# Pricing & Social Influence

**Data Intelligence Applications** 

Meta Samuele

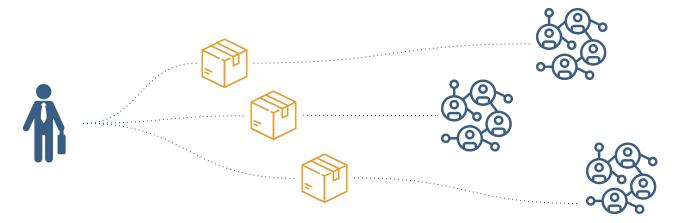
Metaj Stiven Salamino Manuel

Serna Giuseppe



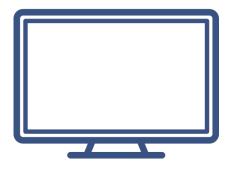
#### 1. The problem

The goal is modeling a scenario in which a seller is pricing some products and spends a given budget on social networks to persuade more and more nodes to buy the products.





# 1. The products



Television

500, 690, 750, 850



Laptop

500, 690, 750, 850



Camera

500, 690, 750, 850



#### 1. The features

**Gender**: Male/Female

**Age**: <18, 18-25, 26-34, 35-50, >50

Location: Africa, Asia, Europe, North America, South America, Australia

Interests: technology, sports, politics, science, economics, health

Authority: a node connected to many neighbors can be seen as an influencer



#### 1. The social networks



Facebook

age



**Twitter** 

interests



Instagram

authority



#### 2. Greedy algorithm

```
greedy_algorithm(graph, budget, k)
```

Search the best set of seeds adding one at the time until we reach the budget

```
montecarlo_sampling(seeds, max_repetitions)
```

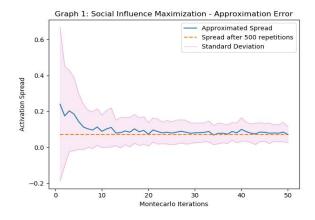
Given a set of seeds, evaluate the spread in the network through different simulations

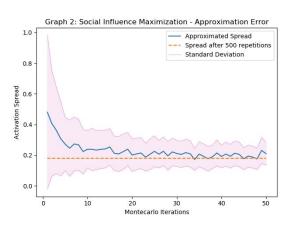
```
approximation_error(graphs, budget, scale_factor, n_exp)
```

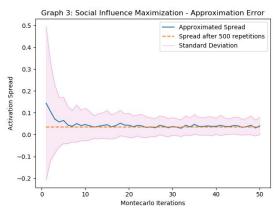
Plot the result of running the greedy algorithm on the different networks



# 2. Greedy algorithm - Results









#### 3. Greedy algorithm over all networks

Now we want to perform jointly social influence in the three social networks

```
cumulative_greedy_algorithm(graphs, budget, k)
```

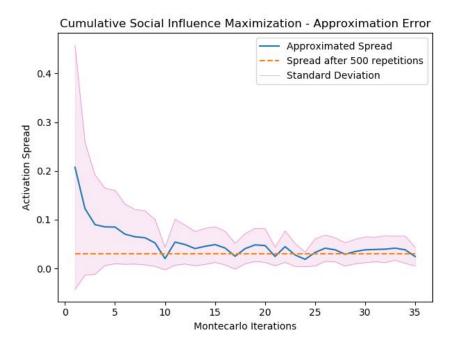
Until the budget is not finished, search in the different networks the seed that will provide the best marginal increase and add it to the set of seeds

```
cumulative_approximation_error(graphs, budget, scale_factor, n_exp)
```

Plot the results of running the cumulative greedy algorithm on the three social networks



### 3. Greedy algorithm over all networks - Results





### 4. Unknown activation probabilities

We consider the adjacency matrix as the true values to which we want to converge

We model each edge as a Bernoulli variable and we define a Beta distribution over them

#### choose\_seeds(graph, budget, epsilon, simulations)

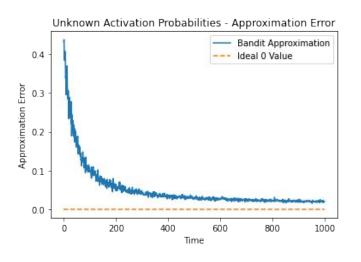
We use the greedy algorithm to select the set of seeds. The parameter epsilon allows to regulate the exploration/exploitation dilemma

