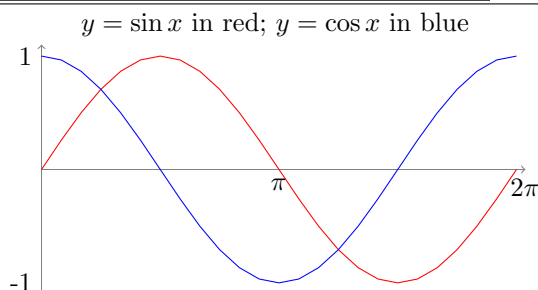


All Students Take Calculus I-All pos. II-sin III-tan IV-cos	Law of Cosines $a^2 = b^2 + c^2 - 2bc \cdot \cos A$	Difference of Cubes $a^3 \pm b^3 = (a \pm b)(a^2 \mp ab + b^2)$	Arc Length $s = r\theta$
Heron's Formula $A = \sqrt{s(s-a)(s-b)(s-c)}$	Change of Base $\log_b m = \frac{\log m}{\log b}$	Choose Formula $C(x, y) = \binom{x}{y} = \frac{x!}{y!(x-y)!}$	Law of Sines $\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$
Degrees to Radians $\frac{A \cdot \pi}{180} = \theta$	Sector Area $A = \frac{1}{2}r^2\theta$	Area of $\Delta$ $Area = ab \cdot \frac{1}{2} \sin C$	Polar to $(x, y)$ $r^2 = x^2 + y^2$ $\tan \theta = \frac{y}{x}$
			$(\log_a b)(\log_c d) = (\log_a d)(\log_c b)$
$z = a + bi$ $ z  = \sqrt{a^2 + b^2}$	$z = r \operatorname{cis} \theta$ $z^n = r^n \operatorname{cis}(n\theta)$	$n$ th roots of $z = r \operatorname{cis} \theta$ $w_k = r^{1/n} \operatorname{cis} \left( \frac{\theta + 2k\pi}{n} \right)$	$z_1 z_2 = r_1 r_2 \operatorname{cis}(\theta_1 + \theta_2)$ $\frac{z_1}{z_2} = \frac{r_1}{r_2} \operatorname{cis}(\theta_1 - \theta_2)$
			$\vec{v} = \langle a, b \rangle = a\hat{i} + b\hat{j}$ $ \vec{v}  = \sqrt{a^2 + b^2}$
			$ c\vec{u}  =  c  \vec{u} $
Dot Product $\vec{u} \cdot \vec{v} = a_1 a_2 + b_1 b_2$	Dot Product Theorem $\vec{u} \cdot \vec{v} =  \vec{u}  \vec{v}  \cos \theta$	$\theta$ between $\vec{u}$ & $\vec{v}$ $\cos \theta = \frac{\vec{u} \cdot \vec{v}}{ \vec{u}  \vec{v} }$	$\vec{u}$ and $\vec{v}$ are perpendicular $\vec{u} \cdot \vec{v} = 0$
			Component of $\vec{u}$ along $\vec{v}$ $(\vec{u} \cdot \vec{v})/ \vec{v} $
			$\operatorname{proj}_{\vec{v}} \vec{u} = \left( \frac{\vec{u} \cdot \vec{v}}{ \vec{v} ^2} \right) \vec{v}$
			Work $W = \vec{F} \cdot \vec{D}$
Trig Identities			
$\sin^2 + \cos^2 = 1$	$\tan^2 + 1 = \sec^2$	$1 + \cot^2 = \csc^2$	$2 \sin u \cos u = \sin(2u)$
			$\cos^2 u - \sin^2 u = \cos(2u)$
			$\frac{2 \tan u}{1 - \tan^2 u} = \tan(2u)$
$\sin u \cos v \pm \cos u \sin v = \sin(u \pm v)$	$\cos u \cos v \mp \sin u \sin v = \cos(u \pm v)$	$\frac{\tan u \pm \tan v}{1 \mp \tan u \tan v} = \tan(u \pm v)$	$\cot = \frac{1}{\tan}$
$\csc = \frac{1}{\sin}$	$\sec = \frac{1}{\cos}$	$\sin\left(\frac{\pi}{2} - u\right) = \cos u$	$\tan\left(\frac{\pi}{2} - u\right) = \cot u$
		$\sec\left(\frac{\pi}{2} - u\right) = \csc u$	$\cos\left(\frac{\pi}{2} - u\right) = \sin u$
$\cot\left(\frac{\pi}{2} - u\right) = \tan u$	$\csc\left(\frac{\pi}{2} - u\right) = \sec u$	$\frac{1 - \cos 2x}{2} = \sin^2 x$	$\frac{1 + \cos 2x}{2} = \cos^2 x$
		$\frac{1 - \cos 2x}{1 + \cos 2x} = \tan^2 x$	$\pm \sqrt{\frac{1 - \cos u}{2}} = \sin \frac{u}{2}$
$\pm \sqrt{\frac{1 + \cos u}{2}} = \cos \frac{u}{2}$	$\frac{1 - \cos u}{\sin u} = \frac{\sin u}{1 + \cos u} = \tan \frac{u}{2}$	$2 \sin \frac{x \pm y}{2} \cos \frac{x \mp y}{2} = \sin x \pm \sin y$	$2 \cos \frac{x + y}{2} \cos \frac{x - y}{2} = \cos x + \cos y$
