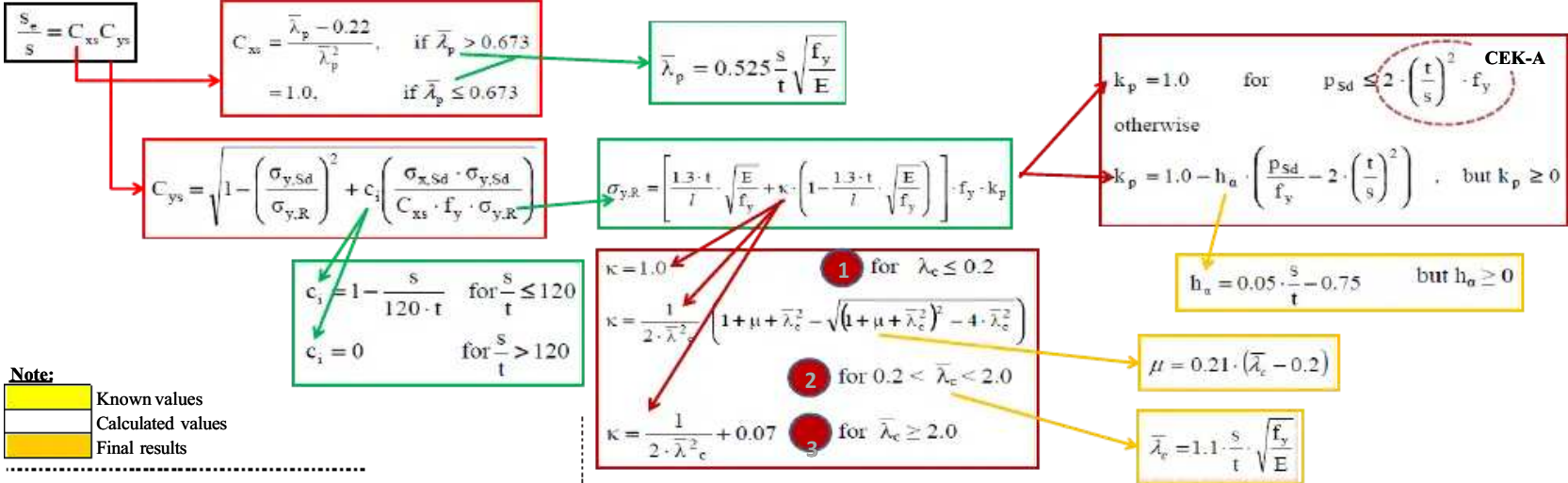


a. Effective Plate Width (s_e)

The effective plate width for a continuous stiffener subjected to longitudinal and transverse stress and shear is calculated as follows:



Note:

	Known values
	Calculated values
	Final results

Known values:

l	4000	mm	plate length or stiffener length
s	1000	mm	plate width, stiffener spacing.
t	20	mm	plate thickness
ρ _w	1025.00	kg/m ³	water density
g	9.81	m/s ²	gravity acceleration
d	15.00	m	hydrostatic pressure depth
f _y	300.00	MPa	characteristic yield strength
E	200.00	GPa	Young modulus of elasticity

Where:

plate length or stiffener length
plate width, stiffener spacing.
plate thickness
water density
gravity acceleration
hydrostatic pressure depth

Loadings:

σ _{x,Sd}	180.00	MPa
σ _{y,Sd}	50.00	MPa
p _{Sd}	150828.75	Pa=N/m ²
p _{Sd}	0.15	MPa

Where:

axial stress in plate and stiffener with compressive stresses as positive
transverse stress in plate and stiffener
design lateral force, for this case is the hydrostatic pressure at d

Reduced plate slenderness:

λ _e	1.017
λ _c	2.130

Where:

reduced plate slenderness in longitudinal direction
reduced plate slenderness in transverse direction

Since λ_p > 0.673, then: C_{xs} = 0.771 []
where: C_{xs} is reduction factor due to stresses in the longitudinal direction

