

CSE 12: PA8

3-3-21

Focus: PA8, Heaps, and
Dijkstra's Algorithm

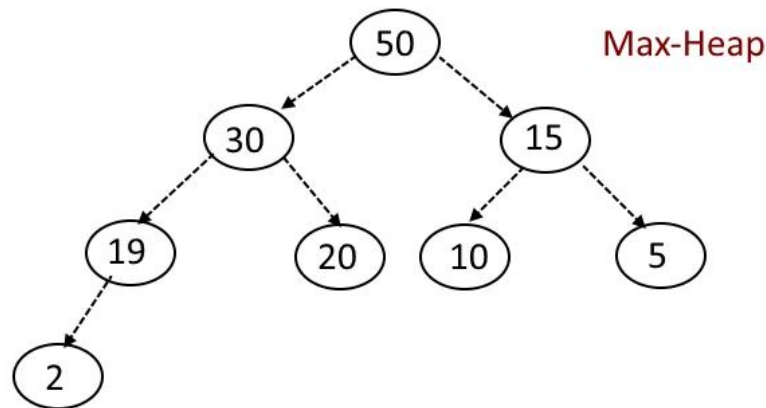
Overview of PA8

- Part I: An Implementation of Heap
 - Create a new file named Heap.java
 - All method headers and descriptions are given in the writeup. You will have to do the whole file from scratch!
 - Make sure to implement the PriorityQueue.java interface methods
- Part II: Implementation of MazeSolver
 - Utilize your heap based PriorityQueue to implement Dijkstra's Algorithm and solve a maze via the shortest path.

Heaps and Priority Queues

Heaps

- A heap is a **complete** tree
 - Every level is full except possibly the last, and all nodes are as far left as possible.
- Implemented with a list
- min/max heap



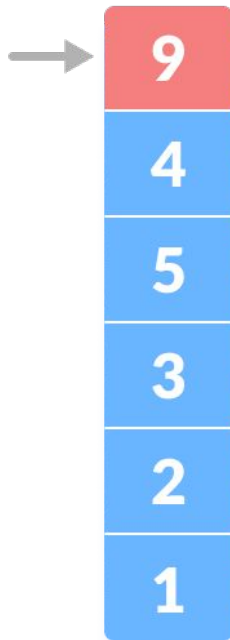
| | | | | | | | | |
|---|----|----|----|----|----|----|---|---|
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| | 50 | 30 | 15 | 19 | 20 | 10 | 5 | 2 |

for Node at i : Left child will be $2i$ and right child will be at $2i+1$ and parent node will be at $[i/2]$.

Priority Queues

- Similar to a queue in the sense that we are adding/removing from the same location each time. However, now there is an order that is based on a priority value
- Methods
 - `poll()`
 - `add()`
 - `peek()`
 - `toArray()`
 - `isEmpty()`

Element with the
highest priority



Heaps vs Priority Queues

Heap is a **Data Structure**

Priority Queue is an **Abstract Data Type (ADT)**

Heaps are the most popular way to implement a Priority Queue because they are efficient at finding the largest or smallest values (the priority). In fact, many times when people refer to a priority queue they are referring to a heap!

You will be creating a Heap class however you will use the Priority Queue interface provided.

What about the helper methods?

Bubble Down

- Used for deleting an element from the heap
- Take last element of heap and put it at the index of the element to be deleted
- Check and Swap
 - a. Min-heap: if replaced element $>$ any child node, swap element with the child that is smaller
 - b. Max-heap: if replaced element $<$ any child node, swap element with the child that is greater
- Keep repeating till conditions are not met

Bubble Up

- Used for inserting an element into the heap
- Insert element at the last leaf of the tree
- Check and Swap
 - a. Min-heap: if inserted element $<$ parent node, swap element with parent node
 - b. Max-heap: if inserted element $>$ parent node, swap element with parent node
- Keep repeating till the inserted element is in place
- <http://btv.melezinek.cz/binary-heap.html>

