

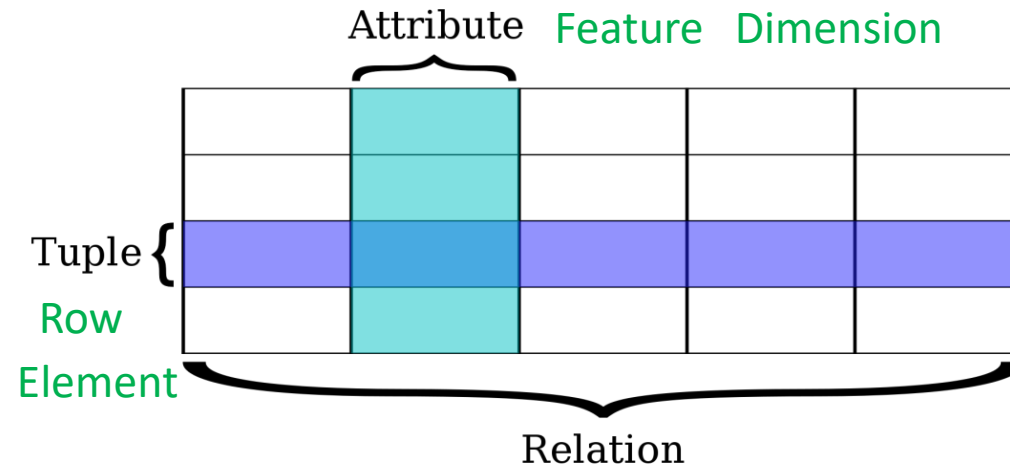
Unsupervised Learning (cont'd)

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1. James, Gareth, et al. *An introduction to statistical learning*. Vol. 6. New York: springer, 2013.
2. Friedman, Jerome, Trevor Hastie, and Robert Tibshirani. *The elements of statistical learning*. Vol. 1. Springer, Berlin: Springer series in statistics, 2001.
3. Kuhn, Max, and Kjell Johnson. *Applied predictive modeling*. New York: Springer, 2013.



What does data look like?



$$\mathbf{x}_i = (x_{i1}, x_{i2}, \dots, x_{ip}) \in \mathbb{R}^p$$

$$X \in \mathbb{R}^{n \times p}$$

Unsupervised Learning: Definitions

- ... algorithms used to draw inferences from datasets consisting of input data without labeled responses.
- ... task of inferring a function to describe hidden structure from unlabeled data.
 - Distribution / Density
 - Summary statistics
 - Clustering
 - Principal Components Analysis



Patterns in data

- They describe structure (patterns) in the data
 - i. Which value(s) occur most frequently?
 - ii. How much does the data vary?
 - iii. How symmetrically does data vary around center?
 - iv. Is data clustered around value(s)?
 - v. Sub-space where data is “concentrated”
- Summary statistics
 - i. Median
 - ii. Variance, Standard Deviation
 - iii. Skewness, Kurtosis
 - iv. Mode
- Multiple dimensions
 - i. Are two features / dimensions correlated
- Clustering
 - Find data elements which are similar.
 - Finding “areas” in space where data is concentrated
- Association Rules
 - Find features (dimensions) which occur together
 - Find features (dimensions) which are “correlated”
- Dimensionality Reduction
 - Find smaller dimensional representations of the data which preserve it’s essential structure.
 - Find subspaces where data varies the most.

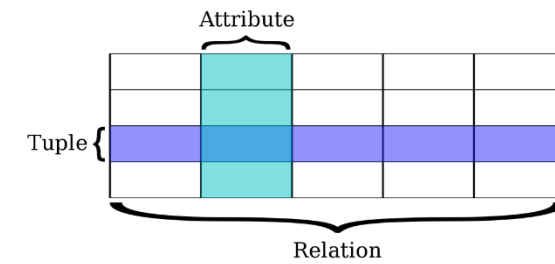


Association Rule Mining

Conceptual Overview



Association Rules



- What does the value of one feature tell us about the value of another feature?
 - People who buy diapers are likely to buy baby powder
 - If (people buy diaper), then (they buy baby powder)
 - Caution : Watch the directionality! ($A \rightarrow B$ does not mean $B \rightarrow A$)
- Association rules
 - Are statements about relations among features (attributes) : across elements (tuples)
 - Use a transaction-itemset data model