Note:

s/t	50.00
c _i	0.583

The reduction factor due to lateral load, k_p:

CEK-A	0.24	MPa; it means p _{Sd}	<=	CEK-A	
Thus k _p	1.000	[]		otherwise, since h _a	1.750 []
				then k _p	1.00052 []

Since, μ = 0.405 [], and λ_c = 2.130 [], then parameter κ: can be found as follows:
(1) κ = 1.000 [] for λ_c ≤ 0.2
(2) κ = 0.198 [] for 0.2 < λ_c < 2.0
(3) κ = 0.180 [] for λ_c ≥ 2.0

Conclusion: κ = 0.180 []
Thus, the plate buckling resistance σ_{y,R} = 95.33 MPa

Now, we can calculate the reduction factor due to stresses in transverse direction, C_{ys} = 0.981 []

Finally: the effective plate width, S_e, is 756.41 mm

Hint:
See Section 7.3
DNV-RP-C201

b. Equivalent axial (N_{sd}) and lateral (q_{sd}) loads

The equivalent **axial force** should be taken as:

$$N_{sd} = \sigma_{x,sd} (A_s + st) + \tau_{if} st$$

$$\tau_{if} = \tau_{sd} - \tau_{crg} \quad \text{for } \tau_{sd} > \frac{\tau_{crl}}{\gamma_M}$$

and tension field action is allowed

$$\tau_{if} = 0 \quad \text{otherwise}$$

$$\tau_{crl} = k_l \cdot 0.904 \cdot E \cdot \left(\frac{t}{s}\right)^2$$

$$\tau_{crg} = k_g \cdot 0.904 \cdot E \cdot \left(\frac{t}{l}\right)^2$$

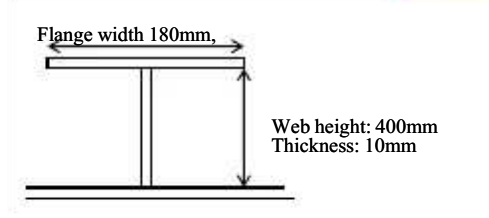
$$k_l = 5.34 + 4 \left(\frac{s}{l}\right)^2, \quad \text{for } l \geq s$$

$$= 5.34 \left(\frac{s}{l}\right)^2 + 4, \quad \text{for } l < s$$

$$k_g = 5.34 + 4 \left(\frac{l}{L_G}\right)^2, \quad \text{for } l \leq L_G$$

$$= 5.34 \left(\frac{l}{L_G}\right)^2 + 4, \quad \text{for } l > L_G$$

Stiffener cross section:



Known values from previous page

l	4000 mm	plate length or stiffener length
s	1000 mm	plate width, stiffener spacing.
t	20 mm	plate thickness
E	200.00 Gpa	Young modulus of elasticity
$\sigma_{x,sd}$	180.00 MPa	axial stress in plate and stiffener with compressive stresses as positive

Known values:

L_G	3000 mm	girder length
w_f	180 mm	flange width
t_f	20 mm	flange thickness
h_w	400 mm	web height
t_w	10 mm	web thickness
τ_{sd}	0.00 MPa	design shear stress
γ_M	1.15 []	resulting material factor

Since $k_l \geq s$, then $k_l = 5.59 []$, where k_l is buckling factor for plate between stiffeners.
 Since $k_g > L_G$, then $k_g = 13.49 []$, where k_g is buckling factor for plate with the stiffeners removed.

