RELATIONAL ALGEBRA

Relations are closed under the Relational Algebra

Unary operators

Selection σ_c

- For each tuple $t \in R$, $t \in \sigma_c(R) \iff$ selection condition c evaluates to true for tuple t.
- Input and output have same schema
- e.g. Find all projects where Judy is the manager: $\sigma_{\rm manager='Judy'}({\rm Projects})$

Selection condition is a boolean expression of one of the following forms:

expression	example	
attribute op constant	$\sigma_{\text{start}=2020}(\text{Projects})$	
$attr_1$ op $attr_2$	$\sigma_{\text{start}=\text{end}}(\text{Projects})$	
$expr_1 \wedge expr_2$	$\sigma_{\text{start}=2020 \land \text{end}=2021}(\text{Projects})$	
$expr_1 \lor expr_2$	$\sigma_{\text{start}=2020 \vee \text{end}=2021}(\text{Projects})$	
$\neg expr$	$\sigma_{\neg(\text{start}=2020)}(\text{Projects})$	
(expr)	-	
• op ∈ {=, <>, <, <, >, >}		

- Precedence: $(), \mathbf{op}, \neg, \wedge, \vee$
- Comparision with null is unknown, arithmetic with null is null

In boolean expressions, treat unknown as literally unknown, and use short circuit evaluation where

Projection π_l

- ullet Projects columns of a table specified in list l
- Order of attributes in l matters
- Duplicates are removed, because a relation is a set of tuples

Example

Teams				
en	pn	hours		
Sarah	BigAI	10		
Sam	BigAI	5		
Sam	BigAI	3		

$\pi_{\rm pn,en}($	Teams)
pn	$\mathbf{e}\mathbf{n}$
BigAI	Sarah
BigAI	Sam

Renaming ρ_l

- Renames attributes of a relation
- Consider R(ename, pname, hours). Rename ename to name, pname to title. Can either specify
- list of all attr.: $\rho_{\text{(name, title, hours)}}(R)$
- or list of renames:

$$\rho_{\text{name}} \leftarrow \text{ename}, \text{ title} \leftarrow \text{pname}(R)$$

Set operations

- ∩, ∪, ×, Set difference (all obvious)
- Note: intersection can be expressed with union and set difference:

$$R \cap S = (R \cup S) - ((R - S) \cup (S - R))$$

The two relations must be union-compatible

Union compatability

Two relations are union-compatible if

- Same number of attributes
- Corresponding attributes have same or compatible domains (different attribute names are ok)

Example The following are union-compatible.

- Employees(name: text, role: text, age: integer)
- Teams(ename: text, pname: text, hours: inte-

Join operations

- Combines \times, σ_c, π_l into a single op
- Simple relational algebra expressions

Inner joins

- Eliminates tuples that do not satisfy matching criteria (i.e. selection)
- Is a selection from cross product

Like θ -Join, but θ must only involve =

θ -Join

$$R \bowtie_{\theta} S = \sigma_{\theta}(R \times S)$$

Equi Join

Natural Join

Like equi join (i.e. only equality operator), but

- \bullet Join is performed over common attr of R and S
- If there are no common attributes, acts like a cross
- product, since selection condition c is vacuously
- Output relation keeps one copy of common attributes

Formally,

$$\stackrel{R}{\bowtie} S = \pi_l(R \bowtie_c \rho_{b_i \leftarrow a_i, \cdots, b_k \leftarrow a_k}(S))$$
 where

- $A = \{a_i, \dots, a_k\}$ is the set of common attr of Rand S
- $c = (a_i = b_i) \land \cdots \land (a_k = b_k)$
- l = list of (attr. of R + attr. of S not in A)

Outer joins

- Inner join + dangling tuples
- A dangling tuple is a tuple that doesn't satisfy the inner join condition, i.e. foreign key not referenced in the relation.

