CS2102

RELATIONAL ALGEBRA

• Relations are closed under the Relational Algebra

Unary operators

Selection σ_c

- For each tuple $t \in R$, $t \in \sigma_c(R) \iff$ selection condition c evaluates to true for tuple t.
- Input and output have same schema
- e.g. Find all projects where Judy is the manager: $\sigma_{\rm manager=`Judy'}({\rm Projects})$

Selection condition is a boolean expression of one of the following forms:

expression	example	
attribute op constant	$\sigma_{\text{start}=2020}(\text{Projects})$	
$attr_1$ op $attr_2$	$\sigma_{\text{start}=\text{end}}(\text{Projects})$	
$expr_1 \wedge expr_2$	$\sigma_{\text{start}=2020 \land \text{end}=2021}(\text{Projects})$	
$expr_1 \lor expr_2$	$\sigma_{\text{start}=2020 \lor \text{end}=2021}(\text{Projects})$	
$\neg expr$	$\sigma_{\neg(\text{start}=2020)}(\text{Projects})$	
(expr)	-	

where

- op $\in \{=, <>, <, \leq, \geq, >\}$
- Precedence: $(), \mathbf{op}, \neg, \wedge, \vee$
- Comparision with null is unknown, arithmetic with null is null

In boolean expressions, treat unknown as literally unknown. e.g.

- false \land unknown = false
- false ∨ unknown = unknown
- ¬ unknown = unknown
- true ∧ unknown = unknown
- true ∨ unknown = true

Projection π_l

- $\bullet\,$ Projects columns of a table specified in list l
- \bullet Order of attributes in l matters
- Duplicates are removed, because a relation is a set of tuples

Example

	•	Team

en	pn	hours	
Sarah	BigAI	10	
Sam	BigAI	5	
Sam	BigAI	3	

$\pi_{\mathrm{pn,en}}(\mathrm{Teams})$			
pn	en		
BigAI	Sarah		
BigAI	Sam		

Renaming ρ_l

• Renames attributes of a relation

Consider R(ename, pname, hours). Rename ename to name, pname to title. Can either specify

- list of all attr.: $\rho_{\text{(name, title, hours)}}(R)$
- or list of renames:

$$\rho_{\text{name}} \leftarrow \text{ename}, \text{title} \leftarrow \text{pname}(R)$$

Set operations

- Union, Intersection, Set difference (all obvious)
- Note: intersection can be expressed with union and set difference:

$$R \cap S = (R \cup S) - ((R - S) \cup (S - R))$$

• The two relations must be union-compatible

Union compatability

Two relations are union-compatible if

- Same number of attributes
- Corresponding attributes have same or compatible domains (different attribute names are ok)

${\bf Example} \quad {\bf The \ following \ are \ union-compatible}.$

- Employees(name: text, role: text, age: integer)
- Teams(ename: text, pname: text, hours: integer)

Cross product

Forms all possible pairs of tuples from the two rela-

Join operations

- Combines \times, σ_c, π_l into a single op
- Simple relational algebra expressions

Inner joins

- Eliminates tuples that do not satisfy matching criteria (i.e. selection)
- Is a selection from cross product

θ -Join

$$R\bowtie_{\theta} S = \sigma_{\theta}(R \times S)$$

Equi Join

Like θ -Join, but θ must only involve =

Natural Join

Like equi join (i.e. only equality operator), but

- • Join is performed over common attributes of R and S
- If there are no common attributes, acts like a cross product, since selection condition c is vacuously true
- Output relation keeps one copy of common attributes

Formally,

$$R \bowtie S = \pi_l(R \bowtie_c \rho_{b_i \leftarrow a_i, \cdots, b_k \leftarrow a_k}(S))$$

where

- $A = \{a_i, \cdots, a_k\}$ is the set of common attributes of R and S
- $c = (a_i = b_i) \land \cdots \land (a_k = b_k)$
- l = list of (attr. of R + attr. of S not in A)

Outer joins

- Inner join + dangling tuples
- A dangling tuple is a tuple that doesn't satisfy the inner join condition, i.e. foreign key not referenced in the relation.