Thus:

τ_{crl}	404.27 MPa
τ_{crg}	60.99 MPa

Since $\tau_{sd} < \frac{\tau_{crl}}{\gamma_M}$ then: $\tau_{if} = 0.00$ MPa

The cross sectional area of stiffener is $A_s = 7600 \text{ mm}^2$;
 and the full plate cross section area $s \cdot t = 20000 \text{ mm}^2$

Therefore, the equivalent axial force, $N_{sd} = 4.968 \text{ MN}$

Note:

	Known values from previous page
	Known values
	Calculated values
	Final results

Hint:

See Section 7.2
 DNV-RP-C201

The equivalent **lateral line load** should be taken as:

$$q_{sd} = (p_{sd} + p_0) \cdot s$$

$$p_0 = (0.6 + 0.4\psi) \cdot C_0 \cdot \sigma_{y1, sd} \quad \text{if } \psi > -1.5$$

$$p_0 = 0 \quad \text{if } \psi \leq -1.5$$

$$\psi = \frac{\sigma_{y2, sd}}{\sigma_{y1, sd}}$$

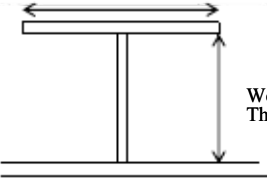
$$C_0 = \frac{W_{es} \cdot f_y \cdot m_e}{k_e \cdot E \cdot t^2 \cdot s}$$

$$k_e = 2 \cdot \left(1 + \sqrt{1 + \frac{10.9 \cdot I_s}{t^3 \cdot s}} \right)$$

Where W_{es} and I_s are determined by cross section analysis

Cross Section Analysis

Flange width 180mm,



Web height: 400mm
Thickness: 10mm

Known values from previous page

t	20 mm	plate thickness
s	1000 mm	plate width, stiffener spacing.
S _e	756.41 mm	the effective plate width

p _{sd}	0.1508 MPa
f _y	300.00 MPa

Section properties:

A _f	3600 mm ²
A _w	4000 mm ²
A _p	20000 mm ²
A _{pes}	15128 mm ²
z _f	430 mm
z _w	220 mm
z _p	10 mm
COG	95.22 mm
d _{f-es}	316.52 mm
d _{w-es}	106.52 mm
d _{pes}	-103.48 mm
c _{es}	344.78 mm

Where:

flange cross section area
web cross section area
plate cross section area, use s.
plate cross section area, use S_e.
flange COG, counted from base
web COG, counted from base
plate COG, counted from base
COG of stiffener + plate, use s.
distance of z_f and COG_{es}
distance of d_w and COG_{es}
distance of d_p and COG_{pes}
distance from COG_{es} to the outer fiber

Section properties:

I _f	120000 mm ⁴
I _w	53333333 mm ⁴
I _p	666667 mm ⁴
I _{pes}	504271 mm ⁴
d _f	334.78 mm
d _w	124.78 mm
d _p	-85.22 mm
I _s	665128696 mm ⁴
z _{pes}	10 mm
COG _{es}	113.48 mm
I _{es}	622003068 mm ⁴
W _{es}	1804044 mm ³

Where:

flange cross section moment of inertia
web cross section moment of inertia
plate cross section moment of inertia, use s.
plate cross section moment of inertia, use S_e.
distance of z_f and COG
distance of d_w and COG
distance of d_p and COG
moment of inertia of stiffener with full plate width
effective plate COG, counted from base
COG of stiffener + plate, use S_e.
moment of inertia of stiffener with effective plate width
section modulus for stiffener with effective plate at flange tip

Then, the factor k_e and C₀ is determined as follows:

k _e	62.24
C ₀	0.001446
ψ	1.00
p ₀	0.0723 MPa

Known values:

m ^c	13.3
σ _{y1, sd}	50.00 MPa
σ _{y2, sd}	50.00 MPa

Note:

m^c ≡ 13.3 for continuous stiffeners or
8.9 for simple supported stiffeners (sniped stiffeners)

Where:

σ_{y1, sd} larger design stress in the transverse direction, with tensile stresses taken as negative
σ_{y2, sd} smaller design stress in the transverse direction, with tensile stresses taken as negative

Finally, the equivalent lateral line load, q_{sd}

q _{sd}	223.11 N/mm
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c.1. Torsional buckling strength of stiffeners