TID	Items
1	Bread, Milk
2	Bread, Diaper, Beer, Eggs
3	Milk, Diaper, Beer, Coke
4	Bread, Milk, Diaper, Beer
5	Bread, Milk, Diaper, Coke



	Beer	Bread	Milk	Diaper	Eggs	Coke
T_1	0	1	1	0	0	0
T_2	1	1	0	1	1	0
T_3	1	0	1	1	0	1
T_4	1	1	1	1	0	0
T_5	0	1	1	1	0	1



Association Rules = Market Basket Analysis?

- Most common use
 - Each basket (purchase) is a row and each item is a column
- Not the only use
 - Can work in any dataset where features take only two use values : 0/1
 - Can work in any dataset where features can be *represented as* taking only two use values : 0/1
 - Preprocessing: Discretization, Feature selection
- Association Rules beyond Market Basket Analysis
 - People who visit webpage X are likely visit webpage Y.
 - Nodes which run a web server are likely to run linux.
 - People who have age-group [30,40] & income [>\$100k] are likely to own home

T_1	0	1	1	0	0	0
T_2	1	1	0	1	1	0
T_3	1	0	1	1	0	1
T_4	1	1	1	1	0	0
T_5	0	1	1	1	0	1



Measures of effectiveness

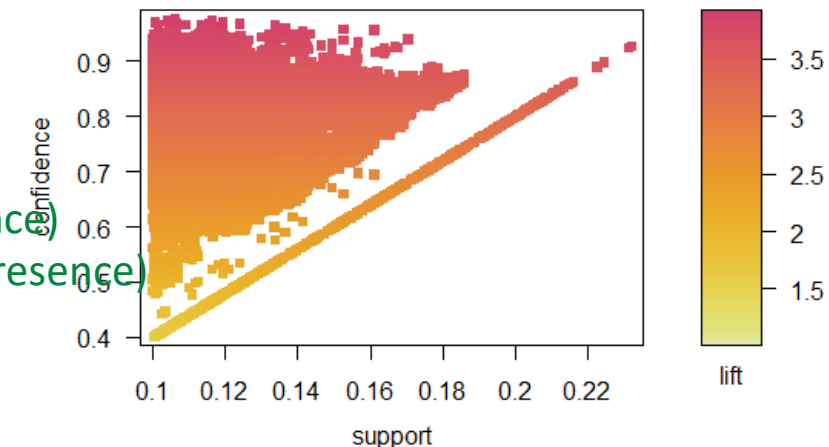
- What do association rules look like?
 - {diapers} \rightarrow {baby powder}
 - {bread, butter} \rightarrow {milk}
 - {bat, ball, pads} \rightarrow {helmet}
 - $X \rightarrow Y :: \text{If } \{X\}, \text{ Then } \{Y\}$
 - If Precondition, Then Conclusion
 - If Antecedent, Then Consequent
- How good / significant is a rule?
 - An association rule is a probabilistic statement
 - How much historical data **supports** your rule?
 - How **confident** are we that the rule holds?
- Support (a.k.a. Coverage) of $X \rightarrow Y$
 - Fraction of rows containing both X & Y
 - $P(X \text{ and } Y)$: Joint Probability
 - $\text{Support}(X \rightarrow Y) = \text{Support}(Y \rightarrow X)$
- Confidence of $X \rightarrow Y$
 - Among rows containing X, fraction of rows containing Y
 - $P(Y|X)$: Conditional Probability
 - $\text{Confidence}(X \rightarrow Y) \neq \text{Confidence}(Y \rightarrow X)$
- What do association rules really look like?
 - $X \xrightarrow{\text{support, confidence}} Y$



Measures of effectiveness (cont'd)