Dijkstra's Algorithm

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
                add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- Create a new heap (pq)
- Push <0, s8> into the pq

TOP

<0, s8>

BOTTOM

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

| square | V | P | RC |
|--------|---|-----|-----|
| s0 | | | inf |
| s1 | | | inf |
| s2 | | | inf |
| s3 | | | inf |
| s4 | | | inf |
| s5 | | | inf |
| s6 | | | inf |
| s7 | | | inf |
| s8 | | --- | inf |
| s11 | | | inf |
| s12 | | | inf |
| s13 | | | inf |
| s14 | | | inf |
| s15 | | | inf |

- Remove the first element of the pq (s8)
- Mark it as visited

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

| <u>square</u> | <u>V</u> | <u>P</u> | <u>RC</u> |
|---------------|----------|----------|-----------|
| s0 | | | inf |
| s1 | | | inf |
| s2 | | | inf |
| s3 | | | inf |
| s4 | | | inf |
| s5 | | | inf |
| s6 | | | inf |
| s7 | | | inf |
| s8 | true | --- | inf |
| s11 | | | inf |
| s12 | | | inf |
| s13 | | | inf |
| s14 | | | inf |
| s15 | | | inf |

BOTTOM

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
                add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- s8 neighbors: s4, s12, s9
- Neighbors to consider: s4, s12 (s9 is a wall)
- For s4, s12
 - o calculate runningCost by adding current's key + s4/s12 cost
 - o If calculated runningCost is less than current runningCost
 - Set previous to s8
 - update runningCost
 - Push <14, s4>, <1, s12>

TOP

| | | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|
| <1, s12> | <14, s4> | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

BOTTOM

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | | | inf |
| s1 | | | inf |
| s2 | | | inf |
| s3 | | | inf |
| s4 | | s8 | 14 |
| s5 | | | inf |
| s6 | | | inf |
| s7 | | | inf |
| s8 | true | --- | inf |
| s11 | | | inf |
| s12 | | s8 | 1 |
| s13 | | | inf |
| s14 | | | inf |
| s15 | | | inf |

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
            add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- Remove the first element of the pq (s12)
- Mark it as visited

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | | | inf |
| s1 | | | inf |
| s2 | | | inf |
| s3 | | | inf |
| s4 | | s8 | 14 |
| s5 | | | inf |
| s6 | | | inf |
| s7 | | | inf |
| s8 | true | --- | inf |
| s11 | | | inf |
| s12 | true | s8 | 1 |
| s13 | | | inf |
| s14 | | | inf |
| s15 | | | inf |

TOP

<14, s4>

BOTTOM

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
                add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- s12 neighbors: s8, s13
- Neighbors to consider: s13 (s8 is visited)
- For s13
 - o calculate runningCost by adding current's key + s13 cost,
 - o If calculated runningCost is less than current runningCost
 - Set previous to s12
 - update runningCost
 - Push <4, s13>

TOP

| | | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|
| <4, s13> | <14, s4> | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

BOTTOM

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | | | inf |
| s1 | | | inf |
| s2 | | | inf |
| s3 | | | inf |
| s4 | | s8 | 14 |
| s5 | | | inf |
| s6 | | | inf |
| s7 | | | inf |
| s8 | true | --- | inf |
| s11 | | | inf |
| s12 | true | s8 | 1 |
| s13 | | s12 | 4 |
| s14 | | | inf |
| s15 | | | inf |

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
            add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- Remove the first element of the pq (s13)
- Mark it as visited

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | | | inf |
| s1 | | | inf |
| s2 | | | inf |
| s3 | | | inf |
| s4 | | s8 | 14 |
| s5 | | | inf |
| s6 | | | inf |
| s7 | | | inf |
| s8 | true | --- | inf |
| s11 | | | inf |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | | | inf |
| s15 | | | inf |

