

- Diode under no biased condition
 - Near the junction the e⁻ from n-type recombine from the free holes from p-type leaving the immobile ions
 - This oppositely charged ions in both sides are called as space charge region
 - The electric field created by the space charge region opposes the diffusion process or recombination process of e⁻ and holes
 - There are two con phenomenon the diffusion ~~and~~ on recombination process.
 - ↳ creates more space charge region and electric field (generated by space charge) that tend to counteract the recombination process.
 - Near the junction no free charge carriers are available so it is called 'depletion region'.

- Diode under forward biased condition

Diode current equation

$$I_D = I_s (e^{\frac{V}{nV_T}} - 1)$$

V_T → Threshhold voltage equivalent of temperature

I_D - current through diode

V - Voltage across diode

n - constant = 1 → (Germanium)

= 2 → (Silicon) ($V < V_T$)

on 1

if ($V > V_T$)

$$V_T = \frac{T(K) \times k}{q}$$

k → Boltzmann constant

q → charge

T → temp in K.

$$1.6 \times 10^{-19} C = 1 \text{ eV}$$

on

$$\boxed{I_D = I_s \left(e^{\frac{kV_D}{T_K}} - 1 \right)}$$

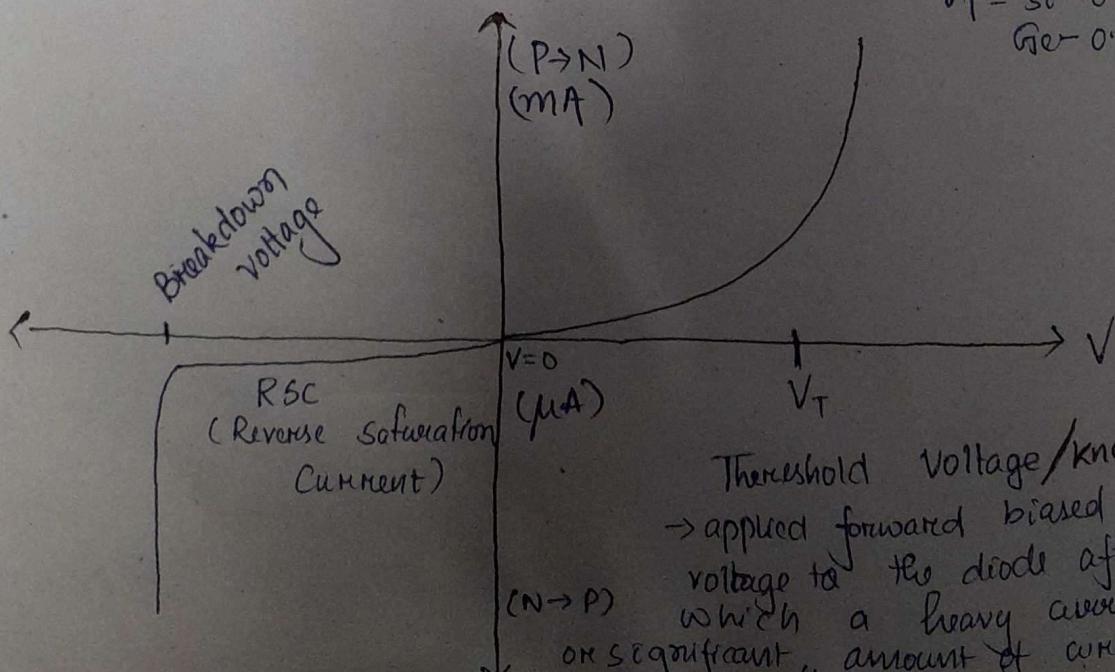
$$k = \frac{11600}{q}$$

V-I characteristics of Diode

For → Germanium
diode the reverse saturation current is higher.

$$V_T - Si - 0.7 V$$

$$Ge - 0.3 V$$



Threshold Voltage/knee voltage
→ applied forward biased voltage to the diode after which a heavy amount of current flows.

- The mechanism due to which there is a current flow due to minority charge carrier is called Avalanche breakdown.
- It is due to the collision with the covalent bonds which results in generation of e-hole pair

Zener

- It occurs in heavily doped diode
- When the reverse voltage increases across the diode also increases (the E·F is created due to the wide depletion region near the junction)
- This high E·F exerts a large force on a bonded electron to tear it out from its covalent bond. Thus a direct rupture of covalent bond produces a large no. of e-hole pairs; thereby increases the reverse current.
- Zener breakdown occurs at lower reverse voltage than avalanche breakdown
- Zener breakdown \uparrow with rise in temp.
- Diode Resistance: we can compute 3 types of resistance
 - R_{DC} → DC resistance
 - R_{AC} → AC resistance.
 - average resistance
- DC: it is the constant voltage by a particular current at that voltage
- average: if the voltage varies within a particular range
- AC resistance the inst resistance value on AC resistance value by diff the current eqn will V_f and

$$R_{\text{ac}} = \frac{26m}{I}$$

(dynamic resistance)

The RSC at 300K for Ge diode is $5\mu\text{A}$. Find the voltage to be applied across the junction to obtain a forward current of $50\mu\text{A}$

$$I_D = I_S (e^{\frac{V}{V_T}} - 1)$$

$$T = 300$$

$$I_S = 5\mu\text{A}$$

$$V_T = \frac{300 \times 1.38 \times 10^{-23}}{1.6 \times 10^{-19}}$$

$$= 0.025 \text{ V}$$

$$= 25 \text{ mV}$$

$$= 26 \text{ mV}$$

$$50 \times 10^{-3} = 5 \times 10^{-6} (e^{\frac{V}{10^3 \times 26}} - 1)$$

$$10^4 = e^{\frac{V}{10^3 \times 26}} - 1$$

$$26 \times 10^{-3} \times \ln(10^4 + 1) = V$$

$$0.239 \text{ V}$$

$$= 0.24 \text{ V}$$

Current flowing through a P-N junction diode is 60 mA for a forward voltage of 0.9 V . Determine static and dynamic resistance offered by the diode.

$$\text{Static} = \frac{0.9}{60 \times 10^{-3}} = \frac{900}{60} = 15$$

$$\text{dynamic} = \frac{26 \times 1}{60 \times 10^{-3}} = \frac{26000}{60} = 433.33 \approx 52$$

Diode equivalent circuit

An eq circuit is combination of elements properly chosen to ^{best} represent the actual characteristics of a component or system in a particular operating loop

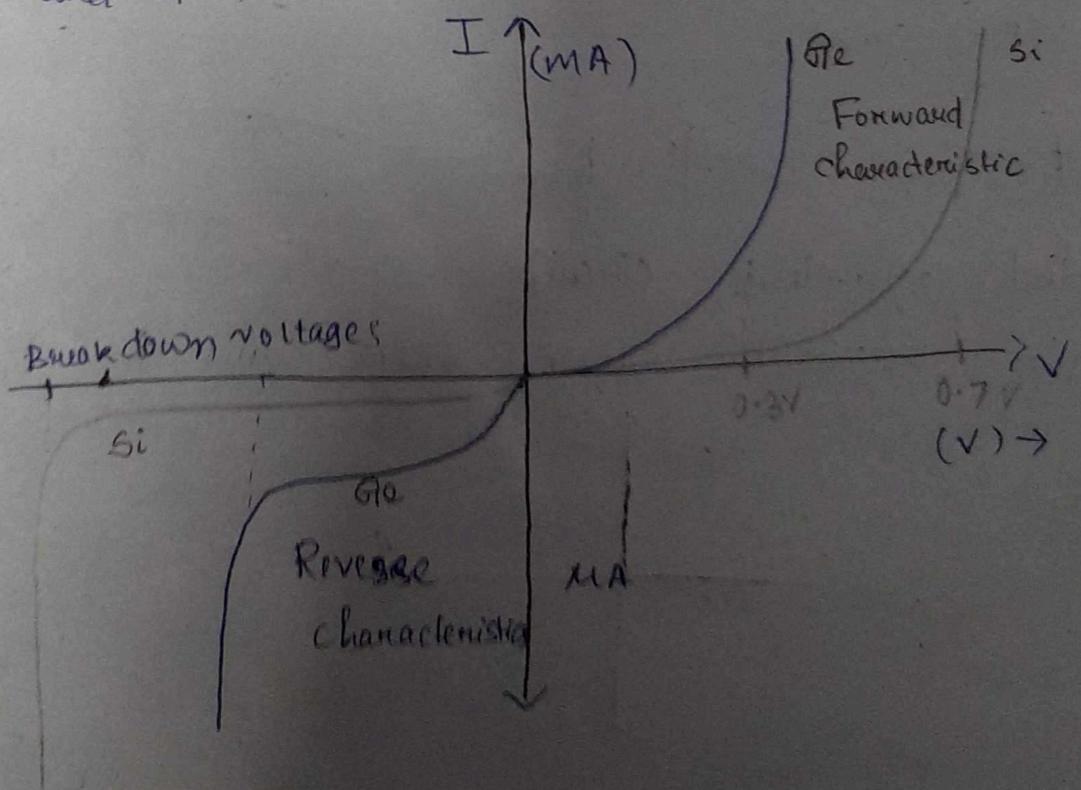
For diode we have 3 diff eq circuit

→ Piece wise linear eq circuit

→ Simplified eq circuit

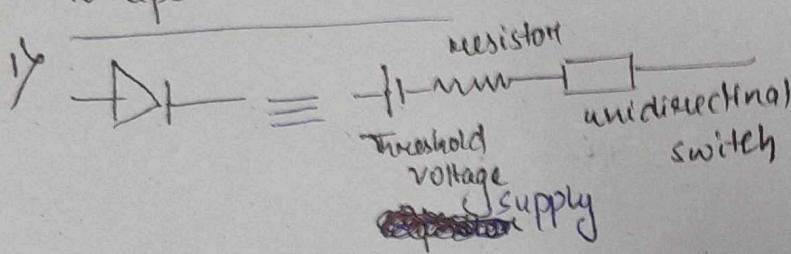
→ ideal eq circuit

Draw and compare V-I characteristics for Si and Ge DIODE



- 1) The threshold voltage for Germanium is 0.3V
 The threshold voltage for Silicon is 0.7V.
- 2) Reverse saturation current is few nanoamperes for Si
 and few microamperes for Ge diode
- 3) The breakdown voltage in reverse characteristic is more for Si than Ge diode.

To replace a diode



piece wise linear equivalent circuit

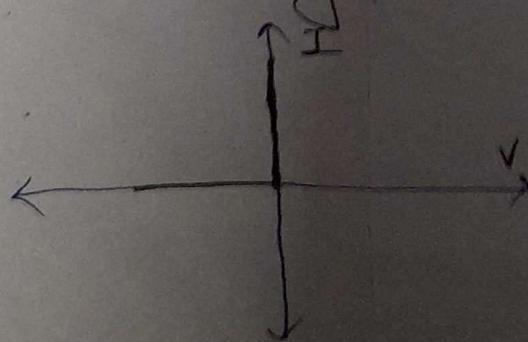
IV) Simplified equivalent circuit

The resistance is ignored as its value is very small.



IV) Ideal equivalent circuit

the threshold voltage is zero and R_{SC} is also zero.



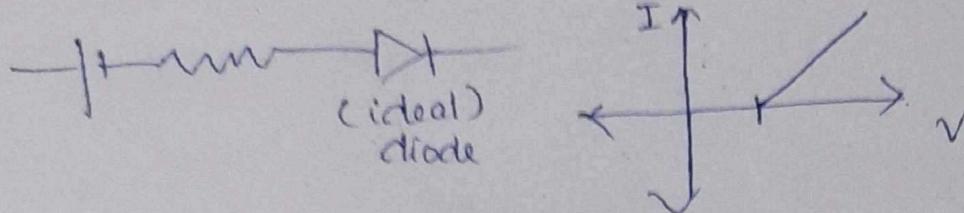
5
II

Diode applications:

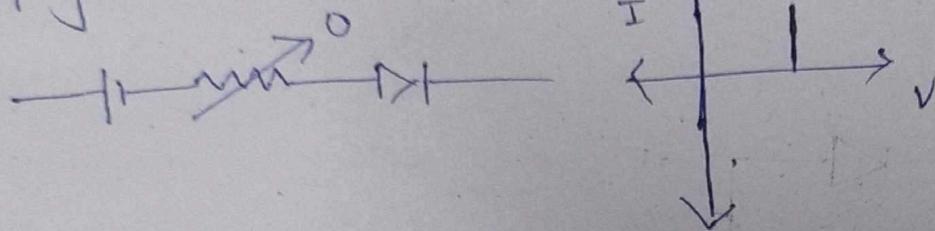
- It is used as a switch (allows the current in one direction) - ideal diode

VI characteristics of

i) Piece wise linear equivalent circuit

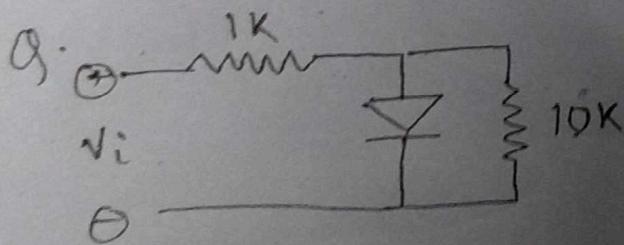


ii) Simplified linear equivalent circuit

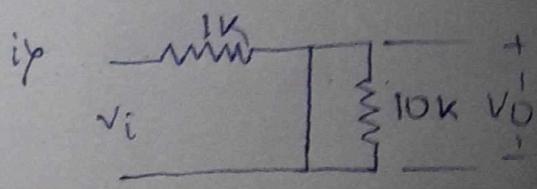


1) Check diode biasing
if diode is reverse biased then replace it with an open circuit

2) If diode is forward biased check its type
→ if it's ideal → short circuit equivalent
→ if it's practical diode → threshold voltage

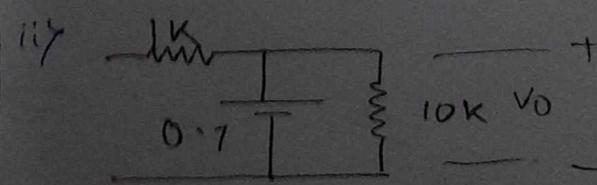


$$v_i = 5V$$



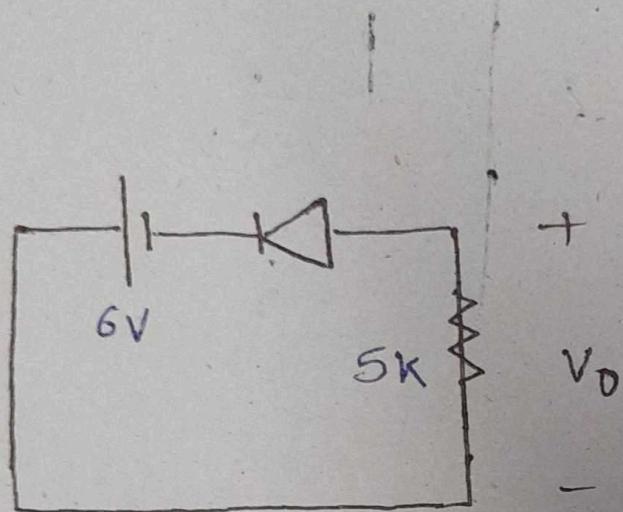
ideal diode

$$v_o = 0$$

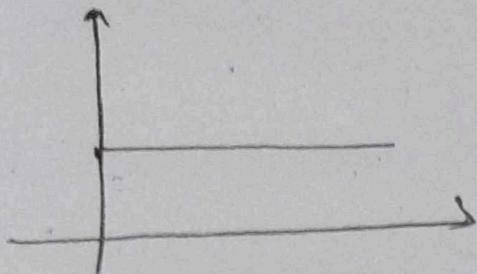


$$v_o = 0.7V$$

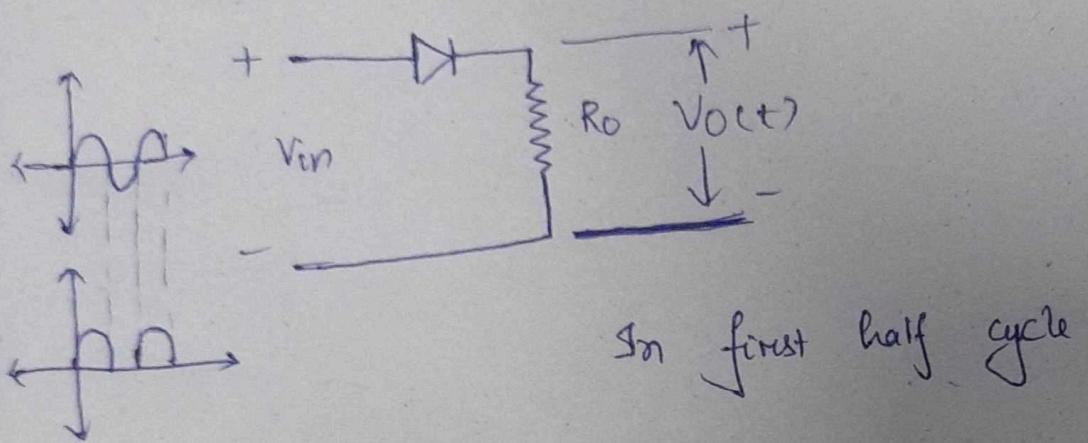
iii



Pure DC Voltage \rightarrow along with direction magnitude
also constant



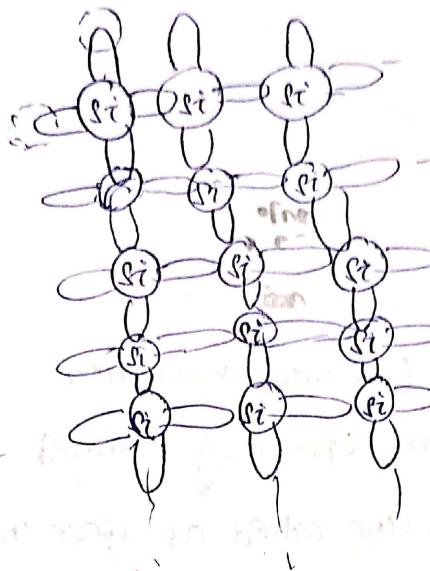
HALF WAVE RECTIFIER



Q Find the half wave rectifier output if the diode
is a Si diode.