Steps

- Perform inner join $M = R \bowtie_{\theta} S$
- ullet To M, add dangling tuples from

 $\begin{cases} R & \text{in left outer join} \bowtie_{\theta} \\ S & \text{in right outer join} \bowtie_{\theta} \\ R \text{ and } S & \text{in full outer join} \bowtie_{\theta} \end{cases}$

 $\bullet\,$ Pad missing attribute values with ${\bf null}$

Formal definitions

 Set of dangling tuples in R, with respect to $R\bowtie_{\theta} S$

$$dangle(R \bowtie_{\theta} S) \subseteq R$$

- null(R) is a n-component tuple of null values, where n is the number of attributes in R
- $$\begin{split} \bullet \ \ \text{Left outer join } (R \bowtie_{\theta} S) \\ &= (R \bowtie_{\theta} S) \cup (\text{dangle}(R \bowtie_{\theta} S) \times \{\text{null}(S)\}) \end{split}$$
- Right outer join $(R \bowtie_{\theta} S)$
- $= (R \bowtie_{\theta} S) \cup (\{\text{null}(R)\} \times \text{dangle}(S \bowtie_{\theta} R))$
- Full outer join $(R \bowtie_{\theta} S)$

$$= (R \bowtie_{\theta} S) \cup \Big((\operatorname{dangle}(R \bowtie_{\theta} S) \times {\operatorname{null}(S)}) \Big)$$

 $\cup (\{\operatorname{null}(R)\} \times \operatorname{dangle}(S \bowtie_{\theta} R)))$

Natural outer joins

- Like natural inner joins
- Only equality operator used for condition
- ullet Join is performed over common attributes of R
- Output relation keeps one copy of common attributes

Complex expressions

There are multiple ways to formulate a query to get the same result, e.g.

- Order of joins
- Order of selection (before/after join)
- Additional projections to minimize intermediate results

Invalid expressions

- Attribute no longer available after projection $\sigma_{\text{role}=\text{`dev'}}(\pi_{\text{name,age}}(Employees))$
- Attribute no longer available after renaming $\sigma_{\text{role}=\text{`dev'}}(\rho_{\text{position}\leftarrow \text{role}}(Employees))$
- • Incompatible attribute types $\sigma_{\text{age=role}}(Employees)$

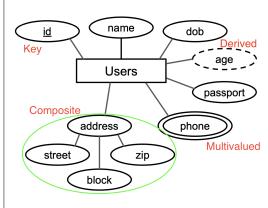
ER MODEL

Entity

- \bullet Objects that are distinguishable from other objects
- Entity set: Collection of entities of the same type

Attribute

- Specific information describing an entity
- Key attr uniquely identifies each entity
- Composite attr composed of multiple other attributes
- Multivalued attr may consist of more than one value for a given entity
- Derived attr derived from other attributes



Relationship

Association among two or more entities

Relationship set

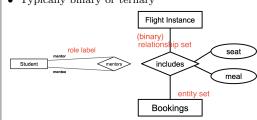
- Collection of relationships of the same type
- Can have their own attributes that further describe the relationship
- $Key(E_i)$ is the attributes of the selected key of entity set E_i

Role

- Describes an entity set's participation in a relationship
- Explicit role label only in case of ambiguities (e.g. same entity set participates in same relationship more than once)

Degree

- An *n*-ary relationship set involves *n* entity roles, where *n* is the degree of the relationship set
- Typically binary or ternary