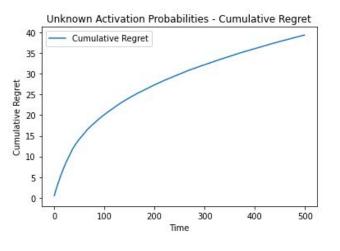
```
influence_episode(seeds, true_graph.adj_matrix)
```

Collect a sample for each edge and observe which edges will activate, updating the Beta parameters



# 4. Unknown activation probabilities - Results







#### 5. Cumulative revenue maximization

We assume to have an unique seasonal phase and that the activations of the graph are known

#### TS\_Learner(n\_arms, arms)

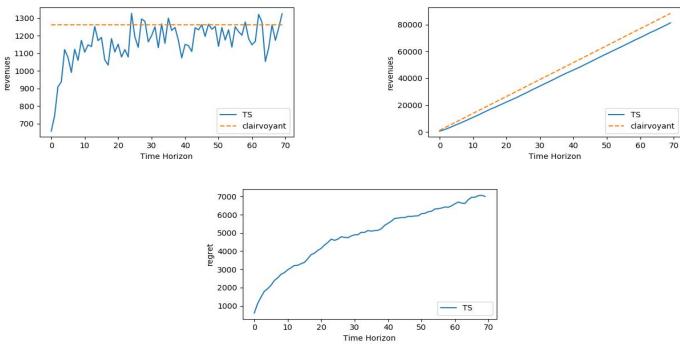
Builds a class to manage the Thompson Sampling operations: the choice of the arm to pull and, given the rewards, the update of the distributions.

#### Environment(n\_arms, probabilities, horizon)

Simulates the environment where the arms are: it gives the rewards based on the real probabilities for the event to occur.

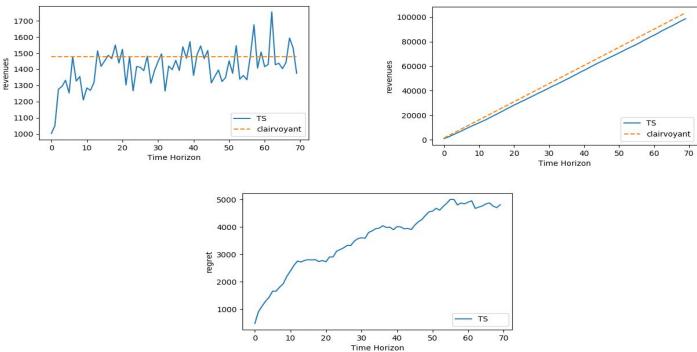


# 5. Cumulative revenue maximization - Results(1)



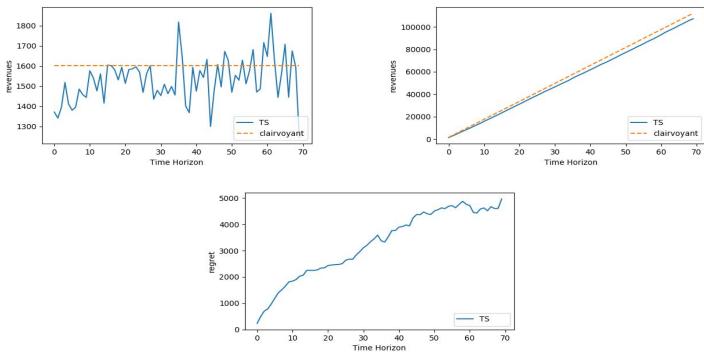


### 5. Cumulative revenue maximization - Results(2)





#### 5. Cumulative revenue maximization - Results(3)





# 6. Pricing with seasonal phases





### 6. Pricing with seasonal phases

We consider now three different phases with abrupt transitions and we still assume to know the activation probabilities of the social networks

#### SWTS\_Learner(n\_arms, arms, window\_size, horizon)

Builds the class to manage the operation of the Thompson Sampling with Sliding Window: the choice of the arm to pull and, given the rewards, the update of the distributions, taking into account only the rewards obtained inside the Sliding Window.

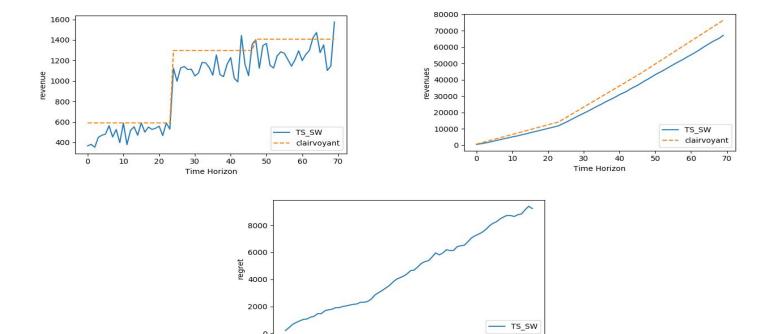
#### Non\_Stationary\_Environment(n\_arms, probabilities, horizon)

Simulates the environment of the arms: it gives the rewards based on the real probabilities for the event to occur, taking into account the phase in that specific moment.