Electronic Components

- Diode
- Transistor
- BPT
- Field Effect Transistor



Mom

Si → 2, 8, 4

4 e⁻ outermost orbital

1 pentavalent dopant

generate one free e⁻

1 free e⁻ → 1 e⁻ ion

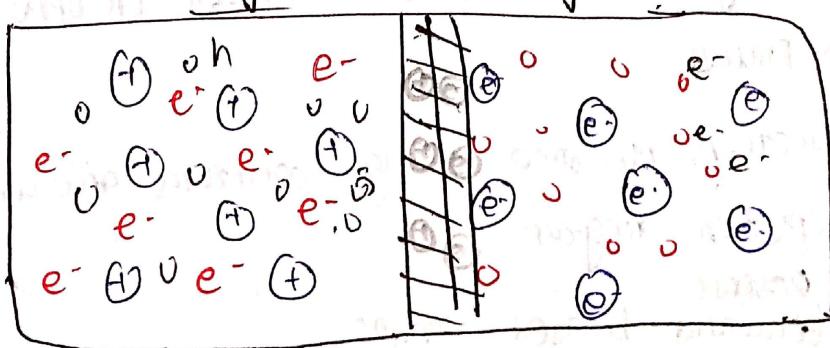
→ At room temp. it may happen that covalent bond will absorb energy and the bond breaks;

→ The e⁻ may absorb from core valency bond to conduction band, and absence of e⁻ is created (e⁺ called hole)

when 1 covalent bond breaks → 1 hole

N-type

P-type

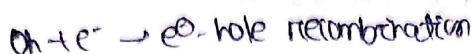
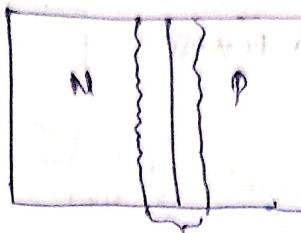
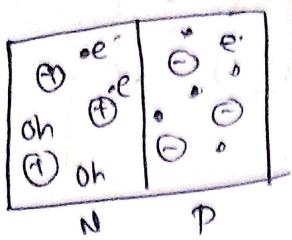


→ whenever a covalent pair breaks, a pair of hole & electron is created. an electron & hole will recombine & form an electron-hole recombination and both will disappear.

Electronic component:

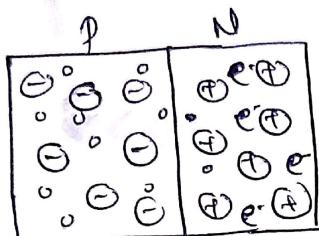
Diode

Bipolar junction transistor



depletion region - region sandwiched between the N & P (depleted region)

Diode under no-bias condition:



P junction:

majority-hole
minority-e⁰

N-junction

majority-e⁰
minority-hole

→ e⁰ and hole both recombine

→ electric field is created inside the diode

→ Near the junction, the e⁰ from N-type, recombine with the P-hole,

leaving immobile ions

→ These oppositely charged ions in both the side of the junction are called space-charge region.

→ The electric field created by the space-charge region opposes the diffusion process (recombination process) of e⁰s and holes

→ There are 2 concurrent phenomenon, that tends to generate more

Space charge & the electric field (generated by space charge) to

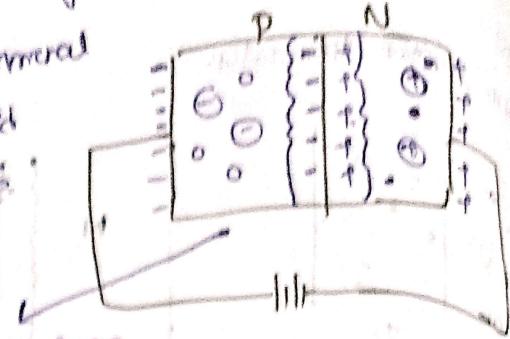
counteract (or) oppose the recombination process

→ Near the junction, no free charge carriers available which is

as depletion region

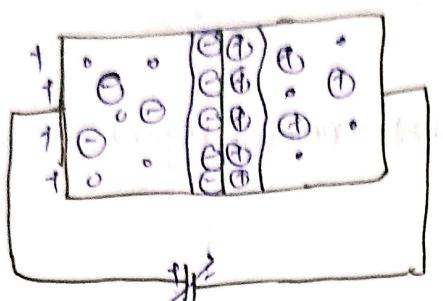
Diodes under Reverse Bias Condition:

- Holes are more attracted by \ominus charge generated by battery
- When P is connected to negative terminal then it is said to be reverse biased
- That low current is called reverse bias



Diodes under Forward Biased Cond:

No free charge carriers are there



More depletion region
space charge layer

Diode Current eqn:

$$I_D = I_S (e^{\frac{V}{nV_T}} - 1)$$

I_D = current to diode

V = voltage across diode

n is a constant value = 1 (for Germanium)

for $n=2$ (silicon) \rightarrow V applied is very low

higher diode $\rightarrow n \geq 1(10)$ \rightarrow V applied \rightarrow threshold current

V_T = $-kT$ volt-equivalent of temperature

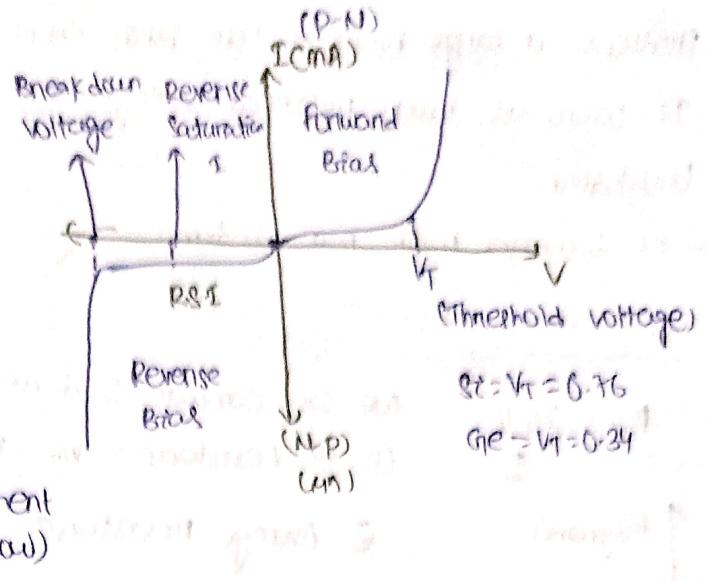
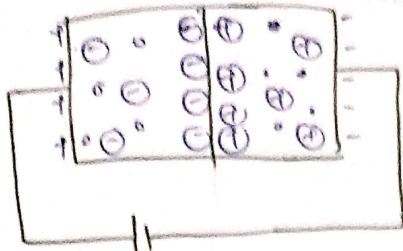
$$V_T = T \cdot k / q \rightarrow \text{charge of } e = 1.6 \times 10^{-19} C$$

Temperature Boltzmann's constant $\rightarrow 1.38 \times 10^{-23}$ Coulomb

$$I_D = I_S (e^{\frac{V_D}{nV_T}} - 1)$$

$$K = \frac{11600}{n}$$

V1 Characteristic of Diode



Threshold voltage is the applied voltage forward biased voltage to the diode after which the significant amt of current flows in the diode.

* Covalent Bond breaking \rightarrow hole pair generate \rightarrow due to collide

Reverse Biased \rightarrow V_1 , $kT/1$, lots of covalent bond break \rightarrow hole pair generate \downarrow minority carriers \leftarrow majority

(That mechanism is called Avalanche breakdown)

* Diode Breakdown:-

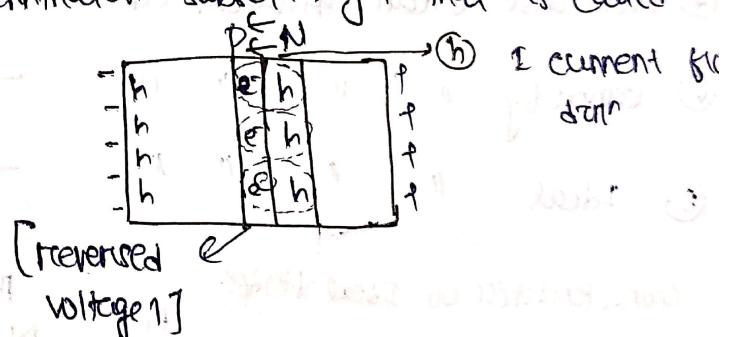
Minority charge carrier concentration subsequently 1 that is called

Diode breakdown

[Reverse biased current \rightarrow

flow due to carrier (minority)]

depletion region 1]



Zener Breakdown:-

It occurs in heavily doped diode. When reverse bias voltage increases, the electric field across diode also

(The electric field is created due to the wide depletion region near the junction. This high E field exerts a large force on a bonded e- to tear out from its covalent bond. Thus the direct structure of covalent bond

produces a large no. of hole pairs, thereby 1 reverse current
It occurs at lower reversed voltage as compared to avalanche
breakdown.

- It decreases with rise in temp

Diode Resistances

$$R_{ac} = \frac{26\eta}{I}$$

we can compute 3 diode resistance

$$\textcircled{1} \text{ DC Resistance} = V/I = \text{fixed}$$

$$\begin{cases} R_{dynamic} \\ R_{instantaneous} \end{cases}$$

$$\textcircled{2} \text{ Average Resistance} = \frac{V_{max} - V_{min}}{I_{max} - I_{min}}$$

If applied voltage varies with range $V_{min} \rightarrow V_{max}$

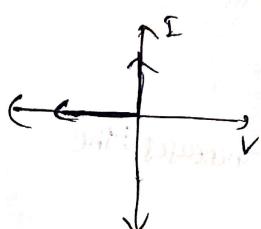
corresponding current varies $I_{min} \rightarrow I_{max}$

- The Instantaneous resistance value = differentiating current eqn w.r.t. applied voltage V_A

- A equivalent circuit combination of element properly chosen to be represent the actual characteristics of a component or system in a particular operating region. for diode we have 3 equivalent circuit



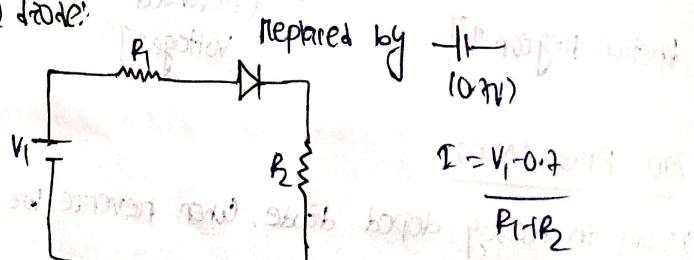
V-I characteristics of Ideal diode:



$$V_{th}(\text{ideal}) = 0$$

$$\text{slope} = 0$$

$$\frac{V}{I} = P = 0$$

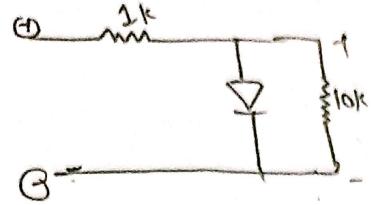


Steps: Check diode biasing

If reverse biased → Replace with open circuit

If forward biased → Check its type

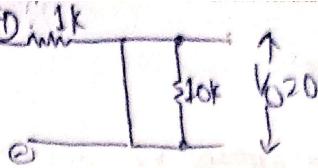
Ideal → short circuit Practical → with threshold



(i) when ideal diode $V_{D,ideal} = 0V$

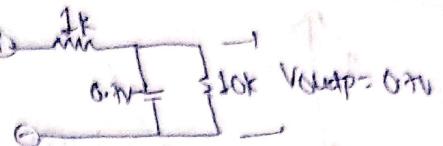
short-circuited

$$V_{output} = 0V$$



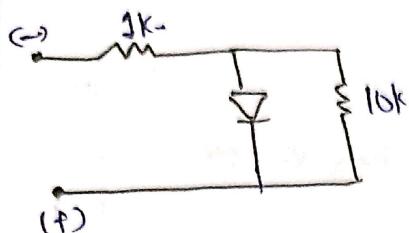
(ii) silicon diode $V_D = 0.7V$

$$V_{output} = 0.7V$$



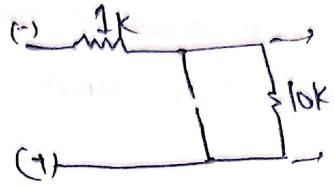
(iii) Germanium diode $V_D = 0.3V$

$$V_{output} = 0.3V$$



Ans

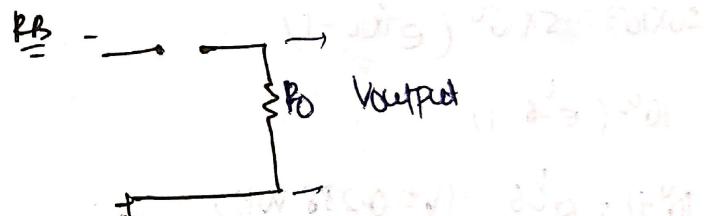
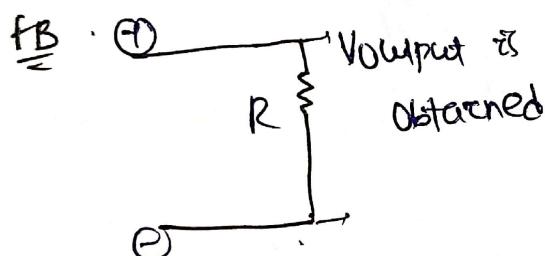
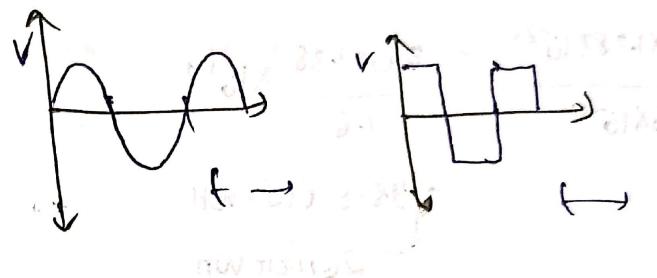
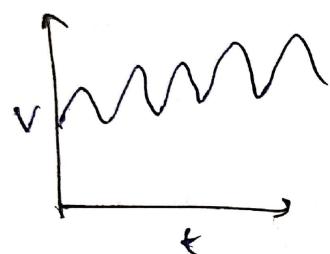
zero diode voltage required



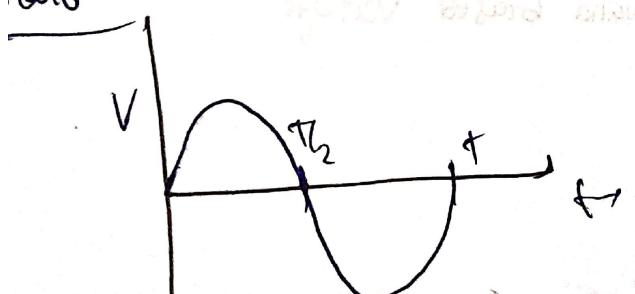
$$V_0 = \frac{10}{11} \times 5 = \frac{50}{11} = 4.5$$