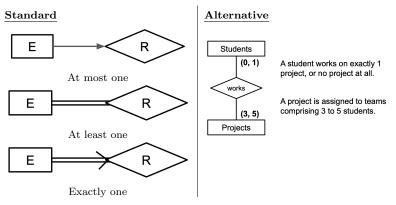
Cardinality constraints

• Upper bound for entity's participation



Participation constraints

- Lower bound for entity's participation
- Partial (default): participation not mandatory
- Total: mandatory (at least 1)



Implementation

Many-to-Many Represent relationship set with a table

Many-to-One

- 1. Represent relationship set between A and B with a table (A_{id}, B_{id}) . Make the ID of the total participation entity set the primary key
- 2. Combine rel. set and total participiation entity set into one table

One-to-One

- 1. Represent relationship set between A and B with a table (A_{id}, B_{id}) . One is unique not null, and the other is the primary key
- 2. Combine relationship set and either entity set into one table

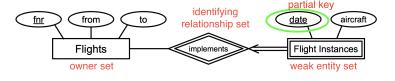
Dependency constraints

Weak entity sets

- Entity set that does not have its own key
- Can only be uniquely identified by considering primary key of owner entity
- Existence depends on existence of owner entity

Partial key

 Set of attributes of weak entity set that uniquely identifies a weak entity, for a given owner entity



Requirements

- $\bullet\,$ Many-to-one relationship from weak entity set to owner entity set
- Weak entity set must have total participation in identifying relationship

Relational mapping

- Entity set \rightarrow table
- Composite/multivalued attributes:
 - 1. Convert to single-valued attributes
 - 2. Additional table with FK constraint
 - 3. Convert to a single-valued attribute (e.g. comma separated string)

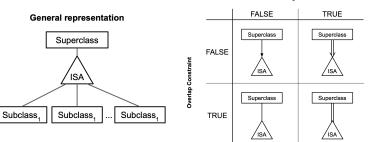
ISA Hierarchies

Used to model generalization/specialization of entity sets

Constraints

Overlap Can a superclass entity belong to multiple subclasses?

Covering Does a superclass entity have to belong to a subclass?



Aggregation

• Abstraction that treats relationships as higher-level entities

FUNCTIONS AND PROCEDURES

- CREATE OR REPLACE helps to re-declare function/procedure if already previously defined
- Code is enclosed within \$\$
- Call a function: SELECT * FROM swap(2, 3);
- Call a procedure: CALL transfer('Alice', 'Bob', 100);

Return types

Return	Type	
Single tuple from table	<table_name></table_name>	
Set of tuples from table	<pre>SET OF <table_name></table_name></pre>	
Single new tuple	RECORD	
Set of new tuples	SET OF RECORD or	
	TABLE(c VARCHAR, x INT)	
No return value	VOID, or use PROCEDURE	
	instead of FUNCTION	
Trigger	TRIGGER	

Control structures

Variables

- DECLARE [<var> <type>] (1 or more when DECLARE keyword is present)
- <var> := <expr>

Selection

• IF ... THEN ...

[ELSIF ... THEN ...]

[ELSE ...] END IF

(0 or more ELSIF)

Repetition

- LOOP ... END LOOP, and EXIT ... WHEN ... (conditional exit)
- WHILE ... LOOP ... END LOOP
- FOR ... IN ... LOOP ... END LOOP
- 1..10 (range, inclusive)

Block

- BEGIN ... END
- For plpgsql, code in the BEGIN-END block is in a transaction

Examples

Note: ${\tt INOUT}$ specifies that the param is both an input and output param

Function

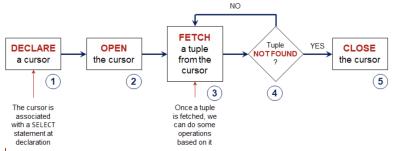
```
CREATE OR REPLACE FUNCTION
swap(INOUT val1 INT, INOUT
val2 INT)
RETURNS RECORD AS $$
DECLARE
temp INT;
BEGIN
temp := val1;
val1 := val2;
val2 := temp;
END;
$$ LANGUAGE plpgsql;
```

