

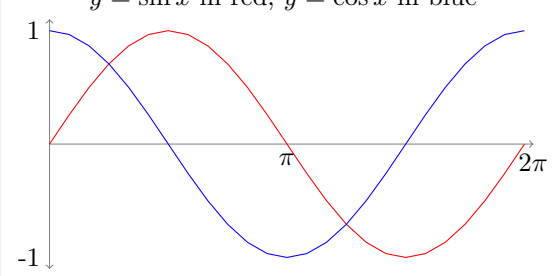
Positive Trigonometric Functions I-All pos. II-sin III-tan IV-cos	Law of Cosines $a^2 = b^2 + c^2 - 2bc \cdot \cos A$	Difference of Cubes $a^3 \pm b^3 = (a \pm b)(a^2 \mp ab + b^2)$	Arc Length $s = r\theta$
Heron's Formula $A = \sqrt{s(s-a)(s-b)(s-c)}$	Change of Base $\log_b m = \frac{\log m}{\log b}$	Choose Formula $C(x, y) = \binom{x}{y} = \frac{x!}{y!(x-y)!}$	Law of Sines $\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$
Degrees to Radians $\frac{A \cdot \pi}{180} = \theta$	Sector Area $A = \frac{1}{2}r^2\theta$	Area of $\Delta$ $Area = ab \cdot \frac{1}{2} \sin C$	Polar to $(x, y)$ $r^2 = x^2 + y^2$ $\tan \theta = \frac{y}{x}$
			$(\log_a b)(\log_c d) = (\log_a d)(\log_c b)$
$z = a + bi$ $ z  = \sqrt{a^2 + b^2}$	$z = r \operatorname{cis} \theta$ $z^n = r^n \operatorname{cis}(n\theta)$	$n$ th roots of $z = r \operatorname{cis} \theta$ $w_k = r^{1/n} \operatorname{cis} \left( \frac{\theta + 2k\pi}{n} \right)$	$z_1 z_2 = r_1 r_2 \operatorname{cis}(\theta_1 + \theta_2)$ $\frac{z_1}{z_2} = \frac{r_1}{r_2} \operatorname{cis}(\theta_1 - \theta_2)$
			$\vec{v} = \langle a, b \rangle = a\hat{i} + b\hat{j}$ $ \vec{v}  = \sqrt{a^2 + b^2}$
			$ c\vec{u}  =  c  \vec{u} $
Dot Product $\vec{u} \cdot \vec{v} = a_1 a_2 + b_1 b_2$	Dot Product Theorem $\vec{u} \cdot \vec{v} =  \vec{u}  \vec{v}  \cos \theta$	$\theta$ between $\vec{u}$ & $\vec{v}$ $\cos \theta = \frac{ \vec{u} \cdot \vec{v} }{ \vec{u}  \vec{v} }$	$\vec{u}$ and $\vec{v}$ are perpendicular $\vec{u} \cdot \vec{v} = 0$
		Component of $\vec{u}$ along $\vec{v}$ $(\vec{u} \cdot \vec{v})/ \vec{v} $	$\operatorname{proj}_{\vec{v}} \vec{u} = \left( \frac{\vec{u} \cdot \vec{v}}{ \vec{v} ^2} \right) \vec{v}$
Work $W = \vec{F} \cdot \vec{D}$			
Trig Identities			
$\sin^2 + \cos^2 = 1$	$\tan^2 + 1 = \sec^2$	$1 + \cot^2 = \csc^2$	$2 \sin u \cos u = \sin(2u)$
		$\cos^2 u - \sin^2 u = \cos(2u)$	$\frac{2 \tan u}{1 - \tan^2 u} = \tan(2u)$
$\sin u \cos v \pm \cos u \sin v = \sin(u \pm v)$		$\cos u \cos v \mp \sin u \sin v = \cos(u \pm v)$	$\frac{\tan u \pm \tan v}{1 \mp \tan u \tan v} = \tan(u \pm v)$
$\cot = \frac{1}{\tan}$			
$\csc = \frac{1}{\sin}$	$\sec = \frac{1}{\cos}$	$\sin\left(\frac{\pi}{2} - u\right) = \cos u$	$\tan\left(\frac{\pi}{2} - u\right) = \cot u$
		$\sec\left(\frac{\pi}{2} - u\right) = \csc u$	$\cos\left(\frac{\pi}{2} - u\right) = \sin u$
$\cot\left(\frac{\pi}{2} - u\right) = \tan u$	$\csc\left(\frac{\pi}{2} - u\right) = \sec u$	$\frac{1 - \cos 2x}{2} = \sin^2 x$	$\frac{1 + \cos 2x}{2} = \cos^2 x$
		$\frac{1 - \cos 2x}{1 + \cos 2x} = \tan^2 x$	$\pm \sqrt{\frac{1 - \cos u}{2}} = \sin \frac{u}{2}$
$\pm \sqrt{\frac{1 + \cos u}{2}} = \cos \frac{u}{2}$		$\frac{1 - \cos u}{\sin u} = \frac{\sin u}{1 + \cos u} = \tan \frac{u}{2}$	$2 \sin \frac{x \pm y}{2} \cos \frac{x \mp y}{2} = \sin x \pm \sin y$