The torsional buckling strength may be calculated as:

$$\frac{f_T}{f_y} = 1.0 \quad \text{when } \bar{\lambda}_T \leq 0.6$$

$$\frac{f_T}{f_y} = \frac{1 + \mu + \bar{\lambda}_T^2 - \sqrt{(1 + \mu + \bar{\lambda}_T^2)^2 - 4\bar{\lambda}_T^2}}{2\bar{\lambda}_T^2}$$

$$\mu = 0.35(\bar{\lambda}_T - 0.6)$$

$$\text{when } \bar{\lambda}_T > 0.6$$

For L- and T-stiffeners f_{ET} :

$$f_{ET} = \beta \frac{A_w + \left(\frac{t_f}{t_w}\right)^2 A_f}{A_w + 3A_f} G \left(\frac{t_w}{h_w}\right)^2 + \frac{\pi^2 E I_x}{3 \left(\frac{A_w}{3} + A_f\right) \left(\frac{t_w}{h_w}\right)^2}$$

$$I_x = \frac{1}{12} A_f b^2 + c^2 \frac{A_f}{1 + \frac{A_f}{A_w}}$$

f_{ET-1}

f_{ET-2}

For flatbar stiffeners f_{ET} :

$$f_{ET} = \left[\beta + 2 \left(\frac{h_w}{t_f} \right)^2 \right] G \left(\frac{t_w}{h_w} \right)^2$$

$$\beta = \frac{3C + 0.2}{C + 0.2}$$

$$\sigma_{j,Sd} = \sqrt{\sigma_{x,Sd}^2 + \sigma_{y,Sd}^2 - \sigma_{x,Sd} \sigma_{y,Sd} + 3\tau_{Sd}^2}$$

$$C = \frac{h_w}{s} \left(\frac{t}{t_w} \right)^3 \sqrt{1 - \eta}$$

$$\eta = \frac{\sigma_{j,Sd}}{f_{cp}} \quad \eta \leq 1.0$$

$$f_{cp} = \frac{f_y}{\sqrt{1 + \bar{\lambda}_y^2}}$$

$$c = 2 - \frac{s}{l}$$

$$\frac{1}{\bar{\lambda}_{e}^2} = \frac{f_y}{\sigma_{j,Sd}} \left(\left(\frac{\sigma_{x,Sd}}{f_{Epx}} \right)^c + \left(\frac{\sigma_{y,Sd}}{f_{Epy}} \right)^c + \left(\frac{\tau_{Sd}}{f_{Ept}} \right)^c \right)^{\frac{1}{c}}$$

$$f_{Epx} = 3.62 E \left(\frac{t}{s} \right)^2$$

$$f_{Epy} = 0.9 E \left(\frac{t}{s} \right)^2$$

$$f_{Ept} = 5.0 E \left(\frac{t}{s} \right)^2$$

Known values from previous page

l	4000 mm	plate length or stiffener length.
s	1000 mm	plate width, stiffener spacing.
t	20 mm	plate thickness
E	200 Gpa	Young modulus of elasticity
$\sigma_{x,Sd}$	180 MPa	axial stress in plate and stiffener
$\sigma_{y,Sd}$	50 MPa	transverse stress in plate and stiffener
τ_{Sd}	0 MPa	design shear stress
w_{fl}	180 mm	flange width = b
t _{fl}	20 mm	flange thickness
h _w	400 mm	web height
t _w	10 mm	web thickness
f _y	300 MPa	characteristic yield strength

Thus:

$$c = 1.75 []$$

Thus:

$$\sigma_{j,Sd} = 160.93 \text{ MPa}$$

Where:

$\sigma_{j,Sd}$ is design von Mises's equivalent stress

Euler buckling strength

f_{Epx}	289.60 MPa	Euler buckling strength for plate due to longitudinal stresses
f_{Epy}	72.00 MPa	Euler buckling strength for plate due to transverse stresses
f_{Ept}	400.00 MPa	Euler buckling shear strength for plate

