

# General Physics I (PHYS 101)

## Lecture 15

### Interference (Contd.)

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- 1 Young's double slit experiment
- 2 Interference on thin films due to reflected light

# Young's double slit experiment

Consider a source of monochromatic light  $S$ .  $A$  and  $B$  are two narrow slits of width  $d$  very close to each other as shown in figure. A screen  $XY$  is placed at a distance  $D$  from slits as shown in figure.

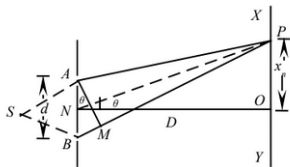


Figure 1

Let  $P$  be the position of  $n^{th}$  bright or dark fringe and  $\theta$  be the angle made by  $NP$  with  $NO$ . A perpendicular  $AM$  is drawn to  $BP$ . Since  $A$

## Young's double slit experiment (contd.)

and B are too close to each other, AM meets NP practically at right angles such that  $\angle BAM = \theta$ . Now, form  $\triangle PNO$ ,

$$\tan \theta = \frac{PO}{NO} = \frac{x_n}{D}$$

And from  $\triangle BAM$ ,  $\sin \theta = \frac{BM}{AB} = \frac{BM}{d}$ . For small angle,  $\sin \theta \approx \tan \theta$ .

So,

$$\therefore \frac{BM}{d} = \frac{x_n}{D}$$

$$\therefore BM = \frac{x_n d}{D}$$

Here BM is the path difference between the waves.

## Young's double slit experiment (contd.)

Now for bright fringes, path difference  $(BM) = n\lambda$

$$\text{or, } \frac{x_n d}{D} = n\lambda$$

$$\therefore x_n = \frac{n\lambda D}{d}$$

This relation gives the distance of  $n^{\text{th}}$  bright fringe from the center of the fringe system.

For  $(n - 1)^{\text{th}}$  bright fringe, we can have

$$x_{n-1} = \frac{(n - 1)\lambda D}{d}$$

## Young's double slit experiment (contd.)

So, the fringe width  $\beta$  is

$$\beta = x_n - x_{n-1} = \frac{n\lambda D}{d} - \frac{(n-1)\lambda D}{d}$$
$$\therefore \beta = \frac{\lambda D}{d}$$

Again for dark fringes, path difference  $(BM) = (2n+1)\frac{\lambda}{2}$

$$\text{or, } \frac{x_n d}{D} = (2n+1)\frac{\lambda}{2}$$

$$\therefore x_n = \frac{(2n+1)\lambda D}{2d}$$

This relation gives the distance of nth dark fringe from the center of the fringe system.

## Young's double slit experiment (contd.)

For  $(n - 1)^{th}$  dark fringe, we can have

$$x_{n-1} = \frac{[2(n - 1) + 1]\lambda D}{2d} = \frac{(2n - 1)\lambda D}{2d}$$

So, the fringe width  $\beta$  is

$$\begin{aligned}\beta &= x_n - x_{n-1} = \frac{(2n + 1)\lambda D}{2d} - \frac{(2n - 1)\lambda D}{2d} \\ \therefore \beta &= \frac{\lambda D}{d}\end{aligned}$$

Thus, the fringe width for dark and bright fringes are equal i.e. fringes in Young's double slit experiment are equally spaced.

# Interference on thin films due to reflected light

Let us consider a thin film of thickness  $t$  and refractive index  $\mu$  as shown in figure. A ray of light AB strikes at point B with angle of incident  $i$ , get reflected along BE and also refracted along BC with angle of refraction  $r$ . At C it again reflected along CD and finally emerges out along DF.



# Interference on thin films due to reflected light (contd.)

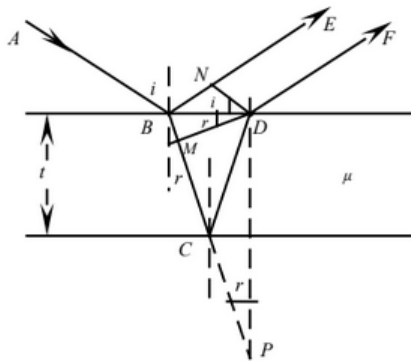


Figure 2

## Interference on thin films due to reflected light (contd.)

Draw perpendiculars  $DN$  and  $DM$  to  $BE$  and  $BC$  such that  $\angle BDN = i$  and  $\angle BDM = r$ . Produce  $BC$  to meet  $DP$  at  $P$  so that  $DP = 2t$  and  $\angle MPD = r$ . Let  $x$  be the path difference between the waves emerging from  $B$  and  $D$  respectively. Then,

$$x = \mu(BC + CD) - BN \quad (1)$$

From Snell's law,

$$\mu = \frac{\sin i}{\sin r} = \frac{BN/BD}{BM/BD} = \frac{BN}{BM}$$

$$\therefore BN = \mu BM$$

## Interference on thin films due to reflected light (contd.)

And also,  $CD = CP$  so equation (1) becomes,

$$\begin{aligned}x &= \mu(BC + CP) - \mu BM \\&= \mu(BP - BM) \\&= \mu PM\end{aligned}$$

From  $\triangle MPD$ ,

$$\cos r = \frac{PM}{PD} = \frac{PM}{2t} \Rightarrow PM = 2t \cos r$$

# Interference on thin films due to reflected light (contd.)

So, path difference is

$$x = 2\mu t \cos r$$

According to electromagnetic theory (Stoke's Law of reflection) :

When a light wave is reflected from the surface of an optically denser medium, it suffers a phase change of  $\pi$  or path difference of  $\frac{\lambda}{2}$  but it suffers no change in phase when reflected at the surface of optically rarer medium. So the corrected path difference becomes,

$$x = 2\mu t \cos r + \frac{\lambda}{2}$$

## Interference on thin films due to reflected light (contd.)

For bright fringes path difference is integral multiple of  $\lambda$  i.e.

$$x = n\lambda$$

$$\therefore 2\mu t \cos r + \frac{\lambda}{2} = n\lambda$$

$$\text{or, } 2\mu t \cos r = n\lambda - \frac{\lambda}{2}$$

$$\therefore 2\mu t \cos r = (2n - 1)\frac{\lambda}{2} \quad (2)$$

For dark fringes path difference is half odd integral multiple of  $\lambda$  i.e.

$$x = (2n + 1)\frac{\lambda}{2}$$

## Interference on thin films due to reflected light (contd.)

$$\therefore 2\mu t \cos r + \frac{\lambda}{2} = (2n+1) \frac{\lambda}{2}$$

$$\text{or, } 2\mu t \cos r = (2n+1) \frac{\lambda}{2} - \frac{\lambda}{2}$$

$$\therefore 2\mu t \cos r = n\lambda \quad (3)$$

Equations (2) and (3) are the required conditions for bright and dark fringes for interference due to reflected light.