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Positive Trigonometric
                                                                                                                                          Arc
                                                                                               Difference of Cubes
                                                           Law of Cosines
                 Functions
                                                                                                                                       Length
                                                                                          a^3 \pm b^3 = (a \pm b)(a^2 \mp ab + b^2)
                                                      a^2 = b^2 + c^2 - 2bc \cdot \cos A
 I-All pos. II-sin III-tan IV-cos
                                                                                                                                       s = r\theta
                                                 Change of Base
                                                                                     Choose Formula
                                                                                                                                    Heron's Formula
                                                \log_b m = \frac{\log m}{\cdot}
                                                                                                                            \sin A
                                                                                                                                                      \sin C
                                                                             C(x,y) =
 A = \sqrt{s(s-a)(s-b)(s-c)}
                                                               \log b
                                                                                       Polar to (x, y)

r^2 = x^2 + y^2

\tan \theta = \frac{y}{x}
 Degrees to Radians
                                  Sector Area
                                                              Area of \Delta
                                    A = \frac{1}{2}r^2\theta
                                                        Area = ab \cdot \frac{1}{2}\sin C
         A \cdot \pi
                                                                                                                 (\log_a b)(\log_c d) = (\log_a d)(\log_c b)
          180
                                                        nth roots of z = r \operatorname{cis} \theta
                                                                                                 z_1 z_2 = r_1 r_2 \operatorname{cis}(\theta_1 + \theta_2) 
 \frac{z_1}{\theta_1} = \frac{r_1}{\theta_2} \operatorname{cis}(\theta_1 - \theta_2)
                                                                                                                                       \vec{v} = \langle a, b \rangle = a\hat{\imath} + b\hat{\jmath}
                                z = r \operatorname{cis} \theta
     z = a + bi
                                                                                                                                                                       |c\vec{u}| = |c||\vec{u}|
 |z| = \sqrt{a^2 + b^2}
                                                                                                                                         |\vec{v}| = \sqrt{a^2 + b^2}
                            z^n = r^n \operatorname{cis}(n\theta)
                                                           \theta between \vec{u} \cdot \vec{v} \vec{v}
                                 Dot Product
                                                                                                                 Component
                                                                                         \vec{u} and \vec{v} are
    Dot Product
                                                                                                                                                                            Work
                                   Theorem
                                                                                                                of \vec{u} along \vec{v}
                                                                                       prependicular
                                                             \cos \theta =
 \vec{u} \cdot \vec{v} = a_1 a_2 + b_1 b_2
                                                                                                                                                                         W = \vec{F} \cdot \vec{D}
                              \vec{u} \cdot \vec{v} = |\vec{u}| |\vec{v}| \cos \theta
                                                                                           \vec{u}\cdot\vec{v}=0
                                                                                                                  (\vec{u}\cdot\vec{v})/|\vec{v}|
                                                                                  Trig Identities
  \sin^2 + \cos^2 = 1 || \tan^2 + 1 = \sec^2 || 1 + \cot^2 = \csc^2 || 2 \sin u \cos u = \sin(2u) ||
                                                                                                                  \cos^2 u - \sin^2 u = \cos(2u) \left| \frac{2 \tan u}{1 - \tan^2 u} = \tan(2u) \right|
         \sin u \cos v \pm \cos u \sin v = \sin(u \pm v) || \cos u \cos v \mp \sin u \sin v = \cos(u \pm v)|
                                             \left|\sin\left(\frac{\pi}{2}-u\right)=\cos u\right|\left|\tan\left(\frac{\pi}{2}-u\right)=\cot u\right|\left|\sec\left(\frac{\pi}{2}-u\right)=\csc u\right|
                                                                    \frac{1-\cos 2x}{2} = \sin^2 x \left| \frac{1+\cos 2x}{2} = \cos^2 x \right|
                                    \csc\left(\frac{\pi}{2}-u\right) = \sec u
    \cot\left(\frac{\pi}{2}-u\right)=\tan u\,|\,|
                                      \frac{1-\cos u}{\sin u} = \frac{\sin u}{1+\cos u} = \tan \frac{u}{2} \left| 2\sin \frac{x\pm y}{2}\cos \frac{x+y}{2} = \sin x \pm \sin y \right| 2\cos \frac{x+y}{2}\cos \frac{x-y}{2} = \cos x + \cos y
       \pm \sqrt{\frac{1+\cos u}{2}} = \cos \frac{u}{2}
        -2\sin\frac{x+y}{2}\sin\frac{x-y}{2} = \cos x - \cos y \sin u \cos v = \frac{1}{2}[\sin(u+v) + \sin(u-v)] \cos u \sin v = \frac{1}{2}[\sin(u+v) - \sin(u-v)]
                                 \cos u \cos v = \frac{1}{2} [\cos(u+v) + \cos(u-v)] |\sin u \sin v = \frac{1}{2} [\cos(u+v) - \cos(u-v)]
                                          Reduced
 Row-Echelon Form
                                                                                     Using matrix inverses (AX = B \Rightarrow X = A^{-1}B)
                                   Row-Echelon Form
   1 2
             -1
                        1
                                       1 \quad 0 \quad 0 \quad -3
                                                                       2 -5
   0 1
                4
                      -7
                                       0 \ 1 \ 0
                                                       1
                                                                       3 -6
                      -2
                                       0 \ 0 \ 1 \ -2
                                                              Matrix Multiplication!
                                             n \times n Matrix Inverse
                                                                                            -3 -6
                                                                                                             0 \ 1 \ 0
                                                                                                                                        0 \ 1 \ 0
                                                                                                                                                          -4 1
                                                                                               6
                                                                                                                                        0 \ 0 \ 1
                                                                                                                                                            1 0
     2 \times 2 Matrix Determinant
                                                      Minor M_{ij}: Take the matrix and
                                                                                                           Cofactor A_{ij}
                                                        delete the ith row and the jth
\det(A) = |A| =
                                                                                                            (-1)^{i+j}M_{ij}
                                     =ad-bc
                                                        column. Find the determinant
                                                                                                                           Common Sums
        n \times n Matrix Determinant (can move along any row/column)
                                    a_{12}
                                    a_{22}
                                                              = a_{11}A_{11} + a_{12}A_{12} + \dots + a_{1n}A_{1n}
\det(A) = |A| =
                                   a_{m2}
                                                     a_{mn}
                                                                                                                      \sum_{n=0}^{n} k^3 = \frac{n^2(n+1)^2}{4}
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Algebra of Functions

