

# Supervised Learning

*Modelling*



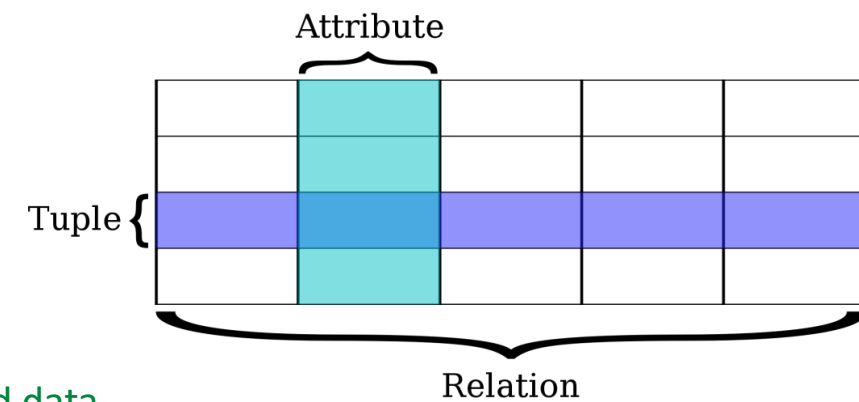
# Unsupervised Learning

- Unsupervised Learning

- Given X
- ... the task of inferring a function to describe hidden structure from unlabeled data.
- Distribution / Density, Summary statistics, Clustering, Association Rules, Dimensionality Reduction

- Supervised Learning

- Given X & y (a particular random variable)
- Find what is the relation between the particular random variable and other random variables
  - What if we are only interested in identifying customers who bought Milk?
- Find how the value of the dependent variable depends on the value of others
- Find how the outcome is related to the features
- Key Variations: Type of outcome / dependent r.v.
  - Numeric (Discrete, Continuous, [0,1])
  - Categorical : Nominal, Ordinal



# The idea of a Model

- Physical
  - a physical copy of an object such as a globe
- Computer
  - a simulation to reproduce behavior of a system
- Scientific
  - a simplified & idealized understanding of physical systems
  - Newton's Law model the physical universe
- Conceptual
  - a representation of a system using general rules & concepts
- Mathematical
  - a representation of a system using mathematical concepts
- Statistical
  - a parameterized set of probability distributions

$$y = 3x + 4$$

$$y = x^2$$

$$y = e^x$$

$$y = \log(x)$$

$$y = \sin(x)$$

*All models are false. Some models are useful.*



# The idea of a Statistical / ML Model

- Model

- A function relates two (or more) variables
- Captures the relation between  $x$  and  $y$
- For every value of  $x$ , there must be a unique value of  $y$
- Data looks like  $\{(x_1, y_1), (x_2, y_2), \dots, (x_i, y_i), \dots, (x_n, y_n)\}$

