import stdio
2 import sys
3
4 def main():
5     n = int(sys.argv[1])
6     stdio.writeln(_harmonic(n))
7
8 def _harmonic(n):
9     total = 0.0
10    for i in range(1, n + 1):
11        total += 1 / i
12    return total
13
14 if __name__ == '__main__':
15     main()
```

When a program is imported as a library, the program's `__name__` attribute is not set to `'__main__'`

>\_ ~/workspace/ipp/programs

>>> import harmonicredux

## Defining Functions

harmonicredux.py

```
1 import stdio
2 import sys
3
4 def main():
5     n = int(sys.argv[1])
6     stdio.writeln(_harmonic(n))
7
8 def _harmonic(n):
9     total = 0.0
10    for i in range(1, n + 1):
11        total += 1 / i
12    return total
13
14 if __name__ == '__main__':
15     main()
```

When a program is imported as a library, the program's `__name__` attribute is not set to `'__main__'`

>\_ ~/workspace/ipp/programs

```
>>> import harmonicredux
>>> _
```



## Defining Functions

harmonicredux.py

```
1 import stdio
2 import sys
3
4 def main():
5     n = int(sys.argv[1])
6     stdio.writeln(_harmonic(n))
7
8 def _harmonic(n):
9     total = 0.0
10    for i in range(1, n + 1):
11        total += 1 / i
12    return total
13
14 if __name__ == '__main__':
15     main()
```

When a program is imported as a library, the program's `__name__` attribute is not set to `'__main__'`

>\_ ~/workspace/ipp/programs

```
>>> import harmonicredux
>>> harmonicredux._harmonic(10)
```

## Defining Functions

harmonicredux.py

```
1 import stdio
2 import sys
3
4 def main():
5     n = int(sys.argv[1])
6     stdio.writeln(_harmonic(n))
7
8 def _harmonic(n):
9     total = 0.0
10    for i in range(1, n + 1):
11        total += 1 / i
12    return total
13
14 if __name__ == '__main__':
15     main()
```

When a program is imported as a library, the program's `__name__` attribute is not set to `'__main__'`

>\_ ~/workspace/ipp/programs

```
>>> import harmonicredux
>>> harmonicredux._harmonic(10)
2.9289682539682538
>>> _
```

## Defining Functions

## Defining Functions

Program: `couponcollectorredux.py`

## Defining Functions

Program: `couponcollectorredux.py`

- Command-line input:  $n$  (int)

## Defining Functions

Program: `couponcollectorredux.py`

- Command-line input:  $n$  (int)
- Standard output: number of coupons one must collect before obtaining one of each of  $n$  types

## Defining Functions

Program: `couponcollectorredux.py`

- Command-line input:  $n$  (int)
- Standard output: number of coupons one must collect before obtaining one of each of  $n$  types

```
>_ ~/workspace/ipp/programs
```

```
$ _
```

## Defining Functions

Program: `couponcollectorredux.py`

- Command-line input:  $n$  (int)
- Standard output: number of coupons one must collect before obtaining one of each of  $n$  types

```
>_ ~/workspace/ipp/programs
```

```
$ python3 couponcollectorredux.py 1000
```



## Defining Functions

Program: `couponcollectorredux.py`

- Command-line input:  $n$  (int)
- Standard output: number of coupons one must collect before obtaining one of each of  $n$  types

```
>_ ~/workspace/ipp/programs
```

```
$ python3 couponcollectorredux.py 1000  
6276  
$ _
```

## Defining Functions

Program: `couponcollectorredux.py`

- Command-line input:  $n$  (int)
- Standard output: number of coupons one must collect before obtaining one of each of  $n$  types

```
>_ ~/workspace/ipp/programs
```

```
$ python3 couponcollectorredux.py 1000
```

```
6276
```

```
$ python3 couponcollectorredux.py 1000
```

## Defining Functions

Program: `couponcollectorredux.py`

- Command-line input:  $n$  (int)
- Standard output: number of coupons one must collect before obtaining one of each of  $n$  types

