CSE 12: PA8

3-3-21

Focus: PA8, Heaps, and

Dijkstra's Algorithm

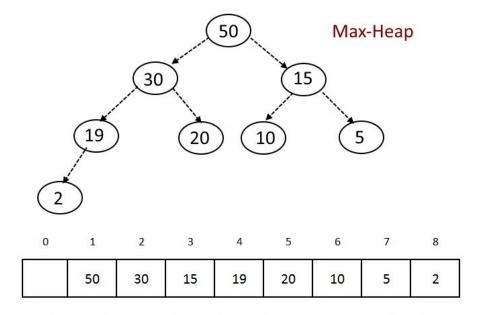
Overview of PA8

- Part I: An Implementation of Heap
 - Create a new file named Heap.java
 - All method headers and descriptions are given in the writeup. You will have to do the whole file from scratch!
 - Make sure to implement the PriorityQueue.java interface methods
- Part II: Implementation of MazeSolver
 - Utilize your heap based PriorityQueue to implement Dijkstra's Algorithm and solve a maze via the shortest path.

Heaps and Priority Queues

Heaps

- A heap is a complete tree
 - Every level is full except possibly the last, and all nodes are as far left as possible.
- Implemented with a list
- min/max heap



for Node at i: Left child will be 2i and right child will be at 2i+1 and parent node will be at [i/2].

Priority Queues

Element with the highest priority

9

4

5

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- Similar to a queue in the sense that we are adding/removing from the same location each time. However, now there is an order that is based on a priority value
- Methods
 - poll()
 - o add()
 - o peek()
 - o toArray()
 - o isEmpty()

Heaps vs Priority Queues

Heap is a **Data Structure**

Priority Queue is an Abstract Data Type (ADT)

Heaps are the most popular way to implement a Priority Queue because they efficient at finding the largest or smallest values (the priority). In fact, many times when people refer to a priority queue they are referring to a heap!

You will be creating a Heap class however you will use the Priority Queue interface provided.

What about the helper methods?

Bubble Down

- Used for deleting an element from the heap
- Take last element of heap and put it at the index of the element to be deleted
- Check and Swap
 - Min-heap: if replaced element > any child node, swap element
 with the child that is smaller
 - b. Max-heap: if replaced element < any child node, swap element with the child that is greater
- Keep repeating till conditions are not met

Bubble Up

- Used for inserting an element into the heap
- Insert element at the last leaf of the tree
- Check and Swap
 - Min-heap: if inserted element < parent node, swap element with parent node
 - b. Max-heap: if inserted element > parent node, swap element with parent node
- Keep repeating till the inserted element is in place
- http://btv.melezinek.cz/binary-heap.html

Dijkstra's Algorithm

```
initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pg is not empty:
     let current = remove the first entry from pq (poll)
     let currentSquare = current's value
     Mark currentSquare as visited
     if currentSquare is the finishing square
         return currentSquare
     else
         for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
                add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)
```

s0	s1	s2	s3
s4	s5	s6	s7
s8	s9	s10	s11
s12	s13	s14	s15

<u>square</u>	<u>v</u>	<u>P</u>	<u>RC</u>
s0			inf
s1			inf
s2			inf
s3			inf
s4			inf
s5			inf
s6			inf
s7			inf
s8			inf
s11			inf
s12			inf
s13			inf
s14			inf
s15			inf

- Create a new heap (pq)
- Push <0, s8> into the pq

TOP					BOTTOM
<0, s8>					

```
initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pg is not empty:
     let current = remove the first entry from pq (poll)
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     Mark currentSquare as visited
     if currentSquare is the finishing square
         return currentSquare
     else
         for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
               add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)
```

s0	s1	s2	s3
s4	s5	s6	s7
s8	s9	s10	s11
s12	s13	s14	s15

<u>square</u>	<u>v</u>	<u>P</u>	<u>RC</u>
s0			inf
s1			inf
s2			inf
s3			inf
s4			inf
s5			inf
s6			inf
s7			inf
s8	true		inf
s11			inf
s12			inf
s13			inf
s14			inf
s15			inf

- Remove the first element of the pq (s8)
- Mark it as visited

TOP					BOTTOM

initialize pq to be a new empty heap add the start square's cost as the key and the start square itself as the value to pq while pg is not empty: let current = remove the first entry from pq (poll) let currentSquare = current's value Mark currentSquare as visited if currentSquare is the finishing square return currentSquare else for each neighbor of currentSquare that isn't a wall and isn't visited let currentCost = current's key plus the neighbors cost if currentCost is less than neighbor's runningCost set the previous of the neighbor to currentSquare set the neighbors runningCost to currentCost