LED \rightarrow display
Diode - Rectifier
 $= 4.5$ drop in

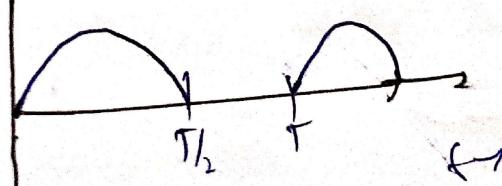
Rectification (DC)



Half-wave:



negative half cycle is not passed through the diode

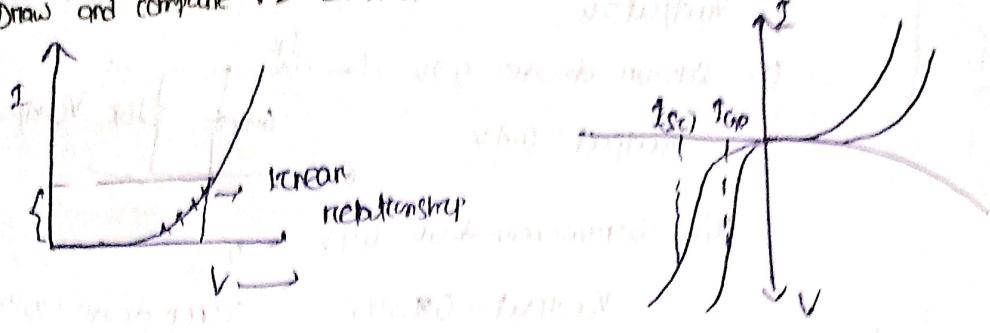


full wave



Assignments:

Draw and compare V-I characteristics of Si & Ge



The reverse S.C at 300K for germanium diode is 5mA . Forward voltage to be supplied across junction to obtain a I for 5mA

$$I_p = I_s (e^{\frac{qV}{kT}} - 1)$$

$$k = 11600 \text{ eV/K}$$

$$q = 1.6 \times 10^{-19} \text{ C}$$

$$n = 1 \quad I_s = 5 \times 10^{-6} \text{ A} \quad I_p = 50 \times 10^{-3} \text{ A}$$

$$V_T = \frac{300 \times 1.38 \times 10^{23}}{1.6 \times 10^{-19}} = \frac{300 \times 1.38}{1.6} \times 10^{-14} = 98.8 \times 10^3 \text{ V/K} = 26 \text{ mV/K}$$

$$50 \times 10^{-3} = 5 \times 10^{-6} (e^{\frac{V}{26}} - 1)$$

$$10^4 + 1 = e^{\frac{V}{26}}$$

$$10^4 + 1 = e^{\frac{V}{26}} \quad (V = 0.238 \text{ V/K})$$

I through P-N junction diode is 6mA . forward biased voltage of 0.9V . static & dynamic R altered by diode

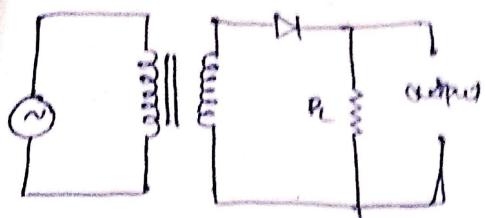
$$R_{\text{static}} = \frac{V}{I} = \frac{0.9\text{V}}{60 \times 10^{-3}\text{A}} = 15\Omega$$

$$R_{\text{dyna}} = \frac{26 \times \eta}{D} = \frac{26 \times 1}{60 \times 10^{-3}} =$$

$$= \frac{26}{60} \times 10^3 \Omega$$

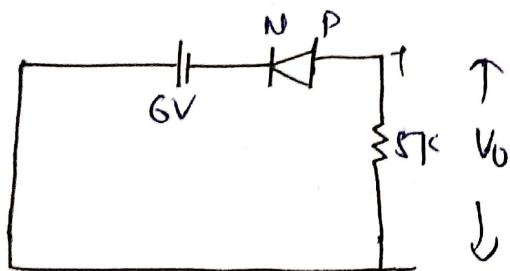
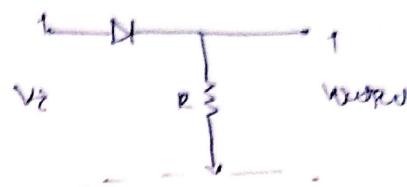
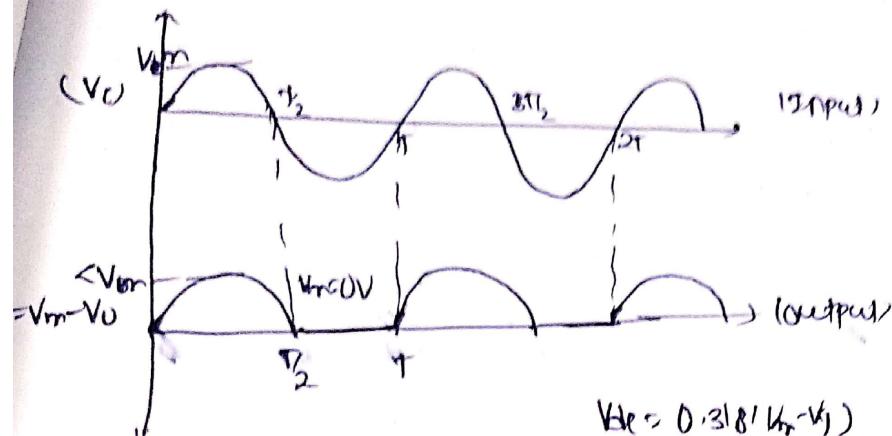
$$= 0.866 \times 10^3 \Omega$$

Half-wave rectification for semiconductor

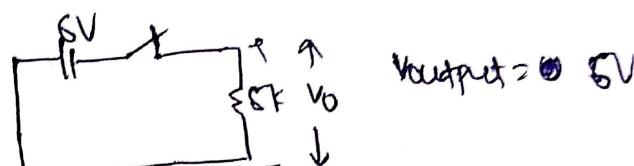


for given diode
threshold voltage $\approx 0.7V$

Diode will conduct from $0.7V$



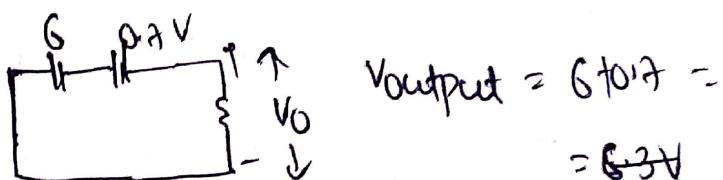
(i) when diode is ideal



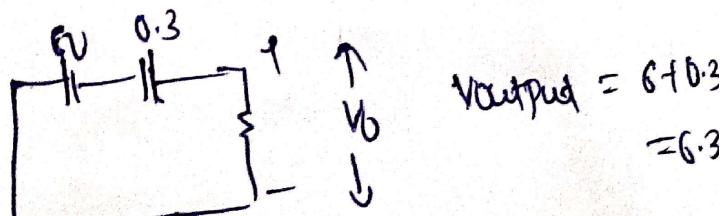
(ii) when diode is reverse biased

$$V_{\text{output}} = 0V$$

(iii) when diode is silicon



(iv) when diode is germanium



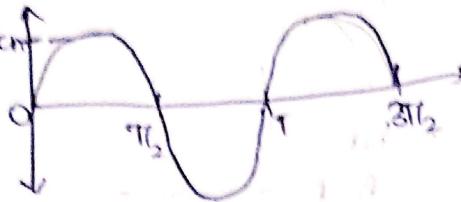
Has the current flows and direction

① Operation

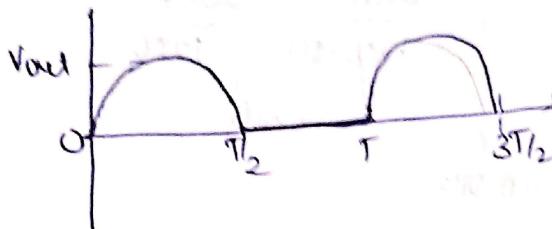
- It converts AC voltage into DC voltage
- It is a type of rectifier that allows only 1-half cycle of an AC voltage waveform to pass while blocking other half cycle.

② waveform

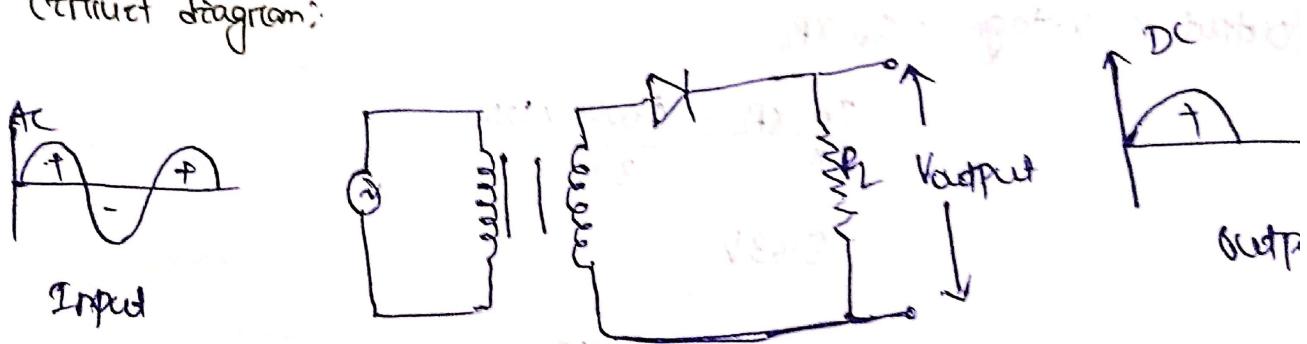
Input :- v_{in}



Output :-



Circuit diagram:

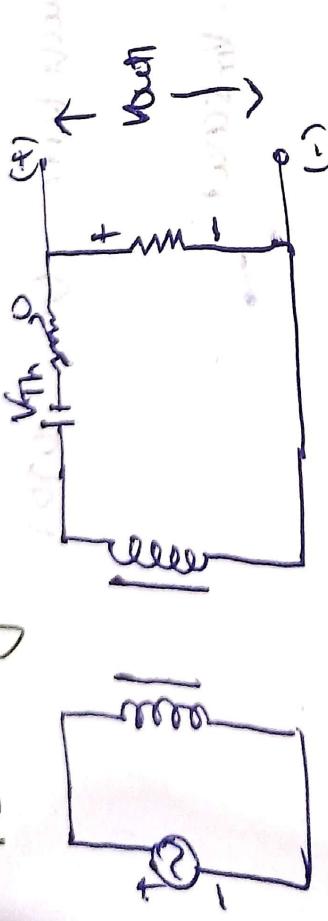


③

Analysis of circuit:

1. A high AC voltage is applied to the primary side of above transformer, the obtained voltage is applied to the diode
2. The diode is forward biased during positive half cycle of and hence desired output is obtained having DC voltage
3. Then diode is reverse biased during negative half cycle it acts like open circuit and no power is obtained

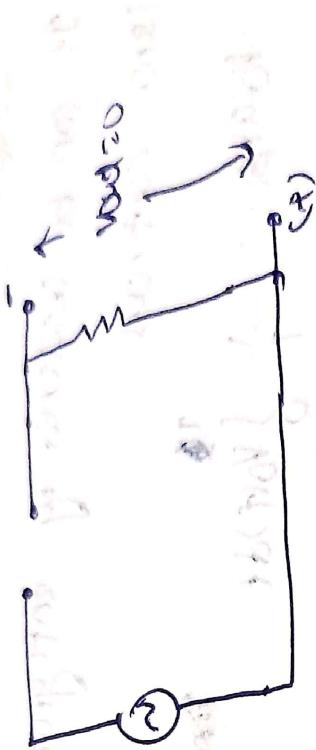
(4) Redrawing of circuit



Forward biased
and hence output is obtained

reverse biased

hence no output is obtained



1.2) Average value :-

It can be obtained by integrating ammeter current (curr. A.M.P.)

Average current

$$\begin{aligned}
 \text{Votavg} &= \frac{1}{T} \int_0^T V_0(t) dt \\
 &= \frac{1}{T} \int_0^T V_m (\sin \omega t) dt = \frac{1}{T} \int_0^T V_0 \sin \omega t dt \\
 &= \frac{1}{T} \int_0^T V_0 \sin \omega t dt \\
 &\Rightarrow \frac{1}{T} \frac{-V_0 \cos \omega t}{\omega} \Big|_0^T \\
 &= \frac{1}{T} \frac{-V_m (\cos \omega t - \cos 0)}{\omega T} \\
 &= -\frac{V_m}{\omega T} (\cos \frac{2\pi}{T} t - 1) \\
 &= -\frac{V_m}{\omega T} (-2) = \frac{V_m}{\omega T}
 \end{aligned}$$

1.3) RMS Value :-

$$\begin{aligned}
 \text{Volt) rms/dc} &= \left[\frac{1}{T_0} \int_0^{T_0} V_0(t)^2 dt \right]^{\frac{1}{2}} \\
 &= \left[\frac{1}{T_0} \int_0^{T_0} V_m^2 \sin^2 \omega t dt \right]^{\frac{1}{2}} \\
 &= \left[\frac{1}{T_0} \int_0^{T_0} V_m^2 \left(1 - \frac{\cos 2\omega t}{2} \right) dt \right]^{\frac{1}{2}} \\
 &= \left(\frac{1}{T_0} \frac{V_m^2 \left[T_0 - \left[\frac{\sin 2\omega t}{2\omega} \right] \Big|_0^{T_0} \right]}{2} \right)^{\frac{1}{2}} \\
 &= \left[\frac{V_m^2}{4} \right]^{\frac{1}{2}} \\
 &= \frac{V_m}{2}
 \end{aligned}$$

Ripple Factor:

It is defined as ratio value of ac component of signal to average value of signal

$$\tau = \sqrt{\frac{\text{rms value of ac component}}{\text{average value of signal}}}$$

$$= \sqrt{\frac{V_{\text{rms}}^2 - V_{\text{dc}}^2}{V_{\text{dc}}^2}}$$

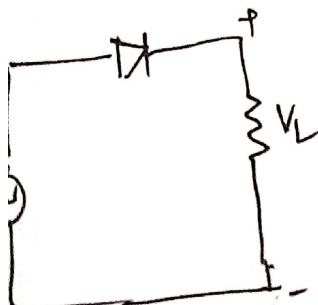
$$= \sqrt{\frac{\left(\frac{V_m}{2}\right)^2 - \left(\frac{V_m}{\pi}\right)^2}{\left(\frac{V_m}{\pi}\right)^2}}$$

$$= \sqrt{\frac{V_{\text{dc}}^2 \left(1 - \frac{1}{4} + \frac{1}{\pi^2}\right)}{V_{\text{dc}}^2 \times \frac{1}{\pi^2}}} = \sqrt{\frac{\pi^2 - 4}{4}}$$

$$\tau = 1.11 \cdot \pi \approx 3.58 \text{ m.s}^{-1}$$

Efficiency

It is ratio of the output power delivered to load system to input power



$$\eta = \frac{\text{Output Power delivered}}{\text{Total Input Power}}$$

$$= \frac{P_{\text{dc to } R_L}}{P_{\text{dc to } R_L + R_{\text{fr}}}}$$

$$= \frac{I_{\text{dc}}^2 R_L}{I_{\text{dc}}^2 (R_L + R_{\text{fr}})}$$

$$= \frac{R_L}{R_L + R_{\text{fr}}} \quad R_{\text{fr}} \rightarrow 0$$

$$= \frac{R_L}{R_L + 0}$$

$$= 40\%$$

A diode (1N5819) is connected to a load resistance of $R_L = 1200 \Omega$. It is connected to a 20V RMS voltage source. Calculate:

(i) AC load current (I_m)

$$I_m = \frac{V_m}{R_L + R_C} = \frac{20\sqrt{2}}{1200 + 150}$$

$$= \frac{20 \times 1.41}{1200}$$

$$= 0.0226$$

(ii) RMS load current (I_{rms})

$$I_{rms} = \frac{I_0}{\sqrt{2}} = \frac{0.0226}{\sqrt{2}}$$

$$= 0.013$$

(iii) Calculate output dc voltage

$$V_{dc} = I_{dc} \times R_L = \frac{I_m}{\pi} \times R_L = \frac{0.0226}{\pi} \times 1200$$

$$= 8.63V$$

(iv) calculate output power

$$P_{output} = \frac{V_{dc}^2}{R_L} = \frac{(8.63)^2}{1200} = \frac{74.47}{1200}$$
$$= 0.062$$

(v) calculate efficiency

$$\eta = \frac{\text{Output Power}}{\text{Input Power}} \times 100 = \frac{I_{dc}^2 R_L}{I_{dc}^2 (R_L + R_C)} \times 100$$

$$= \frac{I_{dc}^2}{I_{dc}^2} \times \frac{R_L}{R_L + R_C}$$

$$= \frac{40\% \times 1200}{1250}$$

$$= 38.4\%$$

Hc

Centre-tapped Rectifier:

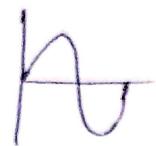
① D.