TOP

<14, s4>

BOTTOM


```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
                add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- s13 neighbors: s12, s9, s14
- Neighbors to consider: s14 (s12 is visited, s9 is a wall)
- For s14
 - o calculate runningCost by adding current's key + s14 cost,
 - o If calculated runningCost is less than current runningCost
 - Set previous to s13
 - update runningCost
 - Push <5, s14>

| TOP | | | | | | | | BOTTOM | |
|----------|----------|--|--|--|--|--|--|--------|--|
| <5, s14> | <14, s4> | | | | | | | | |

BOTTOM

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

| <u>square</u> | <u>V</u> | <u>P</u> | <u>RC</u> |
|---------------|----------|----------|-----------|
| s0 | | | inf |
| s1 | | | inf |
| s2 | | | inf |
| s3 | | | inf |
| s4 | | s8 | 14 |
| s5 | | | inf |
| s6 | | | inf |
| s7 | | | inf |
| s8 | true | --- | inf |
| s11 | | | inf |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | | s13 | 5 |
| s15 | | | inf |

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
            add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- Remove the first element of the pq (s14)
- Mark it as visited

TOP

<14, s4>

BOTTOM

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | | | inf |
| s1 | | | inf |
| s2 | | | inf |
| s3 | | | inf |
| s4 | | s8 | 14 |
| s5 | | | inf |
| s6 | | | inf |
| s7 | | | inf |
| s8 | true | --- | inf |
| s11 | | | inf |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | | | inf |

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
                add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- s14 neighbors: s13, s10, s15
- Neighbors to consider: s15 (s13 is visited, s10 is a wall)
- For s15
 - o calculate runningCost by adding current's key + s15 cost,
 - o If calculated runningCost is less than current runningCost
 - Set previous to s14
 - update runningCost
 - Push <7, s15>

TOP

| | | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|
| <7, s15> | <14, s4> | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

BOTTOM

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | | | inf |
| s1 | | | inf |
| s2 | | | inf |
| s3 | | | inf |
| s4 | | s8 | 14 |
| s5 | | | inf |
| s6 | | | inf |
| s7 | | | inf |
| s8 | true | --- | inf |
| s11 | | | inf |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | | s14 | 7 |

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
            add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- Remove the first element of the pq (s15)
- Mark it as visited

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | | | inf |
| s1 | | | inf |
| s2 | | | inf |
| s3 | | | inf |
| s4 | | s8 | 14 |
| s5 | | | inf |
| s6 | | | inf |
| s7 | | | inf |
| s8 | true | --- | inf |
| s11 | | | inf |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | true | s14 | 7 |

TOP

<14, s4>

BOTTOM

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
                add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- s15 neighbors: s14, s11
- Neighbors to consider: s11 (s14 is visited)
- For s11
 - o calculate runningCost by adding current's key + s11 cost,
 - o If calculated runningCost is less than current runningCost
 - Set previous to s15
 - update runningCost
 - Push <9, s11>

TOP

| | | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|
| <9, s11> | <14, s4> | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|

BOTTOM

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | | | inf |
| s1 | | | inf |
| s2 | | | inf |
| s3 | | | inf |
| s4 | | s8 | 14 |
| s5 | | | inf |
| s6 | | | inf |
| s7 | | | inf |
| s8 | true | --- | inf |
| s11 | | s15 | 9 |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | true | s14 | 7 |

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
            add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- Remove the first element of the pq (s11)
- Mark it as visited

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | | | inf |
| s1 | | | inf |
| s2 | | | inf |
| s3 | | | inf |
| s4 | | s8 | 14 |
| s5 | | | inf |
| s6 | | | inf |
| s7 | | | inf |
| s8 | true | --- | inf |
| s11 | true | s15 | 9 |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | true | s14 | 7 |

TOP

<14, s4>

BOTTOM

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
            add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- s11 neighbors: s10, s7, s15
- Neighbors to consider: s7(s10 is a wall, s15 is visited)
- For s7
 - o calculate runningCost by adding current's key + s7 cost,
 - o If calculated runningCost is less than current runningCost
 - Set previous to s11
 - update runningCost
 - Push <18, s7>

TOP

| | | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|
| <14, s4> | <18, s7> | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

BOTTOM

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | | | inf |
| s1 | | | inf |
| s2 | | | inf |
| s3 | | | inf |
| s4 | | s8 | 14 |
| s5 | | | inf |
| s6 | | | inf |
| s7 | | s11 | 18 |
| s8 | true | --- | inf |
| s11 | true | s15 | 9 |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | true | s14 | 7 |

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
            add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- Remove the first element of the pq (s4)
- Mark it as visited

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | | | inf |
| s1 | | | inf |
| s2 | | | inf |
| s3 | | | inf |
| s4 | true | s8 | 14 |
| s5 | | | inf |
| s6 | | | inf |
| s7 | | s11 | 18 |
| s8 | true | --- | inf |
| s11 | true | s15 | 9 |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | true | s14 | 7 |

TOP

<18, s7>

BOTTOM


