

## Heuristic analysis

**Problem 1** involves 2 pieces of cargo, 2 airplanes and 2 airports. **Problem 2** involves 3 pieces of cargo, 3 airplanes and 3 airports. **Problem 3** involves 4 pieces of cargo, 4 airplanes and 4 airports. Hence, they are increasing in levels of complexity and the timings of the experiment reflect this reality.

Optimal plan for **Problem 1** is - **breadth\_first\_search**

```
D:\Sola\Udacity\AIND\AIND-Planning-master>python run_search.py -p 1 -s 1

Solving Air Cargo Problem 1 using breadth_first_search...

Expansions   Goal Tests   New Nodes
    43         56        180

Plan length: 6 Time elapsed in seconds: 0.030297248042767753
Load(C2, P2, JFK)
Load(C1, P1, SFO)
Fly(P2, JFK, SFO)
Unload(C2, P2, SFO)
Fly(P1, SFO, JFK)
Unload(C1, P1, JFK)
```

Optimal plan for **Problem 2** is - **greedy\_best\_first\_graph\_search** with **h\_1**

```
D:\Sola\Udacity\AIND\AIND-Planning-master>python run_search.py -p 2 -s 7

Solving Air Cargo Problem 2 using greedy_best_first_graph_search with h_1...

Expansions   Goal Tests   New Nodes
    550        552       4950

Plan length: 9 Time elapsed in seconds: 1.2043000047802412
Load(C1, P1, SFO)
Load(C2, P2, JFK)
Load(C3, P3, ATL)
Fly(P1, SFO, JFK)
Fly(P2, JFK, SFO)
Fly(P3, ATL, SFO)
Unload(C3, P3, SFO)
Unload(C2, P2, SFO)
Unload(C1, P1, JFK)
```

Optimal plan for **Problem 3** is - **astar\_search** with **h\_ignore\_preconditions**

```
D:\Sola\Udacity\AIND\AIND-Planning-master>python run_search.py -p 3 -s 9

Solving Air Cargo Problem 3 using astar_search with h_ignore_preconditions...

Expansions   Goal Tests   New Nodes
    5003        5005       44586

Plan length: 12 Time elapsed in seconds: 13.708246864300012
Load(C2, P2, JFK)
Fly(P2, JFK, ORD)
Load(C4, P2, ORD)
Fly(P2, ORD, SFO)
Unload(C4, P2, SFO)
Load(C1, P1, SFO)
Fly(P1, SFO, ATL)
Load(C3, P1, ATL)
Fly(P1, ATL, JFK)
Unload(C3, P1, JFK)
Unload(C2, P2, SFO)
Unload(C1, P1, JFK)
```

In the tables and graphs, I have plotted Performance as **(1/elapsed time x 1000)** for each search method, for comparability. For optimality, I use least plan length, and if there are any ties, I use least expansion or elapsed time. Optimal searches are highlighted in green in the tables.

Findings indicated that Breadth-first and A\* heuristic searches provide optimal results and depth-first does NOT guarantee optimality.

