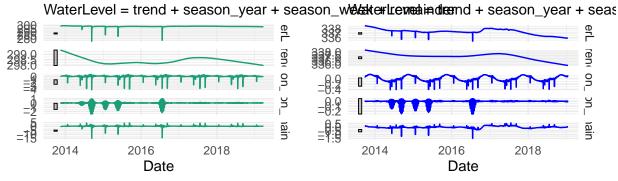
TimeSeriesForecasting_ARIMA_ETS

```
# Time Series Plots
plot_GW036334_1_1data < -GW036334_1_1data %>% ggplot(aes(x = Date, y = WaterLevel)) +
      geom_line(col="#f0027f")+labs(y= "Waterlevel", x = "Date", title = "GW036334_1_1")
plot_GW093067_1_1data <-GW093067_1_1data \%>\% \quad ggplot(aes(x = Date, y = WaterLevel)) + GW093067_1_1data <-GW093067_1_1data <-GW093067_1data <-GW
      geom\_line(col="#d95f02")+labs(y= "Waterlevel", x = "Date", title = "GW093067_1_1")
geom\_line(col="#1b9e77")+labs(y= "Waterlevel", x = "Date", title = "GW036976.1.2")
plot_GW965569.1.2data < -GW965569.1.2data %>% ggplot(aes(x = Date, y = WaterLevel)) +
      geom line(col="blue")+labs(y= "Waterlevel", x = "Date", title = "GW965569.1.2")
(plot_GW036334_1_1data|plot_GW093067_1_1data)/(plot_GW036976.1.2data|plot_GW965569.1.2data)
                        GW036334 1 1
                                                                                                                                                 GW093067_1_1
             342 -
                                                                                                                                       240
     Waterlevel
             340
                                                                                                                               Waterlevel
                                                                                                                                       239
             338
                                                                                                                                       238
                                                                                                                                      237
             336
                                                                                                                                       236
             334 -
                                                          2016
                                                                                                                                                                                                                                           2019
                                                                                                                                                                                            2017
                                                                                                                                                                                                                    2018
                                                                                            2018
                                                                                                                                                                     2016
                         2014
                                                                                                                                              2015
                                                                  Date
                                                                                                                                                                                            Date
                        GW036976.1.2
                                                                                                                                                  GW965569.1.2
             300
                                                                                                                                       338
             295
     Waterlevel
                                                                                                                               Waterlevel
             290
                                                                                                                                       337
             285
                                                                                                                                      336
             280
                                                                                                                                                     2014
                                                                                                                                                                                                                        2018
                         2014
                                                          2016
                                                                                            2018
                                                                                                                                                                                       2016
                                                                  Date
                                                                                                                                                                                             Date
# STL decomposition
dcmp_GW036334_1_1data <- GW036334_1_1data %>% model(stl = STL(WaterLevel))
```

```
STL_GW036334_1_1data<-components(dcmp_GW036334_1_1data) %>% autoplot(col="#f0027f")+labs(title = "GW0363
dcmp_GW093067_1_1data <- GW093067_1_1data %>% model(stl = STL(WaterLevel))
STL_GW093067_1_1data<-components(dcmp_GW093067_1_1data) %% autoplot(col="#d95f02")+labs(title ="GW0930
dcmp_GW036976.1.2data <- GW036976.1.2data %>% model(stl = STL(WaterLevel))
STL_GW036976.1.2data<-components(dcmp_GW036976.1.2data) %% autoplot(col="#1b9e77")+labs(title = "GW0369")
dcmp_GW965569.1.2data <- GW965569.1.2data %>% model(stl = STL(WaterLevel))
STL_GW965569.1.2data <-components(dcmp_GW965569.1.2data) \%>\% \ autoplot(col="blue") + labs(title = "GW965569.1.2data) \%>\% \ autoplot(col="blue") + labs(title = "GW96569.1.2data) \%>\% \ autoplot(col="blue") + labs(title = "GW96569.1.2data) \%>\% \ autoplot(col="blue") + labs(title = "GW96569.1.2data) \ autoplot(col="blue") + labs(title = "GW96569.1.2data) \ autoplot(col="blue") + labs(title = "GW96
STL_decom_data<-(STL_GW036334_1_1data|STL_GW093067_1_1data)/(STL_GW036976.1.2data|STL_GW965569.1.2data)
STL_decom_data
                                                                                                                                                                                        GW093067.1.1
                                                GW036334.1.1
                       WaterLevel = trend + season_year + season_webterlrementindeernd + season_year + seas
                                                                                                                                'n.
                                                                                                                                                                                                                                                                         en.
                                                                                                                                                                                                                                                                         9
                                                                                                                                                                                                                                                                         ain
                           2014
                                                             2016
                                                                                              2018
                                                                                                                                                              2015
                                                                                                                                                                                     2016
                                                                                                                                                                                                             2017
                                                                                                                                                                                                                                     2018
                                                                                                                                                                                                                                                            2019
                                                                   Date
                                                                                                                                                                                                            Date
                                                GW036976.1.2
                                                                                                                                                                                        GW965569.1.2
```



Split the data into 70% of training and 30% of testing.

```
# Split train and test data

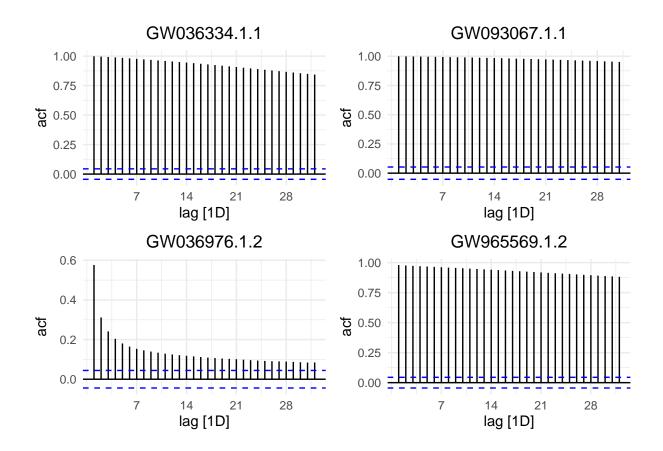
train_split_point <- floor(nrow(GW036334_1_1data)*0.8)
train_wl_GW036334_1_1 <- GW036334_1_1data[1:train_split_point,]</pre>
```

```
test_wl_GW036334_1_1 <- GW036334_1_1data[(train_split_point+1):nrow(GW036334_1_1data),]
train_split_point <- floor(nrow(GW093067_1_1data)*0.8)</pre>
train_wl_GW093067_1_1 <- GW093067_1_1data[1:train_split_point,]</pre>
test_wl_GW093067_1_1 <- GW093067_1_1data[(train_split_point+1):nrow(GW093067_1_1data),]
train_split_point <- floor(nrow(GW036976.1.2data)*0.8)</pre>
train wl GW036976.1.2 <- GW036976.1.2data[1:train split point,]
test_wl_GW036976.1.2 <- GW036976.1.2data[(train_split_point+1):nrow(GW036976.1.2data),]
train_split_point <- floor(nrow(GW965569.1.2data)*0.8)</pre>
train_wl_GW965569.1.2 <- GW965569.1.2data[1:train_split_point,]</pre>
test wl GW965569.1.2 <- GW965569.1.2data[(train split point+1):nrow(GW965569.1.2data),]
# Visualization of train and test set splitting
Train_Vs_Test_GW036334_1_1data \leftarrow GW036334_1_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW036334_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW03634_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW03634_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW03634_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW03634_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW03634_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW03634_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW03634_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW03634_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW03634_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW03634_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) + GW03634_1data \%\% ggplot
    geom\_line(size=1,col="#f0027f")+labs(y="Water Level", x = "Date",title = "GW036334.1.1")+
    geom_vline(xintercept = as.numeric(as.Date(test_wl_GW036334_1_1$Date[1], format="%m/%d/%Y")), linetyp
                        color = "black", size=1.5)+ theme_minimal()+theme(plot.title=element_text(hjust=0.5))
Train_Vs_Test_GW093067_1_1data \leftarrow GW093067_1_1data \%\% ggplot(aes(x = Date, y = WaterLevel)) +
    geom_line(size=1,col="#d95f02")+labs(y="Water Level", x = "Date",title = "GW093067.1.1")+
    geom_vline(xintercept = as.numeric(as.Date(test_wl_GW093067_1_1$Date[1], format="%m/%d/%Y")), linetyp
                        color = "black", size=1.5)+ theme minimal()+theme(plot.title=element text(hjust=0.5))
Train_Vs_Test_GW036976.1.2data <- GW036976.1.2data %>% ggplot(aes(x = Date, y = WaterLevel)) +
    geom_line(size=1,col="#1b9e77")+labs(y= "Water Level", x = "Date",title = "GW036976.1.2")+
    geom_vline(xintercept = as.numeric(as.Date(test_wl_GW036976.1.2$Date[1], format="%m/%d/%Y")), linetyp
                        color = "black", size=1.5)+ theme minimal()+theme(plot.title=element text(hjust=0.5))
Train_Vs_Test_GW965569.1.2data <- GW965569.1.2data \%\% ggplot(aes(x = Date, y = WaterLevel)) +
    geom_line(size=1,col="#CC6666")+labs(y= "Water Level", x = "Date",title = "GW965569.1.2")+
    geom_vline(xintercept = as.numeric(as.Date(test_wl_GW965569.1.2$Date[1], format="%m/%d/%Y")), linetyp
                        color = "black", size=1.5)+ theme_minimal()+theme(plot.title=element_text(hjust=0.5))
Train_Vs_Test<-(Train_Vs_Test_GW036334_1_1data|Train_Vs_Test_GW093067_1_1data)/(Train_Vs_Test_GW036976.
Train_Vs_Test
```



```
# Checking Stationarity
# acf plot

AC1<-GW036334_1_1data %>% ACF(WaterLevel) %>% autoplot()+labs(title ="GW036334.1.1" )+ theme_minimal()+
AC2<-GW093067_1_1data %>% ACF(WaterLevel) %>% autoplot()+labs(title ="GW093067.1.1" )+ theme_minimal()+
AC3<-GW036976.1.2data %>% ACF(WaterLevel) %>% autoplot()+labs(title ="GW036976.1.2" )+ theme_minimal()+
AC4<-GW965569.1.2data %>% ACF(WaterLevel) %>% autoplot()+labs(title ="GW965569.1.2" )+ theme_minimal()+
ACF_PLOTS<-(AC1|AC2)/(AC3|AC4)
ACF_PLOTS
```