Procedure

```
CREATE OR REPLACE PROCEDURE
transfer(
src TEXT, dst TEXT,
amt NUMERIC
) AS $$
UPDATE Accounts
SET balance = balance - amt
WHERE name = src;
UPDATE Accounts
SET balance = balance + amt
WHERE name = dst;
$$ LANGUAGE sql;
```

Cursor

- Declare, Open, Fetch, Check (repeat), Close
- FETCH [PRIOR | FIRST | LAST | ABSOLUTE n] [FROM] <cursor> INTO <var>



Ouestion

Given the table "Scores" from before, write a function to perform the following task:

- 1. Sort the students in "Scores" in descending order of their Mark (break ties arbitrarily)
- 2. For each student, compute the difference between his/her Mark and the Mark of the previous student
 - $\circ\,$ If there is no previous student, use NULL

Solution

```
CREATE OR REPLACE FUNCTION score_gap()
RETURNS TABLE(name TEXT, mark INT, gap INT) AS $$
DECLARE
 curs CURSOR FOR (SELECT * FROM Scores ORDER BY Mark DESC);
  r RECORD; prev INT;
  prev := -1; OPEN curs;
    FETCH curs INTO r;
    EXIT WHEN NOT FOUND;
    name := r.Name; mark := r.Mark;
IF prev >= 0 THEN gap := prev - mark;
                       gap := NULL;
    RETURN NEXT: -- insert into output
    prev := r.mark;
  CLOSE curs;
$$ LANGUAGE plpgsql;
```

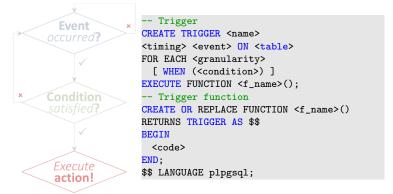
Explanation

- Declare a *cursor* associated with a SELECT statement or is a RECORD to store
 - previous row
- 2. **Open** the cursor which executes the SQL statement and let the cursor point to the **beginning** of the result 3. Fetch a tuple from the cursor by reading the **next** tuple from cursor and assign into the variable
- 4. If the FETCH operation did not
- get any tuple, the loop terminates

 Otherwise, perform the main operation and insert into output
- 5. Close the cursor to release the resources allocated

TRIGGERS

• Note: cannot CREATE OR REPLACE TRIGGER. Need to DROP TRIGGER



Trigger options

Events

- INSERT ON
- DELETE ON
- UPDATE [OF <column>] ON
- INSERT OR DELETE OR UPDATE ON
- Alternatively, use TG_OP variable. Is set to 'INSERT' | 'DELETE' | 'UPDATE'

Timings

- AFTER/BEFORE (after/before event)
- ullet INSTEAD OF (replaces event, only for VIEWS)

Granularity

- FOR EACH ROW (for each tuple encountered)
- FOR EACH STATEMENT (for each statement)

Effect of return value

• OLD / NEW: Modified row before / after the triggering event

Events + Timings	NULL tuple	Non-NULL tuple t
BEFORE INSERT	No insertion	t is inserted
BEFORE UPDATE	No update	t is the updated tuple
BEFORE DELETE	No deletion	Deletion proceeds as normal
AFTER	No effect	No effect

Granularity

- In FOR EACH STATEMENT, doing RETURN NULL will not do anything
- Need to use RAISE EXCEPTION to stop the operation

Trigger condition

- Use WHEN() for conditional check whether a trigger should run
- e.g. WHEN (NEW.StuName = 'Adi')

Usage

- No SELECT in WHEN()
- No NEW in WHEN() for DELETE
- No OLD in WHEN() for INSERT
- No WHEN() for INSTEAD OF