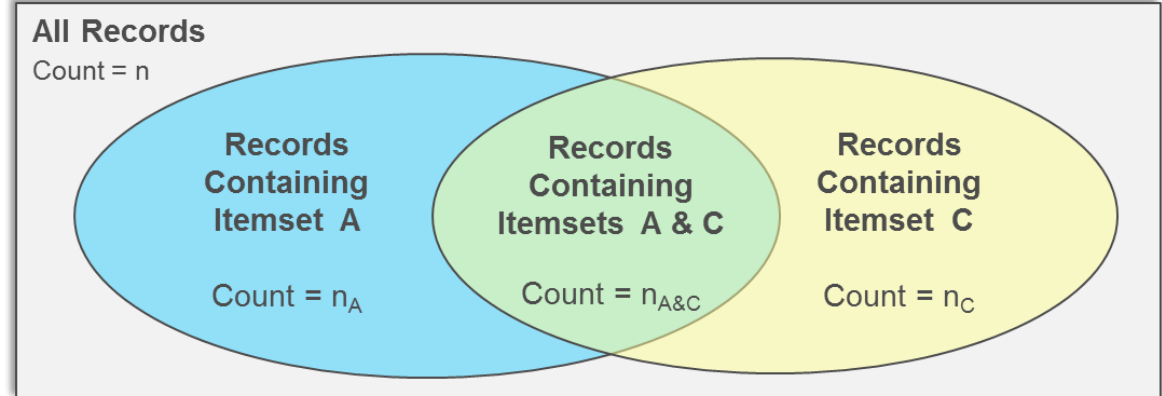
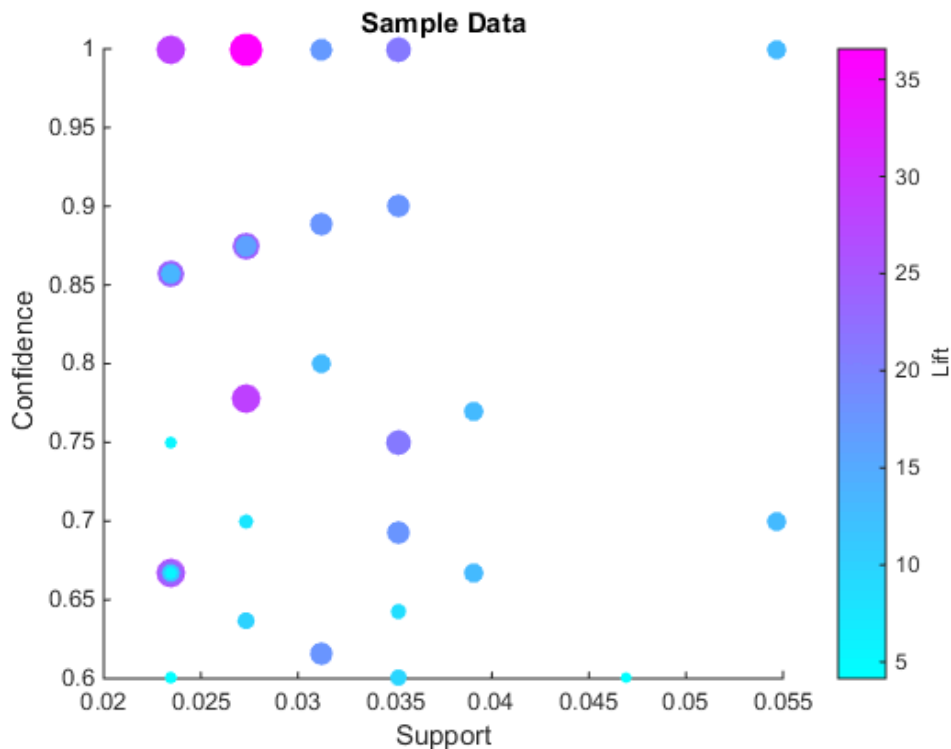
- {Diaper, Beer} → Milk
 - Support = 2/5, Confidence = 2/3
- {Milk} → {Diaper, Beer}
 - Support = 2/5, Confidence = 2/4
- {Milk, Diaper} → Bread
 - Support = 2/5, Confidence = 2/3
- {Milk, Beer} → Diaper?
- Confidence = 1?
 - Caution : Diaper is very popular!
 - Does the inclusion of {Milk, Beer} increase the probability of Diaper?
- Lift
 - Confidence ($X \rightarrow Y$)/Support(Y) or equivalently $P(Y|X) / P(Y)$
 - > 1 : X & Y positively correlated (Presence of X lifts probability of Y's presence)
 - < 1 : X & Y negatively correlated (Presence of X reduces probability of Y's presence)
 - $= 1$ X & Y not correlated