$$y = 3x + 4$$

$$y = x^2$$

$$y = e^x$$

$$y = \log(x)$$

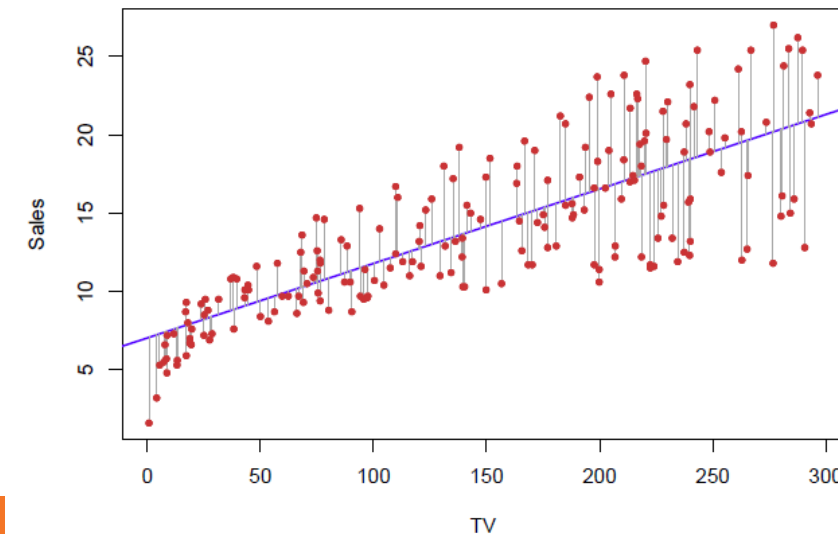
$$y = \sin(x)$$

$$y = f(x)$$

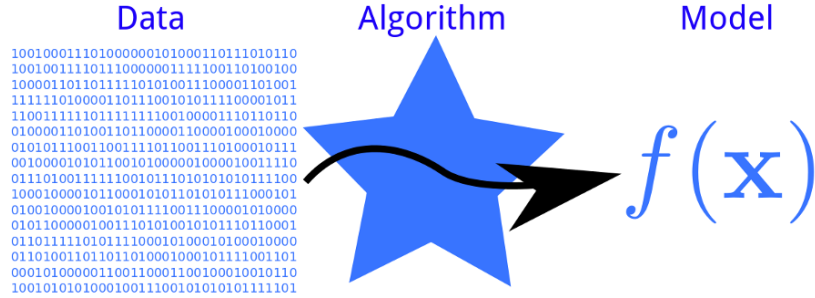
- Statistical Model

- Real world data looks like  $\{(x_1, y_1), (x_1, y_2), \dots, (x_n, y_n)\}$
- Multiple values of  $y$  for a single value of  $x$
- In expectation (on average), “model” captures the relationship between variables
- Effects due to unobserved variables / Errors in measurements : capture by  $\varepsilon$
- Randomness / Stochasticity / Noise : Zero-mean; Normal distribution
- Violations of Assumption is an indication of systemic errors

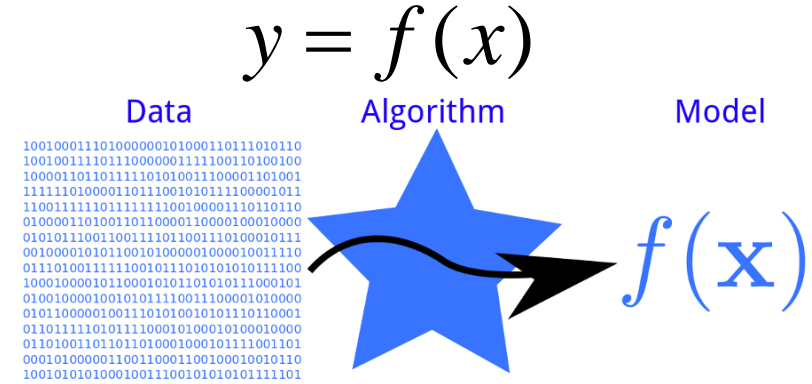
$$y = f(x) + \varepsilon \quad \hat{y} = \hat{f}(x) + 0$$
$$\varepsilon \sim N(0, \sigma) \quad P(y | x)$$



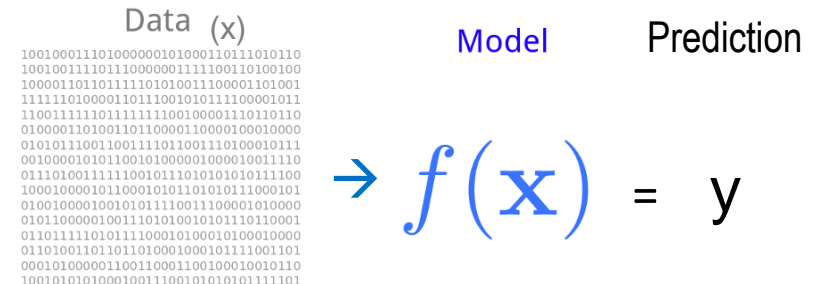
# Un/Supervised Learning



- Given X
  - ... the task of inferring a function to describe hidden structure from unlabeled data.
  - Distribution / Density, Summary statistics, Clustering, Association Rules, Dimensionality Reduction



- Given  $X$  &  $y$  (a particular random variable)
  - Find what is the **relation** between the particular random variable and other random variables
  - Find how the value of the **dependent (particular)** variable depends on the value of others
  - Find how the outcome is related to the **features**
  - Generalize : Make **predictions** about new data