Reduced equivalent slenderness

$$\bar{\lambda}_e = 1.825 []$$

Therefore:

$$f_{cp} = \frac{144.17}{1.12} \text{ MPa}$$

$$c = \frac{0.00}{1.0} []$$

Hint:

See Section 7.5.2
DNV-RP-C201

Known values from previous page

ν	0.3		Poisson's ratio
G	76923.077	MPa	shear modulus
A_w	4000	mm ²	web cross section area
A_f	3600	mm ²	flange cross section area
$b=w_f$	180	mm	flange width = b
e_f	0	mm	flange eccentricity

Thus:

$$I_z = 9720000 \text{ mm}^4$$

(moment of inertia of the stiffeners neutral axis normal to the plane of the plate)

Torsional elastic buckling strength (f_{ET})

I_T	f_{ET-1}	f_{ET-2}	f_{ET}	$\bar{\lambda}_{ET}$	μ	f_T (MPa)
0.8*1 0.4*1	0.0	303.8 1519.2	303.8 1519.2	0.994 0.444	-0.138 -0.034	308.88 308.88

c.2.Characteristic buckling strength

$$\frac{f_{Tb}}{f_T} = 1 \quad \text{when } \bar{\lambda} \leq 0.2$$

$$\bar{\lambda} = \sqrt{\frac{f_T}{f_E}}$$

where:

$f_T = f_y$ for check at plate side.

$f_T = f_y$ for check at stiffener side if

$f_T = f_T$ for check at stiffener side if

$$\bar{\lambda}_{AT} \leq 0.6$$

$$\bar{\lambda}_{AT} > 0.6$$

$$f_E = \pi^2 E \left(\frac{i_e}{l_e} \right)^2$$

$$i_e = \sqrt{\frac{I_e}{A_e}}$$

$$W = \min(W_{ep}, W_{es})$$

$$W_{es} = \frac{I_s}{z_1}$$

$$p_{cr} = \frac{12 W f_y}{l^2 \cdot s \cdot \gamma_M}$$

$$W_{ep} = \frac{I_s}{z_p}$$

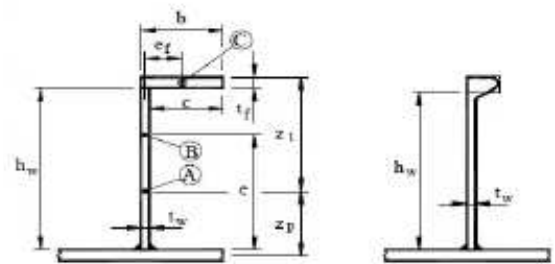
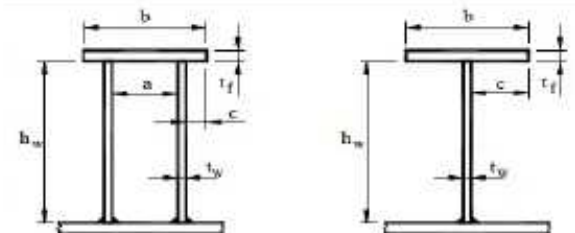
$$\frac{f_{Tb}}{f_T} = \frac{1 + \mu + \bar{\lambda}^2 - \sqrt{(1 + \mu + \bar{\lambda}^2)^2 - 4 \bar{\lambda}^2}}{2 \bar{\lambda}^2} \quad \text{when } \bar{\lambda} > 0.2$$

for check at plate side

$$\mu = \left(0.34 + 0.08 \frac{z_1}{i_e} \right) (\bar{\lambda} - 0.2)$$

for check at stiffener side

$$\mu = \left(0.34 + 0.08 \frac{z_p}{i_e} \right) (\bar{\lambda} - 0.2)$$



A = centroid of stiffener with effective plate flange.
B = centroid of stiffener exclusive of any plate flange.
C = centroid of flange.