$-2 \sin \frac{x + y}{2} \sin \frac{x - y}{2} = \cos x - \cos y$	$\sin u \cos v = \frac{1}{2}[\sin(u + v) + \sin(u - v)]$	$\cos u \sin v = \frac{1}{2}[\sin(u + v) - \sin(u - v)]$	
$\cos u \cos v = \frac{1}{2}[\cos(u + v) + \cos(u - v)]$	$\sin u \sin v = \frac{1}{2}[\cos(u + v) - \cos(u - v)]$		
Row-Echelon Form $\begin{bmatrix} 1 & 2 & -1 & 1 \\ 0 & 1 & 4 & -7 \\ 0 & 0 & 1 & -2 \end{bmatrix}$	Reduced Row-Echelon Form $\begin{bmatrix} 1 & 0 & 0 & -3 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & -2 \end{bmatrix}$	Using matrix inverses ( $AX = B \Rightarrow X = A^{-1}B$ ) $\begin{bmatrix} 2 & -5 \\ 3 & -6 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 15 \\ 36 \end{bmatrix} \Rightarrow \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -2 & \frac{5}{3} \\ -1 & \frac{2}{3} \end{bmatrix} \begin{bmatrix} 15 \\ 36 \end{bmatrix} = \begin{bmatrix} 30 \\ 9 \end{bmatrix}$	
Matrix Multiplication!			
$\begin{bmatrix} 1 & 3 \\ -1 & 0 \end{bmatrix} \begin{bmatrix} -1 & 5 & 2 \\ 0 & 4 & 7 \end{bmatrix} = \begin{bmatrix} 1 \cdot (-1) + 3 \cdot 0 & 1 \cdot 5 + 3 \cdot 4 & 1 \cdot 2 + 3 \cdot 7 \\ (-1) \cdot (-1) + 0 \cdot 0 & (-1) \cdot 5 + 0 \cdot 4 & (-1) \cdot 2 + 0 \cdot 7 \end{bmatrix} = \begin{bmatrix} -1 & 17 & 23 \\ 1 & -5 & -2 \end{bmatrix}$			
$2 \times 2$ Matrix Inverse If $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ then $A^{-1} = \frac{1}{ad - bc} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$		$n \times n$ Matrix Inverse $\left[ \begin{array}{ccc ccc} 1 & -2 & -4 & 1 & 0 & 0 \\ 2 & -3 & -6 & 0 & 1 & 0 \\ -3 & 6 & 15 & 0 & 0 & 1 \end{array} \right] \rightarrow \left[ \begin{array}{ccc ccc} 1 & 0 & 0 & -3 & 2 & 0 \\ 0 & 1 & 0 & -4 & 1 & -\frac{2}{3} \\ 0 & 0 & 1 & 1 & 0 & \frac{1}{2} \end{array} \right]$	
$2 \times 2$ Matrix Determinant $\det(A) =  A  = \begin{vmatrix} a & b \\ c & d \end{vmatrix} = ad - bc$	Minor $M_{ij}$ : Take the matrix and delete the $i$ th row and the $j$ th column. Find the determinant	Cofactor $A_{ij}$ $(-1)^{i+j} M_{ij}$	
Common Sums			
$\sum_{k=1}^n c = nc$			
$\sum_{k=1}^n k = \frac{n(n+1)}{2}$			
$\sum_{k=1}^n k^2 = \frac{n(n+1)(2n+1)}{6}$			
$\sum_{k=1}^n k^3 = \frac{n^2(n+1)^2}{4}$			
$n \times n$ Matrix Determinant (can move along any row/column)			
$\det(A) =  A  = \begin{vmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1} & a_{m2} & \cdots & a_{mn} \end{vmatrix} = a_{11}A_{11} + a_{12}A_{12} + \cdots + a_{1n}A_{1n}$			

Algebra of Functions		Polynomial Synthetic Division	Polynomial Long Division