$2 \cos \frac{x + y}{2} \cos \frac{x - y}{2} = \cos x + \cos y$			
$-2 \sin \frac{x + y}{2} \sin \frac{x - y}{2} = \cos x - \cos y$		$\sin u \cos v = \frac{1}{2}[\sin(u + v) + \sin(u - v)]$	
		$\cos u \sin v = \frac{1}{2}[\sin(u + v) - \sin(u - v)]$	
$\cos u \cos v = \frac{1}{2}[\cos(u + v) + \cos(u - v)]$		$\sin u \sin v = \frac{1}{2}[\cos(u + v) - \cos(u - v)]$	
Row-Echelon Form $\begin{bmatrix} 1 & 2 & -1 & 1 \\ 0 & 1 & 4 & -7 \\ 0 & 0 & 1 & -2 \end{bmatrix}$	Reduced Row-Echelon Form $\begin{bmatrix} 1 & 0 & 0 & -3 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & -2 \end{bmatrix}$	Using matrix inverses ( $AX = B \Rightarrow X = A^{-1}B$ ) $\begin{bmatrix} 2 & -5 \\ 3 & -6 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 15 \\ 36 \end{bmatrix} \Rightarrow \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -2 & \frac{5}{3} \\ -1 & \frac{2}{3} \end{bmatrix} \begin{bmatrix} 15 \\ 36 \end{bmatrix} = \begin{bmatrix} 30 \\ 9 \end{bmatrix}$	
Matrix Multiplication (columns of first = rows of second) $\begin{bmatrix} 1 & 3 \\ -1 & 0 \end{bmatrix} \begin{bmatrix} -1 & 5 & 2 \\ 0 & 4 & 7 \end{bmatrix} = \begin{bmatrix} 1 \cdot (-1) + 3 \cdot 0 & 1 \cdot 5 + 3 \cdot 4 & 1 \cdot 2 + 3 \cdot 7 \\ (-1) \cdot (-1) + 0 \cdot 0 & (-1) \cdot 5 + 0 \cdot 4 & (-1) \cdot 2 + 0 \cdot 7 \end{bmatrix} = \begin{bmatrix} -1 & 17 & 23 \\ 1 & -5 & -2 \end{bmatrix}$			
$2 \times 2$ Matrix Inverse If $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ , then $A^{-1} = \frac{1}{ad - bc} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$		$n \times n$ Matrix Inverse $\left[ \begin{array}{ccc ccc} 1 & -2 & -4 & 1 & 0 & 0 \\ 2 & -3 & -6 & 0 & 1 & 0 \\ -3 & 6 & 15 & 0 & 0 & 1 \end{array} \right] \rightarrow \left[ \begin{array}{ccc ccc} 1 & 0 & 0 & -3 & 2 & 0 \\ 0 & 1 & 0 & -4 & 1 & -\frac{2}{3} \\ 0 & 0 & 1 & 1 & 0 & \frac{1}{2} \end{array} \right]$	
$2 \times 2$ Matrix Determinant $\det(A) =  A  = \begin{vmatrix} a & b \\ c & d \end{vmatrix} = ad - bc$	Minor $M_{ij}$ : Take the matrix and delete the $i$ th row and the $j$ th column. Find the determinant	Cofactor $A_{ij}$ $(-1)^{i+j} M_{ij}$	
$n \times n$ Matrix Determinant (can move along any row/column) $\det(A) =  A  = \begin{vmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1} & a_{m2} & \cdots & a_{mn} \end{vmatrix} = a_{11}A_{11} + a_{12}A_{12} + \cdots + a_{1n}A_{1n}$			
Common Sums $\sum_{k=1}^n c = nc$ $\sum_{k=1}^n k = \frac{n(n+1)}{2}$ $\sum_{k=1}^n k^2 = \frac{n(n+1)(2n+1)}{6}$ $\sum_{k=1}^n k^3 = \frac{n^2(n+1)^2}{4}$			