- Perform inner join $M = R \bowtie_{\theta} S$
- To M, add dangling tuples from in left outer join \mathbb{M}_{θ}

in right outer join \bowtie_{θ} R and S in full outer join \bowtie_{θ}

• Pad missing attribute values with null

Formal definitions

- Set of dangling tuples in R, wrt $R \bowtie_{\theta} S$ $dangle(R \bowtie_{\theta} S) \subseteq R$
- null(R) is a *n*-component tuple of **null** values, where n is the number of attributes in R
- Left outer join $(R \bowtie_{\theta} S)$ $= (R \bowtie_{\theta} S) \cup (\operatorname{dangle}(R \bowtie_{\theta} S) \times {\operatorname{null}(S)})$
- Right outer join $(R \bowtie_{\theta} S)$ $= (R \bowtie_{\theta} S) \cup (\{\text{null}(R)\} \times \text{dangle}(S \bowtie_{\theta} R))$
- Full outer join $(R \bowtie_{\theta} S)$

$$= (R \bowtie_{\theta} S) \cup \Big((\operatorname{dangle}(R \bowtie_{\theta} S) \times {\operatorname{null}(S)})$$

$$\cup ({\operatorname{null}(R)}) \times \operatorname{dangle}(S \bowtie_{\theta} R)) \Big)$$

Natural outer joins

- Like natural inner joins
- Only equality operator used for condition
- ullet Join is performed over common attr of R and S
- Output relation keeps one copy of common attributes

Complex expressions

There are multiple ways to formulate a query to get the same result, e.g.

- Order of joins
- Order of selection (before/after join)
- Additional projections to minimize intermediate results

Invalid expressions

- Attribute no longer available after projection $\sigma_{\text{role}=\text{`dev'}}(\pi_{\text{name,age}}(Employees))$
- Attribute no longer available after renaming $\sigma_{\text{role}=\text{`dev'}}(\rho_{\text{position}\leftarrow\text{role}}(Employees))$
- Incompatible attribute types $\sigma_{\text{age=role}}(Employees)$

RA equivalence rules

$$\begin{split} \sigma_{\theta_1 \wedge \theta_2}(E) &= \sigma_{\theta_1}(\sigma_{\theta_2}(E)) \\ \sigma_{\theta_1}(\sigma_{\theta_2}(E)) &= \sigma_{\theta_2}(\sigma_{\theta_1}(E)) \\ \pi_{L_1}(\pi_{L_2}(\cdots(\pi_{L_n}(E)))) &= \pi_{L_1}(E) \\ \sigma_{\theta}(E_1 \times E_2) &= E_1 \bowtie_{\theta} E_2 \\ \sigma_{\theta_1}(E_1 \bowtie_{\theta_2} E_2) &= E_1 \bowtie_{\theta_1 \wedge \theta_2} E_2 \\ E_1 \bowtie_{\theta} E_2 &= E_2 \bowtie_{\theta} E_1 \\ (E_1 \bowtie E_2) \bowtie E_3 &= E_1 \bowtie (E_2 \bowtie E_3) \end{split}$$

- Selection distributes over \cap , \cup , set difference
- Projection distributes over union

under the following two conditions:

- ∩, ∪ are commutative and associative
- Theta joins are associative in the following way $(E_1 \bowtie_{\theta_1} E_2) \bowtie_{\theta_2 \land \theta_3} E_3 = E_1 \bowtie_{\theta_1 \land \theta_3} (E_2 \bowtie_{\theta_2} E_3),$ where θ_2 involves attributes from E_2 and E_3 only 7. The selection operation distributes over the theta join operation
 - (a) It distributes when all the attributes in the selection condition θ_0 involve only the attributes of one of the expressions (E_1) being joined.
 - $\sigma_{\theta_0}(E_1 \bowtie_{\theta} E_2) = (\sigma_{\theta_0}(E_1)) \bowtie_{\theta} E_2$ (b) It distributes when the selection condition θ_1 involves only

tes when the selection condition
$$\theta_1$$
 invo

the attributes of E_1 and θ_2 involves only the attributes of E_2 $\sigma_{\theta_1 \wedge \theta_2}(E_1 \bowtie_{\theta} E_2) = (\sigma_{\theta_1}(E_1)) \bowtie_{\theta} (\sigma_{\theta_2}(E_2))$

$$\sigma_{\theta_1 \wedge \theta_2}(E_1 \bowtie_{\theta} E_2) = (\sigma_{\theta_1}(E_1)) \bowtie_{\theta} (\sigma_{\theta_2}(E_2))$$
8. The projection operation distributes over the theta join.