Deflection :- It requires a centre-tapped transformer to establish input signal across each of the section of secondary transformer.

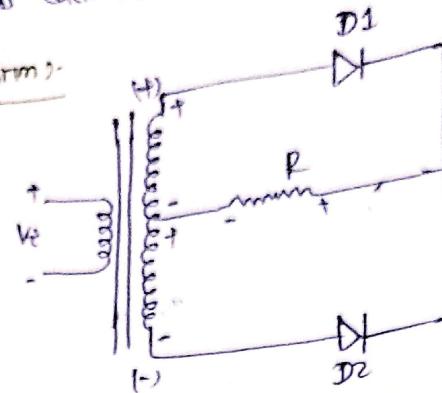
~

Input/output waveform:

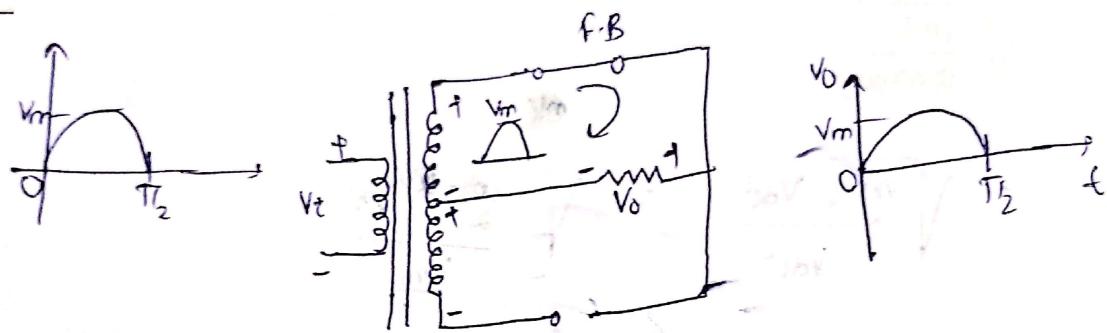
Input



② ,



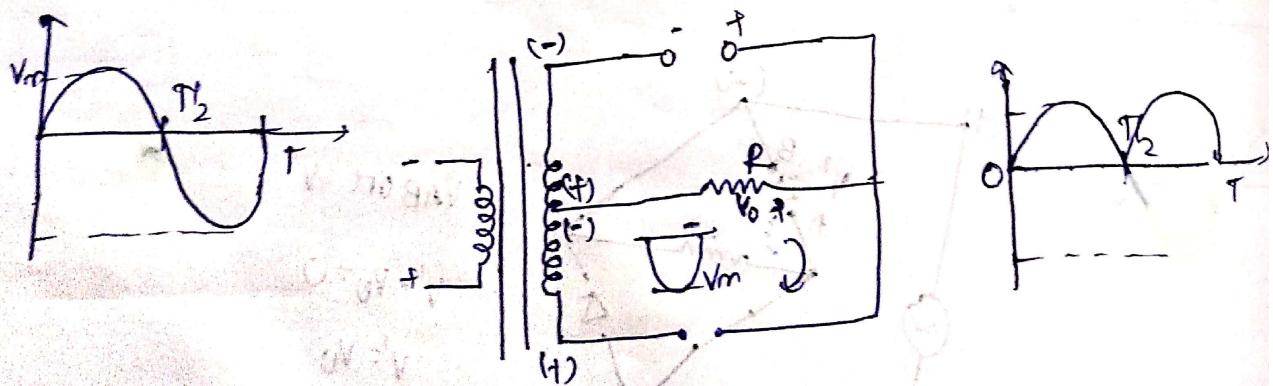
Output



Applying KVL $V_m - V_0 = 0$

$$V_m = V_0$$

for $T/2$ to T



Applying KVL to loop

$$V_0 - V_m = 0$$

$$V_0 = V_m$$

CIRCUIT ANALYSIS :-

- When the V_2 is applied to the primary transformer, D_1 is assumed to be short-circuit (equivalent) and D_2 open-circuit (equivalent). So upper half of the circuit is forward biased, hence some output voltage is obtained across it, while lower-half is reverse-biased, hence no power obtained.
- When negative V_2 is applied to primary transformer, D_2 is assumed to be forward biased and D_1 is reverse biased. Hence some output is obtained across D_2 while no output across D_1 .
- This process repeats itself, and whole waveform is fully rectified.

V_{0dc}

$$\begin{aligned}
 V_{0dc} &= \frac{1}{T_0} \int_0^{T_0/2} v_{0(t)} dt \\
 &\rightarrow \frac{2}{T_0} \int_0^{T_0/2} V_m \sin(\omega t) dt = \frac{2}{T_0} -V_m \left[\frac{\cos(\omega t)}{\omega} \right]_0^{T_0/2} \\
 &= \frac{2}{T_0} \frac{-V_m}{\omega} \left(\cos \frac{2\pi}{T} \times \frac{T}{2} - \cos 0 \right) \\
 &= \frac{2}{T_0} \frac{-V_m}{\frac{2\pi}{T_0}} (-2) \\
 &= \frac{2V_m}{\pi}
 \end{aligned}$$

$V_0 (rms)$

$$V_{0rms} = \left[\frac{1}{T_0} \int_0^{T_0/2} v_{0(t)}^2 dt \right]^{\frac{1}{2}}$$

$$\begin{aligned}
 V_{0rms}^2 &= \frac{2}{T_0} \int_0^{T_0/2} V_m^2 \sin^2(\omega t) dt \\
 &= \frac{2}{T_0} V_m^2 \int_0^{T_0/2} \left[1 - \cos 2\omega t \right] dt \\
 &= \frac{2}{T_0} \times \frac{V_m^2}{2} \int_0^{T_0/2} T - \int_0^{T_0/2} \cos 2\omega t dt \\
 &= \frac{V_m^2}{T_0} \left[\frac{T_0}{2} - \frac{\sin 2\omega t}{2\omega} \right]_0^{T_0/2} \\
 &= \frac{V_m^2 \times \frac{\pi}{2}}{\frac{2\pi}{T_0}} = \frac{V_m^2}{2}
 \end{aligned}$$

$$V_{rms}^2 = \frac{V_m^2}{2}$$

$$V_{rms} = \frac{V_m}{\sqrt{2}}$$

Ripple factor

$$\text{Ripple factor} = \sqrt{\frac{\text{r.m.s component of ac}}{\text{average value}}}$$

$$= \sqrt{\frac{V_{rms}^2 - V_{dc}^2}{V_{dc}^2}}$$

$$= \sqrt{\frac{\frac{V_m^2}{2} - \frac{4V_m^2}{\pi^2}}{\frac{4V_m^2}{\pi^2}}} = \sqrt{\frac{\frac{1 - 4}{2}}{\frac{4}{\pi^2}}}$$

$$= \sqrt{\frac{\pi^2 - 8}{8}}$$

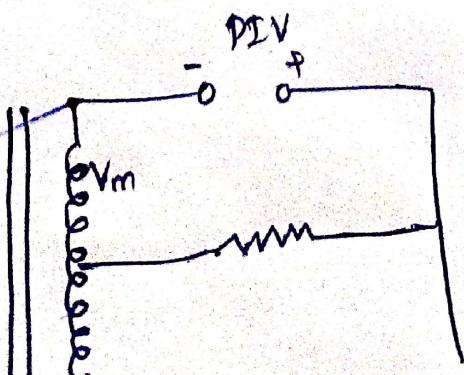
$$= 0.48$$

Efficiency

$$\eta = \frac{\text{Output power delivered}}{\text{Total input power}}$$

$$= \frac{\left(\frac{2V_m}{\pi}\right)^2}{\left(\frac{V_m}{\sqrt{2}}\right)^2} \times 100 = \frac{4}{\frac{1}{2}} \times 100 = \frac{8}{\pi^2} \times 100 \approx 80\%$$

Peak Inverse Voltage



PIV \rightarrow Recombination $f V_R$

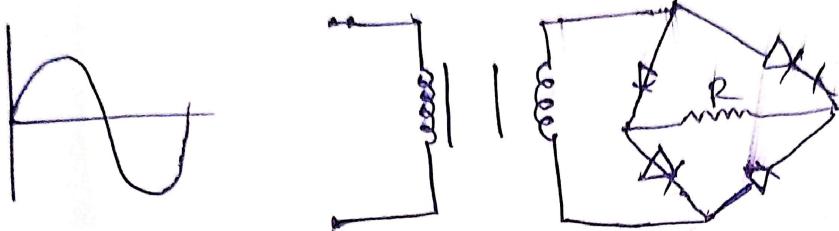
$$\rightarrow V_m + V_m = 2V_m$$

So PIV should be $\geq 2V_m$



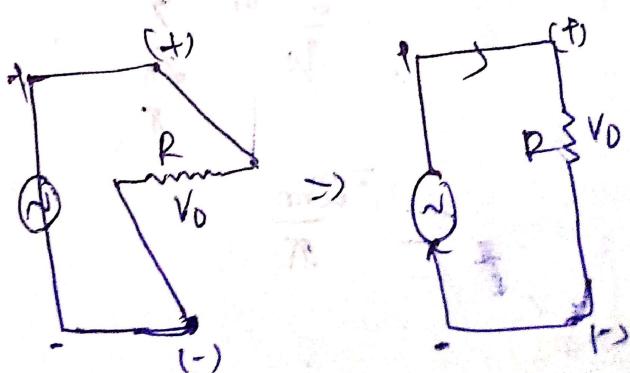
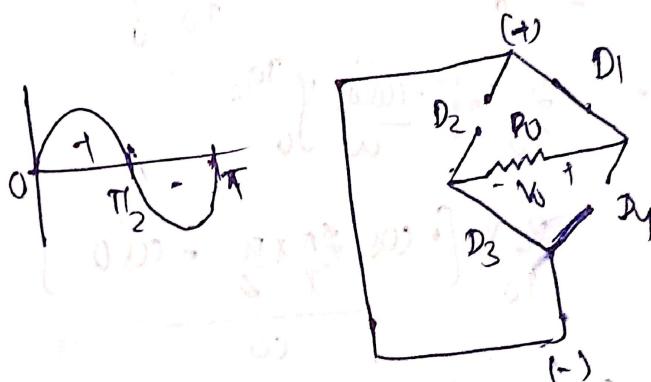
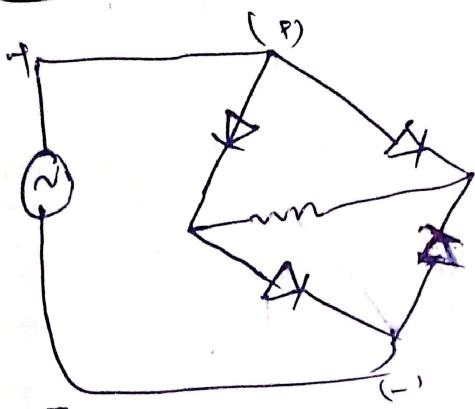
full wave rectifier:-

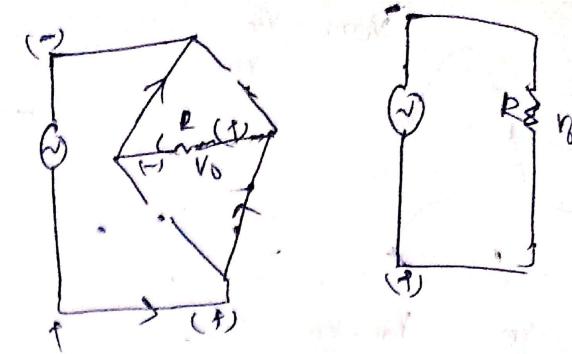
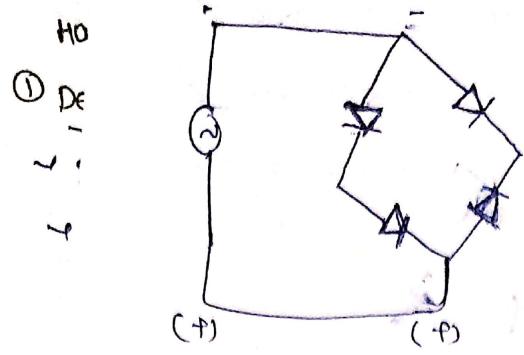
- (1) centre-tap rectifier
- (2) Bridge rectifier



Bridge

Bridge Rectifier:-



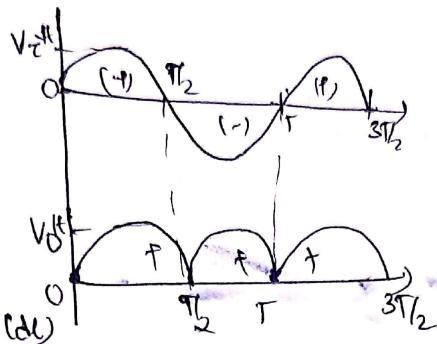


②

Applying KVL to (kt)

$$-V_t + V_0 = 0$$

$$V_0 = V_t$$



$$t > V_m \sin(2\pi f_0 t)$$

(i) V_0 (DC) (ii) V_0 (rms) (iii) $\eta \approx 80\%$

(i) V_0 (DC)

$$V_0 (\text{DC}) = \frac{1}{T_{0/2}} \int_0^{T_{0/2}} V_0(t) dt = \frac{2}{T_0} \int_0^{T_{0/2}} V_m \sin(\omega t) dt$$

$$\Rightarrow \frac{2}{T_0} V_m \left[-\frac{\cos \omega t}{\omega} \right]_0^{T_{0/2}}$$

$$\Rightarrow \frac{2}{T_0} V_m \left[-\cos \frac{2\pi \times T_0}{\omega} - \cos 0 \right]$$

$$= \frac{2}{T_0} V_m \left[\frac{2\pi}{\omega} \right]$$

$$= \frac{2V_m}{\pi}$$

(ii) V_0 (rms)

$$V_{0\text{rms}}^2 = \left[\frac{1}{T_0} \int_0^{T_{0/2}} V_0(t)^2 dt \right]^{\frac{1}{2}}$$

$$V_{0\text{rms}}^2 = \left[\frac{2}{T_0} \left[V_m^2 \sin^2 \omega t \right]_0^{T_{0/2}} \right]$$

$$= \frac{2}{T_0} V_m^2 \left[\frac{1 - \cos 2\omega t}{2} \right]_0^{T_{0/2}}$$

$$= \frac{2Vm^2}{T_0} \left[\left[\frac{\pi}{4} \right] - \left[\frac{\sin 2\omega T_0}{2} \right] \right]$$

$$= \frac{2Vm^2}{T_0} \left[\frac{\pi}{4} \right]$$

$$V_{rms}^2 = \frac{Vm^2}{2}$$

$$\boxed{V_{rms} = \frac{Vm}{\sqrt{2}}}$$

Ripple factor:

$$\gamma = \sqrt{\frac{V_{rms}^2}{\text{average}}}$$

$$= \sqrt{\frac{V_{rms}^2 - V_{dc}^2}{V_{dc}^2}}$$

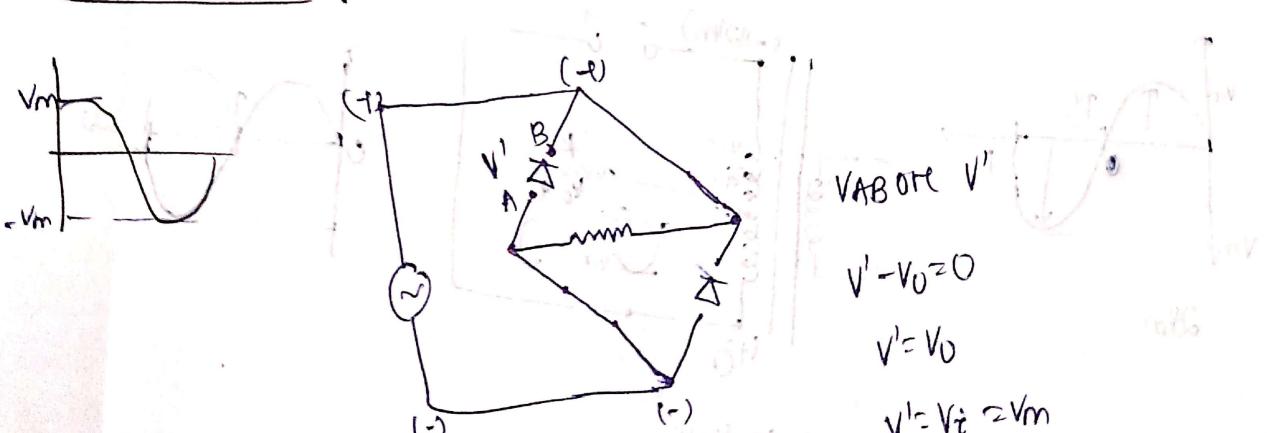
$$\sqrt{\frac{V_{dc}^2 - \frac{4Vm^2}{\pi^2}}{4Vm^2}}$$

$$= \sqrt{\frac{\frac{1}{2} - \frac{4}{\pi^2}}{4}}$$

$$= \sqrt{\frac{\frac{1}{2} - \frac{4}{\pi^2}}{8}}$$

$$= 0.48$$

peak inverse voltage



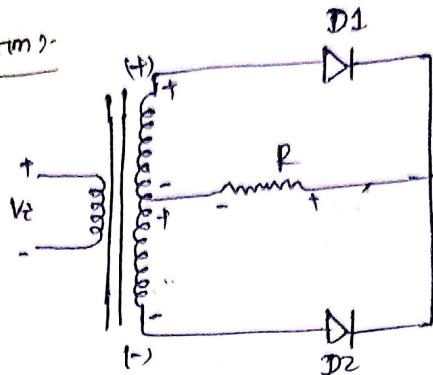
so, peak inverse voltage PIV rating is greater than or equal to V_m