Figure 7-3 Cross-sectional parameters for stiffeners and girders

Known values from previous page

COG	95.22	mm	
I_{es}	622003068	mm ⁴	moment of inertia of stiffener with effective plate width
f_y	300.00	MPa	characteristic yield strength
γ_M	1.15	[]	resulting material factor
l	4000	mm	plate length or stiffener length
s	1000	mm	plate width, stiffener spacing.
A_{pes}	15128	mm ²	COG of stiffener + plate, use s.
p_{sd}	0.15	MPa	design lateral pressure

Calculated values

z_p	85.22	mm	see Figure 7-3
z_t	354.78	mm	see Figure 7-3
W_{ep}	7299016	mm ³	effective elastic section modulus on plate side
W_{es}	1753195	mm ³	effective elastic section modulus on stiffener side
W	1753195	mm ³	elastic section modulus
p_r	0.34	MPa	lateral pressure giving yield in outer-fibre at support.
l_k	3120.57	mm	buckling length
i_e	202.77	mm	effective radius of gyration
f_E	8334.28	MPa	Euler buckling strength

The characteristic buckling strength for check at plate side

f_r	300	MPa	characteristic strength
$\bar{\lambda}$	0.190	[]	
μ	-0.005	[]	
f_k	300	MPa	characteristic buckling strength

The characteristic buckling strength for check at stiffener side

f_r	208	MPa	characteristic strength
$\bar{\lambda}$	0.158	[]	
μ	-0.016	[]	
f_k	208	MPa	characteristic buckling strength

c.3. Shear Stress Resistance

The resistance towards shear stresses τ_{Rd} is found as the minimum of τ_{Rdy} , τ_{Rdl} and τ_{Rds} according to the following:

$$\tau_{Rdy} = \frac{f_y}{\sqrt{3} \cdot \gamma_M}$$

$$\tau_{Rdl} = \frac{\tau_{crl}}{\gamma_M}$$

$$\tau_{Rds} = \frac{\tau_{crs}}{\gamma_M}$$

$$\tau_{crs} = \frac{36 \cdot E}{s \cdot t \cdot l^2} \cdot \sqrt[4]{I_p \cdot I_s^3}$$

$$I_p = \frac{t^3 \cdot s}{10.9}$$

Known values from previous page

f_y	300.00	MPa
γ_M	1.15	[-]
s	1000	mm
t	20	mm
I_s	665128696	mm ⁴
E	200.00	Gpa
l	4000	mm
τ_{crl}	404.27	MPa

where:

f_y characteristic yield strength

γ_M resulting material factor

s plate width, stiffener spacing.

t plate thickness

I_s moment of inertia of stiffener with full plate width.

E Young modulus of elasticity

l span length

τ_{crl} critical shear stress

Calculated values

τ_{crs}	2727.58	MPa
I_p	733945	mm ⁴

τ_{crs} critical shear stress

Therefore:

τ_{Rdy}	150.61	MPa
τ_{Rdl}	351.54	MPa
τ_{Rds}	2371.81	MPa

Thus:

τ_{Rd}	150.61	MPa
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τ_{Rd} design resistance shear stress

Hint:

See Section 7.6
DNV-RP-C201

c.4. The following resistance parameters are used in the interaction equations:

$$N_{Rd} = A_e \frac{f_y}{\gamma_M}$$

$$N_{ks,Rd} = A_e \frac{f_k}{\gamma_M}$$

$$N_{kp,Rd} = A_e \frac{f_k}{\gamma_M}$$

$$M_{s1,Rd} = W_{es} \frac{f_t}{\gamma_M}$$

$$M_{s2,Rd} = W_{es} \frac{f_t}{\gamma_M}$$

$$M_{st,Rd} = W_{es} \frac{f_y}{\gamma_M}$$

$$M_{p,Rd} = W_{ep} \frac{f_y}{\gamma_M}$$

$$N_E = \frac{\pi^2 E A_e}{\left(\frac{l_k}{i_e}\right)^2}$$

Known values from previous page

f_y	300 MPa	characteristic yield strength
γ_M	1.15 []	resulting material factor
A_n	3600 mm ²	Thus: $A_e = 22728$ mm ²
A_w	4000 mm ²	
A_{pes}	15128 mm ²	Where A_e is effective area of stiffener and plate
l_k	3121 mm	
i_e	202.77 mm	
E	200.00 Gpa	
		Thus: $N_E = 189.423$ MN