```
>_ ~/workspace/ipp/programs
```

```
$ python3 couponcollectorredux.py 1000
6276
$ python3 couponcollectorredux.py 1000
7038
$ _
```

## Defining Functions

Program: `couponcollectorredux.py`

- Command-line input:  $n$  (int)
- Standard output: number of coupons one must collect before obtaining one of each of  $n$  types

```
>_ ~/workspace/ipp/programs
```

```
$ python3 couponcollectorredux.py 1000
```

```
6276
```

```
$ python3 couponcollectorredux.py 1000
```

```
7038
```

```
$ python3 couponcollectorredux.py 1000000
```

## Defining Functions

Program: `couponcollectorredux.py`

- Command-line input:  $n$  (int)
- Standard output: number of coupons one must collect before obtaining one of each of  $n$  types

```
>_ ~/workspace/ipp/programs
```

```
$ python3 couponcollectorredux.py 1000  
6276  
$ python3 couponcollectorredux.py 1000  
7038  
$ python3 couponcollectorredux.py 1000000  
13401736  
$ _
```

## Defining Functions

## Defining Functions

couponcollectorredux.py

```
1 import stdarray
2 import stdio
3 import stdrandom
4 import sys
5
6 def main():
7     n = int(sys.argv[1])
8     stdio.writeln(_collect(n))
9
10 def _collect(n):
11     count = 0
12     collectedCount = 0
13     isCollected = stdarray.create1D(n, False)
14     while collectedCount < n:
15         value = _getCoupon(n)
16         count += 1
17         if not isCollected[value]:
18             collectedCount += 1
19             isCollected[value] = True
20     return count
21
22 def _getCoupon(n):
23     return stdrandom.uniformInt(0, n)
24
25 if __name__ == '__main__':
26     main()
```

## Defining Functions



## Defining Functions

Program: `playthattunedeluxe.py`

## Defining Functions

Program: `playthattunedeluxe.py`

- Standard input: sound samples, each characterized by a pitch and a duration

## Defining Functions

Program: `playthattunedeluxe.py`

- Standard input: sound samples, each characterized by a pitch and a duration
- Standard audio output: the sound

## Defining Functions

Program: `playthattunedeluxe.py`

- Standard input: sound samples, each characterized by a pitch and a duration
- Standard audio output: the sound

```
>_ ~/workspace/ipp/programs
```

```
$ _
```

## Defining Functions

Program: `playthattunedeluxe.py`

- Standard input: sound samples, each characterized by a pitch and a duration
- Standard audio output: the sound

```
>_ ~/workspace/ipp/programs
```

```
$ cat ../data/elise.txt
```

## Defining Functions

Program: `playthattunedeluxe.py`

- Standard input: sound samples, each characterized by a pitch and a duration
- Standard audio output: the sound

```
>_ ~/workspace/ipp/programs
```

```
$ cat ../data/elise.txt
7 .125
6 .125
7 .125
...
0 .25
$ _
```

## Defining Functions

Program: `playthattunedeluxe.py`

- Standard input: sound samples, each characterized by a pitch and a duration
- Standard audio output: the sound

```
>_ ~/workspace/ipp/programs
```

```
$ cat ../data/elise.txt
```

```
7 .125
```

```
6 .125
```

```
7 .125
```

```
...
```

```
0 .25
```

```
$ python3 playthattunedeluxe.py < ../data/elise.txt
```

## Defining Functions

Program: `playthattunedeluxe.py`

- Standard input: sound samples, each characterized by a pitch and a duration
- Standard audio output: the sound

```
>_ ~/workspace/ipp/programs  
  
$ cat ../data/elise.txt  
7 .125  
6 .125  
7 .125  
...  
0 .25  
$ python3 playthattunedeluxe.py < ../data/elise.txt  
$ -
```





## Defining Functions

## Defining Functions

playthattunedeluxe.py