(a) Let L_1 and L_2 be attributes of E_1 and E_2 respectively. Sup-

pose that the join condition
$$\theta$$
 involves only attributes in $L_1 \cup L_2$. Then
$$\Pi_{L_1 \cup L_2}(E_1 \bowtie_{\theta} E_2) = (\Pi_{L_1}(E_1)) \bowtie_{\theta} (\Pi_{L_2}(E_2))$$

(b) Consider a join
$$E_1 \bowtie_{\theta} E_2$$
. Let L_1 and L_2 be sets of attributes

from E_1 and E_2 respectively. Let L_3 be attributes of E_1 that are involved in the join condition θ , but are not in $L_1 \cup L_2$, and let L_4 be attributes of E_2 that are involved in the join condition θ , but are not in $L_1 \cup L_2$. Then

$$\Pi_{L_1 \cup L_2}(E_1 \bowtie_{\theta} E_2) = \Pi_{L_1 \cup L_2}((\Pi_{L_1 \cup L_3}(E_1)) \bowtie_{\theta} (\Pi_{L_2 \cup L_4}(E_2)))$$

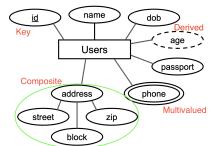
ER MODEL

Entity

- Objs that are distinguishable from other objs
- Entity set: Collection of ent. of the same type

Attribute

- Specific information describing an entity
- Key attr uniquely identifies each entity
- Composite attr composed of multiple other attributes
- Multivalued attr may consist of more than one value for a given entity
- Derived attr derived from other attributes



Relationship

Association among two or more entities

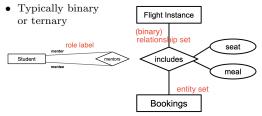
Relationship set

- Collection of relationships of the same type
- Can have their own attributes that further describe the relationship
- $Key(E_i)$ is the attributes of the selected key of entity set E_i

- Describes an entity set's participation
- Explicit role label only in case of ambiguities (e.g. same entity set participates in same relationship more than once)

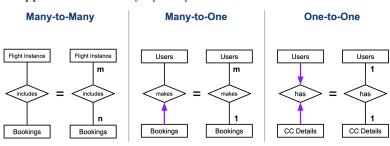
Degree

• An n-ary relationship set involves n entity roles, where n is the degree of the relationship set



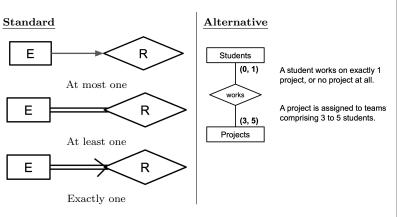
Cardinality constraints

• Upper bound for entity's participation



Participation constraints

- Lower bound for entity's participation
- Partial (default): participation not mandatory
- Total: mandatory (at least 1)



Implementation

Many-to-Many Represent relationship set with a table

Many-to-One

- 1. Represent relationship set between A and B with a table (A_{id}, B_{id}) . Make the ID of the total participation entity set the primary key, OR
- 2. Combine rel. set and total participiation entity set into one table

One-to-One

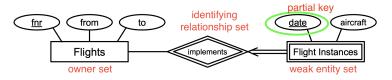
- 1. Represent relationship set between A and B with a table (A_{id}, B_{id}) . One is unique not null, and the other is the primary key, OR
- 2. Combine relationship set and either entity set into one table

Dependency constraints

Weak entity sets

- · Entity set that does not have its own key
- Can only be uniquely identified by considering primary key of owner entity
- · Existence depends on existence of owner entity

• Set of attributes of weak entity set that uniquely identifies a weak entity, for a given owner entity



Requirements

- · Many-to-one relationship from weak entity set to owner entity set
- Weak entity set must have total participation in identifying relationship

Relational mapping

- Entity set → table
- Composite/multivalued attributes:
 - Convert to single-valued attributes, OR
 - 2. Additional table with FK constraint, OR
 - 3. Convert to a single-valued attribute (e.g. comma separated string)

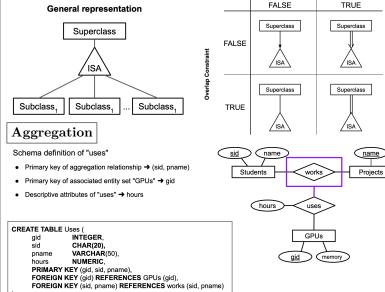
ISA Hierarchies

Used to model generalization/specialization of entity sets

Constraints

Overlap Can a superclass entity belong to multiple subclasses?

Covering Does a superclass entity have to belong to a subclass?



