

Series or Test	Conclusions	Comments
<b>Divergence Test:</b> For any $\sum_{n=1}^{\infty} a_n$ , evaluate $\lim_{n \rightarrow \infty} a_n$ .	If $\lim_{n \rightarrow \infty} a_n = 0$ , the test is inconclusive.  If $\lim_{n \rightarrow \infty} a_n \neq 0$ , the series diverges.	This test cannot prove convergence of a series.
<b>Geometric Series:</b> For $\sum_{n=1}^{\infty} ar^{n-1}$ ,	If $ r  < 1$ , the series converges to $\frac{a}{1-r}$ .  If $ r  \geq 1$ , the series diverges.	Write the series in the form $a + ar + ar^2 + \dots$ .
<b>p-Series:</b> For $\sum_{n=1}^{\infty} \frac{1}{n^p}$ ,	If $p > 1$ , the series converges.  If $p \leq 1$ , the series diverges.	
<b>Alternating Series:</b> For $\sum_{n=1}^{\infty} (-1)^{n+1} b_n$ or $\sum_{n=1}^{\infty} (-1)^n b_n$ ,	If $0 \leq b_{n+1} \leq b_n$ for all $n \geq 1$ and $b_n \rightarrow 0$ , then the series converges.	Only applies to alternating series.
<b>Comparison Test:</b> For $\sum_{n=1}^{\infty} a_n$ with $a_n \geq 0$ , compare with a known series $\sum_{n=1}^{\infty} b_n$ .	If $a_n \leq b_n$ for all $n \geq N$ and $\sum_{n=1}^{\infty} b_n$ converges, then $\sum_{n=1}^{\infty} a_n$ converges.  If $a_n \geq b_n$ for all $n \geq N$ and $\sum_{n=1}^{\infty} b_n$ diverges, then $\sum_{n=1}^{\infty} a_n$ diverges.	Typically used for a series similar to a geometric or p-series. It can sometimes be difficult to find $b_n$ .
<b>Limit Comparison Test:</b> For $\sum_{n=1}^{\infty} a_n$ with $a_n \geq 0$ , compare with a series $\sum_{n=1}^{\infty} b_n$ with $b_n > 0$ by evaluating $L = \lim_{n \rightarrow \infty} \frac{a_n}{b_n}$ .	If $L$ is a real number and $L \neq 0$ , then both $\sum_{n=1}^{\infty} a_n$ and $\sum_{n=1}^{\infty} b_n$ either converge or diverge.  If $L = 0$ and $\sum_{n=1}^{\infty} b_n$ converges, then $\sum_{n=1}^{\infty} a_n$ converges.  If $L = \infty$ and $\sum_{n=1}^{\infty} b_n$ diverges, then $\sum_{n=1}^{\infty} a_n$ diverges.	Typically used for a series similar to a geometric or p-series. Often easier to apply than the comparison test.
<b>Ratio Test:</b> For any $\sum_{n=1}^{\infty} a_n$ , evaluate $\rho = \lim_{n \rightarrow \infty} \left  \frac{a_{n+1}}{a_n} \right $ .	If $0 \leq \rho < 1$ , the series converges absolutely.  If $\rho > 1$ , the series diverges.  If $\rho = 1$ , the test is inconclusive.	Often used for series with factorials or powers of $n$ . Does not require a comparable series $b_n$ .
<b>Integral Test:</b> If there exists a positive, continuous, decreasing function $f$ such that $a_n = f(n)$ for all $n \geq N$ , evaluate $\int_N^{\infty} f(x) dx$ .	$\int_N^{\infty} f(x) dx$ and $\sum_{n=1}^{\infty} a_n$ both converge or both diverge.	Limited to those series for which the corresponding function $f$ can be easily integrated. Does not require a comparable series $b_n$ .