Square Roots
$\sqrt{x^6} = x^3 $
$\sqrt{x^8} = x^4$
$\sqrt{x^7} = x^3 \sqrt{x}$

Absolute Value Inequalities |x| < c -c < x < c |x| > c x < -c or c < x

Distance Formula $A(x_1, y_2) \text{ and } B(x_2, y_2)$ $d(A, B) = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

Midpoint Formula $A(x_1, y_2) \text{ and } B(x_2, y_2)$ $\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$

Equation of a Circle
$$(x-h)^2+(y-k)^2=r^2$$

Point-Slope Form $y-y_1 = m(x-x_1)$

 $\begin{array}{c} {\rm Positive\ Trigonometric} \\ {\rm Functions} \\ {\rm I-All\ II-sin\ III-tan\ IV-cos} \end{array}$

Law of Cosines $a^2 = b^2 + c^2 - 2bc \cdot \cos A$

Joint
Variation
If z is varies
jointly as x and y, z = kxy

Perpendicular Lines $m_2 = -\frac{1}{m_1}$

Average Rate of Change $ARoC = \frac{y \text{ change}}{x \text{ change}} = \frac{f(x_2) - f(x_1)}{x_2 - x_1}$

Difference of Cubes $a^3+b^3 = (a+b)(a^2-ab+b^2)$ $a^3-b^3 = (a-b)(a^2+ab+b^2)$

Standard Form of a Quadratic Function $f(x) = a(x-h)^2 + k$

Vertical Shifts of Graphs

Suppose c > 0.

Graph y = f(x) + c by shifting y = f(x) up c. Graph y = f(x) - c by shifting y = f(x) down c. Horizonal Shifts of Graphs Suppose c > 0. Graph y = f(x - c) by shifting y = f(x) right c. Graph y = f(x + c) by shifting y = f(x) left c. Definition of Log if $a^x = y$, $\log_a y = x$ ArcLength $s = r\theta$

Reflecting Graphs

Graph y = -f(x) by reflecting y = f(x) in the x-axis. Graph y = f(-x) by reflecting y = f(x) in the y-axis. Vertical Stretching of Graphs To graph y = cf(x), graph y = f(x), then if c > 1 strech vertically a by factor of cif 0 < c < 1 shrink vertically a by factor of c Inverse Variation If y is inversly proportional to x, $y = \frac{k}{x}$

Horizontal Stretching of Graphs To graph y = f(cx), graph y = f(x), then if c > 1 shrink horizontally by a factor of $\frac{1}{c}$ if 0 < c < 1 stretch horizontally by a factor of $\frac{1}{c}$

Even and Odd Functions if f(-x) = f(x) f(x) is even if f(-x) = -f(x) f(x) is odd

Heron's Formula $A = \sqrt{s(s-a)(s-b)(s-c)}$

Min or Max of a Quadratic Function $f(x) = x(x-h)^2 + k$ f(h) = k $f(x) = ax^2 + bx + c$ $f(-\frac{b}{2a})$ Change of Base $\log_b m = \frac{\log m}{\log b}$

Completing the Square
With a quadratic in form $ax^2 + bx = c$ $(\frac{1}{2} \cdot b)^2 = c$

Hidden quadratic 1 $x^{-3/2}+2x^{-1/2}+x^{1/2}$ $x^{-3/2}(1+2x+x^2)$ $x^{-3/2}(1+x)^2$

Hidden quadratic 2 $e^{2x} + 2e^x + 1$ $(e^x + 1)^2$

Permutations $p(x,y) = \frac{x!}{(x-y)!}$

Choose Formula $C(x,y) = {x \choose y} = \frac{x!}{y!(x-y)!}$

 $\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$

Degrees to Radians $\frac{A \cdot \pi}{180} = \theta$

Remainder Theorem If $P(x) \div (x-c)$, the remainder = P(c).