-	s8	neigh	bors:	s4,	s12,	s9

if the loop ended, return null (no path found)

- Neighbors to consider: s4, s12 (s9 is a wall)
- For s4, s12
 - calculate runningCost by adding current's key + s4/s12 cost

add the currentCost as key and neighbor as value to the pq (add)

- If calculated runningCost is less than current runningCost
 - Set previous to s8
 - update runningCost
 - Push <14, s4>, <1, s12>

s0	s1	s2	s3	<u>square</u>			
	<u> </u>	<u> </u>		s0			
s4	s5	s6	s7	s1			
s8	s9	s10	s11	s2			
				s3			
s12	s13	s14	s15	s4			
				s5			
1	1	1	1	s6			
14	6	3	9	s7			
	Ü		ŭ	s8			
0	0	0	2	s11			
1	3	1	2	s12			
	ВОТТОМ						
				s14			

ı				
	s 2			inf
	s3			inf
	s4		s8	14
	s 5			inf
	s6			inf
	s7			inf
	s8	true	ł	inf
	s11			inf
	s12		s8	1
	s13			inf
	s14			inf
	s15			inf

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RC

inf

inf

TOP					BOTTOM
<1, s12>	<14, s4>				

```
initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pg is not empty:
     let current = remove the first entry from pq (poll)
     let currentSquare = current's value
     Mark currentSquare as visited
     if currentSquare is the finishing square
         return currentSquare
     else
         for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
               add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)
```

s0	s1	s2	s3
s4	s5	s6	s7
s8	s9	s10	s11
s12	s13	s14	s15

<u>square</u>	<u>v</u>	<u>P</u>	<u>RC</u>
s0			inf
s1			inf
s2			inf
s3			inf
s4		s8	14
s5			inf
s6			inf
s7			inf
s8	true		inf
s11			inf
s12	true	s8	1
s13			inf
s14			inf
s15			inf

- Remove the first element of the pq (s12)
- Mark it as visited

TOP									BOTTOM
<14, s4>									

initialize pq to be a new empty heap add the start square's cost as the key and the start square itself as the value to pq while pg is not empty: let current = remove the first entry from pq (poll) let currentSquare = current's value Mark currentSquare as visited if currentSquare is the finishing square return currentSquare else for ea if the loop end

a	ch n	eighl	bor	of	curre	entSq	uare	that	isn'	t a	wall	and	is	n't	vis	ited
t	cur	rent	Cost	=	curre	ent's	key	plus	the	nei	ghbor	s co	st			
(curr	entC	ost	is	less	than	nei	ghbor	's ru	ınni	ngCos	t				
	set	the	pre	evic	us of	f the	nei	ghbor	to o	curr	entSq	uare				
	set	the	nei	ighb	ors	runni	ngCos	st to	curi	ent	Cost					
	add	the	cur	rer	tCost	t as	key a	and ne	eighb	or	as va	lue	to	the	pq	(add)
d	ed,	retu	rn r	nu11	. (no	path	four	nd)								

- s12 neighbors: s8, s13
- Neighbors to consider: s13 (s8 is visited)
- For s13
 - calculate runningCost by adding current's key + s13 cost,
 - If calculated runningCost is less than current runningCost
 - Set previous to s12
 - update runningCost
 - Push <4, s13>

	s0	s1		s2		s3	-		
	s4	s5	<u>,</u>	s6		s7	-		
	s8	sS)	s10		s11			
S	12	s1:	3	s14		s15	-		
	1	1		1		1			
	14	6		3		9			
	0	0		0		2			
	1	3		1		2			
BOTTOM									

1				
-	s0			inf
	s1			inf
	s2			inf
1	s3			inf
	s4		s8	14
_	s5			inf
	s6			inf
1	s7			inf
4	s8	true		inf
	s11			inf
1	s12	true	s8	1
_	s13		s12	4
	s14			inf
	s15			inf

square

TOP					BOTTOM
<4, s13>	<14, s4>				

```
initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pg is not empty:
     let current = remove the first entry from pq (poll)
     let currentSquare = current's value
     Mark currentSquare as visited
     if currentSquare is the finishing square
         return currentSquare
     else
         for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
               add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)
```

s0	s1	s2	s3
s4	s5	s6	s7
s8	s 9	s10	s11
s12	s13	s14	s15

<u>square</u>	<u>v</u>	<u>P</u>	<u>RC</u>
s0			inf
s1			inf
s2			inf
s3			inf
s4		s8	14
s5			inf
s6			inf
s7			inf
s8	true		inf
s11			inf
s12	true	s8	1
s13	true	s12	4
s14			inf
s15			inf