Deferred triggers

- Triggers that are checked only at the end of a transaction
- CONSTRAINT + DEFERRABLE together indicate that trigger can be deferred
- Only works with AFTER and FOR EACH ROW
- Default is **IMMEDIATE**

```
CREATE CONSTRAINT TRIGGER <name>
AFTER <event> ON 
FOR EACH ROW
 [ WHEN (<condition>) ]
 [ DEFERRABLE INITIALLY [ DEFERRED | IMMEDIATE ] ]
EXECUTE FUNCTION <func_name>();
```

Multiple triggers

- Activation order for the same event on the same table:
- 1. BEFORE statement-level triggers
- 3. AFTER row-level triggers
- 2. BEFORE row-level triggers
- 4. AFTER statement-level triggers
- Within the same category, triggers are activated in alphabetical order
- If BEFORE row-level trigger returns NULL, then subsequent triggers on the same row are omitted

FUNCTIONAL DEPENDENCIES

Basic terminology

Reading FDs $X \to Y$ reads: X (functionally) determines $Y \mid Y$ is functionally dependent on $X \mid X$ implies Y (casual)

Instance An instance r (a table) of a relation R satisfies the FD $\sigma: X \to Y$ with $X \subset R$ and $Y \subset R$, \iff if two tuples of r agree on their X-values, then they agree on their Y-values

Valid instance An instance r of relation R is a valid instance of R with $\Sigma \iff \text{it satisfies } \Sigma$

Violations An instance r of relation R violates a set of FDs $\Sigma \iff$ does not satisfy Σ

Holds

- A relation R with a set of FDs Σ , R with Σ , refers to the set of valid instances of R wrt. to the FDs in Σ
- When a set of FDs Σ holds on a relation R, only consider the valid instances of R with Σ

Trivial $X \to Y$ is trivial $\iff Y \subset X$

Non-trivial $X \to Y$ is non-trivial $\iff Y \not\subset X$

Completely non-trivial $X \to Y$ is completely non-trivial $\iff Y \neq \emptyset$ and $Y \cap X = \emptyset$

Key terminology

Superkey Let $S \subset R$ be a set of attributes of R. S is a superkey of $R \iff S \to R$

Candidate key A superkey such that no proper subset is also a superkey

Primary key Chosen candidate key, or the candidate key if there is only one

Prime attribute An attribute that appears in some candidate key of R with Σ . If not, then it is a non-prime attribute

FD terminology

Closure Let Σ be a set of FDs of a relation R. The closure of Σ , denoted Σ^+ , is the set of all FDs logically entailed by the FDs in Σ

Equivalence Two FDs are equivalent \iff have the same closure

Cover Σ_1 is a cover of Σ_2 (and vice versa) \iff their closure are equivalent

Closure of a set of attributes Let Σ be a set of FDs of a relation R. The closure of a set of attributes $S \subset R$, denoted S^+ , is the set of all attributes that are functionally dependent on S (i.e. what S implies)

$$S^+ = \{ A \in R \mid \exists (S \to \{A\}) \in \Sigma^+ \}$$

Computing attribute closures • Check if any attribute doesn't appear in the RHS

- of any FD. These attributes must appear in the • Compute attribute closure starting with singular
- attributes. Then compute for 2 elements, 3 elements and so on. Note all <u>candidate keys</u> in the process
- If current set of attributes is a superset of some
- previously seen, candidate key, can skip

Armstrong axioms

Reflexivity $\forall X, Y \subset R ((Y \subset X) \Rightarrow (X \to Y))$

Augmentation $\forall X, Y, Z \subset R \left((X \to Y) \Rightarrow (X \cup Z \to Y \cup Z) \right)$

Transitivity $\forall X, Y, Z \subset R \left((X \to Y) \land (Y \to Z) \Rightarrow (X \to Z) \right)$

when applied to Σ

Complete: The rule(s) generate(s) all elements of Σ^+ when applied to Σ

Sound: The rule only generates elements of Σ⁺

- The three inference rules are (individually) sound • The Armstrong axioms are (together) sound and
- Additional rules