```
1 import math
2 import stdarray
3 import stdaudio
4 import stdio
5
6 def main():
7     while not stdio.isEmpty():
8         pitch = stdio.readInt()
9         duration = stdio.readFloat()
10        stdaudio.playSamples(_createRichNote(pitch, duration))
11        stdaudio.wait()
12
13 def _createRichNote(pitch, duration):
14     NOTES_ON_SCALE = 12
15     CONCERT_A = 440.0
16     hz = CONCERT_A * math.pow(2, pitch / NOTES_ON_SCALE)
17     mid = _createNote(hz, duration)
18     hi = _createNote(2 * hz, duration)
19     lo = _createNote(hz / 2, duration)
20     hiAndLo = _superpose(hi, lo, 0.5, 0.5)
21     return _superpose(mid, hiAndLo, 0.5, 0.5)
22
23 def _createNote(hz, duration):
24     SPS = 44100
25     n = int(SPS * duration)
26     note = stdarray.create1D(n + 1, 0.0)
27     for i in range(n + 1):
28         note[i] = math.sin(2 * math.pi * i * hz / SPS)
29     return note
30
31 def _superpose(a, b, aWeight, bWeight):
32     c = stdarray.create1D(len(a), 0.0)
33     for i in range(len(a)):
34         c[i] = a[i] * aWeight + b[i] * bWeight
35     return c
```

## Defining Functions

playthattunedeluxe.py

```
36  
37 if __name__ == '__main__':  
38     main()
```

## Filter, Lambda, Map, and Reduce Functions

## Filter, Lambda, Map, and Reduce Functions

Functions in Python are first-class objects, meaning they can take functions as arguments and return functions as results

## Filter, Lambda, Map, and Reduce Functions

Functions in Python are first-class objects, meaning they can take functions as arguments and return functions as results

`filter(f, seq)` returns those items of `seq` for which `f(item)` is `True`

## Filter, Lambda, Map, and Reduce Functions

Functions in Python are first-class objects, meaning they can take functions as arguments and return functions as results

`filter(f, seq)` returns those items of `seq` for which `f(item)` is `True`

### Example

```
>_ ~/workspace/ipp/programs
```

```
>>> _
```

## Filter, Lambda, Map, and Reduce Functions

Functions in Python are first-class objects, meaning they can take functions as arguments and return functions as results

`filter(f, seq)` returns those items of `seq` for which `f(item)` is `True`

### Example

```
>_ ~/workspace/ipp/programs
```

```
>>> primes = filter(is_prime, range(11))
```



## Filter, Lambda, Map, and Reduce Functions

Functions in Python are first-class objects, meaning they can take functions as arguments and return functions as results

`filter(f, seq)` returns those items of `seq` for which `f(item)` is `True`

### Example

```
>_ ~/workspace/ipp/programs
```

```
>>> primes = filter(is_prime, range(11))  
>>> _
```

## Filter, Lambda, Map, and Reduce Functions

Functions in Python are first-class objects, meaning they can take functions as arguments and return functions as results

`filter(f, seq)` returns those items of `seq` for which `f(item)` is `True`

### Example

```
>_ ~/workspace/ipp/programs
```

```
>>> primes = filter(is_prime, range(11))  
>>> list(primes)
```

## Filter, Lambda, Map, and Reduce Functions

Functions in Python are first-class objects, meaning they can take functions as arguments and return functions as results

`filter(f, seq)` returns those items of `seq` for which `f(item)` is `True`

### Example

```
>_ ~/workspace/ipp/programs
```

```
>>> primes = filter(is_prime, range(11))
>>> list(primes)
[2, 3, 5, 7]
>>> _
```

## Filter, Lambda, Map, and Reduce Functions

## Filter, Lambda, Map, and Reduce Functions

A lambda function is a “disposable” function that we can define just when we need it and then immediately throw it away after we are done using it

## Filter, Lambda, Map, and Reduce Functions

A lambda function is a “disposable” function that we can define just when we need it and then immediately throw it away after we are done using it

### Example

```
>_ ~/workspace/ipp/programs
```

```
>>> _
```

## Filter, Lambda, Map, and Reduce Functions

A lambda function is a “disposable” function that we can define just when we need it and then immediately throw it away after we are done using it

### Example