	Beer	Bread	Milk	Diaper	Eggs	Coke
T_1	0	1	1	0	0	0
T_2	1	1	0	1	1	0
T_3	1	0	1	1	0	1
T_4	1	1	1	1	0	0
T_5	0	1	1	1	0	1



Measures of effectiveness (cont'd)

- Support
- Confidence
- Lift
- Others: Affinity, Leverage



Rule = $A \rightarrow C$

$$\text{Support}(A) = \frac{n_A}{n} \quad \text{Support}(C) = \frac{n_C}{n} \quad \text{Support}(A\&C) = \frac{n_{A\&C}}{n}$$

$$\text{Confidence}(A \rightarrow C) = \frac{\text{Support}(A\&C)}{\text{Support}(A)} = \frac{n_{A\&C}}{n_A}$$

$$\text{Lift}(A\&C) = \frac{\text{Confidence}(A \rightarrow C)}{\text{Support}(C)} = \frac{\text{Support}(A\&C)}{\text{Support}(A) * \text{Support}(C)} = \frac{n * n_{A\&C}}{n_A * n_C}$$

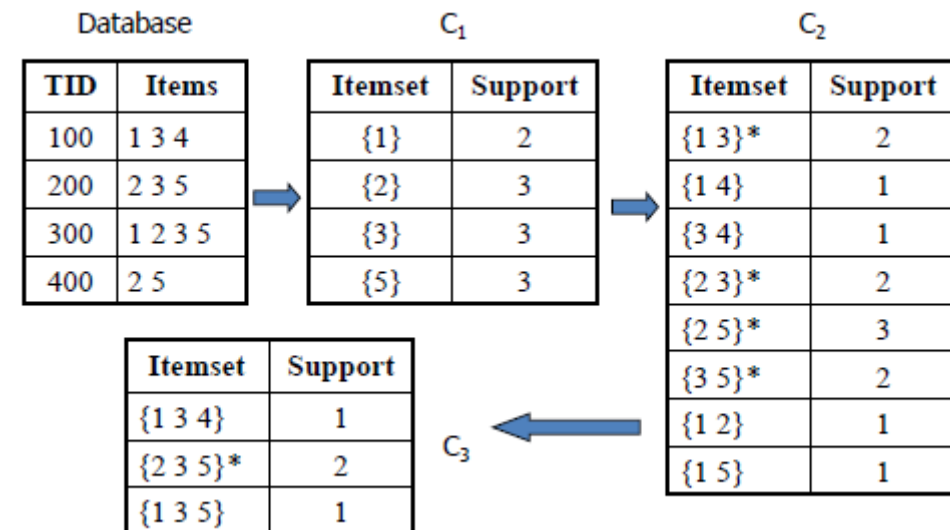
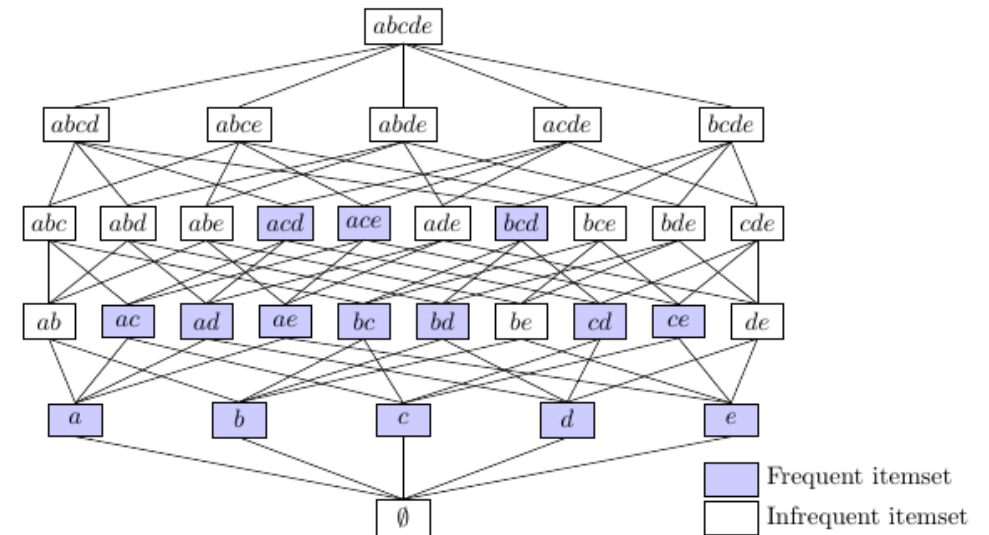
$$\text{Affinity}(A\&C) = \frac{\text{Support}(A\&C)}{\text{Support}(A) + \text{Support}(C) - \text{Support}(A\&C)} = \frac{n_{A\&C}}{n_A + n_C - n_{A\&C}}$$