Centre-tapped Rectifier

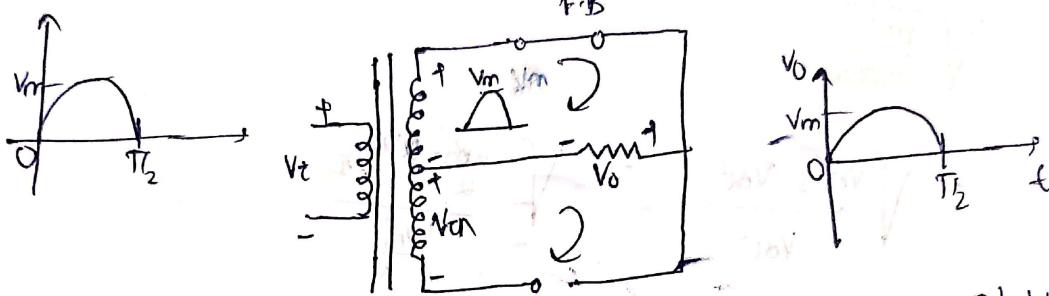
Definition :- It requires a centre-tapped transformer to establish the input signal across each of the section of secondary transformer.

Input/output waveform:-

Input



Output



Applying KVL $V_m - V_o = 0$

$$\boxed{V_m = V_o}$$

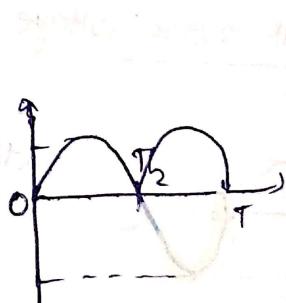
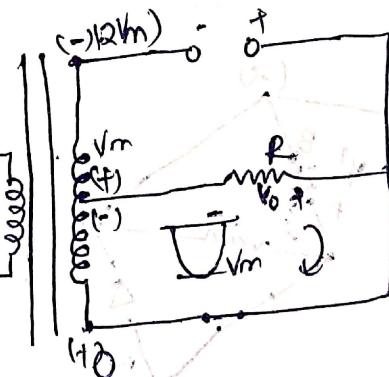
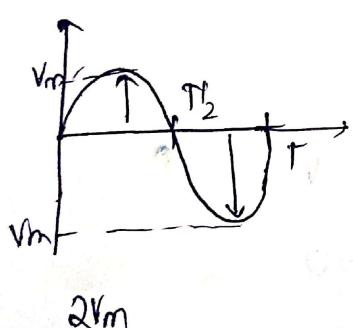
Applying KVL to 2nd loop

$$+V_{CN} + V_{CH} = V_o$$

$$2V_m = V_o$$

for T_2 to T

turn ratio 0 : 1 : 2



Applying KVL to loop

$$V_o - V_m = 0$$

$$\boxed{V_o = V_m}$$

(true)

Disadvantages :- exactly at centre, tapping should be done

Since $PDV \geq 2V_m$. We need emitter diode



CIRCUIT ANALYSIS :

- when +ve V_2 is applied to the primary transformer, D1 is assumed to be short-circuit (equivalent) and D2 open-circuit (equivalent). So upper half of the circuit is forward biased, hence some output voltage is obtained across it, while lower-half is reverse-biased, hence no power obtained
- when negative V_2 is applied to primary transformer, D2 is assumed to be forward biased and D1 is reverse biased, hence some output is obtained across D2 while no output across D1
- This process repeats itself, and whole waveform is fully rectified

$V_{0(alt)}$

$$\begin{aligned}
 V_{0(alt)} &= \frac{1}{T_0} \int_0^{T_0/2} v(t) dt \\
 &\rightarrow \frac{2}{T_0} \int_0^{T_0/2} V_m \sin(\omega t) dt = \frac{2}{T_0} -V_m \left[\frac{\cos(\omega t)}{\omega} \right]_0^{T_0/2} \\
 &= \frac{2}{T_0} -\frac{V_m}{\omega} (\cos(\frac{2\pi}{T} \times \frac{T}{2}) - \cos 0) \\
 &= \frac{2}{T_0} -\frac{V_m}{\frac{2\pi}{T_0}} (-2) \\
 &= \frac{2V_m}{\pi}
 \end{aligned}$$

$V_0 (\text{rms})$

$$V_{0(\text{rms})} = \left[\frac{1}{T_0} \int_0^{T_0/2} v(t)^2 dt \right]^{1/2}$$

$$\begin{aligned}
 V_{0(\text{rms})}^2 &= \frac{2}{T_0} \int_0^{T_0/2} V_m^2 \sin^2(\omega t) dt \\
 &= \frac{2}{T_0} V_m^2 \int_0^{T_0/2} \left[1 - \frac{\cos 2\omega t}{2} \right] dt \\
 &= \frac{2}{T_0} \times \frac{V_m^2}{2} \left[T - \int_0^{T_0/2} \cos 2\omega t dt \right] \\
 &= \frac{V_m^2}{T_0} \left[\frac{T_0}{2} - \frac{\sin 2\omega t}{2\omega} \Big|_0^{T_0/2} \right] \\
 &= \frac{V_m^2 \times \frac{T_0}{2}}{\frac{T_0}{2}} = \frac{V_m^2}{2}
 \end{aligned}$$

How

① DC

$$\approx 5$$

~

Ripple factor

In

② u

$$\gamma_r = \sqrt{\frac{\text{the r.m.s value}}{\text{average value}}}$$

$$\gamma_r = \sqrt{\frac{V_{rms}^2 - V_{dc}^2}{V_{dc}^2}} = \sqrt{\frac{V_m^2 - 4V_m^2}{2 + \frac{4}{\pi^2}}} = \sqrt{\frac{3 - 4}{\frac{4}{\pi^2}}} = \sqrt{\frac{\pi^2 - 8}{8}}$$

or

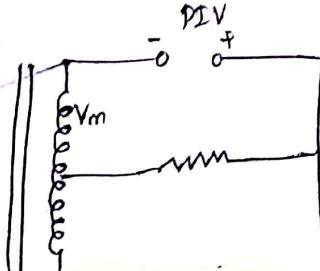
Efficiency

$$\eta = \frac{\text{output power delivered}}{\text{total input power}}$$

$$= \frac{\left(\frac{2I_m}{\pi}\right)^2}{\left(\frac{I_m}{\sqrt{2}}\right)^2} \times 100 = \frac{4}{\frac{1}{2}} \times 100 = \frac{8}{\pi} \times 100 = 80\%$$

Peak Inverse Voltage

③



$$PIV = V_{rectifier} + V_R$$

$$= V_m + V_m = 2V_m$$

So PIV should be $\geq 2V_m$

Comparison

V_{oldc}

V_{rms}

Ripple factor

η

PIV

bridge

$$\frac{2V_m}{\pi}$$

$$\frac{V_{rms}}{\sqrt{2}}$$

$$0.48$$

$$80\%$$

$$\geq V_m$$

centre-tap

$$\frac{2V_m}{\pi}$$

$$\frac{V_m}{\sqrt{2}}$$

$$0.48$$

$$80\%$$

$$\geq 2V_m$$

Digital electronics :-

Topic

① Defn

Number system :-

→ 2¹

Number system

base/radix

Distinct symbols

examples

→

Binary

2

0, 1

10, 111, 1001

,

Octal

8

0, 1, ..., 7

② Wt

Decimal

10

0, 1, ..., 9

I

hexadecimal

0, 1, ..., 9

A, ..., F

O

Decimal

binary

Octal

hexadecimal

0 0 0 0

1 0 0 1

2 0 1 0

3 0 1 1

4 0 1 0 0

5 0 1 0 1

6 0 1 1 0

7 0 1 1 1

8 1 0 0 0

9 1 0 0 1

10 1 0 1 0

11 1 0 1 1

12 1 1 0 0

13 1 1 0 1

14 1 1 1 0

15 1 1 1 1

③

Conversion decimal → binary.

For 25.32 = (11001.1

$$\begin{array}{r} 1000 \\ \downarrow \quad \downarrow \quad \downarrow \\ 2^7 \quad 2^6 \quad 2^5 \\ 2^4 \quad 2^3 \quad 2^2 \quad 2^1 \quad 2^0 \\ 1 \quad 0 \quad 0 \quad 0 \quad 0 \end{array}$$

$$\begin{array}{r} 2 | 25 \\ 2 | 12 - 1 \\ 2 | 6 - 0 \end{array} \text{ binary: } 11001$$

from bottom
to top

$$\begin{array}{r} 32 \\ \times 2 \\ \hline 64 \\ \times 2 \\ \hline 128 \\ \times 2 \\ \hline 56 \\ \times 2 \\ \hline 12 \end{array}$$

from
top
to
bottom



54.78 \rightarrow 1001010.1100

156 112

$$\begin{array}{r}
 2\overline{)54} \\
 2\overline{)27-0} \\
 2\overline{)18-1} \\
 2\overline{)9-0} \\
 2\overline{)4-1} \\
 2\overline{)2-0} \\
 \hline
 1-0 \\
 \hline
 0.24
 \end{array}$$

11.01 = 1011.0000

$$\begin{array}{r}
 2\overline{)11} \\
 2\overline{)5-1} \\
 2\overline{)2-1} \\
 \hline
 1-0 \\
 \hline
 0.01 \\
 \times 2 \\
 \hline
 0.02 \\
 \times 2 \\
 \hline
 0.04 \\
 \times 2 \\
 \hline
 0.08 \\
 \times 2 \\
 \hline
 0.196
 \end{array}$$

decimal \rightarrow octal

54.78 = 66.617

$$\begin{array}{r}
 8\overline{)54} \\
 8\overline{)6-6} \\
 \hline
 0-6 \\
 \times 8 \\
 \hline
 6.24 \\
 \times 8 \\
 \hline
 4.92 \\
 \times 8 \\
 \hline
 1.36 \\
 \times 8 \\
 \hline
 0.12
 \end{array}$$

$$\begin{array}{r}
 8\overline{)18} \\
 8\overline{)10} \\
 \hline
 2-2 \\
 \times 8 \\
 \hline
 16 \\
 \times 8 \\
 \hline
 0-0 \\
 \times 8 \\
 \hline
 0.00
 \end{array}$$

$$\begin{array}{r}
 16\overline{)54} \\
 16\overline{)3-6} \\
 \hline
 0-3 \\
 \times 16 \\
 \hline
 48 \\
 \times 16 \\
 \hline
 2-2 \\
 \times 16 \\
 \hline
 0-0
 \end{array}$$

11.01 = 13.005

$$\begin{array}{r}
 8\overline{)11} \\
 8\overline{)1-3} \\
 \hline
 0-1 \\
 \times 8 \\
 \hline
 0.08 \\
 \times 8 \\
 \hline
 0.64 \\
 \times 8 \\
 \hline
 0.12
 \end{array}$$

decimal \rightarrow hexadecimal

54.78 = 36.127

$$\begin{array}{r}
 0.78 \\
 \times 16 \\
 \hline
 12.48 \\
 \times 16 \\
 \hline
 7.68
 \end{array}$$

11.01 = 11.028

$$\begin{array}{r}
 16\overline{)11} \\
 16\overline{)0-11} \\
 \hline
 0-11 \\
 \times 16 \\
 \hline
 0.16 \\
 \times 16 \\
 \hline
 2.56 \\
 \times 16 \\
 \hline
 8.96
 \end{array}$$

54.78 = 1001010.110

$\frac{1001}{156} \quad \frac{110}{112}$

$$\begin{array}{r}
 2\cancel{6}\cancel{5}4 \\
 2\cancel{2}7\cdot 0 \\
 2\cancel{1}8\cdot 1 \\
 2\cancel{9}\cdot 0 \\
 2\cancel{1}4\cdot 1 \\
 2\cancel{1}2\cdot 0 \\
 \hline
 1\cdot 0
 \end{array}
 \begin{array}{r}
 .78 \\
 \times 2 \\
 \hline
 1.56 \\
 .72 \\
 \hline
 1.12 \\
 .72 \\
 \hline
 0.24
 \end{array}$$

11.01 = 1011.00010

$$\begin{array}{r}
 2\cancel{1}1 \\
 2\cancel{1}5\cdot 1 \\
 2\cancel{2}\cdot 1 \\
 \hline
 1\cdot 0
 \end{array}
 \begin{array}{r}
 .01 \\
 \times 2 \\
 \hline
 0.02 \\
 .72 \\
 \hline
 0.04 \\
 .72 \\
 \hline
 0.08 \\
 .72 \\
 \hline
 0.16
 \end{array}$$

decimal \rightarrow octal

54.78 = 66.617

$$\begin{array}{r}
 8\cancel{5}4 \\
 8\cancel{6}\cdot 6 \\
 \hline
 0\cdot 6
 \end{array}
 \begin{array}{r}
 .78 \\
 \times 8 \\
 \hline
 6.24 \\
 \times 8 \\
 \hline
 4.92 \\
 \times 8 \\
 \hline
 7.36
 \end{array}$$

~~78x8
624x8
492x8
192~~

11.01 = 13.005

$$\begin{array}{r}
 8\cancel{1}1 \\
 8\cancel{1}1\cdot 3 \\
 \hline
 0\cdot 1
 \end{array}
 \begin{array}{r}
 0.01 \\
 \times 8 \\
 \hline
 0.08 \\
 \times 8 \\
 \hline
 0.16
 \end{array}
 \begin{array}{r}
 \times 8 \\
 \hline
 0.12
 \end{array}$$

$$\begin{array}{r}
 8\cancel{7}6 \\
 8\cancel{7}2 \\
 \hline
 0\cdot 72
 \end{array}
 \begin{array}{r}
 16\cancel{5}4 \\
 16\cancel{3}\cdot 6 \\
 \hline
 0\cdot 3
 \end{array}
 \begin{array}{r}
 0.78 \\
 \times 16 \\
 \hline
 12.48 \\
 \times 16 \\
 \hline
 7.68
 \end{array}$$

$$\begin{array}{r}
 16\cancel{1}6 \\
 16\cancel{1}2 \\
 \hline
 0\cdot 12
 \end{array}
 \begin{array}{r}
 16\cancel{1}0 \\
 16\times 1 = 2 \\
 \hline
 896
 \end{array}
 \begin{array}{r}
 86\cancel{1}6 \\
 \hline
 896
 \end{array}$$

11.01 = 11.028

$$\begin{array}{r}
 16\cancel{1}1 \\
 0\cdot 11
 \end{array}
 \begin{array}{r}
 .01 \\
 \times 16 \\
 \hline
 0.16
 \end{array}
 \begin{array}{r}
 \times 16 \\
 \hline
 2.16
 \end{array}
 \begin{array}{r}
 \times 16 \\
 \hline
 8.96
 \end{array}$$