Must be derived during exam

Weak augmentation

If $X \to Y$, then $X \cup Z \to Y$

1. $X \to Y$ (given)

2. We know that $X \subset X \cup Z$

3. $X \cup Z \to X$ (reflexivity)

4. $X \cup Z \rightarrow Y$ (trans. of 3 and 1)

Union

If $X \to Y$ and $X \to Z$, then $X \to Y \cup Z$

Proof 1. $X \to Y$ (given)

2. $X \to Z$ (given) 3. $X \to X \cup Z$ (aug. 2 and X)

4. $X \cup Z \rightarrow Y \cup Z$ (aug. 1 and Z)

5. $X \to Y \cup Z$ (trans. of 3 and 4)

Decomposition

If $X \to Y \cup Z$, then $X \to Y$ and $X \to Z$

1. $X \to Y \cup Z$ (given)

2. $Y \cup Z \rightarrow Y$ (reflexivity)

3. $X \to Y$ (trans. of 1 and 2)

Composition

If $X \to Y$ and $A \to B$, then $X \cup A \to Y \cup B$

Proof

1. $X \to Y$ (given)

2. $A \rightarrow B$ (given) 3. $X \cup A \rightarrow Y \cup A$ (aug. 1 and A)

4. $X \cup A \rightarrow Y$ (decomp. of 3)

5. $X \cup A \rightarrow X \cup B$ (aug. 2 and X)

6. $X \cup A \rightarrow B$ (decomp. of 5)

7. $X \cup A \rightarrow Y \cup B$ (union 4 and 6)

Pseudo-transitivity

If $X \to Y$ and $Y \cup Z \to W$, then $X \cup Z \to W$

Proof

1. $X \to Y$ (given) 2. $Y \cup Z \rightarrow W$ (given)

3. $X \cup Z \rightarrow Y \cup Z$ (aug. of 1 and Z) 4. $X \cup Z \rightarrow W$ (trans. of 3 and 2)

Minimal cover Definition

A set Σ of FDs is minimal if and only if

• RHS of each FD in Σ is minimal, i.e. each FD is

of the form $X \to \{A\}$ \bullet LHS of each FD in Σ is minimal, i.e. for every

- FD in Σ of the form $X \to \{A\}$, there is no FD $Y \to \{A\}$ such that $Y \subset X$ • The set is minimal, i.e. no FD in Σ can be derived
- from other FDs in Σ

A minimal cover of a set of FDs Σ is a set of FDs

 Σ' that is both minimal and equivalent to Σ · Every set of FDs has a minimal cover

Algorithm

1. Simplify RHS of every FD (by splitting FDs so

with the subset)

same LHS

Reachability

a language

- that RHS of each FD is a singleton) 2. Simplify LHS of every FD (for each FD, if a subset of LHS can imply RHS, then replace LHS
- 3. Remove redundant FDs (for each FD, start from LHS. if this FD can be derived using only other FDs, then remove it) 4. (If compact cover is desired) Combine FDs with
- The algorithm always finds a minimal cover
- Some minimal covers may be unreachable
- To reach all minimal covers, the algorithm needs to start from Σ^+
- Anomalies

faculty

	tanh	comp.sut.edu	computer science	computing	Python
	ami	med.sut.edu	pharmacy	medicine	R
,	• Depa	$artment \rightarrow$	faculty is a Fl	D in this	example

- Redundant storage: The faculty of a department is repeated for every student of the department, and every time the student is proficient in
- have the same value for the column department but different values for the column faculty, violating the FD • Deletion anomaly: If we delete the last row, we

• Update anomaly: When 2 rows of the table

- may forget that we have a department of pharmacy, and a faculty of medicine • Insertion anomaly: We cannot record that the
- department of social science exists and the faculty of liberal arts exists, because there is no student from this department or this faculty Solution