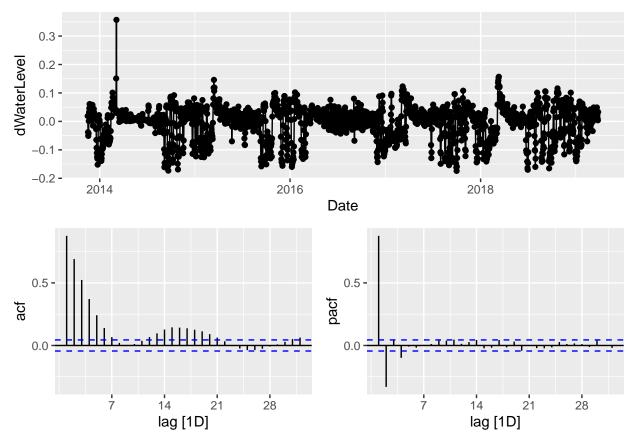
ARIMA Modeling

1

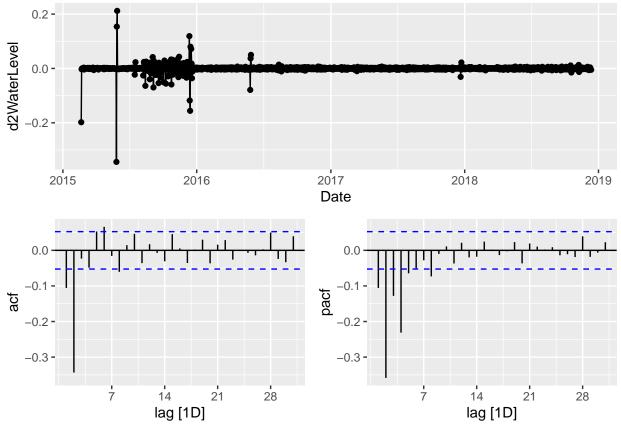
2

```
# Checking number of seasonal and non-seasonal difference required-by Unit Root Test
GW036334_1_1Ndiff<-GW036334_1_1data %>%features(WaterLevel, unitroot_ndiffs)
GW036334_1_1NSdiff<-GW036334_1_1data %>%features(WaterLevel, unitroot_nsdiffs)
GW036334_1_1Ndiff
## # A tibble: 1 x 1
##
     ndiffs
##
      <int>
## 1
          1
GW036334_1_1NSdiff
## # A tibble: 1 x 1
##
     nsdiffs
##
       <int>
GW093067_1_1Ndiff<-GW093067_1_1data %>%features(WaterLevel, unitroot_ndiffs)
GW093067_1_1NSdiff<-GW093067_1_1data %>%features(WaterLevel, unitroot_nsdiffs)
{\tt GW093067\_1\_1Ndiff}
## # A tibble: 1 x 1
##
     ndiffs
##
      <int>
```

```
{\tt GWO93067\_1\_1NSdiff}
## # A tibble: 1 x 1
   nsdiffs
       <int>
##
## 1
GW036976.1.2Ndiff<-GW036976.1.2data %>%features(WaterLevel, unitroot_ndiffs)
GW036976.1.2NSdiff<-GW036976.1.2data %>%features(WaterLevel, unitroot_nsdiffs)
GW036976.1.2Ndiff
## # A tibble: 1 x 1
##
   ndiffs
##
      <int>
## 1
GW036976.1.2NSdiff
## # A tibble: 1 x 1
##
   nsdiffs
##
       <int>
## 1
GW965569.1.2Ndiff<-GW965569.1.2data %>%features(WaterLevel, unitroot_ndiffs)
GW965569.1.2NSdiff<-GW965569.1.2data %>%features(WaterLevel, unitroot_nsdiffs)
GW965569.1.2Ndiff
## # A tibble: 1 x 1
##
   ndiffs
##
      <int>
## 1
          1
GW965569.1.2NSdiff
## # A tibble: 1 x 1
   nsdiffs
##
##
       <int>
## 1
# Convert the data into stationary-ACF and PACF plots-GW036334.1.1
GW036334_1_1data %>%
 mutate(dWaterLevel = difference(WaterLevel)) %>%
  gg_tsdisplay(dWaterLevel, plot_type='partial')
```



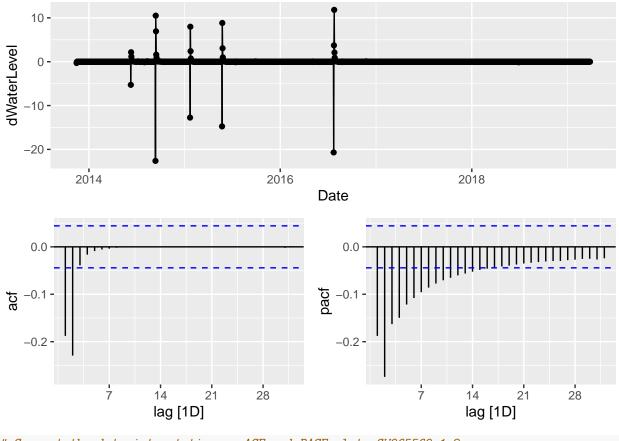
```
# Convert the data into stationary-ACF and PACF plots-GW093067.1.1
GW093067_1_1data %>%
  mutate(dWaterLevel = difference(WaterLevel)) %>%
  mutate(d2WaterLevel = difference(dWaterLevel)) %>%
  gg_tsdisplay(d2WaterLevel, plot_type='partial')
```



```
# Convert the data into stationary-ACF and PACF plots-GW036976.1.2
GW036976.1.2data %>%
  mutate(dWaterLevel = difference(WaterLevel)) %>%
  gg_tsdisplay(dWaterLevel, plot_type='partial')
```

Warning: Removed 1 row(s) containing missing values (geom_path).

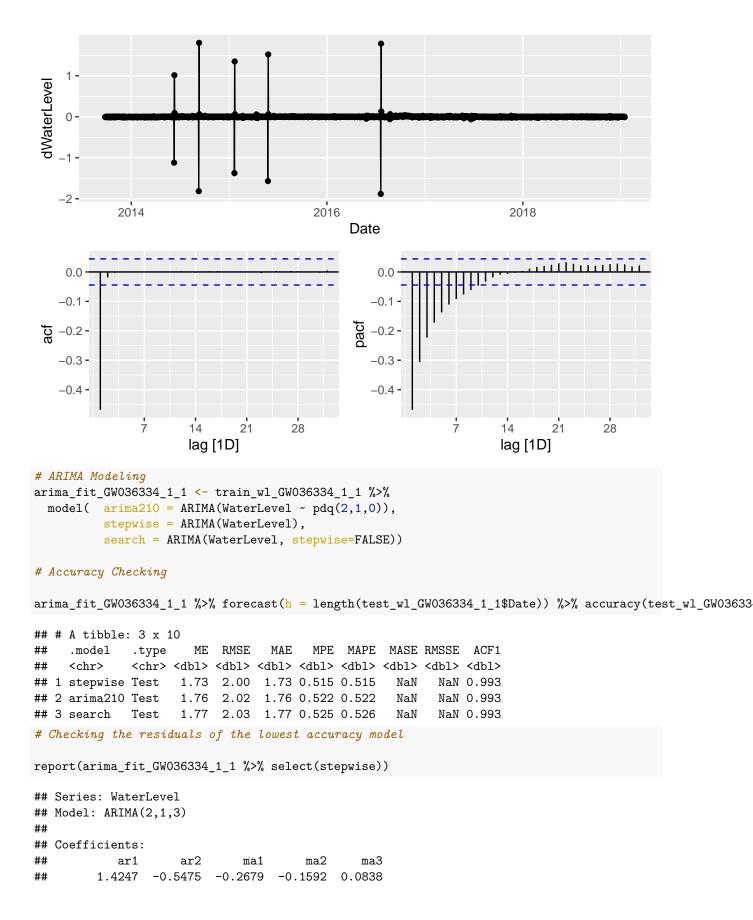
Warning: Removed 1 rows containing missing values (geom_point).



```
# Convert the data into stationary-ACF and PACF plots-GW965569.1.2
GW965569.1.2data %>%
  mutate(dWaterLevel = difference(WaterLevel)) %>%
  gg_tsdisplay(dWaterLevel, plot_type='partial')
```

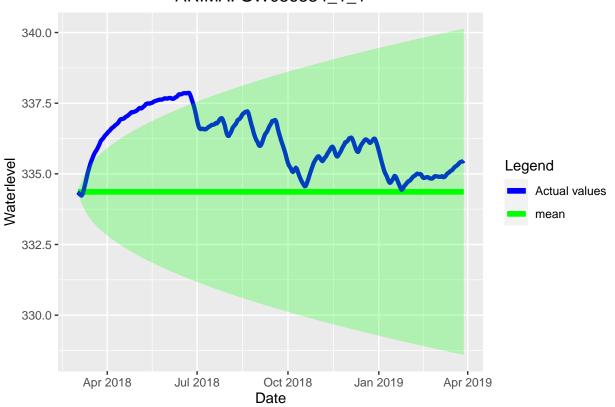
Warning: Removed 1 row(s) containing missing values (geom_path).