FUNCTIONS AND PROCEDURES

- Function CREATE OR REPLACE FUNCTION <name> (<param> <type>, ...) RETURNS <type> AS \$\$ <code> \$\$ LANGUAGE <sql | plpgsql>; - Procedure CREATE OR REPLACE PROCEDURE <name> (<param> <type>, ...) AS \$\$ <code>

\$\$ LANGUAGE <sql | plpgsql>;

- CREATE OR REPLACE helps to re-declare function/procedure if already previously defined
- Code is enclosed within \$\$
- Call a function: SELECT * FROM swap(2, 3);
- Call a procedure: CALT. transfer('Alice', 'Bob', 100):

Return	Type
Single tuple from table	<table_name></table_name>
Set of tuples from table	SET OF <table_name></table_name>
Single new tuple	RECORD
Set of new tuples	SET OF RECORD or
	TABLE(c VARCHAR, x INT)
No return value	VOID, or use PROCEDURE
	instead of FUNCTION
Trigger	TRIGGER

Variables

- DECLARE [<var> <type>] more when DECLARE keyword is present)
- <var> := <expr>

Selection

• IF ... THEN ... [ELSIF ... THEN ...] [ELSE ...] END IF (0 or more ELSIF)

Repetition

- LOOP ... END LOOP, and EXIT ... WHEN ... (conditional exit)
- WHILE ... LOOP ... END LOOP
- FOR ... IN ... LOOP ... END LOOP
- 1..10 (range, inclusive)

Block

- BEGIN ... END
- For plpgsql, code in the BEGIN-END block is in a transaction

Examples

Function

val2 := temp;

\$\$ LANGUAGE plpgsql;

Note: INOUT specifies that the param is both an input and output param

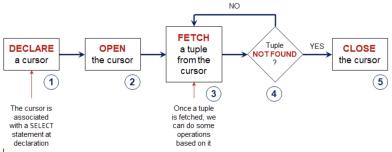
CREATE OR REPLACE FUNCTION swap(INOUT val1 INT, INOUT val2 INT) RETURNS RECORD AS \$\$ DECLARE temp INT; BEGIN temp := val1; val1 := val2;

Procedure

```
CREATE OR REPLACE PROCEDURE
    transfer(
 src TEXT, dst TEXT,
amt NUMERIC
) AS $$
 UPDATE Accounts
 SET balance = balance - amt
  WHERE name = src;
  UPDATE Accounts
 SET balance = balance + amt
  WHERE name = dst;
$$ LANGUAGE sql;
```

Cursor

- Declare, Open, Fetch, Check (repeat), Close
- FETCH [PRIOR | FIRST | LAST | ABSOLUTE n] [FROM] <cursor> INTO <var>



Question

Given the table "Scores" from before, write a function to perform the following task:

- 1. Sort the students in "Scores" in descending order of their Mark (break ties arbitrarily)
- For each student, compute the difference between his/her Mark and the Mark of the previous student
 - \circ If there is no previous student, use NULL

Solution

```
CREATE OR REPLACE FUNCTION score_gap()

RETURNS TABLE(name TEXT, mark INT, gap INT) AS $$

DECLARE

curs CURSOR FOR (SELECT * FROM Scores ORDER BY Mark DESC);

r RECORD; prev INT;

BEGIN

prev := -1; OPEN curs;

LOOP

FETCH curs INTO r;

EXIT HHEN NOT FOUND;

name := r.Name; mark := r.Mark;

IF prev >= 0 THEN gap := prev - mark;

ELSE gap := NULL;

END IF;

RETURN NEXT; -- insert into output

prev := r.mark;

END LOOP;

CLOSE curs;

END;

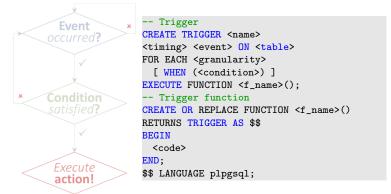
$$ LANGUAGE plpgsql;
```

Explanation

- 1. Declare a *cursor* associated with a SELECT statement
 or is a RECORD to store previous row
- Open the cursor which executes the SQL statement and let the cursor point to the beginning of the result
 Fetch a tuple from the cursor
- by reading the **next** tuple from the cursor by reading the **next** tuple from cursor and assign into the variable
- 4. If the FETCH operation did not get any tuple, the loop terminates
 - Otherwise, perform the **main operation** and insert into output
- 5. **Close** the cursor to release the resources allocated