- Remove the first element of the pq (s13)
- Mark it as visited

TOP					BOTTOM
<14, s4>					

initialize pq to be a new empty heap add the start square's cost as the key and the start square itself as the value to pq while pg is not empty: let current = remove the first entry from pq (poll) let currentSquare = current's value Mark currentSquare as visited if currentSquare is the finishing square return currentSquare else for each neighbor of currentSquare that isn't a wall and isn't visited let currentCost = current's key plus the neighbors cost if currentCost is less than neighbor's runningCost set the previous of the neighbor to currentSquare set the neighbors runningCost to currentCost add the currentCost as key and neighbor as value to the pq (add) if the loop ended, return null (no path found)

-	s13 neighbors:	s12, s9, s14
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- Neighbors to consider: s14 (s12 is visited, s9 is a wall)
- For s14
 - o calculate runningCost by adding current's key + s14 cost,
 - If calculated runningCost is less than current runningCost
 - Set previous to s13
 - update runningCost
 - Push <5, s14>

	s0	s1	s2	s3						
	s4	s5	s6	s7						
	s8	s9	s10	s11						
5	s12	s13	s14	s15						
	1	1	1	1						
	14	6	3	9						
	0	0	0	2						
	1	3	1	2						
L	ВОТТОМ									
	1	1		I						

	square	<u>v</u>	<u>P</u>	<u>RC</u>
+	s0			inf
	s1			inf
	s2			inf
┨	s3			inf
	s4		s8	14
_	s5			inf
	s6			inf
1	s7			inf
4	s8	true		inf
	s11			inf
1	s12	true	s8	1
 	s13	true	s12	4
-	s14		s13	5
	s15			inf

TOP					 BOTTOM
<5, s14>	<14, s4>				

```
initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pg is not empty:
     let current = remove the first entry from pq (poll)
     let currentSquare = current's value
     Mark currentSquare as visited
     if currentSquare is the finishing square
         return currentSquare
     else
         for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
               add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)
```

s0	s1	s2	s3
s4	s5	s6	s7
s8	s 9	s10	s11
s12	s13	s14	s15

<u>square</u>	<u>V</u>	<u>P</u>	<u>RC</u>
s0			inf
s1			inf
s2			inf
s3			inf
s4		s8	14
s5			inf
s6			inf
s7			inf
s8	true		inf
s11			inf
s12	true	s8	1
s13	true	s12	4
s14	true	s13	5
s15			inf

- Remove the first element of the pq (s14)
- Mark it as visited

TOP					BOTTOM
<14, s4>					

initialize pq to be a new empty heap add the start square's cost as the key and the start square itself as the value to pq while pg is not empty: let current = remove the first entry from pq (poll) let currentSquare = current's value Mark currentSquare as visited if currentSquare is the finishing square return currentSquare else for each neighbor of currentSquare that isn't a wall and isn't visited let currentCost = current's key plus the neighbors cost if currentCost is less than neighbor's runningCost set the previous of the neighbor to currentSquare set the neighbors runningCost to currentCost add the currentCost as key and neighbor as value to the pq (add) if the loop ended, return null (no path found)

-	s14 neighbors:	s13, s10, s15
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- Neighbors to consider: s15 (s13 is visited, s10 is a wall)
- For s15
 - calculate runningCost by adding current's key + s15 cost,
 - $\circ \qquad \text{If calculated runningCost is less than current runningCost} \\$
 - Set previous to s14
 - update runningCost
 - Push <7, s15>

<u>\$</u>	s3	s2	s1	s0
	s7	s6	s5	s4
	s11	s10	s9	s8
	s15	s14	s13	s12
	1	1	1	1
	9	3	6	14
	2	0	0	0
	2	1	3	1
	ОТТОМ	В		

<u>square</u>	<u>v</u>	<u>P</u>	<u>RC</u>
s0			inf
s1			inf
s2			inf
s3			inf
s4		s8	14
s5			inf
s6			inf
s7			inf
s8	true	ł	inf
s11			inf
s12	true	s8	1
s13	true	s12	4
s14	true	s13	5
s15		s14	7