# Supervised Learning

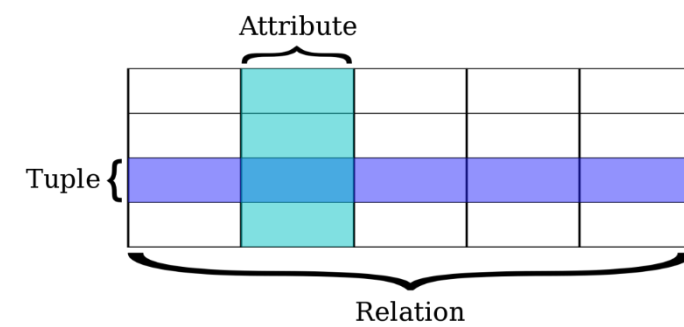
*Variants*



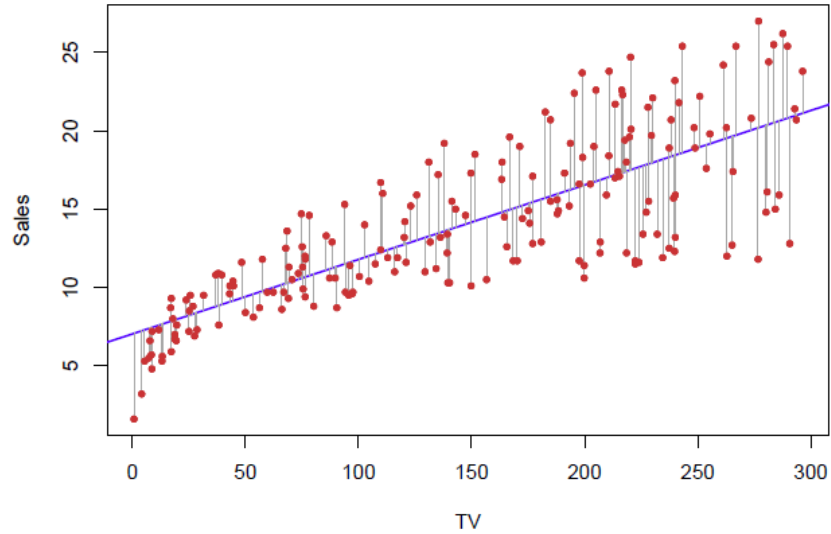
# Un/Supervised Learning Models

- Supervised
  - Dependent vs. Independent Variables
  - Is there a variable of interest? Labelled data?
  - Do you know what you are looking for?
  - View the data as  $\{(x_1, y_1), (x_1, y_2), \dots, (x_n, y_n)\}$
  - Regression vs. Classification
- Unsupervised
  - No clearly defined Dependent Variable
  - Find patterns in data
  - View the data as  $\{(x_1), (x_2), \dots, (x_n)\}$
  - Often, a pre-processing step to Supervised

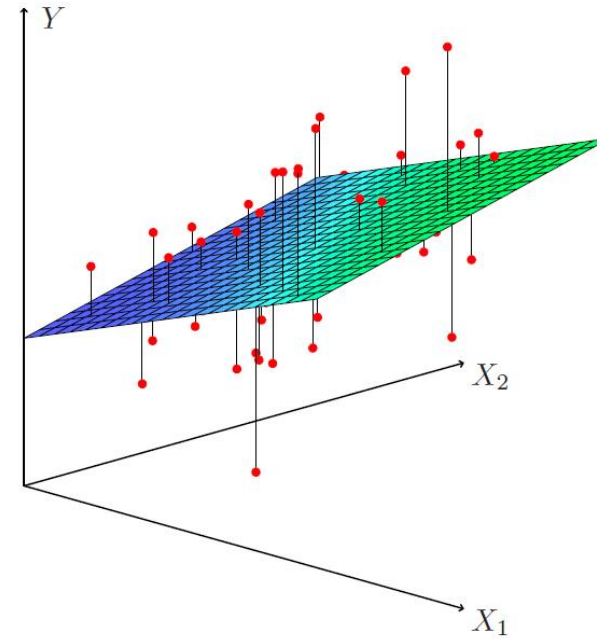
- Parameteric
  - Specify the “form” of  $f$  (*Specify model class*)
  - Learn exact  $f$  (*Learn model parameters*)
  - Restrictive but Interpretive
  - Less data required for learning
- Non-Parameteric
  - Learn model directly (*No restrictions on model class*)
  - Flexible but less Interpretive
- Model-Based vs. Model-Free
  - Models are not the only game in town
  - Model-Based: Linear Regression (What is the model?)
  - Model-Free: Nearest Neighbor, Collaborative Filtering