Warning: Removed 1 rows containing missing values (geom_point).



```
## s.e. 0.1088
                   0.0853
                                       0.0503 0.0331
                             0.1111
##
                                       log likelihood=3465.47
## sigma^2 estimated as 0.0007787:
## AIC=-6918.94
                   AICc=-6918.89
                                     BIC=-6886.8
# Residual Analysis
arima_fit_GW036334_1_1 %>% select(stepwise) %>% gg_tsresiduals(lag=36)
nnovation residuals
     0.2
     0.0
    -0.2
                               2015
                                                  2016
            2014
                                                                     2017
                                                                                        2018
                                                  Date
     0.075 -
                                                     150 -
     0.050
     0.025
                                                    100 -
acf
     0.000
                                                      50 -
   -0.025 -
                                                       0 - i
   -0.050 -
                 <del>'</del>
                                     28
                              21
                       14
                                            35
                                                                -0.2
                                                                           0.0
                                                                                      0.2
                         lag [1D]
                                                                          .resid
# Checking the hypothesis (HO: Residuals are WN vs H1: Residuals show #autocorrelation)
augment(arima_fit_GW036334_1_1) %>%
  filter(.model=='stepwise') %>%
  features(.innov, ljung_box, lag = 10, dof = 3)
## # A tibble: 1 x 3
##
     .model
              lb_stat lb_pvalue
     <chr>
                 <dbl>
                            <dbl>
                  2.87
                            0.896
## 1 stepwise
# HO is not rejected. Hence, Residuals are WN
Forecast\_GW036334\_1\_1 <-arima\_fit\_GW036334\_1\_1 \%>\% select(stepwise) \%>\%
                          forecast(h = length(test_wl_GW036334_1_1$Date))%>%hilo(level=c(95))
Actual_values<-test_wl_GW036334_1_1$WaterLevel
Forecast_GW036334_1_1$Actual_values<-Actual_values
colors <- c("Actual values" = "blue", "mean" = "green")</pre>
```

ARIMA: GW036334_1_1



```
# ARIMA Modeling
arima_fit_GW093067_1_1 <- train_wl_GW093067_1_1 %>%
 model( arima222 = ARIMA(WaterLevel ~ pdq(2,2,2)),
         stepwise = ARIMA(WaterLevel),
         search = ARIMA(WaterLevel, stepwise=FALSE))
# Accuracy Checking
arima_fit_GW093067_1_1 %>% forecast(h = length(test_wl_GW093067_1_1$Date)) %>% accuracy(test_wl_GW09306
## # A tibble: 3 x 10
##
    .model
            .type
                       ME RMSE
                                 MAE
                                        MPE MAPE MASE RMSSE ACF1
             <chr>
                    <dbl> <dbl> <dbl>
                                      <dbl> <dbl> <dbl> <dbl> <dbl> <
NaN 0.985
## 2 stepwise Test 0.0513 0.436 0.319 0.0219 0.135
                                                         NaN 0.985
                                                   NaN
            Test 0.0540 0.437 0.319 0.0231 0.135
                                                   NaN
                                                         NaN 0.985
# Checking the residuals of the lowest accuracy model
```

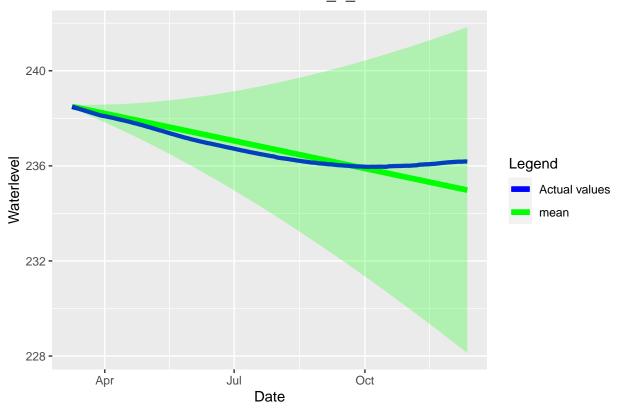
```
report(arima_fit_GW093067_1_1 %>% select(arima222))
## Series: WaterLevel
## Model: ARIMA(2,2,2)
##
## Coefficients:
##
              ar1
                        ar2
                                  ma1
                                           ma2
##
          -0.0360
                   -0.0878
                             -0.4024
                                       -0.5250
## s.e.
           0.0958
                    0.0598
                              0.0931
                                        0.0909
##
## sigma^2 estimated as 0.0003271: log likelihood=3095.85
## AIC=-6181.7
                  AICc=-6181.64
                                    BIC=-6156.62
# Residual Analysis
arima_fit_GW093067_1_1 %>% select(arima222) %>% gg_tsresiduals(lag=36)
     0.1 -
Innovation residuals
     0.0 -
    -0.1 -
    -0.2 -
   -0.3
       2015
                                 2016
                                                           2017
                                                                                      2018
                                                  Date
                                                     120 -
     0.05
                                                      80 -
                                                  count
                                                      40 -
   -0.05 -
                                     28
                              21
                                            35
                                                                    -0.2
                                                            -0.3
                                                                            -0.1
                                                                                    0.0
                                                                                           0.1
                         lag [1D]
                                                                          .resid
# Checking the Hypothesis
augment(arima_fit_GW093067_1_1) %>%
  filter(.model=='arima222') %>%
  features(.innov, ljung_box, lag = 10, dof = 3)
## # A tibble: 1 x 3
##
     .model
               lb_stat lb_pvalue
     <chr>
                 <dbl>
                            <dbl>
## 1 arima222
                  31.2 0.0000580
```

```
# Reject HO. Hence, residuals are not WN.
Forecast_GW093067_1_1<-arima_fit_GW093067_1_1 %>% select(arima222) %>%
    forecast(h = length(test_wl_GW093067_1_1$Date))%>%hilo(level=c(95))
Actual_values<-test_wl_GW093067_1_1$WaterLevel
Forecast_GW093067_1_1$Actual_values<-Actual_values

colors <- c("Actual values" = "blue", "mean" = "green")

Plot_AvsFitted_GW093067_1_1<-Forecast_GW093067_1_1%>%ggplot(aes(x = Date))+
    geom_line(aes(y = .mean,color="mean"),size=2)+
    geom_line(aes(y = Actual_values,color="Actual values"),size=1.5)+
    geom_ribbon(aes(ymin = Forecast_GW093067_1_1$^95%^$lower, ymax = Forecast_GW093067_1_1$^95%^$upper),
    labs(y= "Waterlevel", x = "Date",color = "Legend",title = "ARIMA: GW093067_1_1")+
    scale_color_manual(values = colors)+theme(plot.title=element_text(hjust=0.5))
Plot_AvsFitted_GW093067_1_1
```