<p>Algebra of Functions</p> <p>Let <math>f</math> and <math>g</math> be functions with domains <math>A</math> and <math>B</math>.</p> <p><math>(f + g)(x) = f(x) + g(x)</math> Domain <math>A \cap B</math></p> <p><math>(f - g)(x) = f(x) - g(x)</math> Domain <math>A \cap B</math></p> <p><math>(fg)(x) = f(x)g(x)</math> Domain <math>A \cap B</math></p> <p><math>\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)}</math> Domain <math>\{x \in A \cap B \mid g(x) \neq 0\}</math></p> <p><math>(f \circ g)(x) = f(g(x))</math> Domain <math>\{x \in B \mid g(x) \in A\}</math></p>	<p>Polynomial Synthetic Division</p> $(x^3 + x^2 - 1) \div (x + 2)$ $\begin{array}{r rrrr} -2 & 1 & 1 & 0 & -1 \\ & & -2 & 2 & -4 \\ \hline & 1 & -1 & 2 & -5 \end{array}$ <p>Result is <math>x^2 - x + 2 - \frac{5}{x+2}</math></p>	<p>Polynomial Long Division</p> $\begin{array}{r} x^2 - x + 2 \\ x+2 \overline{) x^3 + x^2 - 1} \\ \underline{-(x^3 + 2x^2)} \phantom{-1} \\ -x^2 \phantom{-1} \\ \underline{-(x^2 + 2x)} \phantom{-1} \\ 2x - 1 \end{array}$
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<p>Rational Roots Theorem</p> $2x^3 + 2x^2 - 3x - 6$ $\pm 1, \pm 2 \quad \pm 1, \pm 2, \pm 3, \pm 6$ <p>Possible rational roots:</p> $\pm 1, \pm \frac{1}{2}, \pm 2, \pm 3, \pm \frac{3}{2}, \pm 6$	<p>Decartes' Rule of Signs</p> <p>Count num. of sign changes</p> $P(x) = 3x^6 + 4x^5 + 3x^3 - x - 3$ <p>1 positive real root</p> $P(-x) = 3x^6 - 4x^5 - 3x^3 + x - 3$ <p>1 or 3 negative real roots</p>	<p>Logarithm Formulas</p> $\log(m \cdot n) = \log m + \log n$ $\log\left(\frac{m}{n}\right) = \log m - \log n$ $\log(m^n) = n \cdot \log m$ $\log_b b^x = x = b^{\log_b x}$	<p>Trigonometric Reciprocals</p> $\cot = \frac{1}{\tan}$ $\csc = \frac{1}{\sin}$ $\sec = \frac{1}{\cos}$
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<p>Horizontal Asymptotes</p> $y = \frac{2x^2 - 4x + 5}{x^2 - 2x + 1}$ <p>Original Equation</p> $= \frac{2x^2}{x^2}$ <p><math>x \rightarrow \infty</math>, other terms <math>\rightarrow</math> tiny</p> $= 2$ <p>Cancel, horizontal asymptote</p>	<p>Slant Asymptotes</p> $y = \frac{x^2 - 4x - 5}{x - 3}$ <p>Original Equation</p> $= x - 1 - \frac{8}{x - 3}$ <p>Divide</p> $= x - 1$ <p><math>x \rightarrow \infty</math>, other terms <math>\rightarrow</math> tiny</p>
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<p>Vertical Asymptotes</p> $y = \frac{2x^2 - 4x + 5}{x^2 - 2x + 1}$ <p>Original Equation</p> $= \frac{2x^2 - 4x + 5}{(2x - 1)(x + 2)}$ <p>Factor demoniator</p> $x = \frac{1}{2} \text{ or } x = -2$ <p>Impossible</p>	<p>End Behavior</p> $y = x^n$ <p><math>n</math> is even</p> $y = -x^n$ <p><math>n</math> is even</p> $y = x^n$ <p><math>n</math> is odd</p> $y = -x^n$ <p><math>n</math> is odd</p>	<p><math>m \times n</math> matrix</p> $\begin{bmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1} & a_{m2} & \cdots & a_{mn} \end{bmatrix}$