TOP BOTT								BOTTOM	
<7, s15>	<14, s4>								

```
initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pg is not empty:
     let current = remove the first entry from pq (poll)
     let currentSquare = current's value
     Mark currentSquare as visited
     if currentSquare is the finishing square
         return currentSquare
     else
         for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
               add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)
```

s0	s1	s2	s3
s4	s5	s6	s7
s8	s 9	s10	s11
s12	s13	s14	s15

<u>square</u>	<u>v</u>	<u> </u>	<u>KC</u>
s0			inf
s1			inf
s2			inf
s3			inf
s4		s8	14
s5			inf
s6			inf
s7			inf
s8	true		inf
s11			inf
s12	true	s8	1
s13	true	s12	4
s14	true	s13	5
s15	true	s14	7

- Remove the first element of the pq (s15)
- Mark it as visited

TOP					воттом
<14, s4>					

initialize pg to be a new empty heap add the start square's cost as the key and the start square itself as the value to pq while pg is not empty: let current = remove the first entry from pg (poll) let currentSquare = current's value Mark currentSquare as visited if currentSquare is the finishing square return currentSquare else for each neighbor of currentSquare that isn't a wall and isn't visited let currentCost = current's key plus the neighbors cost if currentCost is less than neighbor's runningCost set the previous of the neighbor to currentSquare set the neighbors runningCost to currentCost add the currentCost as key and neighbor as value to the pq (add) if the loop ended, return null (no path found)

_	s15	neighb	ors.	s14	s11
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<14, s4>

- Neighbors to consider: s11 (s14 is visited)
- For s11

TOP

<9, s11>

- calculate runningCost by adding current's key + s11 cost,
- If calculated runningCost is less than current runningCost
 - Set previous to s15
 - update runningCost
 - Push <9, s11>

square	s3	s2	s1	s0
s0 s1	s7	s6	s5	s4
s2	s11	s10	s9	s8
s3	s15	s14	s13	s12
s4	310	317	310	312
s5				
s6	1	1	1	1
s7	9	3	6	14
s8	Ū		_	
s11	2	0	0	0
s12	2	1	3	1
s13	ОТТОМ	D		
s14	OT TOW	<u></u>		

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s15

true

true

true

true

true

RC

inf

inf

inf

inf

14

inf

inf

inf

inf

9

4

5

s8

s15

s8

s12

s13

s14

```
initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pg is not empty:
     let current = remove the first entry from pq (poll)
     let currentSquare = current's value
     Mark currentSquare as visited
     if currentSquare is the finishing square
         return currentSquare
     else
         for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
                add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)
```

`			

_	Remove	the first	element	of the	pg (s11)

- Mark it as visited

s0	s1	s2	s3
s4	s5	s6	s7
s8	s9	s10	s11
s12	s13	s14	s15

1	1	1	1
14	6	3	9
0	0	0	2
1	3	1	2

	s0			inf
	s1			inf
	s2			inf
	s3			inf
	s4		s8	14
•	s5			inf
	s6			inf
	s7			inf
	s8	true		inf
	s11	true	s15	9
	s12	true	s8	1
	s13	true	s12	4
	s14	true	s13	5
	s15	true	s14	7

<u>v</u>

square

RC

TOP					BOTTOM
<14, s4>					

initialize pq to be a new empty heap add the start square's cost as the key and the start square itself as the value to pq while pg is not empty: let current = remove the first entry from pq (poll) let currentSquare = current's value Mark currentSquare as visited if currentSquare is the finishing square return currentSquare else for each neighbor of currentSquare that isn't a wall and isn't visited let currentCost = current's key plus the neighbors cost if currentCost is less than neighbor's runningCost set the previous of the neighbor to currentSquare set the neighbors runningCost to currentCost add the currentCost as key and neighbor as value to the pq (add) if the loop ended, return null (no path found)