```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
                add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- s4 neighbors: s0, s5, s8
- Neighbors to consider: s0, s5 (s8 is visited)
- For s0, s5
 - o calculate runningCost by adding current's key + s0/s5 cost
 - o If calculated runningCost is less than current runningCost
 - Set previous to s4
 - update runningCost
 - Push <15, s0>, <20, s5>

TOP

| | | | | | | | | | |
|----------|----------|----------|--|--|--|--|--|--|--|
| <15, s0> | <18, s7> | <20, s5> | | | | | | | |
|----------|----------|----------|--|--|--|--|--|--|--|

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

BOTTOM

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | | s4 | 15 |
| s1 | | | inf |
| s2 | | | inf |
| s3 | | | inf |
| s4 | true | s8 | 14 |
| s5 | | s4 | 20 |
| s6 | | | inf |
| s7 | | s11 | 18 |
| s8 | true | --- | inf |
| s11 | true | s15 | 9 |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | true | s14 | 7 |

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
            add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- Remove the first element of the pq (s0)
- Mark it as visited

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | true | s4 | 15 |
| s1 | | | inf |
| s2 | | | inf |
| s3 | | | inf |
| s4 | true | s8 | 14 |
| s5 | | s4 | 20 |
| s6 | | | inf |
| s7 | | s11 | 18 |
| s8 | true | --- | inf |
| s11 | true | s15 | 9 |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | true | s14 | 7 |

TOP

BOTTOM

| | | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|
| <18, s7> | <20, s5> | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
                add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- s0 neighbors: s1, s4
- Neighbors to consider: s1 (s4 is visited)
- For s1
 - o calculate runningCost by adding current's key + s1 cost
 - o If calculated runningCost is less than current runningCost
 - Set previous to s0
 - update runningCost
 - Push <16, s1>

TOP

| | | | | | | | | | |
|----------|----------|----------|--|--|--|--|--|--|--|
| <16, s1> | <18, s7> | <20, s5> | | | | | | | |
|----------|----------|----------|--|--|--|--|--|--|--|

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

BOTTOM

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | true | s4 | 15 |
| s1 | | s0 | 16 |
| s2 | | | inf |
| s3 | | | inf |
| s4 | true | s8 | 14 |
| s5 | | s4 | 20 |
| s6 | | | inf |
| s7 | | s11 | 18 |
| s8 | true | --- | inf |
| s11 | true | s15 | 9 |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | true | s14 | 7 |

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
            add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- Remove the first element of the pq (s1)
- Mark it as visited

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | true | s4 | 15 |
| s1 | true | s0 | 16 |
| s2 | | | inf |
| s3 | | | inf |
| s4 | true | s8 | 14 |
| s5 | | s4 | 20 |
| s6 | | | inf |
| s7 | | s11 | 18 |
| s8 | true | --- | inf |
| s11 | true | s15 | 9 |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | true | s14 | 7 |