 $\sin = \frac{\text{SOH-CAH-TOA}}{\text{hyp}} \quad \cos = \frac{\text{adj}}{\text{hyp}} \quad \tan = \frac{\text{opp}}{\text{adj}}$

Sector Area $A = \frac{1}{2}r^2\theta$

Direct
Variation
If y is directly proportional to x, y = kx

Population Growth n is population size, r is relative growth rate, t is time $n = n_0 e^{rt}$

Area of Δ $A = ab \cdot \frac{1}{2} \sin C$

Properties of logs $(\log_a b)(\log_c d) = (\log_a d)(\log_c b)$ $\log m + \log n = \log mn$ $\log m - \log n = \log \frac{m}{n}$ $m \log n = \log n^m$

Two-intercept form $\frac{x}{a} + \frac{y}{b} = 1$

 $\begin{aligned} & \text{Quadratic Formula} \\ & x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \end{aligned}$

Slope-Intercept Form y = mx + b

i raised to a power

 $i^1 = i$ $i^2 = -1$

 $i^3 = -i$

 $i^4 = 1$

Complex numbers $\overline{a+bi} = a-bi$ $|a+bi| = \sqrt{(a+bi)(a-bi)}$

Algebra of Functions

Let f and g be functions with domains A and B.

$$(f+g)(x) = f(x) + g(x)$$

Domain $A \cap B$

$$(f-g)(x) = f(x) - g(x)$$

Domain $A \cap B$

$$(fg)(x) = f(x)g(x)$$

Domain $A \cap B$

Domain
$$\{x \in A \cap B \mid g(x) \neq 0\}$$

$$(f \circ g)(x) = f(g(x))$$

Domain $\{x \in B \mid g(x) \in A\}$

Polynomial Synthetic Division

Result is
$$x^2 - x + 2 - \frac{5}{x+2}$$

Polynomial Long Division

Rational Roots Theorem $2x^3 + 2x^2 - 3x - 6$

$$2x^3$$
 -

 $\pm 1, \pm 2, \pm 3, \pm 6$

Possible rational roots:

$$\pm 1, \pm \frac{1}{2}, \pm 2, \pm 3, \pm \frac{3}{2}, \pm 6$$

Decartes' Rule of Signs Count num. of sign changes $P(x) = 3x^6 + 4x^5 + 3x^3 - x - 3$ 1 positive real root $P(-x) = 3x^6 - 4x^5 - 3x^3 + x - 3$

1 or 3 negative real roots

Logarithm Formulas $\log(m \cdot n) = \log m + \log n$

$$\log\left(\frac{m}{n}\right) = \log m - \log n$$

$$\log(m^n) = n \cdot \log m$$

$$\log_b b^x = x = b^{\log_b x}$$

Trigonometric Reciprocals $\cot = \frac{1}{\tan}$ $\sec = \frac{1}{\cos}$

Horizontal Asymptotes

When degree of numerator is same as degree of denominator

$$y = \frac{2x^2 - 4x + 5}{x^2 - 2x + 1}$$
 Original Equation

$$=\frac{2x^2}{2}$$

 $x \to \infty$, other terms $\to \text{tiny}$

$$x^{2}$$

Cancel, horizontal asymptote

If degree of denominator is greater, 0

 $y = \frac{2x^2 - 4x + 5}{x^2 - 2x + 1}$ Original Equation

$$=\frac{2x^2-4+5}{(2x+3)(x+3)}$$

Factor demoniator

$$= \frac{2x^2 - 4 + 5}{(2x - 1)(x + 2)}$$
$$x = \frac{1}{2} \text{ or } x = -2$$

Impossible

Slant Asymptotes

When degree of numerator is one greater than degree of denominator

$$y = \frac{x^2 - 4x - 5}{x - 3}$$

Original Equation

$$=x-1-\frac{8}{x-3}$$
 Divide

$$= x - 1$$

 $x \to \infty$, other terms $\to \text{tiny}$

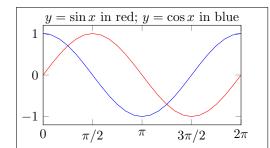
End Behavior

$$n \text{ is even}$$
 $y = x^n$
 $y = -x^n$
 $y = -x^n$

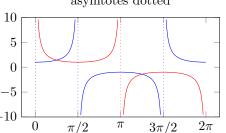
Trig Identities $\sin^2 + \cos^2 = 1$

$$\tan^2 + 1 = \sec^2$$

$$1 + \cot^2 = \csc^2$$



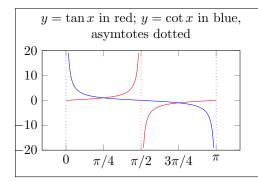
 $y = \csc x$ in red; $y = \sec x$ in blue, asymtotes dotted



sin/cos/csc/sec Graph **Properties**

If in form:

 $y = a\sin k(x - b)$ amplitude |a|, period $2\pi/k$, phase shift b



tan/cot Graph Properties If in form:

 $y = a\sin k(x - b)$ amplitude |a|, period π/k , phase shift b