```
>_ ~/workspace/ipp/programs
```

```
>>> odds = filter(lambda x : x % 2 != 0, range(11))
```

## Filter, Lambda, Map, and Reduce Functions

A lambda function is a “disposable” function that we can define just when we need it and then immediately throw it away after we are done using it

### Example

```
>_ ~/workspace/ipp/programs
```

```
>>> odds = filter(lambda x : x % 2 != 0, range(11))  
>>> _
```



## Filter, Lambda, Map, and Reduce Functions

A lambda function is a “disposable” function that we can define just when we need it and then immediately throw it away after we are done using it

### Example

```
>_ ~/workspace/ipp/programs
```

```
>>> odds = filter(lambda x : x % 2 != 0, range(11))  
>>> list(odds)
```

## Filter, Lambda, Map, and Reduce Functions

A lambda function is a “disposable” function that we can define just when we need it and then immediately throw it away after we are done using it

### Example

```
>_ ~/workspace/ipp/programs
```

```
>>> odds = filter(lambda x : x % 2 != 0, range(11))
>>> list(odds)
[1, 3, 5, 7, 9]
>>> _
```

## Filter, Lambda, Map, and Reduce Functions

## Filter, Lambda, Map, and Reduce Functions

`map(f, seq)` returns a list of the results of applying the function `f` to the items of `seq`

## Filter, Lambda, Map, and Reduce Functions

`map(f, seq)` returns a list of the results of applying the function `f` to the items of `seq`

### Example

```
>_ ~/workspace/ipp/programs
```

```
>>> _
```

## Filter, Lambda, Map, and Reduce Functions

`map(f, seq)` returns a list of the results of applying the function `f` to the items of `seq`

### Example

```
>_ ~/workspace/ipp/programs
```

```
>>> squares = map(lambda x : x ** 2, range(11))
```

## Filter, Lambda, Map, and Reduce Functions

`map(f, seq)` returns a list of the results of applying the function `f` to the items of `seq`

### Example

```
>_ ~/workspace/ipp/programs
```

```
>>> squares = map(lambda x : x ** 2, range(11))  
>>> _
```

## Filter, Lambda, Map, and Reduce Functions

`map(f, seq)` returns a list of the results of applying the function `f` to the items of `seq`

### Example

```
>_ ~/workspace/ipp/programs
```

```
>>> squares = map(lambda x : x ** 2, range(11))  
>>> list(squares)
```



## Filter, Lambda, Map, and Reduce Functions

`map(f, seq)` returns a list of the results of applying the function `f` to the items of `seq`

### Example

```
>_ ~/workspace/ipp/programs
```

```
>>> squares = map(lambda x : x ** 2, range(11))
>>> list(squares)
[0, 1, 4, 9, 16, 25, 36, 49, 64, 81, 100]
>>> _
```

## Filter, Lambda, Map, and Reduce Functions

## Filter, Lambda, Map, and Reduce Functions

`functools.reduce(f, seq)` applies the function `f` of two arguments cumulatively to the items of `seq` to reduce the sequence to a single value

## Filter, Lambda, Map, and Reduce Functions

`functools.reduce(f, seq)` applies the function `f` of two arguments cumulatively to the items of `seq` to reduce the sequence to a single value

### Example

```
>_ ~/workspace/ipp/programs
```

```
>>> _
```

## Filter, Lambda, Map, and Reduce Functions

`functools.reduce(f, seq)` applies the function `f` of two arguments cumulatively to the items of `seq` to reduce the sequence to a single value

### Example

```
>_ ~/workspace/ipp/programs
```

```
>>> total = functools.reduce(lambda x, y: x + y, range(11))
```

## Filter, Lambda, Map, and Reduce Functions

`functools.reduce(f, seq)` applies the function `f` of two arguments cumulatively to the items of `seq` to reduce the sequence to a single value

### Example

```
>_ ~/workspace/ipp/programs
```

```
>>> total = functools.reduce(lambda x, y: x + y, range(11))  
55  
>>> _
```