TOP

BOTTOM

| | | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|
| <18, s7> | <20, s5> | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
                add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- s1 neighbors: s0, s2, s5
- Neighbors to consider: s2, s5 (s0 is visited)
- For s2, s5
 - o calculate runningCost by adding current's key + s2/s5 cost
 - o If calculated runningCost is less than current runningCost
 - Set previous to s1
 - update runningCost
 - Push <17, s2>, <22, s5>

TOP

| | | | | | | | | | |
|----------|----------|----------|--|--|--|--|--|--|--|
| <17, s2> | <18, s7> | <20, s5> | | | | | | | |
|----------|----------|----------|--|--|--|--|--|--|--|

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

BOTTOM

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | true | s4 | 15 |
| s1 | true | s0 | 16 |
| s2 | | s1 | 17 |
| s3 | | | inf |
| s4 | true | s8 | 14 |
| s5 | | s4 | 20 |
| s6 | | | inf |
| s7 | | s11 | 18 |
| s8 | true | --- | inf |
| s11 | true | s15 | 9 |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | true | s14 | 7 |

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
            add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- Remove the first element of the pq (s2)
- Mark it as visited

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | true | s4 | 15 |
| s1 | true | s0 | 16 |
| s2 | true | s1 | 17 |
| s3 | | | inf |
| s4 | true | s8 | 14 |
| s5 | | s4 | 20 |
| s6 | | | inf |
| s7 | | s11 | 18 |
| s8 | true | --- | inf |
| s11 | true | s15 | 9 |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | true | s14 | 7 |

TOP

BOTTOM

| | | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|
| <18, s7> | <20, s5> | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
                add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- s2 neighbors: s1, s3, s6
- Neighbors to consider: s3, s6 (s1 is visited)
- For s3, s6
 - o calculate runningCost by adding current's key + s3/s6 cost
 - o If calculated runningCost is less than current runningCost
 - Set previous to s2
 - update runningCost
 - Push <18, s3>, <20, s6>

TOP

| | | | | | | | | | |
|----------|----------|----------|----------|--|--|--|--|--|--|
| <18, s3> | <18, s7> | <20, s6> | <20, s5> | | | | | | |
|----------|----------|----------|----------|--|--|--|--|--|--|

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

BOTTOM

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | true | s4 | 15 |
| s1 | true | s0 | 16 |
| s2 | true | s1 | 17 |
| s3 | | s2 | 18 |
| s4 | true | s8 | 14 |
| s5 | | s4 | 20 |
| s6 | | s2 | 20 |
| s7 | | s11 | 18 |
| s8 | true | --- | inf |
| s11 | true | s15 | 9 |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | true | s14 | 7 |

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
            add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- Remove the first element of the pq (s3)
- Mark it as visited

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | true | s4 | 15 |
| s1 | true | s0 | 16 |
| s2 | true | s1 | 17 |
| s3 | true | s2 | 18 |
| s4 | true | s8 | 14 |
| s5 | | s4 | 20 |
| s6 | | s2 | 20 |
| s7 | | s11 | 18 |
| s8 | true | --- | inf |
| s11 | true | s15 | 9 |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | true | s14 | 7 |

