## 1

## Discrete Assignment

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**Question** (11.9.3.14) The sum of first three terms of a G.P. is 16 and the sum of next three terms is 128. Determine the first term, the common ratio, and the sum to n terms of the G.P.

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А	n	S	w	e	r

Parameter	Description	Value
<i>x</i> (0)	First term of AP	_
r	Common ratio	_
x(n)	General term of given AP	$x(0)r^nu(n)$
x(0) + x(1) + x(2)	sum of 1st,2nd and 3rd terms	16
x(3) + x(4) + x(5)	sum of 3rd,4th and 5th terms	128

Given:

$$x(0) + x(0)r + x(0)r^2 = 16$$
 (1)

$$x(0)r^3 + x(0)r^4 + x(0)r^5 = 128$$
 (2)

From Equation (1):

$$x(0)(1+r+r^2) = 16 (3)$$

$$x(0) = \frac{16}{1 + r + r^2} \tag{4}$$

$$x(0)r^{3} = \frac{128}{1+r+r^{2}}$$

$$x^{3} = 8$$
(5)

$$r^3 = 8 \tag{6}$$

$$r = 2 \tag{7}$$

$$x(0) = \frac{16}{7} \tag{8}$$

Solving for r in terms of x(0):

$$(x(0) * b)_n = \sum_{k=0}^n 2^k \cdot 1 \tag{9}$$

$$=\frac{2^{n+1}-1}{2-1}\tag{10}$$

$$=2^{n+1}-1\tag{11}$$

So, the sum of the first *n* terms of the sequence  $x(n) = 2^n$  is  $2^{n+1} - 1$ .

$$S_n = \frac{16}{7}(2^n - 1) \tag{12}$$

$$=\frac{16}{7}\cdot 2^n - \frac{16}{7} \tag{13}$$

$$=\frac{16}{7}\cdot(a*b)_n-\frac{16}{7}$$
 (14)

$$=\frac{16}{7}\cdot(2^{n+1}-1)-\frac{16}{7}\tag{15}$$

The Z-transform will be:

$$X(z) = \frac{\frac{16}{7}}{1 - 2z^{-1}} \tag{16}$$