ARIMA: GW093067_1_1

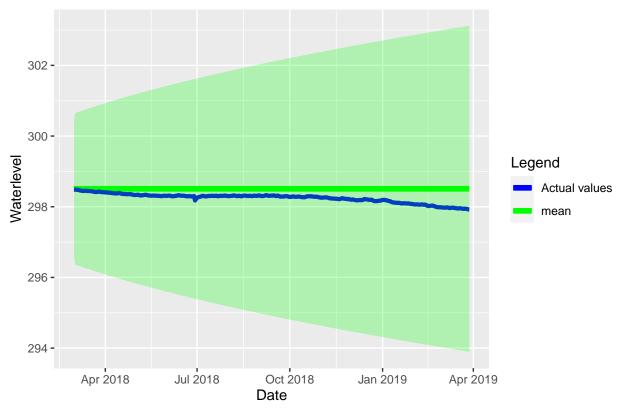


```
## # A tibble: 3 x 10
##
     .model
               .type
                         ME RMSE
                                     MAE
                                              MPE
                                                    MAPE MASE RMSSE ACF1
               <chr> <dbl> <dbl> <dbl>
##
                                            <dbl>
                                                   <dbl> <dbl> <dbl> <dbl>
## 1 arima012 Test -0.260 0.291 0.260 -0.0874 0.0874
                                                                  NaN 0.985
                                                            NaN
              Test -0.361 0.383 0.361 -0.121 0.121
                                                                  NaN 0.983
## 3 stepwise Test -0.361 0.383 0.361 -0.121 0.121
                                                            NaN
                                                                  NaN 0.983
# Checking the residuals of the lowest accuracy model
report(arima_fit_GW036976.1.2 %>% select(arima012))
## Series: WaterLevel
## Model: ARIMA(0,1,2)
## Coefficients:
##
              ma1
                       ma2
##
         -0.4591
                   -0.4313
## s.e.
          0.0227
                    0.0248
##
## sigma^2 estimated as 0.9247: log likelihood=-2161.79
## AIC=4329.59
                  AICc=4329.6
                                BIC=4345.66
# Residual Analysis
arima_fit_GW036976.1.2 %>% select(arima012) %>% gg_tsresiduals(lag=36)
Innovation residuals
     -5 -
    -10 -
    -15 -
   -20 -
                                                 2016
            2014
                                                                   2017
                              2015
                                                                                      2018
                                                 Date
                                                    800 -
     0.10 -
                                                    600 -
     0.05
acf
                                                   400 -
     0.00
                                                    200 -
    -0.05 -
                             21
                                                                          -10
                                           35
                                                            -20
                                                                   -15
                                                                                  -5
                        lag [1D]
                                                                         .resid
# Hypothesis testing
```

augment(arima_fit_GW036976.1.2) %>%

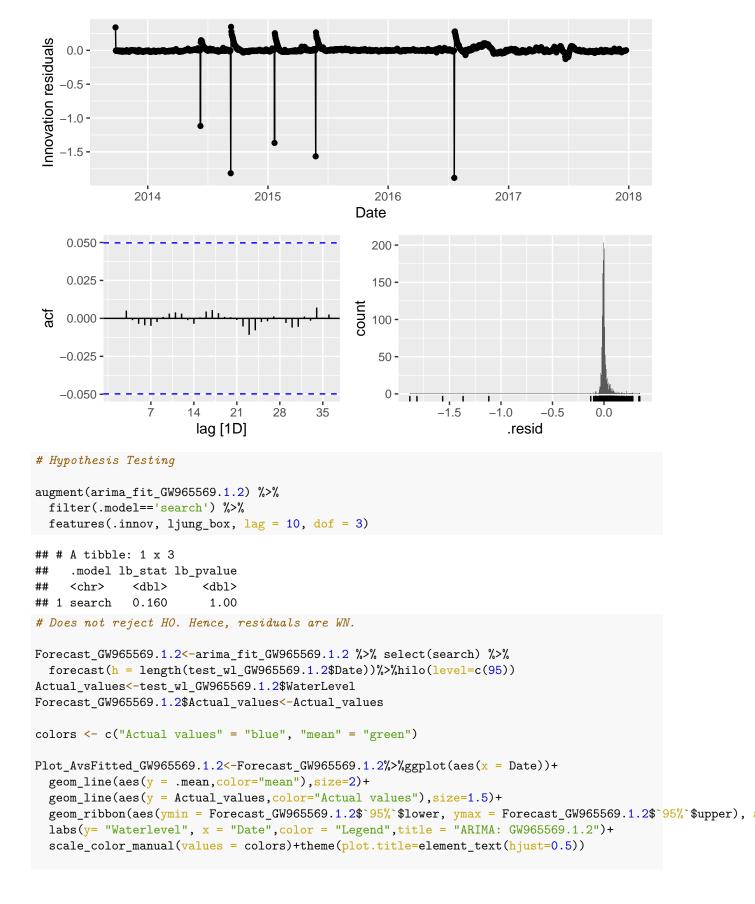
```
filter(.model=='arima012') %>%
     features(.innov, ljung_box, lag = 10, dof = 3)
## # A tibble: 1 x 3
##
              .model
                                     lb_stat lb_pvalue
##
              <chr>>
                                            <dbl>
                                                                       <dbl>
## 1 arima012
                                               30.0 0.0000947
# Reject HO. Hence, residuals are WN.
Forecast_GW036976.1.2<-arima_fit_GW036976.1.2 %>% select(arima012) %>%
     forecast(h = length(test_wl_GW036976.1.2$Date))%>%hilo(level=c(95))
Actual_values<-test_wl_GW036976.1.2$WaterLevel
Forecast_GW036976.1.2$Actual_values<-Actual_values
colors <- c("Actual values" = "blue", "mean" = "green")</pre>
geom_line(aes(y = .mean,color="mean"),size=2)+
     geom_line(aes(y = Actual_values, color="Actual values"), size=1.5)+
     \texttt{geom\_ribbon}(\texttt{aes}(\texttt{ymin} = \texttt{Forecast\_GW036976.1.2\$`95\%`\$lower}, \texttt{ymax} = \texttt{Forecast\_GW036976.1.2\$`95\%`\$upper}), \texttt{weaking}(\texttt{ymin} = \texttt{Forecast\_GW036976.1.2\$`95\%`\$upper})
     labs(y= "Waterlevel", x = "Date", color = "Legend", title = "ARIMA: GW036976.1.2")+
     scale_color_manual(values = colors)+theme(plot.title=element_text(hjust=0.5))
Plot AvsFitted GW036976.1.2
```

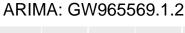
ARIMA: GW036976.1.2

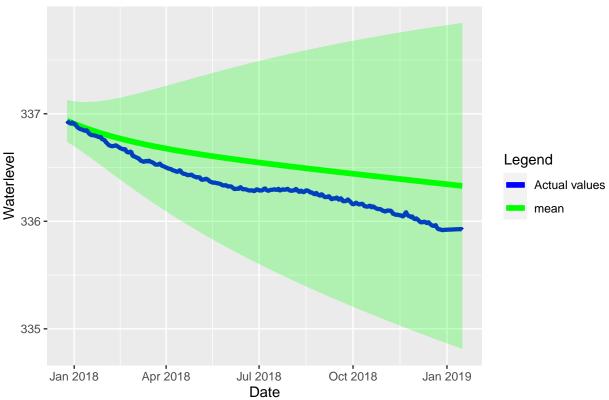


```
# ARIMA Modeling
arima_fit_GW965569.1.2 <- train_wl_GW965569.1.2 %>%
```

```
model( arima011 = ARIMA(WaterLevel ~ pdq(0,1,1)),
          stepwise = ARIMA(WaterLevel),
          search = ARIMA(WaterLevel, stepwise=FALSE))
# Accuracy Checking
arima_fit_GW965569.1.2 %>% forecast(h = length(test_wl_GW965569.1.2$Date)) %>% accuracy(test_wl_GW96556
## # A tibble: 3 x 10
     .model .type
##
                       ME RMSE
                                  MAE
                                           MPE
                                                MAPE MASE RMSSE ACF1
##
     <chr>
             <chr> <dbl> <dbl> <dbl>
                                         <dbl> <dbl> <dbl> <dbl> <dbl> <
## 1 search Test -0.229 0.252 0.229 -0.0682 0.0682
                                                       {\tt NaN}
                                                             NaN 0.988
## 2 arima011 Test -0.409 0.434 0.409 -0.122 0.122
                                                       {\tt NaN}
                                                             NaN 0.987
## 3 stepwise Test -0.409 0.434 0.409 -0.122 0.122
                                                             NaN 0.987
                                                       {\tt NaN}
# Checking the residuals of the lowest accuracy model
report(arima_fit_GW965569.1.2 %>% select(search))
## Series: WaterLevel
## Model: ARIMA(1,1,4) w/ drift
## Coefficients:
##
                                    ma3
                                             ma4 constant
           ar1
                    ma1
                            ma2
##
         0.9851 -1.7875 0.7542 0.0246 0.0154
## s.e. 0.0080 0.0264 0.0526 0.0522 0.0254
##
## sigma^2 estimated as 0.00958: log likelihood=1412.05
## AIC=-2810.09
                 AICc=-2810.02 BIC=-2772.67
# Residual Analysis
arima_fit_GW965569.1.2 %>% select(search) %>% gg_tsresiduals(lag=36)
```