TOP

BOTTOM

| | | | | | | | | | |
|----------|----------|----------|--|--|--|--|--|--|--|
| <18, s7> | <20, s6> | <20, s5> | | | | | | | |
|----------|----------|----------|--|--|--|--|--|--|--|


```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
            add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- s3 neighbors: s2, s7
- Neighbors to consider: s7 (s2 is visited)
- For s7
 - o calculate runningCost by adding current's key + s7 cost
 - o If calculated runningCost is less than current runningCost
 - Set previous to s3
 - update runningCost
 - Push <27, s7>

TOP

| | | | | | | | | | |
|----------|----------|----------|--|--|--|--|--|--|--|
| <18, s7> | <20, s6> | <20, s5> | | | | | | | |
|----------|----------|----------|--|--|--|--|--|--|--|

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

BOTTOM

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | true | s4 | 15 |
| s1 | true | s0 | 16 |
| s2 | true | s1 | 17 |
| s3 | true | s2 | 18 |
| s4 | true | s8 | 14 |
| s5 | | s4 | 20 |
| s6 | | s2 | 20 |
| s7 | | s11 | 18 |
| s8 | true | --- | inf |
| s11 | true | s15 | 9 |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | true | s14 | 7 |

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
            add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- Remove the first element of the pq (s7)
- Mark it as visited

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | true | s4 | 15 |
| s1 | true | s0 | 16 |
| s2 | true | s1 | 17 |
| s3 | true | s2 | 18 |
| s4 | true | s8 | 14 |
| s5 | | s4 | 20 |
| s6 | | s2 | 20 |
| s7 | true | s11 | 18 |
| s8 | true | --- | inf |
| s11 | true | s15 | 9 |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | true | s14 | 7 |

TOP

BOTTOM

| | | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|
| <20, s6> | <20, s5> | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|

```

initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pq is not empty:
    let current = remove the first entry from pq (poll)
    let currentSquare = current's value
    Mark currentSquare as visited
    if currentSquare is the finishing square
        return currentSquare
    else
        for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
            add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- s7 neighbors: s6, s3, s11
- Neighbors to consider: s6 (s3, s11 are visited)
- For s6
 - o calculate runningCost by adding current's key + s6 cost
 - o If calculated runningCost is less than current runningCost
 - Set previous to s7
 - update runningCost
 - Push <21, s6>

TOP

| | | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|
| <20, s6> | <20, s5> | | | | | | | | |
|----------|----------|--|--|--|--|--|--|--|--|

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

BOTTOM

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | true | s4 | 15 |
| s1 | true | s0 | 16 |
| s2 | true | s1 | 17 |
| s3 | true | s2 | 18 |
| s4 | true | s8 | 14 |
| s5 | | s4 | 20 |
| s6 | | s2 | 20 |
| s7 | true | s11 | 18 |
| s8 | true | --- | inf |
| s11 | true | s15 | 9 |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | true | s14 | 7 |

```

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                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
            add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- Remove the first element of the pq (s6)
- Mark it as visited

TOP

<20, s5>

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

BOTTOM

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | true | s4 | 15 |
| s1 | true | s0 | 16 |
| s2 | true | s1 | 17 |
| s3 | true | s2 | 18 |
| s4 | true | s8 | 14 |
| s5 | | s4 | 20 |
| s6 | true | s2 | 20 |
| s7 | true | s11 | 18 |
| s8 | true | --- | inf |
| s11 | true | s15 | 9 |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | true | s14 | 7 |

```

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                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
            add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)

```

- Return finish square

TOP

<20, s5>

BOTTOM

| | | | |
|-----|-----|-----|-----|
| s0 | s1 | s2 | s3 |
| s4 | s5 | s6 | s7 |
| s8 | s9 | s10 | s11 |
| s12 | s13 | s14 | s15 |

| | | | |
|----|---|---|---|
| 1 | 1 | 1 | 1 |
| 14 | 6 | 3 | 9 |
| 0 | 0 | 0 | 2 |
| 1 | 3 | 1 | 2 |

| square | V | P | RC |
|--------|------|-----|-----|
| s0 | true | s4 | 15 |
| s1 | true | s0 | 16 |
| s2 | true | s1 | 17 |
| s3 | true | s2 | 18 |
| s4 | true | s8 | 14 |
| s5 | | s4 | 20 |
| s6 | true | s2 | 20 |
| s7 | true | s11 | 18 |
| s8 | true | --- | inf |
| s11 | true | s15 | 9 |
| s12 | true | s8 | 1 |
| s13 | true | s12 | 4 |
| s14 | true | s13 | 5 |
| s15 | true | s14 | 7 |