



- 1 Two randomly selected groups of students, with similar ranges of abilities, take the same examination in different rooms. One group of 140 students takes the examination with background music playing. The other group of 210 students takes the examination in silence. Each student is awarded a grade for their performance in the examination and the numbers from each group gaining each grade are shown in the following table.

|                  | Grade awarded |    |    |
|------------------|---------------|----|----|
|                  | A             | B  | C  |
| Background music | 49            | 51 | 40 |
| Silence          | 93            | 68 | 49 |

Test at the 10% significance level whether grades awarded are independent of whether background music is playing during the examination. [6]

This image shows a full page of handwriting practice paper. It features 20 evenly spaced horizontal dashed lines across the entire width of the page, providing a guide for letter height and placement. The background is plain white, and there are no margins or additional markings.

- 2 The times, in milliseconds, taken by a computer to perform a certain task were recorded on 10 randomly chosen occasions. The times were as follows.

6.44    6.16    5.62    5.82    6.51    6.62    6.19    6.42    6.34    6.28

It is claimed that the median time to complete the task is 6.4 milliseconds.

- (a)** Carry out a Wilcoxon signed-rank test at the 5% significance level to test this claim. [6]

[illegible]

- (b)** State an underlying assumption that is made when using a Wilcoxon signed-rank test. [1]

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**3** The continuous random variable  $X$  has probability density function  $f$  given by

$$f(x) = \begin{cases} \frac{3}{16}(2 - \sqrt{x}) & 0 \leq x < 1, \\ \frac{3}{16\sqrt{x}} & 1 \leq x \leq 9, \\ 0 & \text{otherwise.} \end{cases}$$

(a) Find  $E(X)$ .

[3]

[illegible]

The random variable  $Y$  is such that  $Y = \sqrt{X}$ .

- (b)** Find the probability density function of  $Y$ . [5]

This image shows a full page of a handwriting practice worksheet. It consists of approximately 20 horizontal rows. Each row is defined by two parallel dotted lines, creating a series of uniform gaps for letter height. The lines are evenly spaced across the entire page, providing a guide for consistent letter formation. There is no text or other markings on the page.

- 4 A company has two different machines,  $X$  and  $Y$ , each of which fills empty cups with coffee. The manager is investigating the volumes of coffee,  $x$  and  $y$ , measured in appropriate units, in the cups filled by machines  $X$  and  $Y$  respectively. She chooses a random sample of 50 cups filled by machine  $X$  and a random sample of 40 cups filled by machine  $Y$ . The volumes are summarised as follows.

$$\Sigma x = 15.2 \quad \Sigma x^2 = 5.1 \quad \Sigma y = 13.4 \quad \Sigma y^2 = 4.8$$

The manager claims that there is no difference between the mean volume of coffee in cups filled by machine  $X$  and the mean volume of coffee in cups filled by machine  $Y$ .

Test the manager's claim at the 10% significance level.

[9]

This image shows a full page of a handwriting practice worksheet. It consists of multiple rows of horizontal dashed lines spaced evenly down the page, providing a guide for letter height and placement. The background is plain white, and there are no other markings or text present.



- 5** A large number of children are competing in a throwing competition. The distances, in metres, thrown by a random sample of 8 children are as follows.

19.8    22.1    24.4    21.5    20.8    26.3    23.7    25.0

- (a) Assuming that distances are normally distributed, test, at the 5% significance level, whether the population mean distance thrown is more than 22.0 metres. [7]

[illegible]



- (b) Find a 95% confidence interval for the population mean distance thrown. [3]

- 6 A bag contains 4 red balls and 6 blue balls. Rassa selects two balls at random, without replacement, from the bag. The number of red balls selected by Rassa is denoted by  $X$ .

(a) Find the probability generating function,  $G_X(t)$ , of  $X$ . [2]

[illegible]

Rassa also tosses two coins. One coin is biased so that the probability of a head is  $\frac{2}{3}$ . The other coin is biased so that the probability of a head is  $p$ . The probability generating function of  $Y$ , the number of heads obtained by Rassa, is  $G_Y(t)$ . The coefficient of  $t$  in  $G_Y(t)$  is  $\frac{7}{12}$ .

**(b)** Find  $G_Y(t)$ . [3]

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

The random variable  $Z$  is the sum of the number of red balls selected and the number of heads obtained by Rassa.

- (c) Find the probability generating function of  $Z$ , expressing your answer as a polynomial. [3]

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- (d) Use the probability generating function of  $Z$  to find  $E(Z)$ . [2]

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