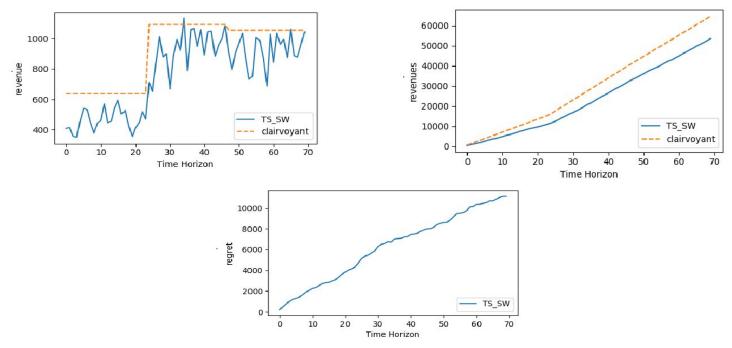
# 6. Pricing with seasonal phases - Results(1)

Time Horizon



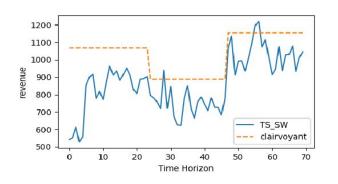


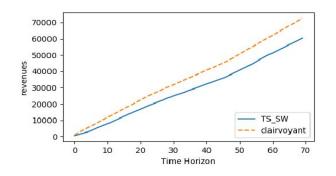
### 6. Pricing with seasonal phases - Results(2)

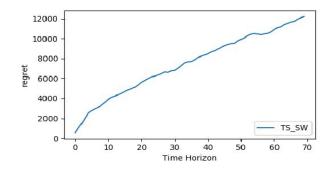




# 6. Pricing with seasonal phases - Results(3)





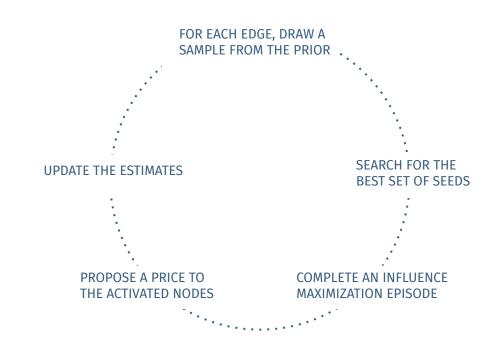




### 7. Pricing and social influence learning

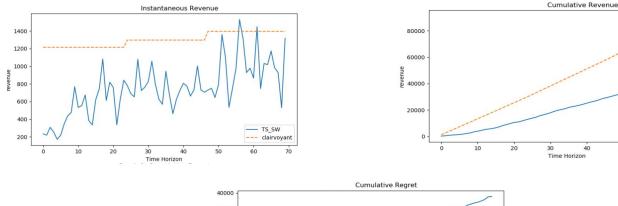
Now we cannot consider the activation probabilities as known a priori

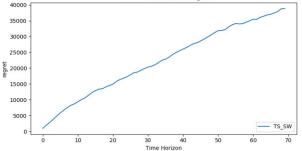
The seller needs to learn both the activation probabilities and the conversion rate curves simultaneously





# 7. Pricing and social influence learning - Results(1)







- TS\_SW

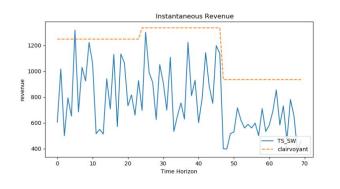
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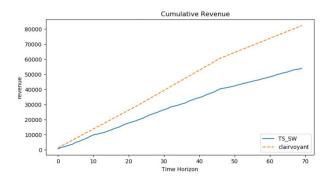
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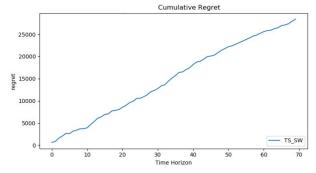
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# 7. Pricing and social influence learning - Results(2)









# 7. Pricing and social influence learning - Results(3)