TRIGGERS

Note: cannot CREATE OR REPLACE TRIGGER. Need to DROP TRIGGER



Trigger options

Events

- INSERT ON
- DELETE ON
- INSERT OR DELETE OR UPDATE ON
- Alternatively, use TG_OP variable.
 Is set to 'INSERT' | 'DELETE' | 'UPDATE'

Timings

- AFTER/BEFORE (after/before event)
- \bullet INSTEAD OF (replaces event, only for <code>VIEWS</code>)

Granularity

- FOR EACH ROW (for each tuple encountered)
- FOR EACH STATEMENT (for each statement)

Effect of return value

• OLD / NEW: Modified row before / after the triggering event

Events + Timings	NULL tuple	Non-NULL tuple t
BEFORE INSERT	No insertion	t is inserted
BEFORE UPDATE	No update	t is the updated tuple
BEFORE DELETE	No deletion	Deletion proceeds as normal
AFTER	No effect	No effect

Granularity

- In for each statement, doing return null will not do anything
- Need to use RAISE EXCEPTION to stop the operation

Trigger condition

- Use WHEN() for conditional check whether a trigger should run
- e.g. WHEN (NEW.StuName = 'Adi')

Usage

- No SELECT in WHEN()
- No NEW in WHEN() for DELETE
- No OLD in WHEN() for INSERT
- No WHEN() for INSTEAD OF

Deferred triggers

- $\bullet\,$ Triggers that are checked only at the end of a transaction
- CONSTRAINT + DEFERRABLE together indicate that trigger can be deferred
- Only works with AFTER and FOR EACH ROW
- Default is IMMEDIATE

```
CREATE CONSTRAINT TRIGGER <name>
AFTER <event> ON 
FOR EACH ROW
[ WHEN (<condition>) ]
[ DEFERRABLE INITIALLY [ DEFERRED | IMMEDIATE ] ]
EXECUTE FUNCTION <func_name>();
```

Multiple triggers

- Activation order for the same event on the same table:
- 1. BEFORE statement-level triggers
- 3. AFTER row-level triggers
- 2. BEFORE row-level triggers
- 4. AFTER statement-level triggers
- Within the same category, triggers are activated in alphabetical order
- If BEFORE row-level trigger returns NULL, then subsequent triggers on the same row are omitted

FUNCTIONAL DEPENDENCIES

Basic terminology

Reading FDs $X \to Y$ reads: X (functionally) determines $Y \mid Y$ is functionally dependent on $X \mid X$ implies Y (casual)

Instance An instance r (a table) of a relation R satisfies the FD $\sigma: X \to Y$ with $X \subset R$ and $Y \subset R$, \iff if two tuples of r agree on their X-values, then they agree on their Y-values

Valid instance An instance r of relation R is a valid instance of R with $\Sigma \iff$ it satisfies Σ

Violations An instance r of relation R violates a set of FDs $\Sigma \iff$ does not satisfy Σ

Holds

- A relation R with a set of FDs Σ , R with Σ , refers to the set of valid instances of R wrt. to the FDs in Σ
- When a set of FDs Σ holds on a relation R, only consider the valid instances of R with Σ

Trivial $X \to Y$ is trivial $\iff Y \subset X$

Non-trivial $X \to Y$ is non-trivial $\iff Y \not\subset X$

Completely non-trivial $X \to Y$ is completely non-trivial $\iff Y \neq \emptyset$ and $Y \cap X = \emptyset$

Key terminology

Superkey Let $S \subset R$ be a set of attributes of R. S is a superkey of $R \iff S \to R$

Candidate key A superkey such that no proper subset is also a superkey

Primary key Chosen candidate key, or the candidate key if there is only one

Prime attribute An attribute that appears in some candidate key of R with Σ . If not, then it is a non-prime attribute

FD terminology

Closure Let Σ be a set of FDs of a relation R. The closure of Σ , denoted Σ^+ , is the set of all FDs logically entailed by the FDs in Σ

Equivalence Two FDs are equivalent \iff have the same closure

Cover Σ_1 is a cover of Σ_2 (and vice versa) \iff their closure are equivalent

Closure of a set of attributes Let Σ be a set of FDs of a relation R. The closure of a set of attributes $S \subset R$, denoted S^+ , is the set of all attributes that are functionally dependent on S (i.e. what S implies)

$$S^{+} = \{ A \in R \mid \exists (S \to \{A\}) \in \Sigma^{+} \}$$

Computing attribute closures Check if any attribute doesn't appear in the RHS of any FD. These attributes must appear in the