-	s11	neighbors:	s10, s7, s15	
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- Neighbors to consider: s7(s10 is a wall, s15 is visited)
- For s7
 - calculate runningCost by adding current's key + s7 cost,
 - $\circ \qquad \text{If calculated runningCost is less than current runningCost} \\$
 - Set previous to s11
 - update runningCost
 - Push <18, s7>

s0	s1	s2	s3	-				
s4	s5	s6	s7					
s8	s9	s10	s11					
s12	s13	s14	s15	-				
1	1	1	1					
14	6	3	9					
0	0	0	2					
1	3	1	2					
		В	ОТТОМ					

	square	<u>v</u>	<u>P</u>	<u>RC</u>
	s0			inf
	s1			inf
	s2			inf
	s3			inf
	s4		s8	14
•	s5			inf
	s6			inf
	s7		s11	18
	s8	true		inf
	s11	true	s15	9
	s12	true	s8	1
1	s13	true	s12	4
	s14	true	s13	5
	s15	true	s14	7

TOP					BOTTOM
<14, s4>	<18, s7>				

```
initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pg is not empty:
     let current = remove the first entry from pq (poll)
     let currentSquare = current's value
     Mark currentSquare as visited
     if currentSquare is the finishing square
         return currentSquare
     else
         for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
               add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)
```

s0	s1	s2	s3
s4	s5	s6	s7
s8	s9	s10	s11
s12	s13	s14	s15

<u>square</u>	<u>V</u>	<u>P</u>	<u>RC</u>
s0			inf
s1			inf
s2			inf
s3			inf
s4	true	s8	14
s5			inf
s6			inf
s7		s11	18
s8	true		inf
s11	true	s15	9
s12	true	s8	1
s13	true	s12	4
s14	true	s13	5
s15	true	s14	7

- Remove the first element of the pq (s4)
- Mark it as visited

TOP					BOTTOM
<18, s7>					

initialize pg to be a new empty heap add the start square's cost as the key and the start square itself as the value to pq while pg is not empty: let current = remove the first entry from pg (poll) let currentSquare = current's value Mark currentSquare as visited if currentSquare is the finishing square return currentSquare else for each neighbor of currentSquare that isn't a wall and isn't visited let currentCost = current's key plus the neighbors cost if currentCost is less than neighbor's runningCost set the previous of the neighbor to currentSquare set the neighbors runningCost to currentCost add the currentCost as key and neighbor as value to the pg (add) if the loop ended, return null (no path found)

s0	s 1	s2	s 3
s4	s5	s6	s7
s8	s9	s10	s11
s12	s13	s14	s15

3

14

9

2

2

s14

s15

s0		s4	
s1			
s2			
s3			
s4	true	s8	
s 5		s4	
s6			
s7		s11	
s8	true	1	
s11	true	s15	
s12	true	s8	
s13	true	s12	

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square

RC

15

inf

inf

inf

14

20

inf

18

inf

9

4

5

s13

s14

true

true

- s4 neighbors: s0, s5, s8
- Neighbors to consider: s0, s5 (s8 is visited)
- For s0, s5
 - calculate runningCost by adding current's key + s0/s5 cost
 - $\circ \qquad \text{If calculated runningCost is less than current runningCost} \\$
 - Set previous to s4
 - update runningCost
 - Push <15, s0>, <20, s5>

TOP						BOTTOM
<15, s0>	<18, s7>	<20, s5>				

```
initialize pg to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pg is not empty:
     let current = remove the first entry from pq (poll)
     let currentSquare = current's value
     Mark currentSquare as visited
     if currentSquare is the finishing square
         return currentSquare
     else
         for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
               add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)
```

s0	s1	s2	s3
s4	s5	s6	s7
s8	s9	s10	s11
s12	s13	s14	s15

s2		
s3		
s4	true	s8
s5		s4
s6		
s7		s11
s8	true	
s11	true	s15
s12	true	s8

s13

s14

s15

٧

true

square

s0

s1

RC

15

inf

inf

inf

14

20

inf

18

inf

9

s12

s13

s14

true

true

true

s4

- Remove the first element of the pq (s0)
- Mark it as visited

TOP					BOTTOM
<18, s7>	<20, s5>				

initialize pq to be a new empty heap add the start square's cost as the key and the start square itself as the value to pq while pg is not empty: let current = remove the first entry from pq (poll) let currentSquare = current's value Mark currentSquare as visited if currentSquare is the finishing square return currentSquare else for each neighbor of currentSquare that isn't a wall and isn't visited let currentCost = current's key plus the neighbors cost if currentCost is less than neighbor's runningCost set the previous of the neighbor to currentSquare set the neighbors runningCost to currentCost add the currentCost as key and neighbor as value to the pq (add) if the loop ended, return null (no path found)