$$\text{Leverage}(A\&C) = \text{Support}(A\&C) - [\text{Support}(A) * \text{Support}(C)] = \frac{n_{A\&C}}{n} - \frac{n_A * n_C}{n^2}$$



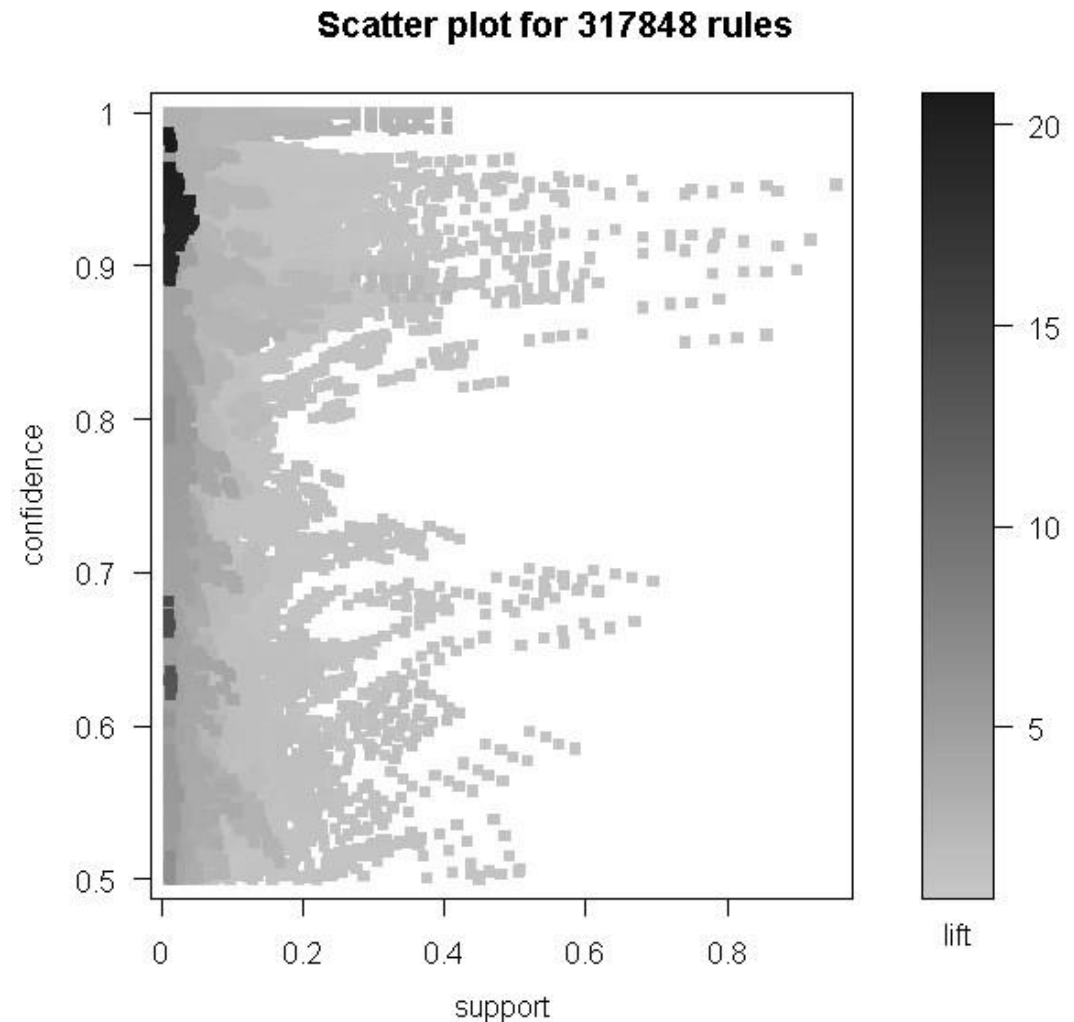
Apriori

- Key Idea
 - If $\{a,c,f\}$ is frequent, $\{a,c\}$ must be frequent
 - Downward closure a.k.a. anti-monotonicity
- Algorithm
 - Find all frequent 1-itemsets (frequent \rightarrow > support)
 - Find all frequent 2-itemsets for filtered 1-itemsets
 - Find all frequent 3-itemsets for filtered 2-itemsets
 - ...
- Salient Features
 - Exploits downward closure to optimize search
 - Lower Support \rightarrow Higher computational complexity
 - Confidence, Lift as post-processing filters



Example : Apriori in R

```
data("AdultUCI");  
Adult = as(AdultUCI, "transactions");  
rules = apriori(Adult, parameter=list(support=0.01, confidence=0.5));
```



<https://www.r-bloggers.com/association-rule-learning-and-the-apriori-algorithm/>



Apriori : Limitations

- Computational Complexity
 - How long does it take to run?
 - How much memory does it need?
- Approaches
 - Throw more compute / RAM at it
 - Parallelize
 - Increase support
 - Leverage item hierarchy
 - Another algorithm?
- Rare patterns
 - Rules with low support but maybe very valuable
 - People who buy _____ likely to buy luxury cars
- When sequence of transactions matters
 - Define a sequence as an item
 - Combinatorial Explosion : Computational Complexity
 - Read-Up!



Association Rules : Summary

- Association Rules
 - Are probabilistic statements
 - About relations among features - across elements
 - Use a transaction-itemset data model
 - The strength (statistical significance) of an association rule is measured using support, confidence, lift etc.
