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Maximum size square sub-matrix with all 1s

Given a binary matrix, find out the maximum size square sub-matrix with all 1s.

For example, consider the below binary matrix.

```
      0
      1
      1
      0
      1

      1
      1
      0
      1
      0

      0
      1
      1
      1
      0

      1
      1
      1
      1
      1

      0
      0
      0
      0
      0
```

The maximum square sub-matrix with all set bits is

```
1 1 1
1 1 1
1 1 1
```

Algorithm:

Let the given binary matrix be M[R][C]. The idea of the algorithm is to construct an auxiliary size matrix S[][] in which each entry S[i][j] represents size of the square sub-matrix with all 1s including M[i][j] where M[i][j] is the rightmost and bottommost entry in sub-matrix.

```
1) Construct a sum matrix S[R][C] for the given M[R][C].
    a)Copy first row and first columns as it is from M[][] to S[][]
    b)For other entries, use following expressions to construct S[][]
    If M[i][j] is 1 then
        S[i][j] = min(S[i][j-1], S[i-1][j], S[i-1][j-1]) + 1
        Else /*If M[i][j] is 0*/
        S[i][j] = 0
2) Find the maximum entry in S[R][C]
3) Using the value and coordinates of maximum entry in S[i] print
```

3) Using the value and coordinates of maximum entry in S[i], print sub-matrix of M[][]

For the given M[R][C] in above example, constructed S[R][C] would be:

```
0 1 1 0 1
```

```
1 1 0 1 0
  1 1 1
         0
1
  1
    2
       2
1
  2
    2
       3
         1
0
  0
    0
       0
         0
```

The value of maximum entry in above matrix is 3 and coordinates of the entry are (4, 3). Using the maximum value and its coordinates, we can find out the required sub-matrix.

```
#include<stdio.h>
#define bool int
#define R 6
#define C 5
void printMaxSubSquare(bool M[R][C])
  int i,j;
  int S[R][C];
  int max_of_s, max_i, max_j;
  /* Set first column of S[][]*/
  for(i = 0; i < R; i++)</pre>
     S[i][0] = M[i][0];
  /* Set first row of S[][]*/
  for(j = 0; j < C; j++)
     S[0][j] = M[0][j];
  /* Construct other entries of S[][]*/
  for(i = 1; i < R; i++)
    for(j = 1; j < C; j++)
      if(M[i][j] == 1)
        S[i][j] = min(S[i][j-1], S[i-1][j], S[i-1][j-1]) + 1;
        S[i][j] = 0;
    }
  }
  /* Find the maximum entry, and indexes of maximum entry
     in S[][] */
  \max_{0} s = S[0][0]; \max_{i} s = 0; \max_{j} s = 0;
  for(i = 0; i < R; i++)</pre>
    for(j = 0; j < C; j++)
      if(max_of_s < S[i][j])
         max_of_s = S[i][j];
         max_i = i;
         max_j = j;
      }
    }
  }
  printf("\n Maximum size sub-matrix is: \n");
  for(i = max_i; i > max_i - max_of_s; i--)
    for(j = max_j; j > max_j - max_of_s; j--)
    {
      printf("%d ", M[i][j]);
```

```
printf("\n");
/* UTILITY FUNCTIONS */
/* Function to get minimum of three values */
int min(int a, int b, int c)
 int m = a;
 if (m > b)
   m = b;
 if (m > c)
    m = c;
  return m;
/* Driver function to test above functions */
int main()
 bool M[R][C] = \{\{0, 1, 1, 0, 1\},
                    {1, 1, 0, 1, 0},
                    \{0, 1, 1, 1, 0\},\
                    \{1, 1, 1, 1, 0\},\
                    {1, 1, 1, 1, 1},
                    {0, 0, 0, 0, 0};
 printMaxSubSquare(M);
  getchar();
```

Run on IDE

Time Complexity: O(m*n) where m is number of rows and n is number of columns in the given matrix.

Auxiliary Space: O(m*n) where m is number of rows and n is number of columns in the given matrix.

Algorithmic Paradigm: Dynamic Programming

Please write comments if you find any bug in above code/algorithm, or find other ways to solve the same problem

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