To conversion of no. from any other number system

① DE

System

$$101.10 \rightarrow 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0$$

∴

$$(101)_2 = (?)_{10}$$

$$= 2^3 + 2^1 + 2^0$$

∴

$$10101$$

② u

$$\text{Decimal} = 2^0 \times 1 + 2^2 \times 1 + 2^4 \times 1$$

$$= 1 + 4 + 16 = 21$$

$$110.011 = 2^1 \times 1 + 2^2 \times 1 = 8.375 = 6.375$$

$$0 \times 2^1 + 1 \times 2^{-2} + 1 \times 2^{-3}$$

$$= \frac{1}{4} + \frac{1}{8} = \frac{3}{8} = 0.375$$

$$(57.38)_8 = 8^0 \times 5 + 8^1 \times 3 = 5 + 24 = 29$$

$$2 \times 8^{-1} = \frac{2}{8} = \frac{1}{4} = 0.25$$

$$(57.38)_{16} \quad B \rightarrow 11$$

$$7 \times 16^0 + 5 \times 16^1 + 3 \times 16^{-1} + 11 \times 16^{-2}$$

$$= 87.2304$$

Binary Base=2

Octal base=8 2^3

Hexadecimal base=16

$$\begin{array}{r} 1 \\ 1 \\ 0 \\ 1 \\ \downarrow \\ 00(1010) \\ \downarrow \quad \downarrow \\ 1 \quad 2 \end{array}$$

$$(12)_8 = (?)_{16}$$

$$(001010)_2 = (A)_{16}$$

$$\begin{array}{r} 01001101011.01 \\ \boxed{2} \quad \boxed{3} \quad \boxed{5} \quad \boxed{3} \\ \therefore 12353.01_8 \end{array}$$

$$\begin{array}{r} 01001101011.0100 \\ \boxed{4} \quad \boxed{14} \quad \boxed{11} \\ 2^1 + 2^2 + 2^3 + 2^4 \\ = 41411.04 \end{array}$$

$$\begin{array}{r} 41411.04 \\ \cancel{12353.01}_8 \\ = (4EB.4)_{16} \end{array}$$

convert $(B9F \cdot AE)_{16}$ to octal = $(11918, 10147)$

$$\begin{array}{r} B \quad 9 \quad F \quad A \quad E \\ \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \\ 01011 \quad 1001 \quad 1111 \quad 1010 \quad 1110 \end{array} = 01011100111110101110$$

$10^3 \times 2^3$
 $10^2 \times 2^2$

complement :-

$\begin{array}{r} 111010 \\ 000101 \end{array} \rightarrow 1$ complement

$\begin{array}{r} 111010 \\ 000101 \end{array} + 1$

$\begin{array}{r} 000110 \\ 000110 \end{array} \rightarrow 2$ complement

$$\begin{array}{r} +0 \\ 0 \end{array} \quad \begin{array}{r} +1 \\ 1 \end{array}$$

$0 \rightarrow 1$
 $1 \rightarrow 1$
 $10 \rightarrow 1$
 11

$$\begin{array}{r} 1111 \\ 0000 \\ +1 \\ \hline 0001 \end{array}$$

Assignment

Find 1's complement of 1011.11

for 2's complement add 1 to last significant digit (may be de
ferred or _____)

$$\begin{array}{r} 1011.11 \\ 1's \rightarrow 0100.00 \\ +1 \\ \hline 0100.01 \end{array}$$

Representation of binary numbers

If no. is the put 0 in last
-ve " 1 in last

$3 \rightarrow 011$ } represented as
 $-3 \rightarrow 111$ sign magnitude

		Sign magnitude no		
① Date	+2	<u>0</u>	<u>10</u>	= 010
$\sim \$7$		Sign	magnitude	
~ 1	+3	<u>0</u>	<u>111</u>	= 0111
V	-5	<u>01</u>	<u>11</u>	= 111
② wa	-2	<u>1</u>	<u>10</u>	= 110
Ir	-12	<u>1</u>	<u>1100</u>	= 11100
	+6	<u>0</u>	<u>110</u>	= 0110

In binary no. system there are 3 different ways to represent a -ve number

- sign magnitude representation
- 1's complement representation
- 2's complement representation

Sign-magnitude

$$\begin{array}{r} \text{+5} \\ \text{-5} \end{array} \quad \begin{array}{l} \text{0 } \underline{10} \\ \text{1 } \underline{10} \end{array} \quad \rightarrow \quad \begin{array}{l} 010 \\ 110 \end{array}$$

1. 1's complement:

→ check the no.

→ If the no. is +ve positive no. using sign magnitude formed then take 1's complement of that no.

2. If the no. is -ve

→ the sign magnitude
then it's 1's complement

$$\underline{SM} = 0110$$

$$S'1' = 0110$$

$$C21 = 0110$$

$$C22 =$$

$$SM = 1110$$

$$S'1' =$$

$$\underline{\underline{0110}}$$

$$C11 = 1001$$

$$C21 = 1010$$

Other mag

sum 11

Binary Arithmetic Operation

$$\begin{array}{r} 0011010 \\ 0001100 \\ \hline 00100110 \end{array}$$

$$110.10 + 111.10 = 110.00$$

$$\begin{array}{r} 110.10 \\ 111.10 \\ \hline 1010.00 \end{array}$$

Subtraction:

$$\begin{array}{r} 10110 \\ -11011 \\ \hline 00001 \end{array}$$

$$\begin{array}{r} 0 \\ -1 \\ 0 \\ \hline 0 \end{array} \quad \begin{array}{r} 1 \\ 0 \\ 1 \\ \hline 1 \end{array} \quad \begin{array}{r} 0 \\ 1 \\ 1 \\ \hline 1 \end{array} \quad \begin{array}{r} 0 \\ 1 \\ 1 \\ \hline 1 \end{array}$$

$$\begin{array}{r} +1 \\ 1 \\ \hline 0 \\ 10 \\ 1 \\ \hline 1 \\ 1 \end{array}$$

Subtract 1100 from 11010

$$\begin{array}{r} 11011 \\ -10110 \\ \hline 00101 \end{array}$$

$$\begin{array}{r} 11010 \\ -1100 \\ \hline 01110 \end{array}$$

Binary multiplication:

$$\begin{array}{r} 1010 \\ \times 1001 \\ \hline 0000 \\ 0000 \\ 1010 \\ 0000 \\ \hline 1011010 \end{array}$$

$$\begin{array}{r} 1010 \times 1001 \\ \hline 1010 \end{array}$$

$$\begin{array}{r} 1001.11 \\ \times 10.1 \\ \hline 0001 \end{array}$$

$$\begin{array}{r} 1001.11 \times 101 \\ \hline 0001 \\ 100111 \\ 000000 \\ 01100111 \\ \hline 10011000011 \end{array}$$



$$\begin{array}{r}
 101 \\
 + 110 \\
 \hline
 001001 \\
 \hline
 110 \\
 \hline
 0011
 \end{array}$$

$$\begin{array}{r}
 101 \\
 - 100 \\
 \hline
 01010 \\
 - 00101 \\
 \hline
 00001 \\
 \hline
 10000
 \end{array}$$

Logic gates :-

Gate

NOT (A)
011

Symbol

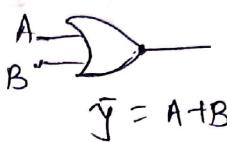


T.T

<u>A</u>	<u>A'</u>
1	0
0	1

OR

($A + B$)
(Sensitive to input 1)

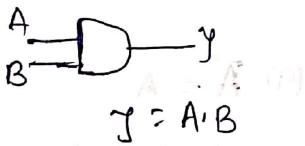


$$Y = A + B$$

<u>A</u>	<u>B</u>	<u>$A+B$</u>
0	0	0
0	1	1
1	0	1
1	1	1

AND

(Sensitive to
input 0)



$$Y = A \cdot B$$

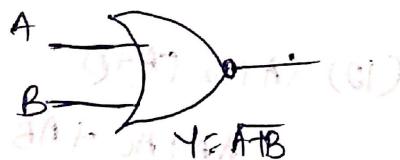
$$(A \cdot B) + (A \cdot 0) = A$$

$$A \cdot B + A \cdot 0 = A$$

$$A \cdot B + A \cdot 1 = A$$

<u>A</u>	<u>B</u>	<u>$A \cdot B$</u>
0	0	0
0	1	0
1	0	0
1	1	1

NOR



$$Y = \overline{A+B}$$

<u>A</u>	<u>B</u>	<u>$\overline{A+B}$</u>
0	0	1
0	1	0
1	0	0
1	1	0

NAND

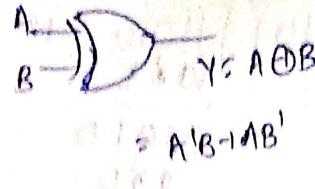


$$Y = \overline{A \cdot B}$$

<u>A</u>	<u>B</u>	<u>$\overline{A \cdot B}$</u>
0	0	1
0	1	1
1	0	1
1	1	0

How
① Def

Ex-OR



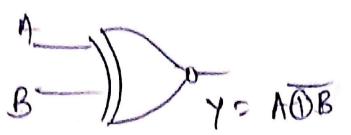
$$Y = A \oplus B$$

$$= A'B + AB'$$

A	B	$A \oplus B$
0	0	0
0	1	1
1	0	1
1	1	0

② a

Ex-NOR



$$= \overline{A'B + AB'}$$

A	B	$A \oplus B$
0	0	1
0	1	0
1	0	0
1	1	1

Boolean Algebra:

$$\begin{array}{l} A \\ 1 + 1 = 1 \\ 0 + 0 = 0 \end{array}$$

$$(5) (1) A + \bar{A} = A \quad (5) A \cdot 0 = A$$

$$(2) A \cdot A = A \quad (6) A \cdot 0 = 0$$

$$(3) A + 1 = 1 \quad (7) A + \bar{A} = 1$$

$$(4) A \cdot 1 = A \quad (8) A \cdot \bar{A} = 0$$

$$(9) \bar{\bar{A}} = A$$

$$(10) A + A\bar{B} = A$$

$$(11) A + \bar{A}B = A + B$$

$$(12) (A+B)(A+C) = A+BC$$

③

$$(10) A + A\bar{B}$$

$$= A(1 + \bar{B})$$

$$= A$$

$$(11) A + \bar{A}B$$

$$= (A + A)(A + \bar{B})$$

$$= A + \bar{A}B$$

$$(12) (A+B)(\bar{A}+C)$$

$$= AA + AC + AB + BC$$

$$= A + AC + AB + BC$$

$$= A(B+C)$$

3 laws of boolean algebra

(1) commutative law

$$A + B = (B + A) \text{ (OR operation)}$$

$$A \cdot B = B \cdot A \text{ (AND operation)}$$

Associative law:-

$$(A+B)+C = A+(B+C)$$

Distributive law:-

$$A \cdot (B+C) = (A \cdot B) + (A \cdot C)$$

$$A+(B \cdot C) = (A+B) \cdot (A+C)$$

(Valid in boolean algebra but not in mathematical algebra)

De-morgan's theorem:

$$(1) \overline{A+B} = \overline{A} \cdot \overline{B}$$

De-morgan's theorem is defined as,

$$(2) \overline{AB} = \overline{A} + \overline{B}$$

$$(A+B)(\overline{A}+C) = (A+B) \cdot (\overline{A} \cdot C + B \cdot C)$$

$$= A \cdot A + A \cdot C + B \cdot A + B \cdot C$$

$$(1) (A+AB) = (A+A) \cdot (A+B)$$
$$= A(1+B)$$
$$= A$$

$$(1) (A+\overline{AB}) = (A+\overline{A}) \cdot (A+\overline{B})$$
$$= 1 \cdot (A+\overline{B})$$
$$= (A+\overline{B})$$

$$(1) (A+B)(A+C) = AA + AC + AB + BC$$
$$= A + AC + AB + BC$$
$$= A(\overline{C} + 1) + B = A(HC + B) + BC$$
$$= \overline{A} + B = A+BC$$

Proof of De-morgan's theorem:

Let A and B be 2 input, then according to de-morgan's theorem
following can be proved

$$1. \bar{A} \cdot \bar{B} = \bar{A+B}$$

$$2. \bar{A+B} = \bar{A} \cdot \bar{B}$$

A	B	$\bar{A} \cdot \bar{B}$	$A+B$	$\bar{A+B}$	$\bar{A} \cdot \bar{B}$	$\bar{A+B}$	\bar{A}	$\bar{A} \cdot \bar{B}$	$\bar{A+B}$
1	0	0	1	1	0	1	0	1	0
0	0	0	0	1	1	1	1	1	1
0	1	0	1	1	0	0	1	1	0
1	1	1	1	0	0	0	0	0	0

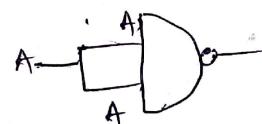
NAND, NOR gates are called universal logic gates
(we can replace any other gate with these 2 gates)

NAND:



NAND:

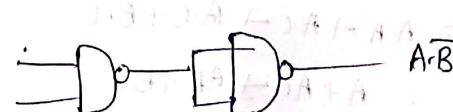
$$Y = \bar{A} \cdot \bar{B} = \bar{A+B}$$



AND:



using NAND gate



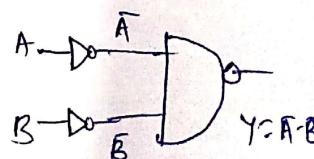
OR:

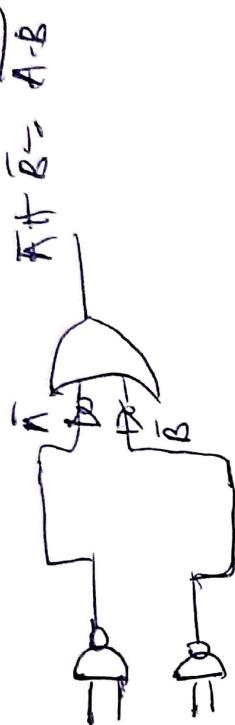
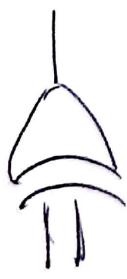


$$\bar{A} \cdot \bar{B}' = \bar{A} + \bar{B}$$

$$\Leftrightarrow Y = A+B$$

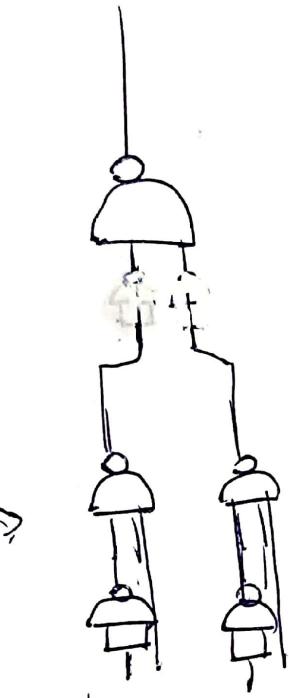
NAND:



NANDEX-OR gate

$$\text{Y} = A'B + B'A$$

$$\text{Y} = \overline{A \cdot B}$$



$$\text{Y} = \overline{A \oplus B}$$

Implement EX-OR, EX-NOR using min NAND gate
show that NOR gate is also universal gate

gate is also universal gate

NOR gate as Universal gate:

(2) OR



$$Y = \overline{(A+B)}$$
$$= A+B$$



ANB

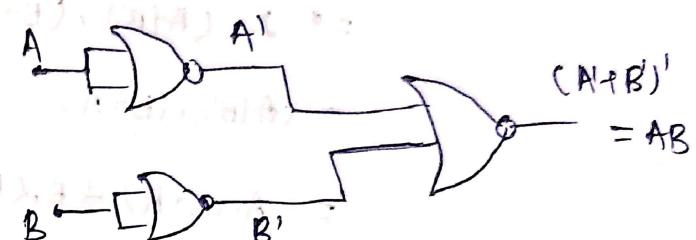


$$Y = A \cdot B$$

$$(A+B)' = A'B'$$

$$(A'+B')' = A''B'' = AB$$

$$Y = (A'+B')' = AB$$



EX-OR



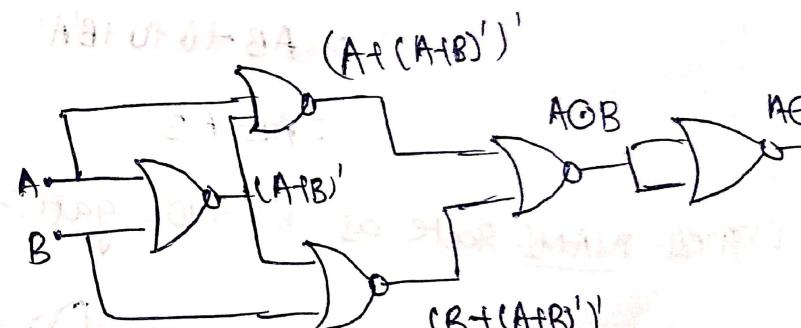
$$Y = A \oplus B$$

$$(A+(A \cdot B))'$$

$$= (A+\overline{A \cdot B})'$$

$$= \overline{A} \cdot \overline{A \cdot B}$$

$$= \overline{A} \cdot \overline{A} + \overline{A} \cdot B$$
$$= 0 + A'B = A'B$$



$$(B+(A+B))' = B \cdot (A+B)$$

$$= B \cdot A + B \cdot B$$

$$= \overline{B} \cdot A$$

$$= B'A$$

$$Y = (A+(A \cdot B))' \rightarrow (B+(A+B))'$$

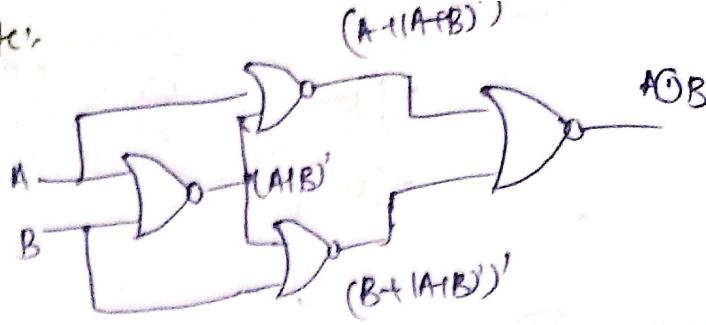
$$= A'B + B'A$$

NOR as EX-NOR gate:

EX-NOR



$$Y = AB! + A!B$$



Gate No.	Inputs	Output
1	A, B	(A+B)'
2	A, (A+B)'	(A+(A+B))'
3	(A+B)', B	(B+(A+B))'
4	(A+(A+B))', (B+(A+B))'	AB + A!B (B+(A+B))'

$$Y = \overline{(A+(A+B))'} + (B+(A+B))'$$

$$= \overline{(A+(A+B))} \cdot \overline{(B+(A+B))}$$

$$= (A+(A+B)) \cdot (B+(A+B))$$

$$= (A+A') \cdot (A+B) \cdot (B+A) \cdot (B+B')$$

$$= 1 \cdot (A+B) \cdot (B+A) \cdot 1$$

$$= (A+B) \cdot (B+A)$$

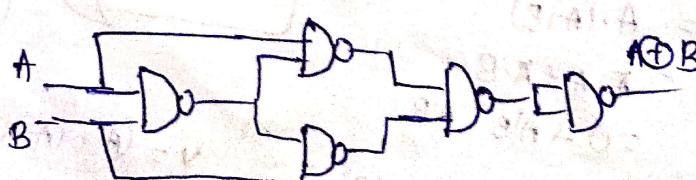
$$= A \cdot (B+A) + B \cdot (B+A)$$

$$= AB + AA' + B'B + B'A'$$

$$= AB + 0 + 0 + B'A'$$

$$= AB + A'B'$$

Express NAND gate as EX-NOR gate:-



Boolean Algebra

use the Rules of Boolean Algebra to express as boolean functions.

$$f_1(A, B, C) = A'B'C' + A'BC + AB'C' + AB'C + ABC' + ABC$$

$$= A'B(C+C') + AB'(C+C') + AB(C+C')$$

$$= A'B(1) + AB'(1) + AB(1) \quad (\text{as } C+C'=1)$$

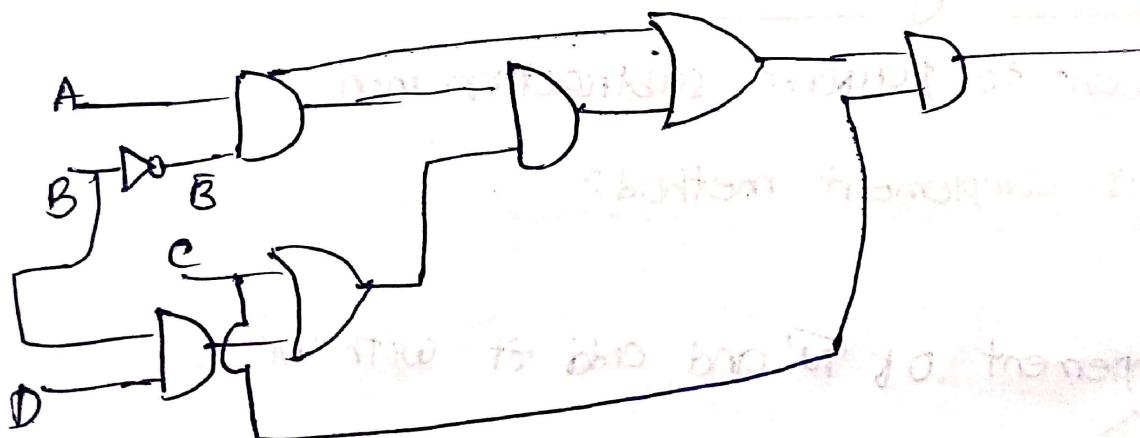
$$\Rightarrow A'B + AB' + AB$$

$$= A'B + A(B+B')$$

$$= A'B + A$$

$$= A+B$$

$$f_2(A, B, C) = (AB' (C+BD) + A'B') C$$



$$f = (AB' (C+BD)) + A'B' C$$

$$= (AB'C + ABD' + A'B') C$$

$$\therefore (AB'C + A'B') C \quad \therefore AB'C \cdot C \rightarrow A'B' C$$

$$= B' (A + AC)$$

$$= AB'C + A'B' C$$

$$= B'C (A + A')$$

$$= B'C (1)$$

$$= B'C$$

$$\begin{aligned}
 F &= \overline{AB} \cdot (A+B) + AB \cdot (\overline{A} + \overline{B}) \\
 &\Rightarrow \overline{AB} + (\overline{A} + B) + AB \cdot (\overline{A} + \overline{B}) \cdot \overline{C} \\
 &= AB + \overline{A} \cdot \overline{C} + AB \cdot (\overline{A} + \overline{B}) \cdot \overline{C} \\
 &\Rightarrow AB + \overline{A} \cdot \overline{C} + AB \cdot \overline{C}^0 \\
 &\Rightarrow AB + \overline{A} \cdot \overline{C} + \overline{A} \cdot \overline{C}^0 \\
 &\Rightarrow \overline{A} \cdot \overline{B} + \overline{A} \cdot \overline{C} + \overline{A} \cdot \overline{C}^0 \\
 &\Rightarrow \overline{A} \cdot (B + \overline{C})
 \end{aligned}$$

Simplify $AB + \overline{AC} + BC = AB + \overline{AC}$

$$\begin{aligned}
 AB + \overline{AC} + BC &\quad AB + \overline{AC} + BC \cdot 1 \\
 &= AB + C(\overline{A} + B) \quad \Rightarrow AB + \overline{A}(1 + BC) \\
 &= AB + C \cdot \overline{A} + C \cdot B \quad \Rightarrow AB + \overline{A} + BC \\
 &= AB + C \cdot \overline{A} + C \cdot B \quad \Rightarrow AB + \overline{A} + \overline{C} + BC \\
 &\quad \Rightarrow AB + \overline{A} + \overline{C} + \overline{C}B \\
 &\quad \Rightarrow AB + \overline{A} + \overline{C} \\
 &\quad \Rightarrow AB + \overline{AC}
 \end{aligned}$$

Binary subtraction using complement:-

Let us say we want to perform subtraction $M - N$

Subtraction using 1's complement method:

Step :-

(1) Add the 1's complement of 'N' and add it with 'M'

(2)

if no carry comes

if carry comes

→ Result is -ve

(N is higher than M)

→ put a -ve sign

→ take 1's complement

of addition result

110 010

1's complement of N = 101

$$\begin{array}{r}
 +110 \\
 +101 \\
 \hline
 1011
 \end{array}$$

carrying bits

Add the carry with the result

$$\begin{array}{r}
 011 \\
 +100 \\
 \hline
 100
 \end{array}$$

Subtract 010 with 110

N = 110 1's complement 001

$$\begin{array}{r}
 010 \\
 +001 \\
 \hline
 011
 \end{array}$$

1's complement -100

$$\begin{array}{r}
 M \leftarrow 1011 \\
 N \leftarrow 1101 \\
 \hline
 \end{array}$$

$\therefore N$'s 1's $\rightarrow 0010$

$$\begin{array}{r}
 1011 \\
 +0010 \\
 \hline
 1101
 \end{array}$$

- (0010)

Subtraction using 2's complement method

(1) Add 2's complement of N with M

If carrying comes

If no carrying comes

\rightarrow simply discard

\rightarrow Result is $-ve$ @

that carrying

\rightarrow put a $-ve$ sign

\rightarrow Take 2's complement of addition result

1011

1101

2's complement of N $\rightarrow 1101 \rightarrow 0010$

$$\begin{array}{r}
 0010 \\
 +1101 \\
 \hline
 0011
 \end{array}$$

$$\begin{array}{r}
 1011 \\
 0011 \\
 \hline
 1010
 \end{array}$$

Result

$= -(0101)$

2's complement of N \rightarrow

0100

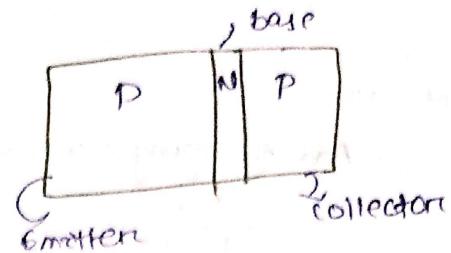
$$\begin{array}{r}
 0100 \\
 +1101 \\
 \hline
 0101
 \end{array}$$

$$\begin{array}{r}
 0101 \\
 +0010 \\
 \hline
 0010
 \end{array}$$

(X)

Result: 10010

J₁ J₂
FB FB
RB RB
RB RB
FB RB
RB FB



(1) Structure

Emitter → heavily doped

base → least doped

collector → moderately doped

(2) Doping

(3) Physical width

V_{BE}

J₁ (E-B) J₂ (B-C)
Emitter-base junction base-collector junction

FB	FB	Saturation region (ON switch)
RB	RB	Cutoff region (OFF switch)
FB	RB	Active region (amplifier)
RB	FB	Reverse Active region

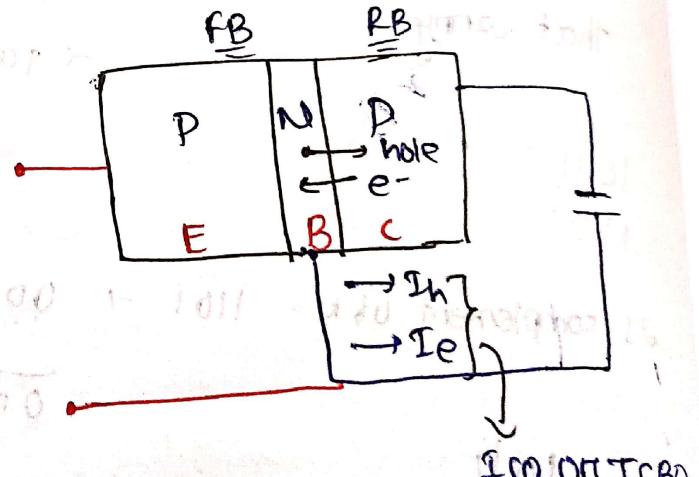
Reverse Active region:

* Emitter is heavily doped

high concentration of holes

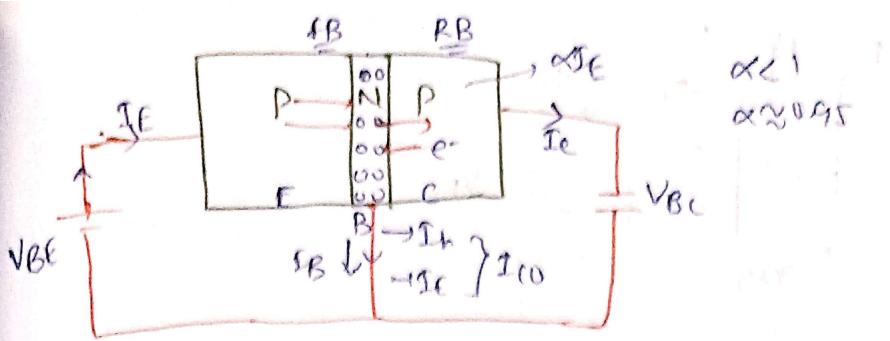
* Forward bias (majority carriers can pass the junction)

* Reverse bias (minority carriers can not pass the junction)



* I_{CBO} is the current flowing through collector & base when junction is open

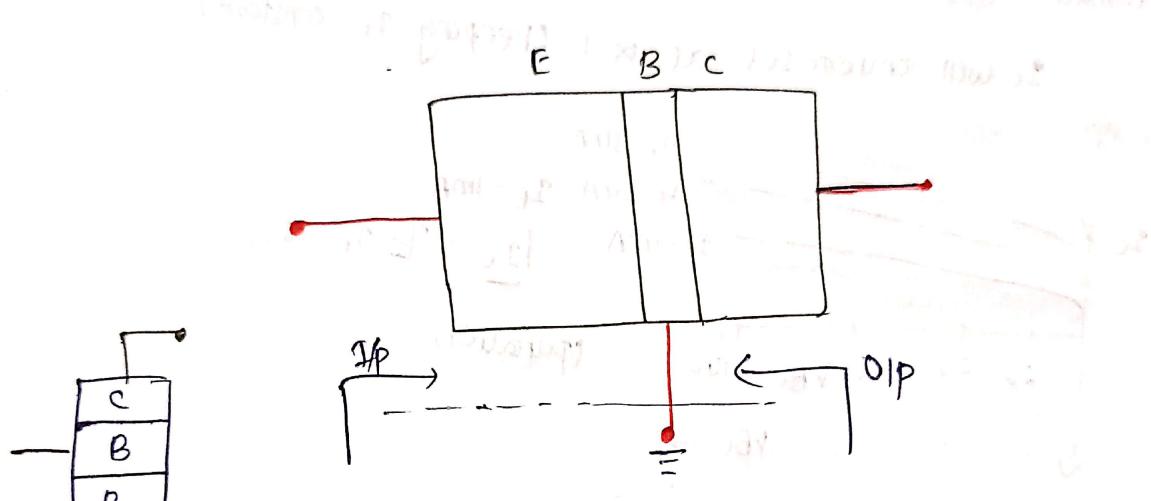
→ magnitude is sum of I_h



So Net current $I_E = \alpha I_F + I_{CO}$ (as both are flowing from base to collector)

$$I_E = I_C + I_B$$

Discuss the construction and current flow mechanism of transistor in Active region of operation.

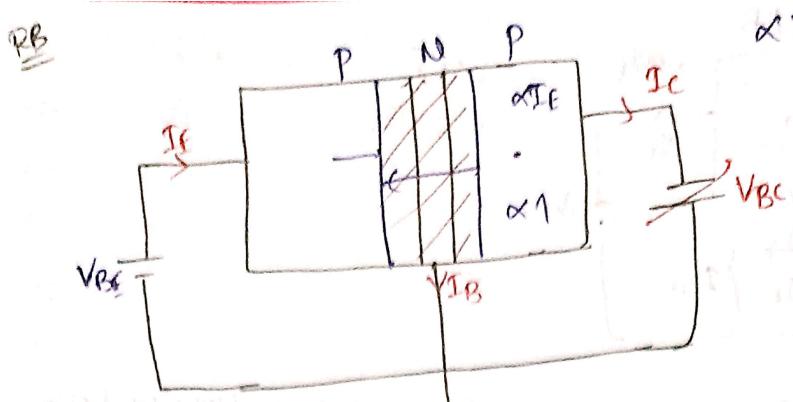


Input current = I_F Output current = I_C

Input Voltage = V_{BE} Output Voltage = V_{CE}

Output characteristics of transistor in common base configuration:-

- (i) In common base configuration output current is independent of output voltage.
- Output terminals are collector and base output terminals.
- (ii) So, the output characteristics is graph between output voltage (V_{CB}) to output current (I_{CO}) keeping OIP constant.
- ⇒ BJT is a current controlled voltage source.