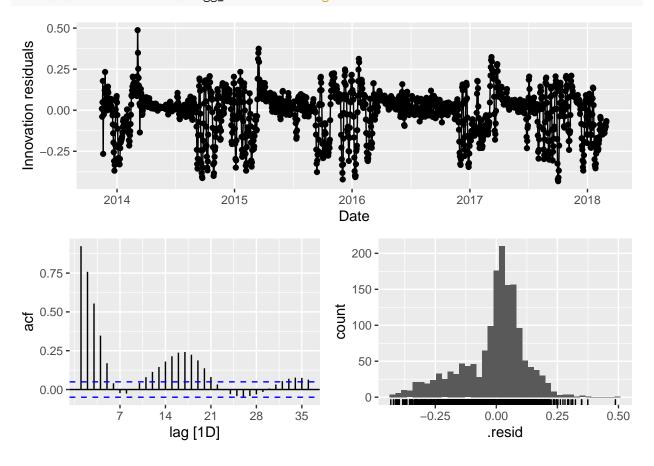
ETS Modeling

```
fit1<-train_wl_GW036334_1_1 %>%
  model(ses = ETS(WaterLevel ~ error("A") + trend("N") + season("N")),
        hlm = ETS(WaterLevel ~ error("A") + trend("N") + season("A")),
        ahw = ETS(WaterLevel ~ error("A") + trend("A") + season("A")),
        auto1 = ETS(WaterLevel ~ error("A") + trend("N") + season("M")),
        auto2 = ETS(WaterLevel ~ error("A") + trend("A") + season("N")),
        auto3 = ETS(WaterLevel ~ error("A") + trend("A") + season("M")),
        auto4 = ETS(WaterLevel ~ error("A") + trend("Ad") + season("N")),
        auto5 = ETS(WaterLevel ~ error("A") + trend("Ad") + season("A")),
        auto6 = ETS(WaterLevel ~ error("A") + trend("Ad") + season("M")),
        ses1 = ETS(WaterLevel ~ error("M") + trend("N") + season("N")),
       hlm1 = ETS(WaterLevel ~ error("M") + trend("N") + season("A")),
        ahw1 = ETS(WaterLevel ~ error("M") + trend("A") + season("A")),
        auto11 = ETS(WaterLevel ~ error("M") + trend("N") + season("M")),
       auto21 = ETS(WaterLevel ~ error("M") + trend("A") + season("N")),
        auto31 = ETS(WaterLevel ~ error("M") + trend("A") + season("M")),
        auto41 = ETS(WaterLevel ~ error("M") + trend("Ad") + season("N")),
        auto51 = ETS(WaterLevel ~ error("M") + trend("Ad") + season("A")),
        auto61 = ETS(WaterLevel ~ error("M") + trend("Ad") + season("M"))
  )
```

 $fit1 \%\% forecast(h = length(test_wl_GW036334_1_1\$Date)) \%\% accuracy(test_wl_GW036334_1_1) \%\% arranged fit1 \%\% forecast(h = length(test_wl_GW036334_1_1\$Date)) \%\% accuracy(test_wl_GW036334_1_1) \%\% arranged fit1 \%\% forecast(h = length(test_wl_GW036334_1_1) \%\% accuracy(test_wl_GW036334_1_1) \%\% arranged fit1 \%\% forecast(h = length(test_wl_GW036334_1_1) \%\% accuracy(test_wl_GW036334_1_1) \%\% arranged fit1 \%\% forecast(h = length(test_wl_GW036334_1_1) \%\% forecast(h = length(test_wl_GW036334_1) \%\% forecast(h = length(h =$

```
## # A tibble: 18 x 10
##
      .model .type
                       ME RMSE
                                  MAE
                                         MPE MAPE MASE RMSSE ACF1
             <chr> <dbl> <dbl> <dbl> <dbl> <dbl> <
                                                   <dbl> <dbl> <dbl>
##
             Test
                     1.68
                           1.95
                                 1.68 0.498 0.499
                                                     NaN
                                                            NaN 0.993
                                 1.70 0.505 0.506
                                                     NaN
                                                            NaN 0.993
##
    2 auto11 Test
                     1.70
                           1.97
                           1.97
                                 1.71 0.506 0.507
    3 hlm1
             Test
                     1.70
                                                     NaN
                                                            NaN 0.993
##
                           1.97
                                 1.71 0.506 0.507
                                                            NaN 0.993
##
    4 ses
             Test
                     1.71
                                                     NaN
##
    5 ses1
             Test
                     1.71
                           1.97
                                 1.71 0.506 0.507
                                                     NaN
                                                            NaN 0.993
                                 1.71 0.507 0.507
                                                            NaN 0.993
##
    6 hlm
             Test
                     1.71
                           1.97
                                                     NaN
##
    7 auto41 Test
                     1.87
                           2.12
                                 1.87 0.554 0.555
                                                     NaN
                                                            NaN 0.993
##
    8 auto4 Test
                     1.88
                           2.13
                                 1.88 0.559 0.559
                                                     NaN
                                                            NaN 0.993
                           2.15
                                 1.90 0.565 0.565
                                                            NaN 0.993
    9 auto51 Test
                     1.90
                                                     NaN
## 10 auto6
             Test
                     2.40
                           2.63
                                 2.40 0.714 0.714
                                                     NaN
                                                            NaN 0.991
                                 2.63 0.781 0.781
  11 auto5
             Test
                     2.63
                           2.82
                                                     NaN
                                                            NaN 0.989
## 12 auto61 Test
                     3.02
                           3.20
                                 3.02 0.898 0.898
                                                     NaN
                                                            NaN 0.987
## 13 auto2
             Test
                     6.02
                           6.36
                                 6.03 1.79
                                             1.79
                                                     NaN
                                                            NaN 0.984
                     6.03
                           6.36
                                 6.03 1.79
                                                     NaN
## 14 auto21 Test
                                             1.79
                                                            NaN 0.984
## 15 ahw1
             Test
                     8.83
                           9.52
                                 8.83 2.63
                                                     NaN
                                                            NaN 0.988
## 16 ahw
                     9.96 10.8
                                 9.96 2.97
                                             2.97
                                                     NaN
                                                            NaN 0.989
             Test
## 17 auto31 Test
                   10.6
                         11.6
                                10.6
                                      3.16
                                             3.16
                                                     NaN
                                                            NaN 0.989
## 18 auto3 Test
                   12.1
                         13.2
                                12.1
                                      3.60
                                             3.60
                                                     NaN
                                                            NaN 0.990
```

fit1 %>% select(auto1) %>% gg_tsresiduals(lag=36)



```
augment(fit1) %>%
 features(.innov, ljung_box, lag=24, dof=4)
## # A tibble: 18 x 3
##
      .model lb_stat lb_pvalue
##
      <chr>
              <dbl>
                        <dbl>
## 1 ahw
              1587.
                            0
## 2 ahw1
             1320.
                            0
## 3 auto1 3518.
                            0
## 4 auto11 2461.
                            0
## 5 auto2
              262.
                            0
## 6 auto21 262.
                            0
## 7 auto3
                            0
              2775.
## 8 auto31 1457.
                            0
## 9 auto4
              255.
                            0
## 10 auto41 259.
                            0
## 11 auto5
            1060.
                            0
## 12 auto51 1269.
                            0
                            0
## 13 auto6
              977.
## 14 auto61 1421.
                            0
## 15 hlm
              2507.
                            0
## 16 hlm1
              2508.
                            0
## 17 ses
              3084.
                            0
## 18 ses1
              3088.
                            0
# auto1 is the best model, but residuals are not WN
Forecast_GW036334_1_1_ETS<-fit1 %>% select(auto1) %>%
 forecast(h = length(test_wl_GW036334_1_1$Date))%>%hilo(level=c(95))
Actual_values<-test_wl_GW036334_1_1$WaterLevel
Forecast_GW036334_1_1_ETS$Actual_values<-Actual_values
colors <- c("Actual values" = "blue", "mean" = "green")</pre>
Plot_AvsFitted_GW036334_1_1_ETS<-Forecast_GW036334_1_1_ETS%-%ggplot(aes(x = Date))+
  geom_line(aes(y = .mean,color="mean"),size=2)+
  geom_line(aes(y = Actual_values, color="Actual values"), size=1.5)+
  geom_ribbon(aes(ymin = Forecast_GW036334_1_1_ETS$\`95%`\$lower, ymax = Forecast_GW036334_1_1_ETS$\`95%`\$
  labs(y= "Waterlevel", x = "Date",color = "Legend",title = "ETS: GW036334_1_1")+
  scale_color_manual(values = colors)+theme(plot.title=element_text(hjust=0.5))
Plot_AvsFitted_GW036334_1_1_ETS
```