Let f and g be functions with domains A and B.

$$(f+g)(x) = f(x) + g(x)$$
 Domain $A \cap B$

$$(f-g)(x) = f(x) - g(x)$$
 Domain $A \cap B$

$$(fg)(x) = f(x)$$
 $g(x)$ Domain $A \cap B$

$$\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)} \qquad \qquad \text{De}$$

Domain
$$\{x \in A \cap B \mid g(x) \neq 0\}$$

$$(f \circ g)(x) = f(g(x))$$

Domain
$$\{x \in B \mid g(x) \in A\}$$

Polynomial Synthetic Division

Result is
$$x^2 - x + 2 - \frac{5}{x+2}$$

Polynomial Long Division

$$\begin{array}{r}
x+2) \overline{\smash{)} x^3 + x^2 - 1} \\
\underline{-x^3 - 2x^2} \\
-x^2 \\
\underline{-x^2 + 2x}
\end{array}$$

Rational Roots Theorem $2x^3 + 2x^2 - 3x - 6$ $\pm 1, \pm 2, \pm 3, \pm 6$ $\pm 1, \pm 2$ Possible rational roots: $\pm 1, \pm \frac{1}{2}, \pm 2, \pm 3, \pm \frac{3}{2}, \pm 6$

Decartes' Rule of Signs
Count num. of sign changes
$$P(x) = 3x^6 + 4x^5 + 3x^3 - x - 3$$
1 positive real root
$$P(-x) = 3x^6 - 4x^5 - 3x^3 + x - 3$$
1 or 3 negative real roots

Logarithm Formulas
$$\log(m \cdot n) = \log m + \log n$$
$$\log\left(\frac{m}{n}\right) = \log m - \log n$$
$$\log(m^n) = n \cdot \log m$$
$$\log_b b^x = x = b^{\log_b x}$$