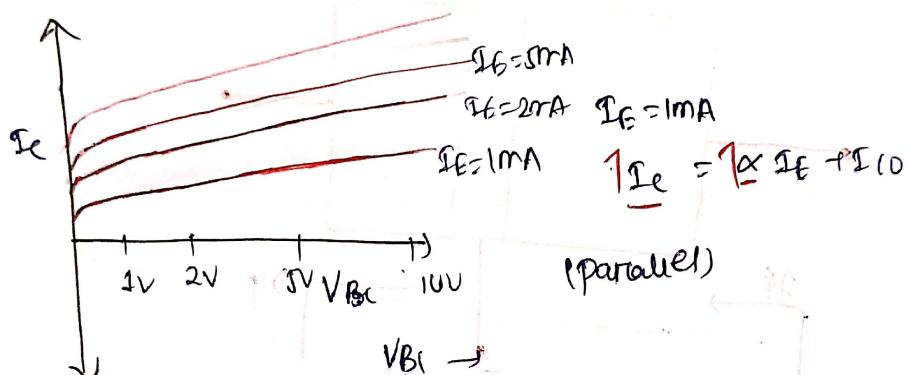


→ when forward biased, depletion layer will increases

$$I_C = \alpha I_E + I_{C0}$$

→ when Reverse biasing potential, reverse saturation current remains constant

I_C will increases as α if (keeping I_E constant)



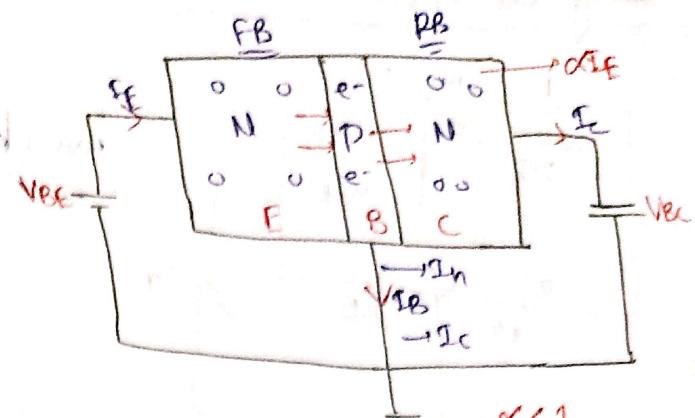
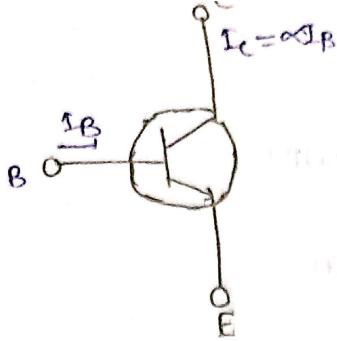
Active Region of operation:- (NPN)

- The active region is defined as region in which the emitter-base junction is forward biased and collector-base junction is reverse-biased
- A transistor while in this region will act as amplifier
- This region lies between cutoff and saturation

Hence Emitter-base → forward biased

base-collector → Reverse biased

- Here width of base-emitter junction is small, while compared to the width of collector-base junction.



$$\text{Hence } V_{BE} = V_B - V_E > 0 \\ \Rightarrow V_B > V_E$$

$$V_{CB} = V_C - V_B > 0 \\ V_C > V_B$$

$$\text{So } V_C > V_B > V_E$$

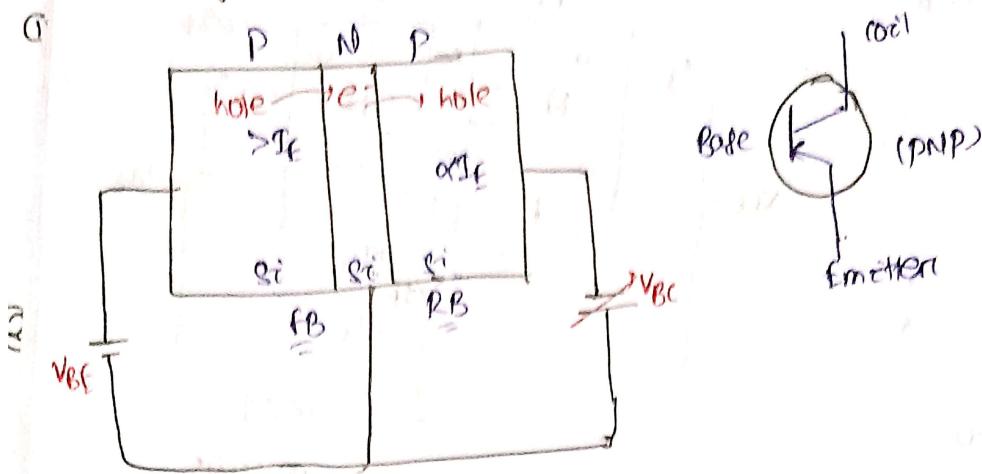
PRINCIPLE :-

- (i) usually base of NPN transistors are thin and lightly doped, so it has fewer holes as compared to the electrons in emitter.
- (ii) The recombination of holes in the base with electrons in emitter region will constitute flow of base current.
- (iii) Then the remaining large number of electrons in emitter will cross reverse biased collector junction in the form of collector current.
- (iv) According to Kirchhoff's current law, the emitter current is equal to the sum of collector current and base current.
- (v) Generally, the base current I_B will remain small when compared to collector current and emitter current.

$$I_F = I_C + I_B$$

- (vi) In transistor, if collection current I_C ~ collection temperature T , then resistance will get reduced hence collector I_c will increase, this phenomenon is known as thermal runaway in BJT.

Early effect / base-width modulation



→ Due to reverse biasing, width of depletion layer increases.

→ When $V_{BC} \downarrow \rightarrow$ depletion layer will increase.

→ Depletion layer will be more towards base than collector.

→ Due to narrower region, electron-hole recombⁿ will decrease.

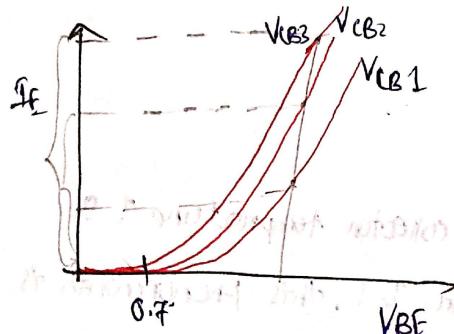
So, $\frac{V_{CB1}}{V_{CB2}} \rightarrow \alpha^2$
 $\frac{I_E1}{I_E2} \rightarrow \alpha^2$

→ If value of I_E increases due to increasing concentration gradient, this effect of effective width variation is called as base-width modulation / Early effect due to reverse biasing potential V_{CB} .

Input characteristics:

→ It is the curve between V_{BE} and I_E for fixed values of parameters.

→ It has requirement of (0.7V) .



$$V_{CB3} > V_{CB2} > V_{CB1}$$

$$I_C = \alpha I_E + I_{CBO}$$

$I_C \approx \alpha I_E$ because I_{CBO} is due to minority carriers so less than $I_E = I_C$ and $I_O = I_C$

Transistor in common base configuration can never be employed as current amplifier.

$$\alpha = \frac{I_E}{I_C} \quad \alpha < 1$$

α is current amplification factor in common base configuration.





	IIP	OIP
V _{OH}	V _{BE}	V _{CE}
Cut-off	I _B	I _C

$$\beta = \frac{I_C}{I_B}$$

β is the current amplification factor in common

$$\beta = \frac{I_C}{I_B}$$

$$I_E = I_C + I_B$$

$$\frac{I_E}{I_B} = \frac{I_C + I_B}{I_B} = \frac{I_C}{I_B} + 1$$

$$I = \alpha + \frac{I_C}{\beta I_B} \quad (I_B = \frac{I_C}{\beta})$$

$$I = \alpha + \frac{\alpha}{\beta}$$

$$I - \alpha = \frac{\alpha}{\beta} \Rightarrow \boxed{\beta = \frac{\alpha}{I - \alpha}}$$

$$\alpha = \frac{I_C}{I_E}$$

$$I_E = I_C + I_B$$

$$I_E = \frac{I_C}{\alpha}$$

$$\frac{I_C}{I_B} = \frac{I_C + I_B}{I_B} = 1 + \frac{I_B}{I_B}$$

$$\frac{I_C}{\alpha I_B} = \beta + 1$$

$$\Rightarrow \frac{\beta}{\alpha} = \beta + 1$$

$$\boxed{\alpha = \frac{\beta}{1 + \beta}}$$

Value of β ranges between 40 to 1000

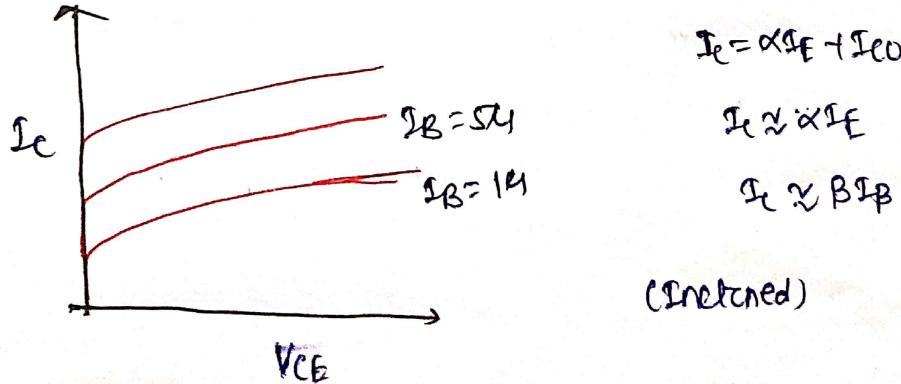
$$\beta = \frac{0.5}{0.5} = 1$$

$$\beta = \frac{0.6}{1 - 0.6} = \frac{0.6}{0.4} = 1.5$$

with increasing α, β

Output characteristics of CE

Output characteristic for CE configuration is the graph between output voltage V_{CE} and I_C keeping input current I_B constant



* find regions, active, saturation and cut-off region in the characteristic curve

part characteristics

keeping voltage const, curve between V_{CE} and I_E

keeping V_{CE} const

$$V_{CE} = 7V$$

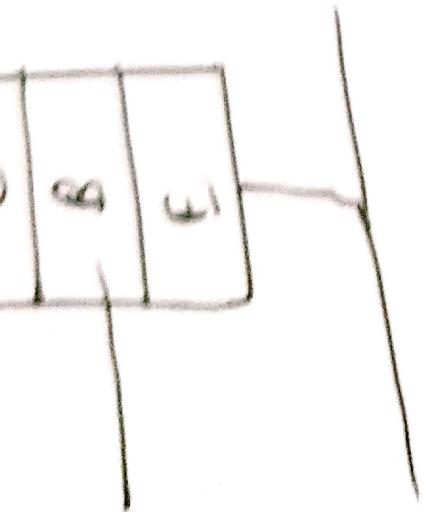
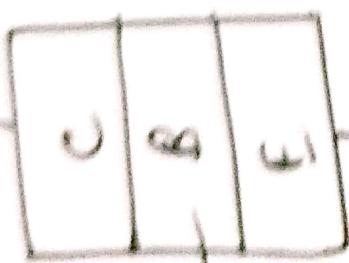
$$I_E = 10A$$

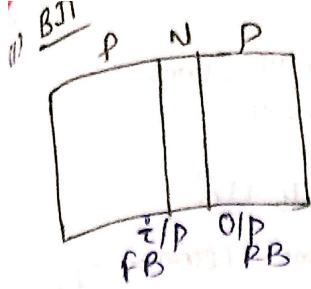
$$V_{CE} = 20V$$

I_E

V_{CE}

$$V_{CE_1} > V_{CE_2} > V_{CE_3}$$





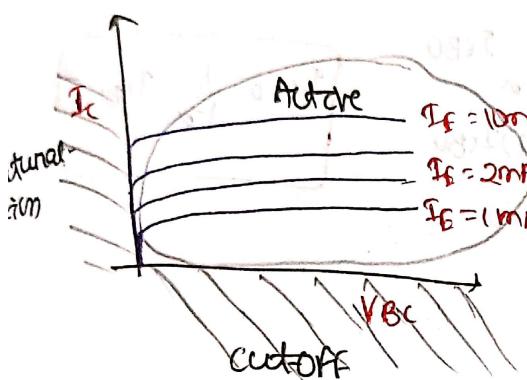
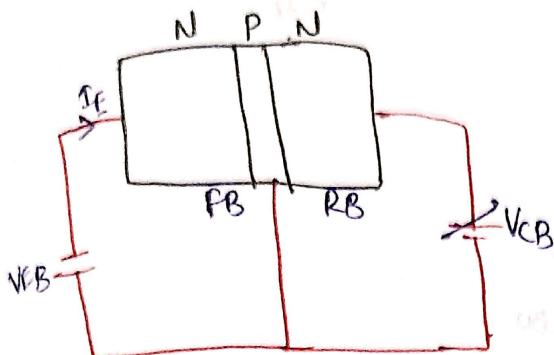
Due to hole αe^-

$$I_C = \alpha I_E + I_{CO}$$

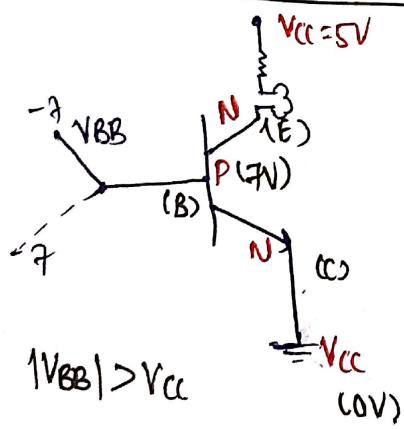
$$I_F = I_C + I_B$$

$I_C = \alpha I_F$, $I_F > I_B$

Due to transfer of resistors, it is called transistor



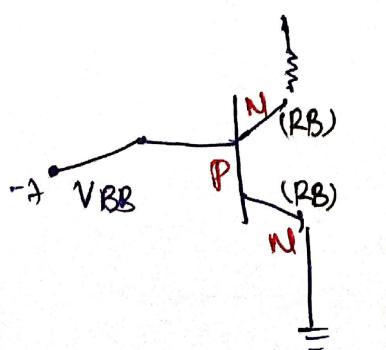
Transistor as a switch:



(cutoff \rightarrow (RB) \rightarrow OFF)

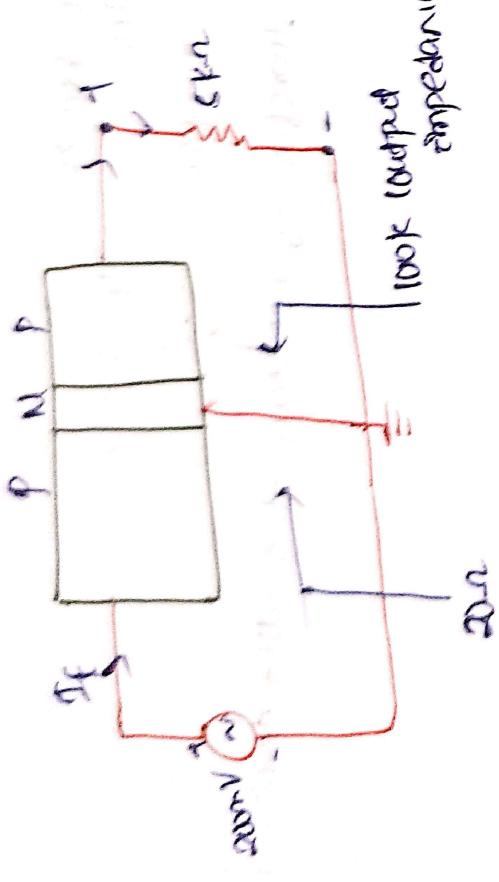
Saturation \rightarrow (FB) \rightarrow ON

Since both junctions are forward-biased, it will act as short-circuit \rightarrow Emitter-collector junction.



Since both junc's are reverse-biased, it will act as off-switch

(open circuit) \rightarrow NO current will flow through it



$$I_C = \frac{200mV}{20\Omega} = 10mA$$

$$\begin{aligned} I_C &= \alpha I_E + I_{CEO} \\ &\approx I_E \quad (\text{since } \alpha \approx 1) \\ &\approx I_C \end{aligned}$$

look (output impedance)

$$I_C = \alpha I_E + I_{CEO}$$

$$= \alpha (I_C + I_B) + I_{CEO}$$

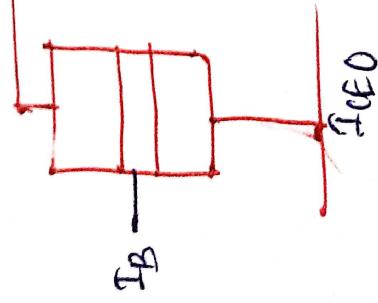
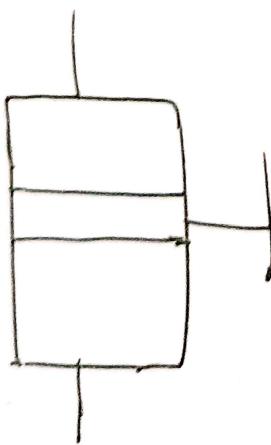
$$I_C - \alpha I_C = \alpha I_B + I_{CEO}$$

$$I_C(1-\alpha) = \alpha I_B + I_{CEO}$$

$$I_C = \frac{\alpha}{1-\alpha} I_B + \frac{1}{1-\alpha} I_{CEO}$$

$$I_C = \beta I_B + (1/\alpha) I_{CEO}$$

$$= \beta I_B + I_{CEO}$$



$$\boxed{I_{CEO} = \frac{1}{1-\alpha} I_{CEO}}$$