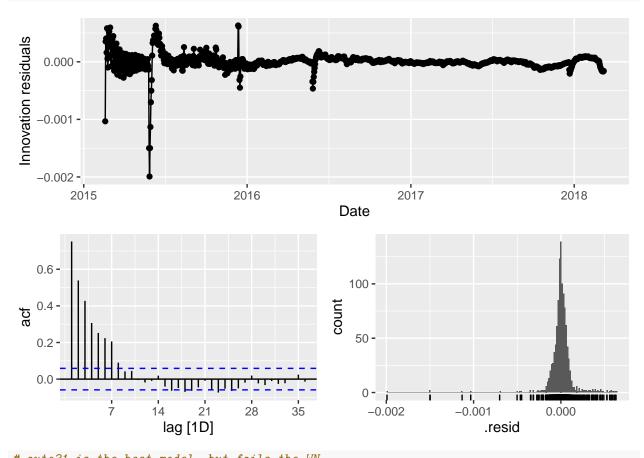




```
fit2<-train wl GW093067 1 1 %>%
  model(ses = ETS(WaterLevel ~ error("A") + trend("N") + season("N")),
        hlm = ETS(WaterLevel ~ error("A") + trend("N") + season("A")),
        ahw = ETS(WaterLevel ~ error("A") + trend("A") + season("A")),
        auto1 = ETS(WaterLevel ~ error("A") + trend("N") + season("M")),
        auto2 = ETS(WaterLevel ~ error("A") + trend("A") + season("N")),
        auto3 = ETS(WaterLevel ~ error("A") + trend("A") + season("M")),
        auto4 = ETS(WaterLevel ~ error("A") + trend("Ad") + season("N")),
        auto5 = ETS(WaterLevel ~ error("A") + trend("Ad") + season("A")),
        auto6 = ETS(WaterLevel ~ error("A") + trend("Ad") + season("M")),
        ses1 = ETS(WaterLevel ~ error("M") + trend("N") + season("N")),
       hlm1 = ETS(WaterLevel ~ error("M") + trend("N") + season("A")),
        ahw1 = ETS(WaterLevel ~ error("M") + trend("A") + season("A")),
        auto11 = ETS(WaterLevel ~ error("M") + trend("N") + season("M")),
        auto21 = ETS(WaterLevel ~ error("M") + trend("A") + season("N")),
        auto31 = ETS(WaterLevel ~ error("M") + trend("A") + season("M")),
        auto41 = ETS(WaterLevel ~ error("M") + trend("Ad") + season("N")),
        auto51 = ETS(WaterLevel ~ error("M") + trend("Ad") + season("A")),
        auto61 = ETS(WaterLevel ~ error("M") + trend("Ad") + season("M"))
  )
fit2 %>% forecast(h = length(test_wl_GW093067_1_1$Date)) %>% accuracy(test_wl_GW093067_1_1) %>% arrange
## # A tibble: 18 x 10
```

```
##
      <chr>
             <chr>
                      <dbl> <dbl> <dbl>
                                            <dbl> <dbl> <dbl> <dbl> <dbl> <
    1 auto31 Test
##
                    -0.123   0.394   0.342   -0.0518   0.144
                                                                 NaN 0.984
                                                           NaN
##
              Test
                    -0.0412 0.397 0.320 -0.0172 0.135
                                                                 NaN 0.985
                     0.0990 0.463 0.321
                                          0.0421 0.136
##
    3 auto2
             Test
                                                                 NaN 0.985
                                                           NaN
##
    4 auto21 Test
                     0.102
                            0.465 0.322
                                          0.0435 0.136
                                                           NaN
                                                                 NaN 0.985
    5 ahw1
                     0.718
                             1.04
                                   0.719
                                          0.304
                                                 0.304
                                                                 NaN 0.987
##
              Test
                                                           NaN
                                                                 NaN 0.987
             Test
                     0.970
                            1.33
                                   0.970
                                          0.411
                                                  0.411
    6 auto3
                                                           NaN
                    -1.36
                                          -0.575
                                                  0.575
##
    7 auto41 Test
                             1.53
                                   1.36
                                                           NaN
                                                                 NaN 0.992
##
    8 auto4
             Test
                    -1.37
                             1.54
                                   1.37
                                          -0.580
                                                  0.580
                                                           NaN
                                                                 NaN 0.992
                             1.58
                                                  0.599
##
    9 auto51 Test
                    -1.42
                                   1.42
                                         -0.599
                                                           NaN
                                                                 NaN 0.992
## 10 auto5
             Test
                    -1.43
                             1.59
                                   1.43
                                         -0.604
                                                  0.604
                                                           NaN
                                                                 NaN 0.992
                    -1.46
  11 auto61 Test
                             1.62
                                   1.46
                                          -0.616
                                                  0.616
                                                                 NaN 0.991
##
                                                           NaN
  12 auto6
             Test
                    -1.46
                             1.62
                                   1.46
                                         -0.616
                                                  0.616
                                                           NaN
                                                                 NaN 0.991
                    -1.76
                             1.93
                                   1.76
                                                  0.746
## 13 ses
             Test
                                          -0.746
                                                           NaN
                                                                 NaN 0.990
## 14 ses1
             Test
                    -1.76
                             1.93
                                   1.76
                                          -0.746
                                                  0.746
                                                                 NaN 0.990
                                                           NaN
## 15 hlm
             Test
                    -1.76
                             1.93
                                   1.76
                                          -0.746
                                                  0.746
                                                           NaN
                                                                 NaN 0.990
## 16 hlm1
             Test
                    -1.77
                             1.94
                                          -0.748
                                                  0.748
                                                                 NaN 0.990
                                   1.77
                                                           NaN
## 17 auto11 Test
                    -1.77
                             1.94
                                   1.77
                                          -0.749
                                                  0.749
                                                           NaN
                                                                 NaN 0.990
## 18 auto1
                   -1.86
                             2.01
                                   1.86
                                         -0.785
                                                  0.785
                                                                 NaN 0.990
             Test
                                                           NaN
```

fit2 %>% select(auto31) %>% gg_tsresiduals(lag=36)



auto31 is the best model, but fails the WN

Forecast_GW093067_1_1_ETS<-fit2 %>% select(auto31) %>%
 forecast(h = length(test_wl_GW093067_1_1\$Date))%>%hilo(level=c(95))
Actual_values<-test_wl_GW093067_1_1\$WaterLevel</pre>

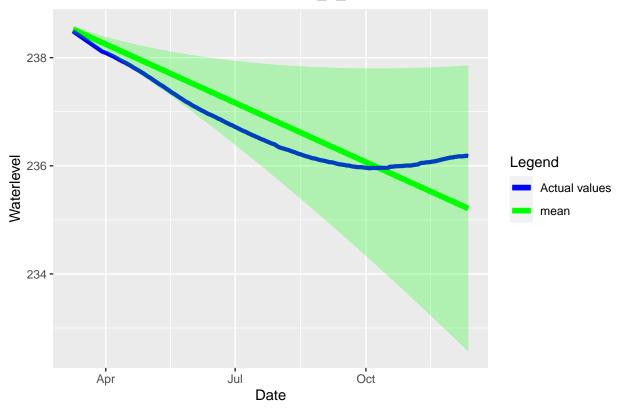
```
Forecast_GW093067_1_1_ETS$Actual_values<-Actual_values

colors <- c("Actual values" = "blue", "mean" = "green")

Plot_AvsFitted_GW093067_1_1_ETS<-Forecast_GW093067_1_1_ETS%>%ggplot(aes(x = Date))+
    geom_line(aes(y = .mean,color="mean"),size=2)+
    geom_line(aes(y = Actual_values,color="Actual values"),size=1.5)+
    geom_ribbon(aes(ymin = Forecast_GW093067_1_1_ETS$`95%`$lower, ymax = Forecast_GW093067_1_1_ETS$`95%`$
    labs(y= "Waterlevel", x = "Date",color = "Legend",title = "ETS: GW093067_1_1")+
    scale_color_manual(values = colors)+theme(plot.title=element_text(hjust=0.5))

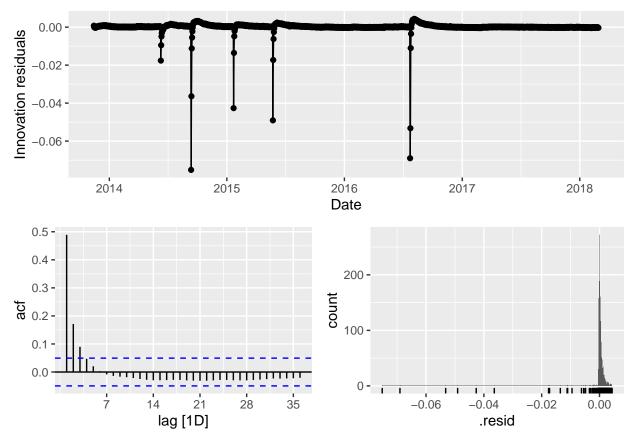
Plot_AvsFitted_GW093067_1_1_ETS
```