- s0 neigh	bors: s1, s4
------------	--------------

- Neighbors to consider: s1 (s4 is visited)
- For s1
 - calculate runningCost by adding current's key + s1 cost
 - If calculated runningCost is less than current runningCost
 - Set previous to s0
 - update runningCost
 - Push <16, s1>

	s0	s1	1	s2	S	3	
	s4	s5	5	s6	S	₅ 7	
	s8	sS)	s10	s	11	•
5	s12	s1	3	s14	S	15	-
	1	1		1		1	
	14	6		3	,	9	
	0	0		0	;	2	
	1	3		1	,	2	
				E	OTT	ОМ	-

square	<u>v</u>	<u>P</u>	RC
s0	true	s4	15
s1		s0	16
s2			inf
s3			inf
s4	true	s8	14
s5		s4	20
s6			inf
s7		s11	18
s8	true	-	inf
s11	true	s15	9
s12	true	s8	1
s13	true	s12	4
s14	true	s13	5
s15	true	s14	7

TOP						BOTTOM
<16. s1>	<18, s7>	<20, s5>				

```
initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pg is not empty:
     let current = remove the first entry from pq (poll)
     let currentSquare = current's value
     Mark currentSquare as visited
     if currentSquare is the finishing square
         return currentSquare
     else
         for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
               add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)
```

s0	s1	s2	s3
s4	s5	s6	s7
s8	s9	s10	s11
s12	s13	s14	s15

			-		
40	-11	01 <i>E</i>	s3		
13	s14	s15	s4	true	S
			s5		S
1	1	1	s6		
6	3	9	s7		S'
		Ü	s8	true	
0	0	2	s11	true	S
3	1	2	s12	true	s
			l I		

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true

true

square

s0

s1

s2

s13

s14

s15

true

true

true

s12

s13

s14

RC

15

16

inf

inf

14

20

inf

18

inf

9

4

5

s4

s0

-	Remove	the first e	element	of the p	oq (s1)
---	--------	-------------	---------	----------	---------

Mark it as visited

TOP					BOTTOM
<18, s7>	<20, s5>				

initialize pq to be a new empty heap add the start square's cost as the key and the start square itself as the value to pq while pg is not empty: let current = remove the first entry from pq (poll) let currentSquare = current's value Mark currentSquare as visited if currentSquare is the finishing square return currentSquare else for each neighbor of currentSquare that isn't a wall and isn't visited let currentCost = current's key plus the neighbors cost if currentCost is less than neighbor's runningCost set the previous of the neighbor to currentSquare set the neighbors runningCost to currentCost add the currentCost as key and neighbor as value to the pq (add) if the loop ended, return null (no path found)

-	s1	neig	jhbo	ors:	s0,	s2,	s5	
---	----	------	------	------	-----	-----	----	--

- Neighbors to consider: s2, s5 (s0 is visited)
- For s2, s5
 - calculate runningCost by adding current's key + s2/s5 cost
 - o If calculated runningCost is less than current runningCost
 - Set previous to s1
 - update runningCost
 - Push <17, s2>, <22, s5>

	s4	s5	s6	s7	
	s8	s9	s10	s11	
	s12	s13	s14	s15	
	1	1	1	1	
	14	6	3	9	
t	0	0	0	2	
	1	3	1	2	
			Е	оттом	

s2

s1

s3

square	<u>v</u>	<u>P</u>	RC
s0	true	s4	15
s1	true	s0	16
s2		s1	17
s3			inf
s4	true	s8	14
s5		s4	20
s6			inf
s7		s11	18
s8	true	-	inf
s11	true	s15	9
s12	true	s8	1
s13	true	s12	4
s14	true	s13	5
s15	true	s14	7

TOP						BO
<17. s2>	<18. s7>	<20. s5>				

```
initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pg is not empty:
     let current = remove the first entry from pq (poll)
     let currentSquare = current's value
     Mark currentSquare as visited
     if currentSquare is the finishing square
         return currentSquare
     else
         for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
               add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)
```

s0	s1	s2	s3
s4	s5	s6	s7
s8	s 9	s10	s11
s12	s13	s14	s15

s15

true

s14

<u>square</u>	<u>v</u>	<u>P</u>	<u>RC</u>
s0	true	s4	15
s1	true	s0	16
s2	true	s1	17
s3			inf
s4	true	s8	14
s5		s4	20
s6			inf
s7		s11	18
s8	true	ł	inf
s11	true	s15	9
s12	true	s8	1
s13	true	s12	4
s14	true	s13	5

