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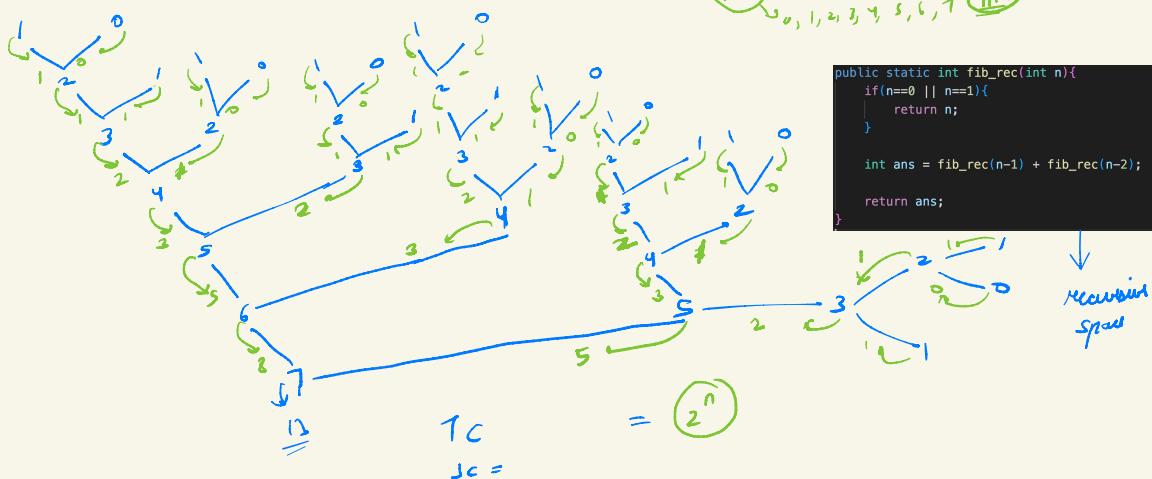
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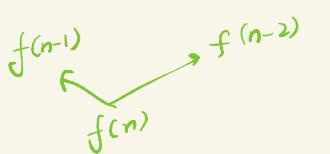


# Get the  $n^{\text{th}}$  term  
 $\Rightarrow 0, 1, 1, \textcircled{2}, 3, 5, 8, 13, 21, 34, 55, 89, \dots$   
 $2 \rightarrow 1, 3 \rightarrow 2$  memorization



```
public static int fib_rec(int n){
    if(n==0 || n==1){
        return n;
    }
    int ans = fib_rec(n-1) + fib_rec(n-2);
    return ans;
}
```

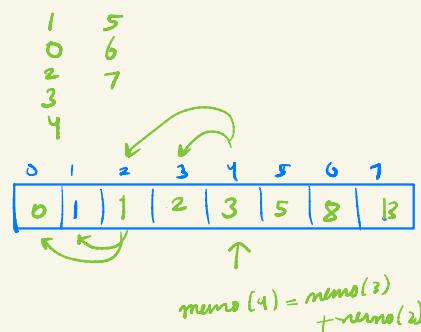
overlapping subproblems



recursion space  
 $O(n)$



$T_C = O(n)$   
 $SC = O(n) + \text{rec. sp.}$



```
public static int fib_memo(int n, int[] memo){
    if(n==0 || n==1){
        return memo[n]=n;
    }
    if(memo[n]!=0) return memo[n];
    int ans = fib_memo(n-1,memo) + fib_memo(n-2,memo);
    return memo[n]=ans;
}
```

- 1) Find the flow, write the for loop
- 2) Replace return with continue;
- 3) Remove memorization line {why?}
- 4) Replace calls with df.

```

public static int tab(int N, int[] memo){
    for(int n=0; n<=N; n++){
        if(n==0 || n==1){
            memo[n]=n;
            continue;
        }

        // if(memo[n]!=0) return memo[n];

        int ans = memo[n-1] + memo[n-2]; //fib_memo(n-1,memo) + fib_memo(n-2,memo)

        memo[n]=ans;
    }

    return memo[N];
}

```

$$n=0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12$$

$$Tc = O(n)$$

$$Sc = O(1)$$

0	1	2	3	4	5	6	7	8	9	10	11	12
0	1	1	2	3	5	8	13	21	34	55	89	144

```

public static int tabulation(int n){
    int[] dp = new int[n+1];

    dp[0] = 0;
    dp[1] = 1;

    for(int i=2; i<=n; i++){
        dp[i] = dp[i-1] + dp[i-2];
    }

    return dp[n];
}

```

Recursion ( ↴ )

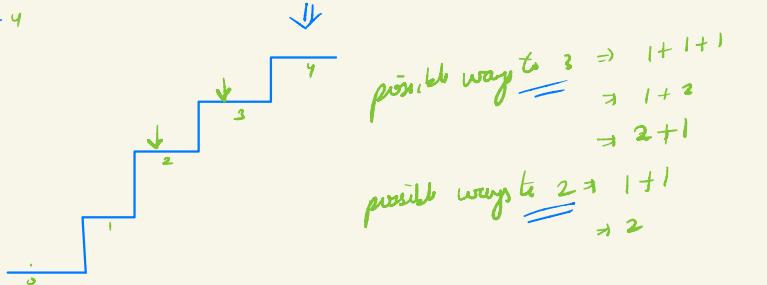


Memorization ( ) add two lines

↓  
Tabulation ( )

