

Applications of PCA and Image Compression (Lab 1)

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November 21, 2017

1 Applications of PCA

The iris dataset becomes easier to analyse in lower dimensions without the redundancy. Figure 1 shows clearly linearly separable data, as does Figure 2, which also shows tighter clustering for parts of the data. Not much can be analysed without the labels, but with them one could draw better conclusions from seeing the data represented in these subspaces.

Figure 3 on the other hand, doesn't reveal much information about the data. There is no clear separation and there is little to no clustering to speak of. From observing the 3 figures, we can clearly see the principal components' variance reduces from first to last, as it should.

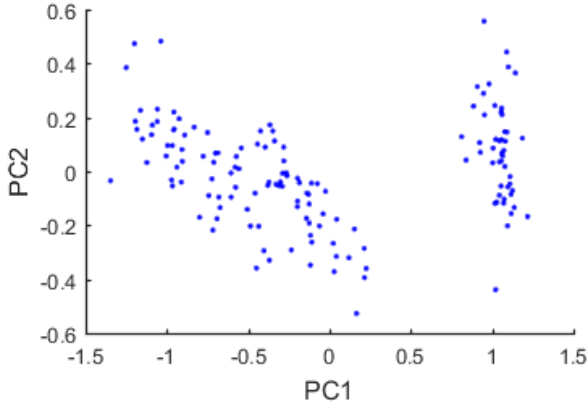


Figure 1: Results in subspace PC_1 - PC_2 .

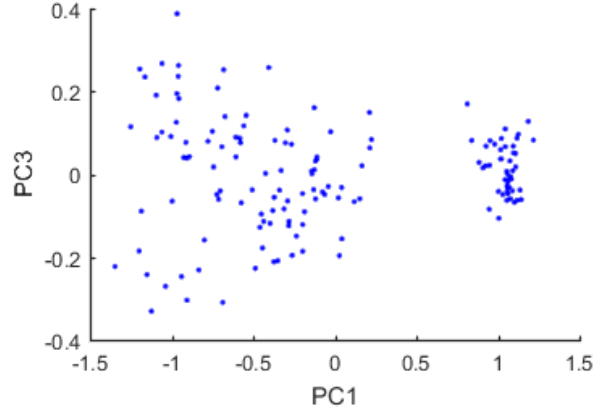


Figure 2: Results in subspace PC_1 - PC_3 .

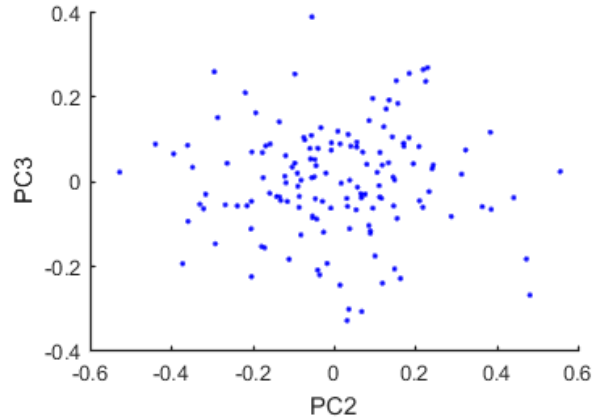


Figure 3: Results in subspace PC_2 - PC_3 .

2 Image Compression

For the image compression of the digits, I used PCA with SVD because the data has more dimensions (features) than examples. Since our examples are images, each pixel of the images is a feature. At a width by height of 28

by 28, that's 784 pixels or 784 features. The images (examples), however, were only 300 in the train dataset.

In order to have a satisfactory compression system, I use 47 principal components where the Proportion of Variance is 90.05% based on

$$PoV = \frac{\sum_{i=1}^k \lambda_i}{\sum_{i=1}^d \lambda_i}$$

By comparison, at $k = 46$ we only get a PoV of 89.77%, so $k = 47$ is the first value at which we achieve a satisfactory $PoV \geq 90\%$ as shown in Figure 4.

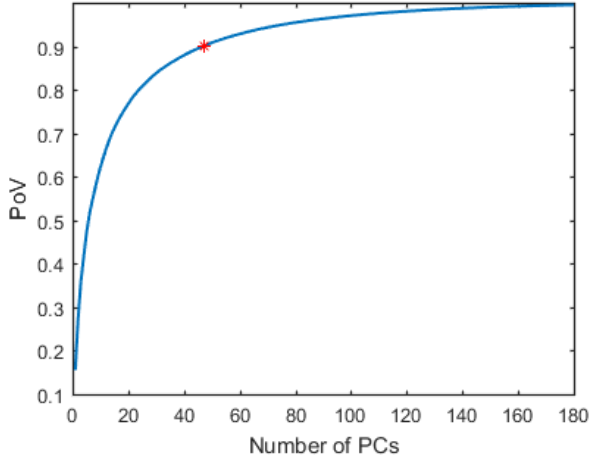


Figure 4: PoV for each k . Red mark at $k = 47$.

At 47 principal components, we also observe a good size compression on disk. After using matlab's save function to save each dataset on disk separately, I established that the default uncompressed test dataset is of size 4985 bytes, while the compressed version of the test dataset is only 3837 bytes, which is a size compression of roughly 23.03%.

On Figure 5 we can see the original test dataset images, before any compression and on Figure 6 we can see the same images after reconstruction using 47 PCs.

On Figure 7 we see the reconstructed images. The left column contains the images compressed and reconstructed using 1 to 25 PCs and the right column shows the images made with PCs between 26 and 50.



Figure 5: Original uncompressed test images.



Figure 6: Reconstructed images using 47 PCs.

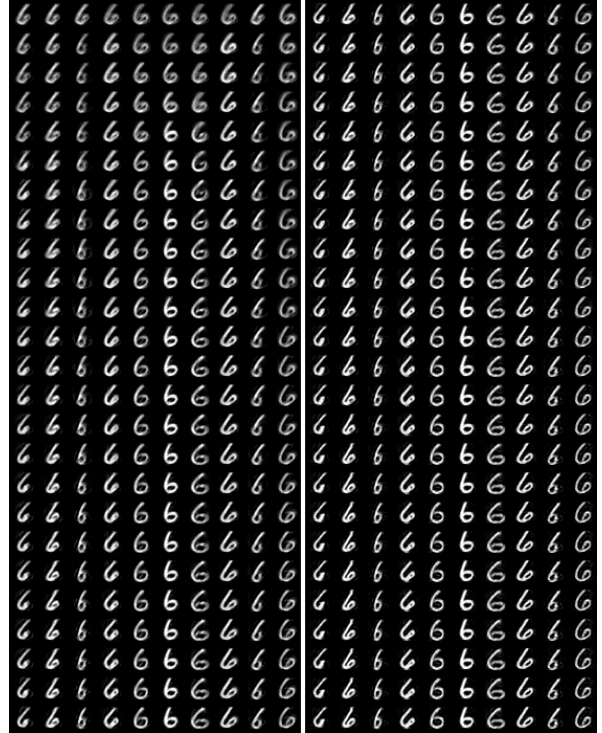


Figure 7: Reconstructed images in order of number of PCs used from 1 to 50.