

Assignment 17.

State Peterson's algorithm. List its properties and prove each of them.

SHARED: $\text{inter}[0] = \text{inter}[1] = \text{false}$, $\text{turn_to_wait} = \text{doesn't matter}$.

Code for process 0.

```
inter[0] = True
turn_to_wait = 0
while ((inter[1] == True) AND (turn_to_wait == 0)) { // busy waiting }
<CS>
inter[0] = False
```

Code for process 1.

```
inter[1] = True
turn_to_wait = 1
while ((inter[0] == True) AND (turn_to_wait == 1)) { // busy waiting }
<CS>
inter[1] = False
```


Mutual exclusion:

Assume for the sake of the contradiction that the Peterson's algorithm doesn't provide mutual exclusion. Then, the only way to get such a situation is either:

- $\text{turn_to_wait} = 0$ and $\text{turn_to_wait} = 1$: it's trivial that's this isn't possible.
- $\text{turn_to_wait} = 0$ and $\text{inter}[0] = \text{false}$: Assuming $\text{turn_to_wait} = 0$, we show that inter must be true. Indeed, since $\text{turn_to_wait} = 0$, $\text{inter}[0]$ is true by the algorithm rules (if not then the process 0 just finish the CS and then if he is interested once again he must state $\text{inter}[0] = \text{true}$). Thus, this case cannot happen in anytime on the algorithm.
- $\text{turn_to_wait} = 1$ and $\text{inter}[1] = \text{false}$: similar argument than $\text{turn_to_wait} = 0$ and $\text{inter}[0] = \text{false}$.
- $\text{inter}[0] = \text{false}$ and $\text{inter}[1] = \text{false}$: Trivially, the value of $\text{inter}[0]$ is changed only in the process 1 and the same with $\text{inter}[1]$ in the process 0. Then, every time that any process either 1 or 2 is interested to enter in the CS, he turn the value of the inter of the other process to true. Then there is no way to get $\text{inter}[0] = \text{false}$ and $\text{inter}[1] = \text{false}$.

No one of those situation can happen, which confirm the claim. ■

Deadlock free:

Since `turn_to_wait` is either 0 or 1 but can't be both at the same time, it's trivial that Peterson's provide deadlock freedom. 

Starvation free:

Assume for the sake of the contradiction that the Peterson's algorithm doesn't provide starvation freedom. Then, the only way to get such a situation is either:

- `inter[1] = true` and `turn_to_wait = 1` forever: If `inter[1] = true`, we can affirm that process 1 is interested. Then both of processes interested, by the deadlock free property we have than one of the two enter in the CS. Assuming that process 1 enter in the CS (else we do not have `inter[1] = true` and `turn_to_wait = 1`), when process 1 enter in the exit code, he turn `inter[1]` to false. Now process 0 is able to enter in the process, if he gets running time. If he doesn't, and process 1 is once again interested by enter in the CS, we will have `turn_to_wait = 1`, and then, only process 0 can enter in the CS. Contradicting the claim that `inter[1] = true` and `turn_to_wait = 1` forever.
- `inter[0] = true` and `turn_to_wait = 0` forever: with a similar argument than above, we conclude the claim.

No one of those situation can happen, which confirm the claim. 