$n=4$

0, 1, 1, 2, 3, 5, 8



$$\text{ways}(n) = \text{ways}(s) + \text{ways}(w)$$

↓      ↓

1      2

$$f(n) = f(n-1) + f(n-2)$$

↳ fibonacci

possible ways to 4  $\Rightarrow$

1+1+1+1  
1+2+1  
2+1+1  


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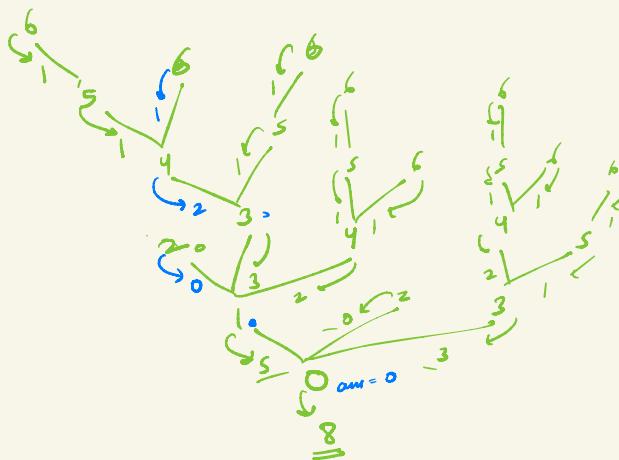
1+1+2  
2+2

3	3	0	2	2	3
0	1	2	3	4	5

6

min(ans(i))<sup>n</sup>

memoiz<sup>2</sup>



idm = 5  
jump = 12  
 $\underline{\underline{5+2}}$

```
public int countWays(int idx, int[] arr){  

    if(idx == arr.length){  

        return 1;  

    }  
  

    int ans = 0;  

    for(int jump=1; jump<=arr[idx]; jump++){  

        if(idx + jump <= arr.length)  

            ans += countWays(idx+jump, arr);  

    }  
  

    return ans;  
}
```

3	3	0	2	2	3
0	1	2	3	4	5

2	3
6	1
5	0
4	

0	1	2	3	4	5	6
8	5	0	3	2	1	1



```
public static int countWays_memo(int idx, int[] arr, int[] memo){
    if(idx == arr.length){
        return memo[idx]=1;
    }

    if(memo[idx]!=0) return memo[idx];

    int ans = 0;
    for(int jump=1; jump<=arr[idx]; jump++){
        if(idx + jump <= arr.length)
            ans += countWays_memo(idx+jump, arr,memo);
    }

    return memo[idx] = ans;
}
```

0	1	2	3	4	5
3	3	0	2	2	3

dp(s)

memo(4)  
5  
6

memo(s)

number of ways  
to reach n from s

break till  
10:45

0	1	2	3	4	5	6
8	5	0	3	2	1	1

idn = 6543210  
jump = 123

ans = 5 + 0 + 3 = 8

```
public int countWays_tabulation(int idx, int[] arr, int[] memo){
    for(int id=arr.length; id>=0; id--){
        if(id == arr.length){
            memo[id]=1;
            continue;
        }

        int ans = 0;
        for(int jump=1; jump<=arr[id]; jump++){
            if(id + jump <= arr.length)
                ans += memo[id+jump]; //countWays_memo(id+jump, arr,memo);
        }

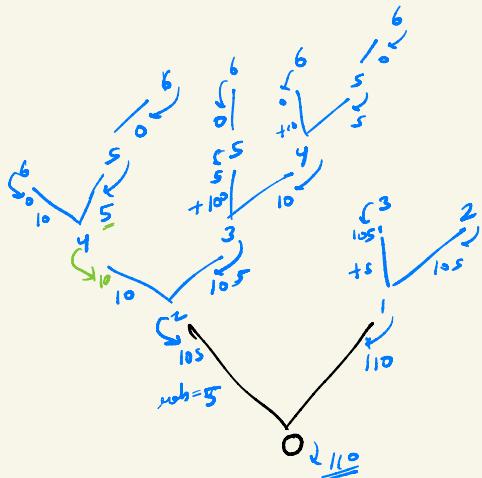
        memo[id] = ans;
    }

    return memo[0];
}
```

0	1	2	3	4	5
5	5	10	100	10	5

↑

165



ans: 5, 5, 10, 100, 10, 5  
↑

0	1	2	3	4	5	6
110	110	105	105	10	5	0

dp(i)  
maximum choice  
if at start from i th  
idx

$$m = 5 + 105$$

$$nr \geq 110$$

day sum → 9  
why  
rec mem ( )  
tab ( )

```
public int findMax_tabulation(int idx, int[] arr, int[] memo){
    for(idx=arr.length; idx>=0; idx--){
        if(idx == arr.length){
            memo[idx]=0;
            continue;
        }

        int rob=arr[idx];
        int notRob=0;

        if(idx+2<=arr.length)
            rob += memo[idx+2]; //findMax_memo(idx+2, arr,memo);

        notRob = memo[idx+1]; //findMax_memo(idx+1, arr,memo);

        int ans = Math.max(rob,notRob);

        memo[idx]=ans;
    }
}

return memo[0];
}
```