# Supervised Learning : Linear Regression



$p=1$



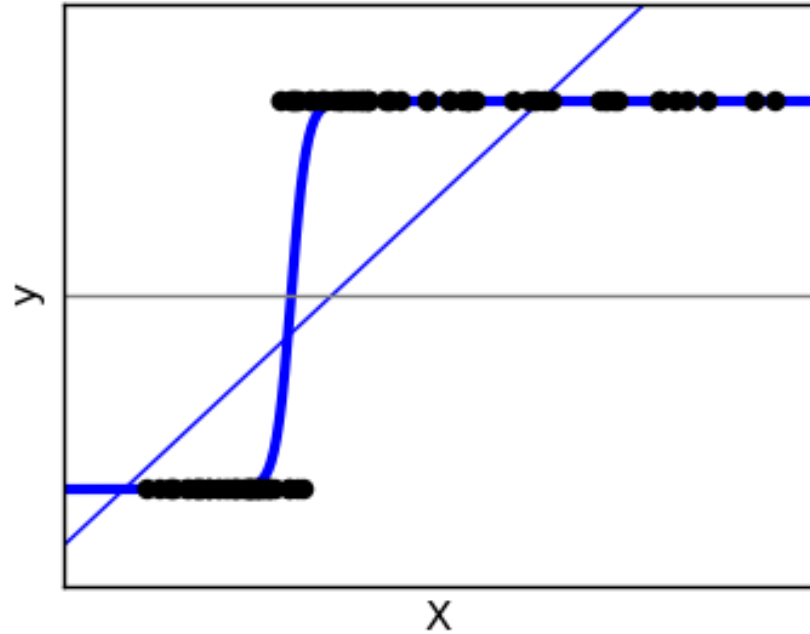
$p=2$

$p > 2$  ?