- Remove the first element of the pq (s2)
- Mark it as visited

TOP					BOTTOM
<18, s7>	<20, s5>				

initialize pq to be a new empty heap add the start square's cost as the key and the start square itself as the value to pq while pg is not empty: let current = remove the first entry from pq (poll) let currentSquare = current's value Mark currentSquare as visited if currentSquare is the finishing square return currentSquare else for each neighbor of currentSquare that isn't a wall and isn't visited let currentCost = current's key plus the neighbors cost if currentCost is less than neighbor's runningCost set the previous of the neighbor to currentSquare set the neighbors runningCost to currentCost add the currentCost as key and neighbor as value to the pq (add) if the loop ended, return null (no path found)

s0	s1	s2	s3
s4	s5	s6	s7
s8	s9	s10	s11
s12	s13	s14	s15

6

14

9

2

<u>square</u>	<u>V</u>	<u>P</u>	<u>RC</u>
s0	true	s4	15
s1	true	s0	16
s2	true	s1	17
s3		s2	18
s4	true	s8	14
s5		s4	20
s6		s2	20
s7		s11	18
s8	true		inf
s11	true	s15	9
s12	true	s8	1
s13	true	s12	4
s14	true	s13	5
s15	true	s14	7

- s2 neighbors: s1, s3, s6
- Neighbors to consider: s3, s6 (s1 is visited)
- For s3, s6
 - calculate runningCost by adding current's key + s3/s6 cost
 - If calculated runningCost is less than current runningCost
 - Set previous to s2
 - update runningCost
 - Push <18, s3>, <20, s6>

TOP						BOTTOM
<18, s3>	<18, s7>	<20, s6>	<20, s5>			

```
initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pg is not empty:
     let current = remove the first entry from pq (poll)
     let currentSquare = current's value
     Mark currentSquare as visited
     if currentSquare is the finishing square
         return currentSquare
     else
         for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
               add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)
```

s0	s1	s2	s3
s4	s5	s6	s7
s8	s9	s10	s11
s12	s13	s14	s15

14

<u> </u>	_	-	
s0	true	s4	15
s1	true	s0	16
s2	true	s1	17
s3	true	s2	18
s4	true	s8	14
s5		s4	20
s6		s2	20
s7		s11	18
s8	true		inf
s11	true	s15	9
s12	true	s8	1
s13	true	s12	4

square

s14

s15

true

true

s13

s14

- Remove the first element of the pq (s3)
- Mark it as visited

TOP						BOTTOM
<18, s7>	<20, s6>	<20, s5>				

initialize pq to be a new empty heap add the start square's cost as the key and the start square itself as the value to pq while pg is not empty: let current = remove the first entry from pq (poll) let currentSquare = current's value Mark currentSquare as visited if currentSquare is the finishing square return currentSquare else for each neighbor of currentSquare that isn't a wall and isn't visited let currentCost = current's key plus the neighbors cost if currentCost is less than neighbor's runningCost set the previous of the neighbor to currentSquare set the neighbors runningCost to currentCost add the currentCost as key and neighbor as value to the pq (add) if the loop ended, return null (no path found)

s0	s1	s2	s3
s4	s5	s6	s7
s8	s 9	s10	s11
s12	s13	s14	s15

6

14

9

<u>square</u>	<u>V</u>	<u>P</u>	<u>RC</u>
s0	true	s4	15
s1	true	s0	16
s2	true	s1	17
s3	true	s2	18
s4	true	s8	14
s5		s4	20
s6		s2	20
s7		s11	18
s8	true		inf
s11	true	s15	9
s12	true	s8	1
s13	true	s12	4
s14	true	s13	5
s15	true	s14	7

-	s3 neighbors: s2, s7
---	----------------------

- Neighbors to consider: s7 (s2 is visited)
- For s7
 - calculate runningCost by adding current's key + s7 cost
 - If calculated runningCost is less than current runningCost
 - Set previous to s3
 - update runningCost
 - Push <27, s7>