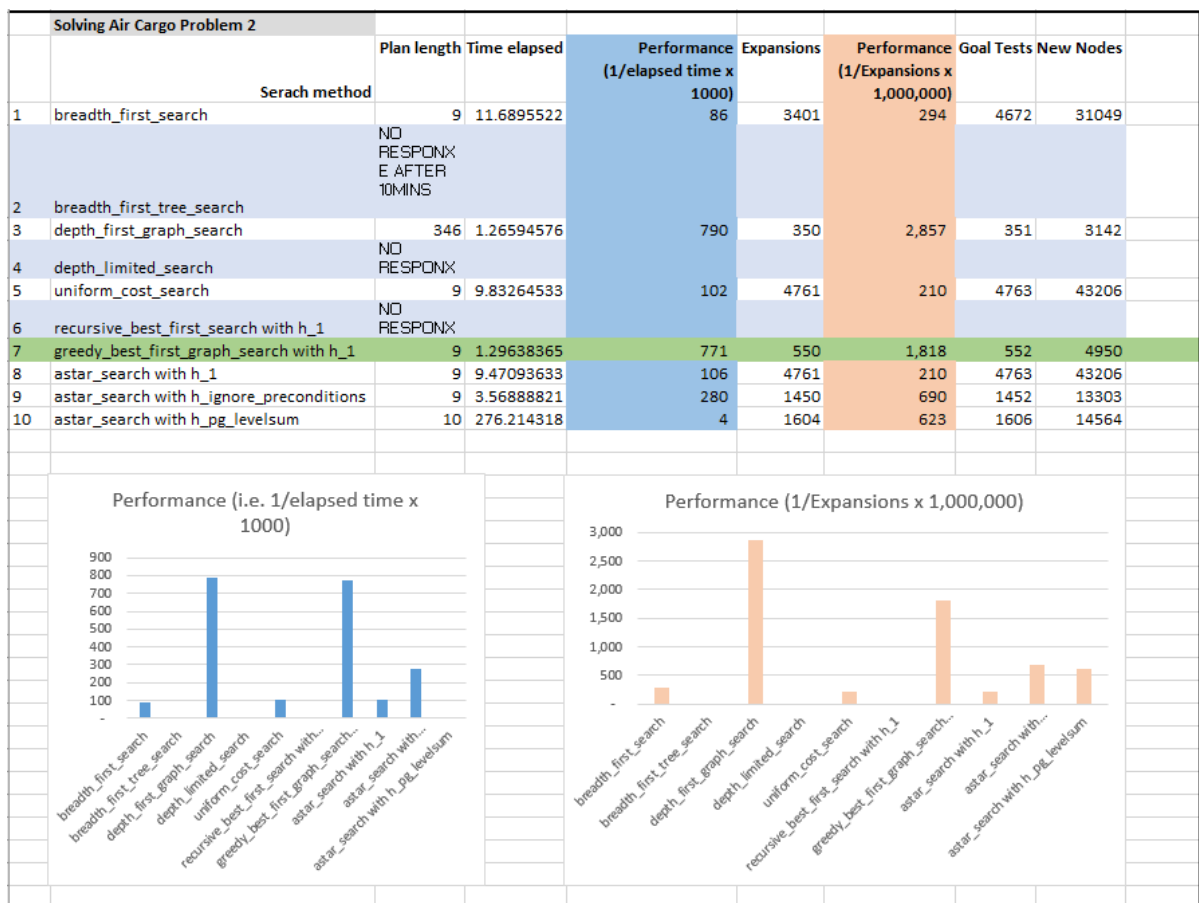
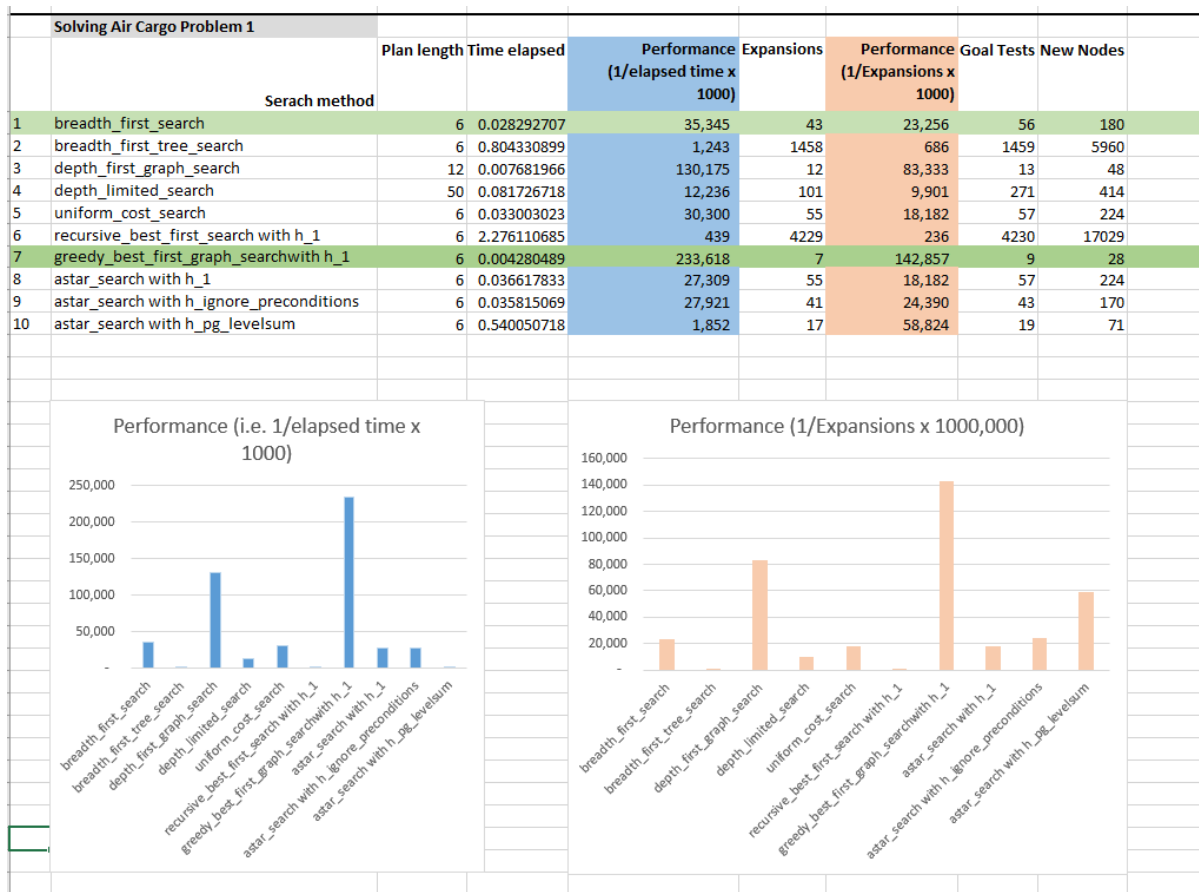
If the number of expansion is taken as a measure of performance (**i.e.  $1/\text{expansions} * 1000,000$** ), reflecting the intuition that the higher the expansions, the worse the performance - i.e. the search with the least number of expansions is the best performer since it is taking fewer steps before hitting the goal) it is found that this measure follows the same trend as the measure of performance as a function of elapsed time.