ETS: GW093067_1_1



```
fit3<-train_wl_GW036976.1.2 %>%
  model(ses = ETS(WaterLevel ~ error("A") + trend("N") + season("N")),
    hlm = ETS(WaterLevel ~ error("A") + trend("A") + season("A")),
    ahw = ETS(WaterLevel ~ error("A") + trend("A") + season("A")),
    auto1 = ETS(WaterLevel ~ error("A") + trend("N") + season("M")),
    auto2 = ETS(WaterLevel ~ error("A") + trend("A") + season("N")),
    auto3 = ETS(WaterLevel ~ error("A") + trend("A") + season("M")),
    auto4 = ETS(WaterLevel ~ error("A") + trend("Ad") + season("N")),
    auto5 = ETS(WaterLevel ~ error("A") + trend("Ad") + season("A")),
    auto6 = ETS(WaterLevel ~ error("M") + trend("N") + season("N")),
    hlm1 = ETS(WaterLevel ~ error("M") + trend("N") + season("A")),
    ahw1 = ETS(WaterLevel ~ error("M") + trend("A") + season("A")),
    auto11 = ETS(WaterLevel ~ error("M") + trend("N") + season("M")),
```

```
auto21 = ETS(WaterLevel ~ error("M") + trend("A") + season("N")),
        auto31 = ETS(WaterLevel ~ error("M") + trend("A") + season("M")),
        auto41 = ETS(WaterLevel ~ error("M") + trend("Ad") + season("N")),
        auto51 = ETS(WaterLevel ~ error("M") + trend("Ad") + season("A")),
        auto61 = ETS(WaterLevel ~ error("M") + trend("Ad") + season("M"))
  )
fit3 %>% forecast(h = length(test_wl_GW036976.1.2$Date)) %>% accuracy(test_wl_GW036976.1.2) %>% arrange
## # A tibble: 18 x 10
##
      .model .type
                       ME RMSE
                                   MAE
                                           MPE
                                                 MAPE MASE RMSSE ACF1
      <chr> <chr> <dbl> <dbl> <dbl>
##
                                         <dbl> <dbl> <dbl> <dbl> <dbl> <
    1 auto31 Test -0.212 0.239 0.212 -0.0710 0.0711
                                                         NaN
                                                               NaN 0.897
    2 hlm
             Test -0.194 0.241 0.199 -0.0649 0.0668
                                                               NaN 0.880
                                                         NaN
## 3 hlm1
             Test -0.199 0.243 0.203 -0.0666 0.0680
                                                               NaN 0.911
## 4 auto61 Test -0.200 0.244 0.204 -0.0670 0.0683
                                                         {\tt NaN}
                                                               NaN 0.919
    5 auto5 Test -0.203 0.247 0.207 -0.0681 0.0694
                                                               NaN 0.920
                                                         {\tt NaN}
## 6 ahw1
                   0.205 0.248 0.211 0.0687 0.0707
                                                               NaN 0.923
             Test
                                                         {\tt NaN}
                                                               NaN 0.929
## 7 auto51 Test -0.209 0.251 0.212 -0.0703 0.0712
                                                         {\tt NaN}
## 8 auto1 Test -0.238 0.269 0.238 -0.0799 0.0800
                                                         {\tt NaN}
                                                               NaN 0.967
## 9 auto4 Test -0.243 0.275 0.243 -0.0814 0.0814
                                                         \mathtt{NaN}
                                                               NaN 0.985
## 10 auto41 Test -0.243 0.275 0.243 -0.0814 0.0814
                                                         {\tt NaN}
                                                               NaN 0.985
             Test -0.243 0.275 0.243 -0.0815 0.0815
## 11 ses
                                                         {\tt NaN}
                                                               NaN 0.985
             Test -0.243 0.275 0.243 -0.0815 0.0815
                                                               NaN 0.985
## 12 ses1
                                                         {\tt NaN}
## 13 auto3 Test -0.257 0.285 0.257 -0.0860 0.0860
                                                         {\tt NaN}
                                                               NaN 0.944
## 14 auto11 Test -0.263 0.293 0.263 -0.0881 0.0881
                                                         {\tt NaN}
                                                               NaN 0.984
## 15 auto21 Test -0.308 0.349 0.308 -0.103 0.103
                                                               NaN 0.987
                                                         {\tt NaN}
## 16 auto2 Test -0.316 0.358 0.316 -0.106 0.106
                                                         {\tt NaN}
                                                               NaN 0.987
## 17 auto6 Test -0.351 0.405 0.356 -0.118 0.119
                                                         {\tt NaN}
                                                               NaN 0.956
             Test -0.430 0.503 0.433 -0.144 0.145
                                                         {\tt NaN}
                                                               NaN 0.962
fit3 %>% select(auto31) %>% gg_tsresiduals(lag=36)
```



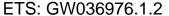
```
# auto31 is the best mode!

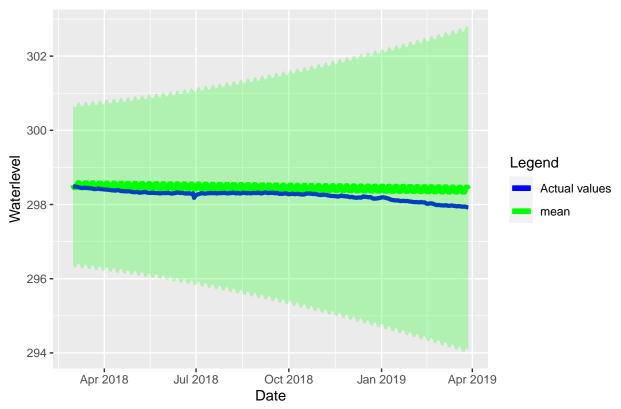
Forecast_GW036976.1.2_ETS<-fit3 %>% select(auto31) %>%
    forecast(h = length(test_wl_GW036976.1.2$Date))%>%hilo(level=c(95))
Actual_values<-test_wl_GW036976.1.2$WaterLevel
Forecast_GW036976.1.2_ETS$Actual_values<-Actual_values

colors <- c("Actual values" = "blue", "mean" = "green")

Plot_AvsFitted_GW036976.1.2_ETS<-Forecast_GW036976.1.2_ETS%>%ggplot(aes(x = Date))+
    geom_line(aes(y = .mean,color="mean"),size=2)+
    geom_line(aes(y = Actual_values,color="Actual values"),size=1.5)+
    geom_ribbon(aes(ymin = Forecast_GW036976.1.2_ETS$^95%^$lower, ymax = Forecast_GW036976.1.2_ETS$^95%^$
    labs(y= "Waterlevel", x = "Date",color = "Legend",title = "ETS: GW036976.1.2")+
    scale_color_manual(values = colors)+theme(plot.title=element_text(hjust=0.5))

Plot_AvsFitted_GW036976.1.2_ETS
```



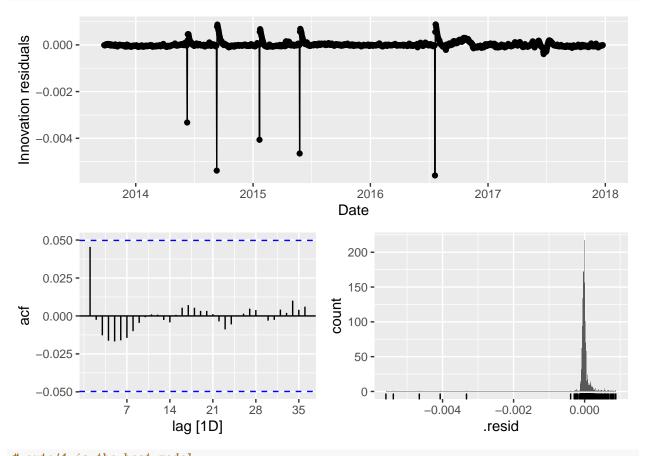


```
fit4<-train wl GW965569.1.2 %>%
  model(ses = ETS(WaterLevel ~ error("A") + trend("N") + season("N")),
        hlm = ETS(WaterLevel ~ error("A") + trend("N") + season("A")),
        ahw = ETS(WaterLevel ~ error("A") + trend("A") + season("A")),
        auto1 = ETS(WaterLevel ~ error("A") + trend("N") + season("M")),
        auto2 = ETS(WaterLevel ~ error("A") + trend("A") + season("N")),
        auto3 = ETS(WaterLevel ~ error("A") + trend("A") + season("M")),
        auto4 = ETS(WaterLevel ~ error("A") + trend("Ad") + season("N")),
        auto5 = ETS(WaterLevel ~ error("A") + trend("Ad") + season("A")),
        auto6 = ETS(WaterLevel ~ error("A") + trend("Ad") + season("M")),
        ses1 = ETS(WaterLevel ~ error("M") + trend("N") + season("N")),
       hlm1 = ETS(WaterLevel ~ error("M") + trend("N") + season("A")),
        ahw1 = ETS(WaterLevel ~ error("M") + trend("A") + season("A")),
        auto11 = ETS(WaterLevel ~ error("M") + trend("N") + season("M")),
        auto21 = ETS(WaterLevel ~ error("M") + trend("A") + season("N")),
        auto31 = ETS(WaterLevel ~ error("M") + trend("A") + season("M")),
        auto41 = ETS(WaterLevel ~ error("M") + trend("Ad") + season("N")),
        auto51 = ETS(WaterLevel ~ error("M") + trend("Ad") + season("A")),
        auto61 = ETS(WaterLevel ~ error("M") + trend("Ad") + season("M"))
  )
fit4 %>% forecast(h = length(test wl GW965569.1.2$Date)) %>% accuracy(test wl GW965569.1.2) %>% arrange
```