Thus:

$$\rightarrow N_{Rd} = 5.93 \text{ MN}$$

Hint:

See Section 7.7.3
DNV-RP-C201

For plate:

f_k	300 MPa	characteristic buckling strength
W_{ep}	7299016 mm ³	effective elastic section modulus on plate side

Thus:

$$\rightarrow N_{kp,Rd} = 5.93 \text{ MN}$$

For stiffener:

f_k	208 MPa	characteristic buckling strength
W_{es}	1753195 mm ³	effective elastic section modulus on stiffener side

Thus:

$$\rightarrow N_{ks,Rd} = 4.12 \text{ MN}$$

For:	Then:	Thus:
$l_T = 0.4 \cdot l$	$\rightarrow f_r = f_y = 300.00$ MPa	$\rightarrow M_{s1,Rd} = 457.36$ MN.mm
$l_T = 0.8 \cdot l$	$\rightarrow f_r = f_T = 208.48$ MPa	$\rightarrow M_{s2,Rd} = 317.83$ MN.mm

$M_{st,Rd}$	457.36 MN.mm
$M_{p,Rd}$	1904.09 MN.mm

$$M_{1,Sd} = \frac{q_{sd} l^2}{12} \quad M_{2,Sd} = \frac{q_{sd} l^2}{24} \quad u = \left(\frac{\tau_{sd}}{\tau_{Rd}} \right)^2$$

Since:

q_{sd}	223.110 N/mm
l	4000 mm

Then:

$M_{1,Sd}$	297.480 MN.mm
$M_{2,Sd}$	148.740 MN.mm

Because:

τ_{sd}	0.00 MPa
τ_{Rd}	150.61 MPa

Then:

$$u = 0.00 []$$

Where: q_{sd} is the equivalent lateral line load.

e. Interaction formulas

For continuous stiffeners the following four interaction equations need to be fulfilled

Lateral pressure on plate side:

$$1 \quad \frac{N_{Sd}}{N_{ks,Rd}} + \frac{M_{1,Sd} - N_{Sd} \cdot z^*}{M_{s1,Rd} \left(1 - \frac{N_{Sd}}{N_E} \right)} + u \leq 1$$

$$2 \quad \frac{N_{Sd}}{N_{kp,Rd}} - 2 \cdot \frac{N_{Sd}}{N_{Rd}} + \frac{M_{1,Sd} - N_{Sd} \cdot z^*}{M_{p,Rd} \left(1 - \frac{N_{Sd}}{N_E} \right)} + u \leq 1$$

$$3 \quad \frac{N_{Sd}}{N_{kr,Rd}} - 2 \cdot \frac{N_{Sd}}{N_{Rd}} + \frac{M_{2,Sd} + N_{Sd} \cdot z^*}{M_{st,Rd} \left(1 - \frac{N_{Sd}}{N_E} \right)} + u \leq 1$$

$$4 \quad \frac{N_{Sd}}{N_{kp,Rd}} + \frac{M_{2,Sd} + N_{Sd} \cdot z^*}{M_{p,Rd} \left(1 - \frac{N_{Sd}}{N_E} \right)} + u \leq 1$$

Known values from previous page

N_{Sd} **4.968** MN the equivalent axial force

Assume: z^* **0** mm the distance from the neutral axis of the effective section to the working point of the axial force

Finally:

EQ.1	1.874	>	1	NOK!
EQ.2	-0.170	<=	1	OK
EQ.3	-0.504	<=	1	OK
EQ.4	0.918	<=	1	OK

Thus:

Conclusion

The plate panel cannot resist buckling.

The reason:

We can see that the equivalent axial force is larger than the stiffener buckling load capacity.

Hint:

See Section 7.7.1
DNV-RP-C201