 $\bullet\,$ Compute attribute closure starting with singular attributes. Then compute for 2 elements, 3 ele ments and so on. Note all candidate keys in the process

• If current set of attributes is a superset of some previously seen, candidate key, can skip Armstrong axioms

Reflexivity $\forall X, Y \subset R ((Y \subset X) \Rightarrow (X \to Y))$ Augmentation

when applied to Σ

$\forall X, Y, Z \subset R \left((X \to Y) \Rightarrow (X \cup Z \to Y \cup Z) \right)$ Transitivity

$\forall X, Y, Z \subset R \left((X \to Y) \land (Y \to Z) \Rightarrow (X \to Z) \right)$ Remarks • Sound: The rule only generates elements of Σ^+

Complete: The rule(s) generate(s) all elements of Σ^+ when applied to Σ The three inference rules are (individually) sound

- The Armstrong axioms are (together) sound and
- Additional rules Must be derived during exam Weak augmentation

If $X \to Y$, then $X \cup Z \to Y$

1. $X \to Y$ (given)

2. We know that $X \subset X \cup Z$

3. $X \cup Z \to X$ (reflexivity) 4. $X \cup Z \rightarrow Y$ (trans. of 3 and 1)

- Union If $X \to Y$ and $X \to Z$, then $X \to Y \cup Z$
- 1. $X \to Y$ (given) 2. $X \to Z$ (given)
- 3. $X \to X \cup Z$ (aug. 2 and X) 4. $X \cup Z \rightarrow Y \cup Z$ (aug. 1 and Z)
- 5. $X \to Y \cup Z$ (trans. of 3 and 4) Decomposition

If $X \to Y \cup Z$, then $X \to Y$ and $X \to Z$

1. $X \to Y \cup Z$ (given) 2. $Y \cup Z \rightarrow Y$ (reflexivity)

3. $X \to Y$ (trans. of 1 and 2)

Composition If $X \to Y$ and $A \to B$, then $X \cup A \to Y \cup B$

Proof

- 1. $X \to Y$ (given) 2. $A \to B$ (given)
- 3. $X \cup A \rightarrow Y \cup A$ (aug. 1 and A) 4. $X \cup A \rightarrow Y$ (decomp. of 3)

5. $X \cup A \rightarrow X \cup B$ (aug. 2 and X)

- 6. $X \cup A \rightarrow B$ (decomp. of 5)
- 7. $X \cup A \rightarrow Y \cup B$ (union 4 and 6)
- Pseudo-transitivity If $X \to Y$ and $Y \cup Z \to W$, then $X \cup Z \to W$

Proof

1. $X \to Y$ (given)

3. $X \cup Z \rightarrow Y \cup Z$ (aug. of 1 and Z)

4. $X \cup Z \rightarrow W$ (trans. of 3 and 2)

A relation R with a set of FDs Σ is in BCNF \iff 2. $Y \cup Z \to W$ (given) for every FD $X \to \{A\} \in \Sigma^+$,

- either $X \to \{A\}$ is trivial, or

A set Σ of FDs is minimal if and only if

Minimal cover

Definition

- RHS of each FD in Σ is minimal, i.e. each FD is
- of the form $X \to \{A\}$ • LHS of each FD in Σ is minimal, i.e. for every
- FD in Σ of the form $X \to \{A\}$, there is no FD $Y \to \{A\}$ such that $Y \subset X$ The set is minimal, i.e. no FD in Σ can be derived
- from other FDs in Σ

A minimal cover of a set of FDs Σ is a set of FDs Σ' that is both minimal and equivalent to Σ

- Every set of FDs has a minimal cover
- Algorithm 1. Simplify RHS of every FD (by splitting FDs so

that RHS of each FD is a singleton)

- Simplify LHS of every FD (for each FD, if a subset of LHS can imply RHS, then replace LHS with the subset)
- LHS. if this FD can be derived using only other FDs, then remove it) (If compact cover is desired) Combine FDs with

Remove redundant FDs (for each FD, start from

same LHS Reachability The algorithm always finds a minimal cover

To reach all minimal covers, the algorithm needs

computing Python

medicine

• Some minimal covers may be unreachable

to start from Σ^+

Anomalies userid domain faculty language department

pharmacy

tanh comp.sut.edu computer science tanh comp.sut.edu computer science med.sut.edu ami

a language

•	• Department \rightarrow faculty is a FD in this example
۱,	• Redundant storage: The faculty of a depart-
ment is repeated for every student of the depart-	
	ment, and every time the student is proficient in