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<p><math>y = \sin x</math> in red; <math>y = \cos x</math> in blue</p> 	<p>sin/cos Graph Properties</p> <p>If in form:</p> $y = a \sin k(x - b)$ <p>amplitude <math> a </math>, period <math>2\pi/k</math>, phase shift <math>b</math></p>	<p>Allowed row operations</p> <ol style="list-style-type: none"> <li>1. Add a multiple of one row to another</li> <li>2. Multiply a row by a nonzero constant</li> <li>3. Interchange two rows</li> </ol>
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<p>If <math>\begin{cases} ax + by = r \\ cx + dy = s \end{cases}</math>, then <math>x = \frac{\begin{vmatrix} r &amp; b \\ s &amp; d \end{vmatrix}}{\begin{vmatrix} a &amp; b \\ c &amp; d \end{vmatrix}}</math> and <math>y = \frac{\begin{vmatrix} a &amp; r \\ c &amp; s \end{vmatrix}}{\begin{vmatrix} a &amp; b \\ c &amp; d \end{vmatrix}}</math></p>	<p>Vertical Parabola</p> $x^2 = 4py$ <p><math>V(0, 0)</math>, <math>F(0, p)</math>, directrix <math>y = -p</math></p>	<p>Ellipse</p> $\frac{x^2}{(a \text{ or } b)^2} + \frac{y^2}{(a \text{ or } b)^2} = 1$ $c^2 = a^2 - b^2$	<p>Eccentricity</p> $e = \frac{c}{a}$
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<p>Hyperbola</p> $\frac{x \text{ or } y^2}{a^2} - \frac{x \text{ or } y^2}{b^2} = 1$ $c^2 = a^2 + b^2$	<p>Shifted Conic</p> <p><math>V(h, k)</math>, <math>x</math> to <math>(x - h)</math>, <math>y</math> to <math>(y - k)</math></p>	<p>Polar Conics</p> $r = \frac{ed}{1 \pm e(\cos \text{ or } \sin)\theta}$	<p>Derivative Formula</p> $f^{-1}(a) = \lim_{h \rightarrow 0} \frac{f(a+h) - f(a)}{h}$	<p>Area</p> $A = \lim_{n \rightarrow \infty} \sum_{k=1}^n f(x_k) \Delta x$ $\Delta x = \frac{b - a}{n}$ $x_k = a + k \Delta x$
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<p>Horizontal Parabola</p> $y^2 = 4px$ <p><math>V(0, 0)</math>, <math>F(p, 0)</math>, directrix <math>x = -p</math></p>	<p>Parabolas</p> <p>Latus rectum is <math> 4p </math></p>	<p>Ellipses</p> $a^2 > b^2$ <p><math>x^2</math> first of terms means more horizontal, major axis length is <math>2a</math>, minor axis length is <math>2b</math>, latus rectum is <math>\frac{2b^2}{a}</math>, foci on major axis <math>F(\pm c, 0)</math> or <math>F(0, \pm c)</math></p>	<p><b>Hyperbolas</b> <math>a^2</math> forms positive term with <math>x</math> or <math>y</math>, horizontal when <math>x^2</math> is first of terms, <math>V(\pm a, 0)</math> or <math>V(0, \pm a)</math>, <math>B(0, \pm b)</math> or <math>B(\pm b, 0)</math>, transverse axis length is <math>2a</math>, conjugate axis length is <math>2b</math>, asymptote slopes <math>\pm \frac{b}{a}</math> or <math>\pm \frac{a}{b}</math>, foci on transverse axis <math>F(\pm c, 0)</math> or <math>F(0, \pm c)</math>, latus rectum is <math>\frac{2b^2}{a}</math></p>
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