Let $f$ and $g$ be functions with domains $A$ and $B$ . $(f + g)(x) = f(x) + g(x)$ Domain $A \cap B$ $(f - g)(x) = f(x) - g(x)$ Domain $A \cap B$ $(fg)(x) = f(x)g(x)$ Domain $A \cap B$ $\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)}$ Domain $\{x \in A \cap B \mid g(x) \neq 0\}$ $(f \circ g)(x) = f(g(x))$ Domain $\{x \in B \mid g(x) \in A\}$		$(x^3 + x^2 - 1) \div (x + 2)$ $-2 \left  \begin{array}{rrrr} 1 & 1 & 0 & -1 \\ & -2 & 2 & -4 \\ \hline 1 & -1 & 2 & -5 \end{array} \right.$	$x^2 - x + 2$ $x + 2 \overline{) x^3 + x^2 - 1}$ $\underline{-(x^3 + 2x^2)}$ $-x^2$ $\underline{-(x^2 + 2x)}$ $2x - 1$
Rational Roots Theorem $2x^3 + 2x^2 - 3x - 6$ $\pm 1, \pm 2$ $\pm 1, \pm 2, \pm 3, \pm 6$ Possible rational roots: $\pm 1, \pm \frac{1}{2}, \pm 2, \pm 3, \pm \frac{3}{2}, \pm 6$	Decartes' Rule of Signs Count num. of sign changes $P(x) = 3x^6 + 4x^5 + 3x^3 - x - 3$ 1 positive real root $P(-x) = 3x^6 - 4x^5 - 3x^3 + x - 3$ 1 or 3 negative real roots	Logarithm Formulas $\log(m \cdot n) = \log m + \log n$ $\log\left(\frac{m}{n}\right) = \log m - \log n$ $\log(m^n) = n \cdot \log m$ $\log_b b^x = x = b^{\log_b x}$	Other trig stuff $\cot = \frac{1}{\tan}$ $\csc = \frac{1}{\sin}$ $\sec = \frac{1}{\cos}$
Horizontal Asymptotes $y = \frac{2x^2 - 4x + 5}{x^2 - 2x + 1}$ Original Equation $= \frac{2x^2}{x^2}$ $x \rightarrow \infty$ , other terms $\rightarrow$ tiny $= 2$ Cancel, horizontal asymptote		Slant Asymptotes $y = \frac{x^2 - 4x - 5}{x - 3}$ Original Equation $= x - 1 - \frac{8}{x - 3}$ Divide $= x - 1$ $x \rightarrow \infty$ , other terms $\rightarrow$ tiny	
Vertical Asymptotes $y = \frac{2x^2 - 4x + 5}{x^2 - 2x + 1}$ Original Equation $= \frac{2x^2 - 4x + 5}{(2x - 1)(x + 2)}$ Factor demoniator $x = \frac{1}{2}$ or $x = -2$ Impossible		End Behavior $y = x^n$ $y = -x^n$ $n$ is even $n$ is even $y = x^n$ $y = -x^n$ $n$ is odd $n$ is odd	$m \times n$ matrix $\begin{bmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1} & a_{m2} & \cdots & a_{mn} \end{bmatrix}$
		sin/cos Graph Properties If in form: $y = a \sin k(x - b)$ amplitude $ a $ , period $2\pi/k$ , phase shift $b$	
Allowed row operations 1. Add a multiple of one row to another 2. Multiply a row by a nonzero constant 3. Interchange two rows			
If $\begin{cases} ax + by = r \\ cx + dy = s \end{cases}$ then $x = \frac{\begin{vmatrix} r & b \\ s & d \end{vmatrix}}{\begin{vmatrix} a & b \\ c & d \end{vmatrix}}$ and $y = \frac{\begin{vmatrix} a & r \\ c & s \end{vmatrix}}{\begin{vmatrix} a & b \\ c & d \end{vmatrix}}$	Parabola $x^2 = 4py$ $V(0, 0)$ , $F(0, p)$ , directrix $y = -p$	Ellipse $\frac{x^2}{(a \text{ or } b)^2} + \frac{y^2}{(a \text{ or } b)^2} = 1$ $c^2 = a^2 - b^2$	
Eccentricity $e = \frac{c}{a}$			
Hyperbola $\frac{x^2}{ab^2} - \frac{y^2}{b^2} = 1$ $c^2 = a^2 + b^2$	General Conic $\frac{d(P, F)}{d(P, l)} = e$	Polar Conics $r = \frac{ed}{1 \pm e(\cos \text{ or } \sin)\theta}$	Derivative Formula $f^{-1}(a) = \lim_{h \rightarrow 0} \frac{f(a + h) - f(a)}{h}$
Area $A = \lim_{n \rightarrow \infty} \sum_{k=1}^n f(x_k) \Delta x$ $\Delta x = \frac{b - a}{n}$ $x_k = a + k\Delta x$			