• Update anomaly: When 2 rows of the table have the same value for the column department

but different values for the column faculty, vio-

- lating the FD • **Deletion anomaly**: If we delete the last row, we may forget that we have a department of pharmacy, and a faculty of medicine
- ${\bf Insertion\ anomaly:}\ {\bf We\ cannot\ record\ that\ the}$ department of social science exists and the faculty of liberal arts exists, because there is no student from this department or this faculty

• In all cases, the solution is to remove faculty from the original table, and create a new table with de-

- partment and faculty In the case of the update anomaly, to enforce the
- FD, we also need to make department the primary key of the new table Normalization

Normal forms Recognize designs that enforce FDs through main

SQL constraints (PK, unique, not null, FK)

• Protect data against anomalies Normalization

enforces FDs by means of the main SQL constraints

Boyce-Codd Normal Form

Transform (decompose) a poor design into one that

• X is a superkey

2. If some R_i is not in BCNF, then FALSE. Else Decomposition

Decomposition A decomposition of table R is

a set of tables $\{R_1, R_2, \cdots, R_n\}$ such that R =

A binary decomp is lossless-join ← full outer

A binary decomp of R into R₁ and R₂ is lossless-

• A decomp is lossless-join if there exists a sequence

of binary lossless-join decomp that generates that

join if $R = R_1 \cup R_2$ and either $R_1 \cap R_2 \to R_1$ or

natural join of its two fragments equal the initial

Binary decomposition Decomp with n=2

Check if decomp. set of relations is in BCNF 1. Compute attribute closures of the original set,

and project FDs to each relation R_i

Projected FDs A set Σ of projected FDs on R', from R with Σ where $R' \subset R$, is the set of FDs equivalent to the set of FDs $X \to Y$ in Σ^+ such that $X \subset R'$ and $Y \subset R'$ Dependency preserving A decomp of R with

 Σ into R_1, R_2, \dots, R_n with respective projected

FDs $\Sigma_1, \Sigma_2, \cdots, \Sigma_n$ is dependency preserving \iff

 $\Sigma^+ = (\Sigma_1 \cup \cdots \cup \Sigma_n)^+$ Check lossless-join

 $R_1 \cap R_2 \to R_2$

Terminology

 $R_1 \cup \cdots \cup R_n$

Lossless-join definitions

table. Otherwise it is lossy

1. Compute attribute closures of the original set 2. For some pair (R_i, R_j) , $i \neq j$,

- Check that $R_i \cap R_i \to R_i$ or $R_i \cap R_i \to R_i$ • If yes, then replace R_i, R_j with $R_i \cup R_j$ and repeat Step 2-3.
- If no, then try next pair 3. If there was a sequence of unions that resulted
 - in a single relation that has all attributes, then TRUE. Else FALSE
- Check dependency-preserving 1. Let R be the original set of relations. Can re-

place R with minimal cover if found. Let Y be the union of projected FDs to each relation

2. For each FD in R, check that we can derive it in

Can get different results depending on order of

Y. If some FD could not be derived, then that FD was not preserved, then FALSE. Else TRUE

Decomposition algorithm • Guarantees lossless decomp, but may not be dependency preserving

Let $X \to Y$ be a FD in Σ that violates the BCNF definition (not trivial, and X not superkey). Use it to decompose R into R_1 and R_2 :

FD chosen

 R₁ = X⁺ • $R_2 = (R - X^+) \cup X$

Then, check whether R_1 and R_2 with respective pro-

jected FDs Σ_1 and Σ_2 are in BCNF. Repeat decomp algo for the fragments which are not.

3NF Definition A relation R with a set of FDs Σ is in 3NF \iff

• $X \to \{A\}$ is trivial, or X is a superkey, or

for every FD $X \to \{A\} \in \Sigma^+$,

- A is a prime attribute Note that BCNF implies 3NF
- 3NF Synthesis Guarantees a lossless, dependency preserving de-

comp in 3NF • For each FD $X \to Y$ in the compact minimal

- cover, create a relation $R_i = \overline{X \cup Y}$ unless it already exists, or is subsumed by another relation
- If none of the created relations contains one of the keys, pick a candidate key and create a relation with that candidate key