A tibble: 18 x 10

```
##
                        ME RMSE
                                    MAE
                                            MPE MAPE
                                                      MASE RMSSE
      .model .type
##
                     <dbl> <dbl> <dbl>
                                         <dbl> <dbl> <dbl>
                                                             <dbl> <dbl>
      <chr> <chr>
##
    1 auto41 Test
                    -0.462 0.516 0.462 -0.138 0.138
                                                               NaN 0.991
                    -0.468 0.522 0.468 -0.139 0.139
                                                               NaN 0.991
##
             Test
                                                         \mathtt{NaN}
##
    3 auto61 Test
                    -0.468 0.523 0.468 -0.139 0.139
                                                         NaN
                                                               NaN 0.990
                    -0.472 0.526 0.472 -0.140 0.140
##
    4 auto5
             Test
                                                         \mathtt{NaN}
                                                               NaN 0.990
                    -0.476 0.529 0.476 -0.142 0.142
    5 auto6
             Test
                                                         NaN
                                                               NaN 0.990
##
    6 auto51 Test
                    -0.505 0.561 0.505 -0.150 0.150
                                                         NaN
                                                               NaN 0.990
##
    7
      auto31 Test
                     0.461 0.584 0.461
                                         0.137 0.137
                                                         NaN
                                                               NaN 0.994
##
    8 ahw
              Test
                     0.466 0.590 0.466
                                         0.139 0.139
                                                         NaN
                                                               NaN 0.993
##
    9 auto3
             Test
                     0.469 0.594 0.469
                                         0.140 0.140
                                                         NaN
                                                               NaN 0.994
## 10 auto2
             Test
                     0.479 0.606 0.479
                                         0.143 0.143
                                                               NaN 0.994
                                                         NaN
  11 auto21 Test
                     0.480 0.606 0.480
                                         0.143 0.143
                                                         NaN
                                                               NaN 0.994
             Test
                     0.491 0.619 0.491
                                         0.146 0.146
## 12 ahw1
                                                               NaN 0.993
## 13 hlm1
             Test
                    -0.613 0.666 0.613 -0.182 0.182
                                                               NaN 0.989
                                                         {\tt NaN}
## 14 hlm
             Test
                    -0.617 0.669 0.617 -0.183 0.183
                                                         {\tt NaN}
                                                               NaN 0.989
## 15 ses
             Test
                    -0.619 0.671 0.619 -0.184 0.184
                                                               NaN 0.990
                                                         {\tt NaN}
## 16 ses1
             Test
                    -0.619 0.671 0.619 -0.184 0.184
                                                         NaN
                                                               NaN 0.990
             Test
                   -0.625 0.677 0.625 -0.186 0.186
                                                               NaN 0.989
## 17 auto1
                                                         {\tt NaN}
## 18 auto11 Test -0.625 0.677 0.625 -0.186 0.186
                                                         \mathtt{NaN}
                                                               NaN 0.990
```

fit4 %>% select(auto41) %>% gg_tsresiduals(lag=36)



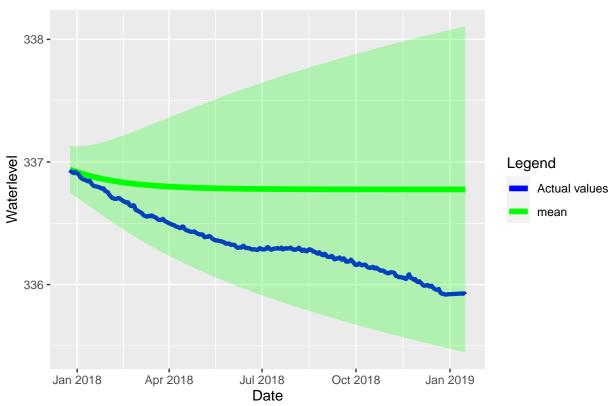
auto41 is the best model
Forecast_GW965569.1.2_ETS<-fit4 %>% select(auto41) %>%

```
forecast(h = length(test_wl_GW965569.1.2$Date))%>%hilo(level=c(95))
Actual_values<-test_wl_GW965569.1.2$WaterLevel
Forecast_GW965569.1.2_ETS$Actual_values</pre>
colors <- c("Actual values" = "blue", "mean" = "green")

Plot_AvsFitted_GW965569.1.2_ETS<-Forecast_GW965569.1.2_ETS%>%ggplot(aes(x = Date))+
    geom_line(aes(y = .mean,color="mean"),size=2)+
    geom_line(aes(y = Actual_values,color="Actual values"),size=1.5)+
    geom_ribbon(aes(ymin = Forecast_GW965569.1.2_ETS$`95%`$lower, ymax = Forecast_GW965569.1.2_ETS$`95%`$
    labs(y= "Waterlevel", x = "Date",color = "Legend",title = "ETS: GW965569.1.2")+
    scale_color_manual(values = colors)+theme(plot.title=element_text(hjust=0.5))

Plot_AvsFitted_GW965569.1.2_ETS
```

ETS: GW965569.1.2



Comparision of best modeling structure out of ARIMA and ETS

```
# Time Series Cross Validation

train_wl_GW036334_1_1 %>%
    slice(-n()) %>%
    stretch_tsibble(.init = 1560,.step = 1) %>%
    model(
        stepwise = ARIMA(WaterLevel),
```

```
auto1 = ETS(WaterLevel ~ error("A") + trend("N") + season("M"))
 ) %>%
 forecast(h = 1) \%
 accuracy(train_wl_GW036334_1_1,by=c(".model")) %>%
 select(.model, RMSE:MAPE) %>%
 arrange(MAPE)
## Warning in sqrt(diag(best$var.coef)): NaNs produced
## # A tibble: 2 x 5
                                    MAPE
##
    .model
              RMSE
                              MPE
                      MAE
##
    <chr>>
              <dbl> <dbl>
                            <dbl>
                                    <dbl>
## 1 stepwise 0.0188 0.0133 -0.00174 0.00397
## 2 auto1
            0.0837 0.0826 -0.0247 0.0247
# Time Series Cross Validation
train wl GW093067 1 1 %>%
 slice(-n()) %>%
 stretch_tsibble(.init = 1107,.step = 1) %>%
 model(
   arima222 = ARIMA(WaterLevel ~ pdq(2,2,2)),
   auto31 = ETS(WaterLevel ~ error("M") + trend("A") + season("M"))
 ) %>%
 forecast(h = 1) \%
 accuracy(train_wl_GW093067_1_1,by=c(".model")) %>%
 select(.model, RMSE:MAPE) %>%
 arrange(MAPE)
## # A tibble: 2 x 5
##
    .model
               RMSE
                       MAE
                                MPE
                                      MAPE
##
    <chr>
              <dbl>
                      <dbl>
                              <dbl>
                                      <dbl>
## 1 arima222 0.00510 0.00504 -0.00211 0.00211
## 2 auto31 0.0391 0.0378 -0.0159 0.0159
# Time Series Cross Validation
train wl GW036976.1.2 %>%
 slice(-n()) %>%
 stretch_tsibble(.init = 1544,.step = 1) %>%
   arima012 = ARIMA(WaterLevel ~ pdq(0,1,2)),
   auto31 = ETS(WaterLevel ~ error("M") + trend("A") + season("M"))
 ) %>%
 forecast(h = 1) \%
 accuracy(train_wl_GW036976.1.2,by=c(".model")) %>%
 select(.model, RMSE:MAPE) %>%
```

```
arrange (MAPE)
## # A tibble: 2 x 5
                                MPE
##
    .{\tt model}
              RMSE
                       MAE
                                      MAPE
##
    <chr>
             <dbl> <dbl>
                              <dbl>
                                      <dbl>
## 1 arima012 0.0267 0.0256 -0.00857 0.00857
## 2 auto31 0.0683 0.0604 -0.0202 0.0202
# Time Series Cross Validation
train wl GW965569.1.2 %>%
 slice(-n()) %>%
 stretch_tsibble(.init = 1544,.step = 1) %>%
 model(
   search = ARIMA(WaterLevel, stepwise=FALSE),
   auto41 = ETS(WaterLevel ~ error("M") + trend("Ad") + season("N"))
 ) %>%
 forecast(h = 1) \%
 accuracy(train_wl_GW965569.1.2,by=c(".model")) %>%
 select(.model, RMSE:MAPE) %>%
 arrange(MAPE)
## # A tibble: 2 x 5
##
    .model
              RMSE
                       MAE
                                MPE
                                      MAPE
                     <dbl>
##
    <chr>
             <dbl>
                              <dbl>
                                      <dbl>
## 1 search 0.00585 0.00494 -0.00130 0.00147
## 2 auto41 0.0100 0.00921 -0.00273 0.00273
# Residual plots
res1<-arima_fit_GW036334_1_1 %>% select(stepwise) %>% residuals()
res1_PLOT1<-res1 %>% ACF() %>% autoplot(size = 3)+
 labs(y= "acf", x = "lag", title = "GW036334.1.1")+
 theme(plot.title=element_text(hjust=0.5))
## Response variable not specified, automatically selected `var = .resid`
res2<-arima_fit_GW093067_1_1 %>% select(arima222) %>% residuals()
res2_PLOT1<-res2 %>% ACF() %>% autoplot(size = 3)+
 labs(y= "acf", x = "lag", title = "GW093067.1.1")+
 theme(plot.title=element_text(hjust=0.5))
## Response variable not specified, automatically selected `var = .resid`
res3<-arima_fit_GW036976.1.2 %>% select(arima012) %>% residuals()
res3_PLOT1<-res3 %>% ACF() %>% autoplot(size = 3)+
 labs(y= "acf", x = "lag", title = "GW036976.1.2")+
 theme(plot.title=element_text(hjust=0.5))
## Response variable not specified, automatically selected `var = .resid`
res4<-arima_fit_GW965569.1.2 %>% select(search) %>% residuals()
res4_PLOT1<-res4 %>% ACF() %>% autoplot(size = 3)+
 labs(y= "acf", x = "lag", title = "GW965569.1.2")+
 theme(plot.title=element text(hjust=0.5))
```

Response variable not specified, automatically selected `var = .resid`
Residual_Plots<-(res1_PLOT1|res2_PLOT1)/(res3_PLOT1|res4_PLOT1)
Residual_Plots</pre>