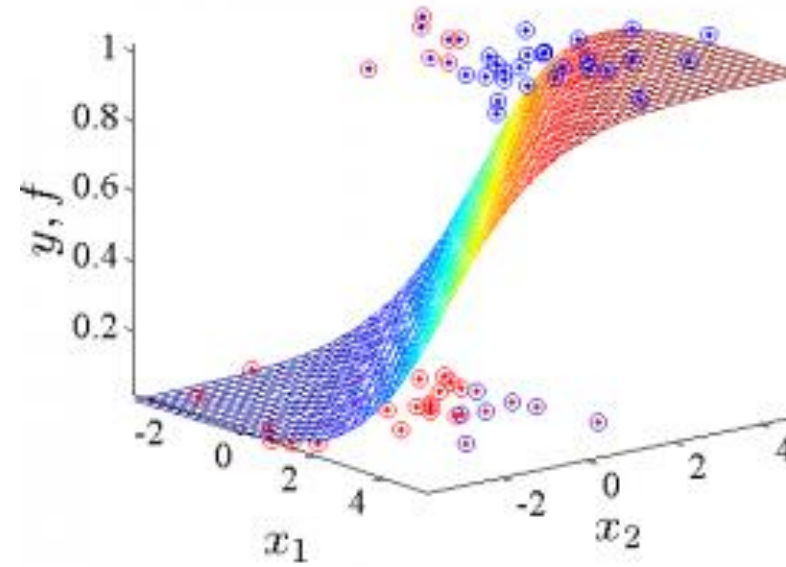




# Supervised Learning : Binary classification



$p=1$

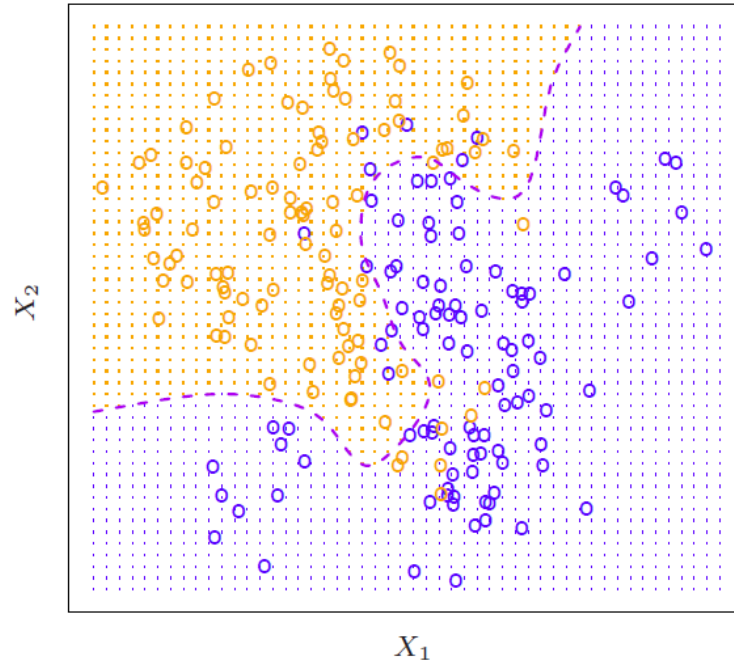


$p=2$

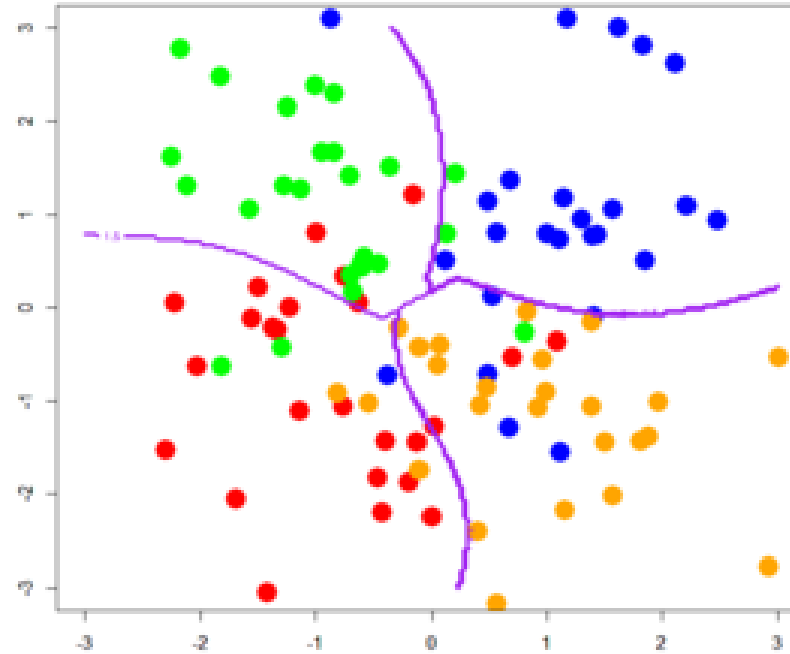
$p > 2$



# Supervised Learning : From Binary to Multi Class



$p=2$



$p=2$

$p > 2$  ?



# SL: Variant Summary

- Numeric  $y$ 
  - Given input data  $x$ ,  $f(x)$  is a numeric value
  - Regression: Linear, polynomial, lasso
  - Time Series :  $y = xt+1$
- Numeric  $y$  in  $[0,1]$ 
  - Given input data  $x$ ,  $f(x)$  is a numeric value in between 0,1 (e.g. probability)
  - Regression: Logistic
- Categorical  $y$ 
  - Given input data  $x$ ,  $f(x)$  is a label / class / category (e.g. churn or not)
  - Classification: knn, logistic, decision tree, svm
- Ordinal  $y$ 
  - Learn  $f(x)$  such that given input data  $x$ ,  $f(x)$  is a rank (e.g. 1st, 2nd , ...)
  - Ranking