#### A\* with level-sum heuristics vs A\* with ignore preconditions

|  | Plan length | Time elapsed |
|--|-------------|--------------|
| <b>Problem 1</b>                         |             |              |
| astar_search with h_ignore_preconditions | 6           | 0.035815069  |
| astar_search with h_pg_levelsum          | 6           | 0.540050718  |
| <b>Problem 2</b>                         |             |              |
| astar_search with h_ignore_preconditions | 9           | 3.568888215  |
| astar_search with h_pg_levelsum          | 10          | 276.214318   |
| <b>Problem 3</b>                         |             |              |
| astar_search with h_ignore_preconditions | 12          | 13.74856524  |
| astar_search with h_pg_levelsum          | 13          | 649.09177    |

In all three problems A\* with ignore conditions performed better than A\* with level- sum both in terms of optimality and speed.

Overall from the figures, the best search method is the **astar\_search with h\_ignore\_preconditions** because it achieves optimality in all the three problems with appropriate time performance. In some of the problem it was not the best in terms of time performance (e.g. slower than the non-heuristic **breadth\_first\_search** in problem 1) this is in line with the table **Comparing uninformed search strategies** in section 3.4.7 of Norvig and Russells' Artificial Intelligence - A Modern Approach, third Edition where BFS is shown to be faster than other search methods.



| Solving Air Cargo Problem 3 |  |            | Plan length | Time elapsed | Performance<br>(1/elapsed time x 1000) | Expansions | Performance<br>(1/Expansions x 1,000,000) | Goal Tests | New Nodes |
|-----------------------------|--|------------|-------------|--------------|--|------------|---|------------|-----------|
|                             | Serach method                            |            |             |              |  |            |   |            |           |
| 1                           | breadth_first_search                     | 12         | 84.6760679  | 12           | 14491                                  | 69         | 17947                                     | 128184     |           |
| 2                           | breadth_first_tree_search                | NO RESPONX |             |              |  |            |   |            |           |
| 3                           | depth_first_graph_search                 | 1878       | 16.243707   | 62           | 1948                                   | 513        | 1949                                      | 16253      |           |
| 4                           | depth_limited_search                     | NO RESPONX |             |              |  |            |   |            |           |
| 5                           | uniform_cost_search                      | 12         | 40.7464876  | 25           | 17783                                  | 56         | 17785                                     | 155920     |           |
| 6                           | recursive_best_first_search with h_1     | NO RESPONX |             |              |  |            |   |            |           |
| 7                           | greedy_best_first_graph_search with h_1  | 22         | 9.46143708  | 106          | 4031                                   | 248        | 4033                                      | 35794      |           |
| 8                           | astar_search with h_1                    | 12         | 41.1189822  | 24           | 17783                                  | 56         | 17785                                     | 155920     |           |
| 9                           | astar_search with h_ignore_preconditions | 12         | 13.7485652  | 73           | 5003                                   | 200        | 5005                                      | 44586      |           |
| 10                          | astar_search with h_pg_levelsum          | 13         | 649.09177   | 2            | 2911                                   | 344        | 2913                                      | 25097      |           |
|                             |  |            |             |              |  |            |   |            |           |
|                             |  |            |             |              |  |            |   |            |           |
|                             |  |            |             |              |  |            |   |            |           |

Performance (i.e. 1/elapsed time x 1000)

| Search Method                            | Performance (i.e. 1/elapsed time x 1000) |
|--|--|
| breadth_first_search                     | 12                                       |
| breadth_first_tree_search                | 0  |
| depth_first_graph_search                 | 62                                       |
| depth_limited_search                     | 0  |
| uniform_cost_search                      | 25                                       |
| recursive_best_first_search with h_1     | 0  |
| greedy_best_first_graph_search with h_1  | 106                                      |
| astar_search with h_1                    | 24                                       |
| astar_search with h_ignore_preconditions | 73                                       |
| astar_search with h_pg_levelsum          | 2  |

Performance (1/Expansions x 1,000,000)

| Search Method                            | Performance (1/Expansions x 1,000,000) |
|--|--|
| breadth_first_search                     | 69                                     |
| breadth_first_tree_search                | 0                                      |
| depth_first_graph_search                 | 513                                    |
| depth_limited_search                     | 0                                      |
| uniform_cost_search                      | 56                                     |
| recursive_best_first_search with h_1     | 0                                      |
| greedy_best_first_graph_search with h_1  | 248                                    |
| astar_search with h_1                    | 56                                     |
| astar_search with h_ignore_preconditions | 200                                    |
| astar_search with h_pg_levelsum          | 344                                    |