TOP						BOTTOM
<18, s7>	<20, s6>	<20, s5>				

```
initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pg is not empty:
     let current = remove the first entry from pq (poll)
     let currentSquare = current's value
     Mark currentSquare as visited
     if currentSquare is the finishing square
         return currentSquare
     else
         for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
               add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)
```

s0	s1	s2	s3
s4	s5	s6	s7
s8	s 9	s10	s11
s12	s13	s14	s15

9

s15

true

s14

<u>square</u>	<u>v</u>	<u>P</u>	<u>RC</u>
s0	true	s4	15
s1	true	s0	16
s2	true	s1	17
s3	true	s2	18
s4	true	s8	14
s5		s4	20
s6		s2	20
s7	true	s11	18
s8	true		inf
s11	true	s15	9
s12	true	s8	1
s13	true	s12	4
s14	true	s13	5

- Remove the first element of the pq (s7)
- Mark it as visited

TOP					BOTTOM
<20, s6>	<20, s5>				

initialize pq to be a new empty heap add the start square's cost as the key and the start square itself as the value to pq while pg is not empty: let current = remove the first entry from pq (poll) let currentSquare = current's value Mark currentSquare as visited if currentSquare is the finishing square return currentSquare else for each neighbor of currentSquare that isn't a wall let currentCost = current's key plus the neighbors if currentCost is less than neighbor's runningCost set the previous of the neighbor to currentSqu set the neighbors runningCost to currentCost add the currentCost as key and neighbor as val if the loop ended, return null (no path found)

and	is	n't	vis	ited	
s co t	st				
uare					
lue	to	the	pq	(add)	

- s7 neighbors: s6, s3, s11
- Neighbors to consider: s6 (s3, s11 are visited)
- For s6
 - calculate runningCost by adding current's key + s6 cost
 - If calculated runningCost is less than current runningCost
 - Set previous to s7
 - update runningCost
 - Push <21, s6>

s0	s1	s2	s3			
s4	s5	s6	s7			
s8	s9	s10	s11			
s12	s13	s14	s15			
1	1	1	1			
14	6	3	9			
0	0	0	2			
1	3	1	2			
		В	оттом			

<u>square</u>	<u>V</u>	<u>P</u>	<u>RC</u>
s0	true	s4	15
s1	true	s0	16
s2	true	s1	17
s3	true	s2	18
s4	true	s8	14
s5		s4	20
s6		s2	20
s7	true	s11	18
s8	true	ł	inf
s11	true	s15	9
s12	true	s8	1
s13	true	s12	4
s14	true	s13	5
s15	true	s14	7

TOP					BOTTOM
<20, s6>	<20, s5>				

```
initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pg is not empty:
     let current = remove the first entry from pq (poll)
     let currentSquare = current's value
     Mark currentSquare as visited
     if currentSquare is the finishing square
         return currentSquare
     else
         for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
               add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)
```

s0	s1	s2	s3
s4	s5	s6	s7
s8	s9	s10	s11
s12	s13	s14	s15

<u>square</u>	<u>v</u>	<u>P</u>	<u>RC</u>
s0	true	s4	15
s1	true	s0	16
s2	true	s1	17
s3	true	s2	18
s4	true	s8	14
s5		s4	20
s6	true	s2	20
s7	true	s11	18
s8	true		inf
s11	true	s15	9
s12	true	s8	1
s13	true	s12	4
s14	true	s13	5
s15	true	s14	7

- Remove the first element of the pq (s6)
- Mark it as visited

TOP					BOTTOM
<20, s5>					

```
initialize pq to be a new empty heap
add the start square's cost as the key
and the start square itself as the value to pq
while pg is not empty:
     let current = remove the first entry from pq (poll)
     let currentSquare = current's value
     Mark currentSquare as visited
    if currentSquare is the finishing square
         return currentSquare
     else
         for each neighbor of currentSquare that isn't a wall and isn't visited
            let currentCost = current's key plus the neighbors cost
            if currentCost is less than neighbor's runningCost
                set the previous of the neighbor to currentSquare
                set the neighbors runningCost to currentCost
                add the currentCost as key and neighbor as value to the pq (add)
if the loop ended, return null (no path found)
```

s0	s1	s2	s3
s4	s5	s6	s7
s8	s9	s10	s11
s12	s13	s14	s15

14

square	<u>v</u>	<u>P</u>	<u>RC</u>
s0	true	s4	15
s1	true	s0	16
s2	true	s1	17
s3	true	s2	18
s4	true	s8	14
s5		s4	20
s6	true	s2	20
s7	true	s11	18
s8	true		inf
s11	true	s15	9
s12	true	s8	1
s13	true	s12	4
s14	true	s13	5
s15	true	s14	7

-	Return	finish	square
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TOP					BOTTOM
<20, s5>					