Trigonometric
Reciprocals
$$\cot = \frac{1}{\tan}$$

$$\csc = \frac{1}{\sin}$$

$$\sec = \frac{1}{\cos}$$

$$y = \frac{2x^2 - 4x + 5}{x^2 - 2x + 1}$$
 Original Equation
$$2x^2$$

$$x\to\infty, \text{other terms}\to \text{tiny}$$

Slant Asymptotes
$$x^2 - 4x - 5$$

$$y = \frac{x^2 - 4x - 5}{x - 3}$$
 Original Equation

$$= x - 1 - \frac{8}{x - 3} \quad \text{Divide}$$

$$= x - 1$$

$$x \to \infty$$
, other terms $\to \text{tiny}$

Vertical Asymptotes

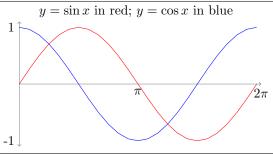
$$y = \frac{2x^2 - 4x + 5}{x^2 - 2x + 1}$$
 Original Equation
$$= \frac{2x^2 - 4 + 5}{(2x - 1)(x + 2)}$$
 Factor demoniator

$$x = \frac{1}{2} \text{ or } x = -2$$

Impossible

End Behavior
$$y = x^{n} \xrightarrow{f} y = -x^{n} \xrightarrow{f} y = -x^{n} \xrightarrow{f} y = x^{n} \xrightarrow{f} y = -x^{n} \xrightarrow{f} y$$

$$\begin{bmatrix} m \times n \text{ matrix} \\ a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1} & a_{m2} & \cdots & a_{mn} \end{bmatrix}$$



sin/cos Graph Properties If in form:

 $y = a \sin k(x - b)$ amplitude |a|, period $2\pi/k$, phase shift b

Allowed row operations

- 1. Add a multiple of one row to another
- 2. Multiply a row by a nonzero constant
- 3. Interchange two rows

If
$$\begin{cases} ax + by = r \\ cx + dy = s \end{cases}$$
, then $x = \begin{vmatrix} r & b \\ s & d \end{vmatrix}$ and $y = \begin{vmatrix} a & r \\ c & s \end{vmatrix}$

Vertical Parabola
$$x^2 = 4py$$
 $V(0,0), F(0,p),$ directrix $y = -p$

Ellipse

$$\frac{x^2}{(a \text{ or } b)^2} + \frac{y^2}{(a \text{ or } b)^2} = 1$$

$$c^2 = a^2 - b^2$$

Eccentricity
$$e = \frac{c}{a}$$
,

$$\frac{x \text{ or } y^2}{a^2} - \frac{x \text{ or } y^2}{b^2} = 1$$
$$c^2 = a^2 + b^2$$

General
Conic
$$\frac{d(P, F)}{d(P, l)} = e$$

$$r = \frac{\text{Polar Conics}}{1 \pm e(\cos \text{ or } \sin)\theta}$$

Derivative Formula
$$f^{-1}(a) = \lim_{h \to 0} \frac{f(a+h) - f(a)}{h}$$

Derivative Formula
$$f^{-1}(a) = \lim_{h \to 0} \frac{f(a+h) - f(a)}{h}$$

$$A = \lim_{n \to \infty} \sum_{k=1}^{n} f(x_k) \Delta x$$

$$\Delta x = \frac{b-a}{n}$$

$$x_k = a + k\Delta x$$

Horizontal Parabola $y^2 = 4px$ V(0,0), F(p,0),directrix x = -p

Parabolas Latus rectum is |4p|

Ellipses $a^2 > b^2$

 x^2 first of terms means more horizontal, major axis length is 2a, minor axis length is 2b, latus rectum is $\frac{2b^2}{a}$, foci on major axis $F(\pm c,0)$ or $F(0,\pm c)$

Hyperbolas a^2 forms positive term with x or y, horizontal when x^2 is first of terms, $V(\pm a, 0)$ or $V(0, \pm a)$, $B(0, \pm b)$ or $B(\pm b, 0)$, transverse axis length is 2a, conjugate axis length is 2b, asymtote slopes $\pm \frac{b}{a}$ or $\pm \frac{a}{b}$, foci on transverse axis $F(\pm c,0)$ or $F(0,\pm c)$, latus rectum is $\frac{2b^2}{c}$