- Applications
 - Market Basket Analysis
 - Any dataset where features take values : 0/1
 - Can work in any dataset where features can be *represented as* taking only two use values : 0/1
 - Preprocessing: Discretization, Feature selection
- Apriori
 - Input : Dataset, minsupport
 - Output: association rules
 - Exploits downward closure to optimize search
 - Lower Support → Higher computational complexity
 - Confidence, Lift as post-processing filters
- FP Growth
 - Scan the DB only twice;
 - Summarize itemsets in an efficient data structure (FP-Tree)
 - Extract frequent itemsets from the FP-Tree



Unsupervised Learning: Summary

- ... algorithms used to draw inferences from datasets consisting of input data without labeled responses.
- ... the task of inferring a function to describe hidden structure from unlabeled data.
 - Distribution / Density
 - Summary statistics
 - Clustering: Find data elements (rows) which are similar.
 - **Association Rules**: Find features (dimensions) which are correlated
 - Dimensionality Reduction: Find smaller dimensional representations which preserve data's essential structure.
- Unsupervised
 - Association Rules: Find patterns when we don't know what we are looking for.
 - {Diaper, Beer} → **Milk**
 - {Milk} → {Diaper, Beer}
 - {Milk, Diaper} → **Beer**
- Supervised
 - What if we are only interested in identifying customers who bought Milk?
 - Split the customer base into two classes: Customers who bought Milk and who did not.
 - Binary classification problem : Given purchases of other customers



Q?

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