• In all cases, the solution is to remove faculty from

- the original table, and create a new table with department and faculty In the case of the update anomaly, to enforce the
- FD, we also need to make department the primary key of the new table

Normalization Normal forms

• Recognize designs that enforce FDs through main

- SQL constraints (PK, unique, not null, FK) • Protect data against anomalies
- Normalization

for every FD $X \to \{A\} \in \Sigma^+$,

Transform (decompose) a poor design into one that

enforces FDs by means of the main SQL constraints

Boyce-Codd Normal Form A relation R with a set of FDs Σ is in BCNF \iff

- either $X \to \{A\}$ is trivial, or
- \bullet X is a superkey

- 1. Compute attribute closures of the original set,
- and project FDs to each relation R_i 2. If some R_i is not in BCNF, then FALSE. Else

Check if decomp. set of relations is in BCNF

Decomposition

Terminology

Decomposition A decomposition of table R is a set of tables $\{R_1, R_2, \cdots, R_n\}$ such that R =

 $R_1 \cup \cdots \cup R_n$

Binary decomposition Decomp with n=2Lossless-join definitions • A binary decomp is lossless-join \iff full outer

- natural join of its two fragments equal the initial table. Otherwise it is lossy A binary decomp of R into R_1 and R_2 is losslessjoin if $R = R_1 \cup R_2$ and either $R_1 \cap R_2 \to R_1$ or
- $R_1 \cap R_2 \to R_2$ • A decomp is lossless-join if there exists a sequence of binary lossless-join decomp that generates that
- from R with Σ where $R' \subset R$, is the set of FDs equivalent to the set of FDs $X \to Y$ in Σ^+ such that $X \subset R'$ and $Y \subset R'$ Dependency preserving A decomp of R with Σ into R_1, R_2, \dots, R_n with respective projected FDs $\Sigma_1, \Sigma_2, \cdots, \Sigma_n$ is dependency preserving \iff

Projected FDs A set Σ of projected FDs on R',

Check lossless-join 1. Compute attribute closures of the original set

 $\Sigma^+ = (\Sigma_1 \cup \dots \cup \Sigma_n)^+$

- 2. For some pair (R_i, R_j) , $i \neq j$, • Check that $R_i \cap R_j \to R_i$ or $R_i \cap R_j \to R_j$
 - If yes, then replace R_i, R_j with $R_i \cup R_j$ and repeat Step 2-3.
- If no, then try next pair 3. If there was a sequence of unions that resulted
 - in a single relation that has all attributes, then TRUE. Else FALSE

Check dependency-preserving 1. Let R be the original set of relations. Can re-

the union of projected FDs to each relation 2. For each FD in R, check that we can derive it in Y. If some FD could not be derived, then that

place R with minimal cover if found. Let Y be

FD was not preserved, then FALSE. Else TRUE Decomposition algorithm

definition (not trivial, and X not superkey). Use it

• Guarantees lossless decomp, but may not be dependency preserving

to decompose R into R_1 and R_2 :

- Can get different results depending on order of FD chosen
- Let $X \to Y$ be a FD in Σ that violates the BCNF

• $R_1 = X^+$ • $R_2 = (R - X^+) \cup X$

Then, check whether R_1 and R_2 with respective projected FDs Σ_1 and Σ_2 are in BCNF. Repeat decomp algo for the fragments which are not.

3NF Definition A relation R with a set of FDs Σ is in 3NF \iff

• $X \to \{A\}$ is trivial, or \bullet X is a superkey, or

for every FD $X \to \{A\} \in \Sigma^+$,

• A is a prime attribute

Note that BCNF implies 3NF

with that candidate key

3NF Synthesis Guarantees a lossless, dependency preserving de-

comp in 3NF

- ullet For each FD $X \to Y$ in the compact minimal cover, create a relation $R_i = X \cup Y$ unless it already exists, or is subsumed by another relation
- If none of the created relations contains one of the keys, pick a candidate key and create a relation