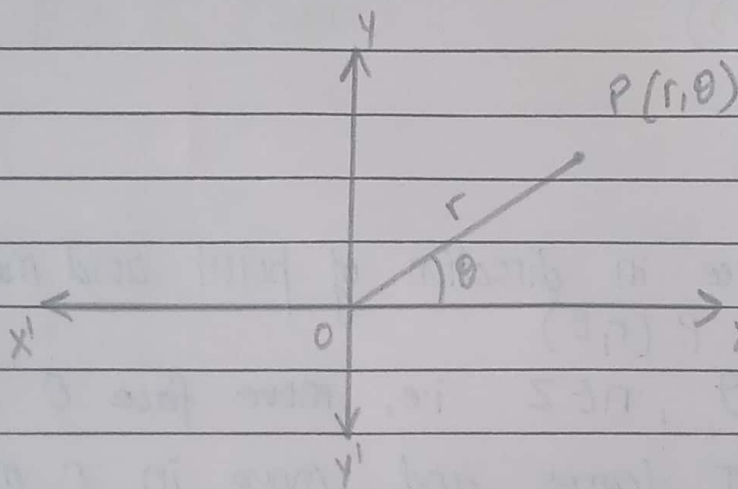


Unit : 1

COORDINATE SYSTEM

Polar Coordinates:

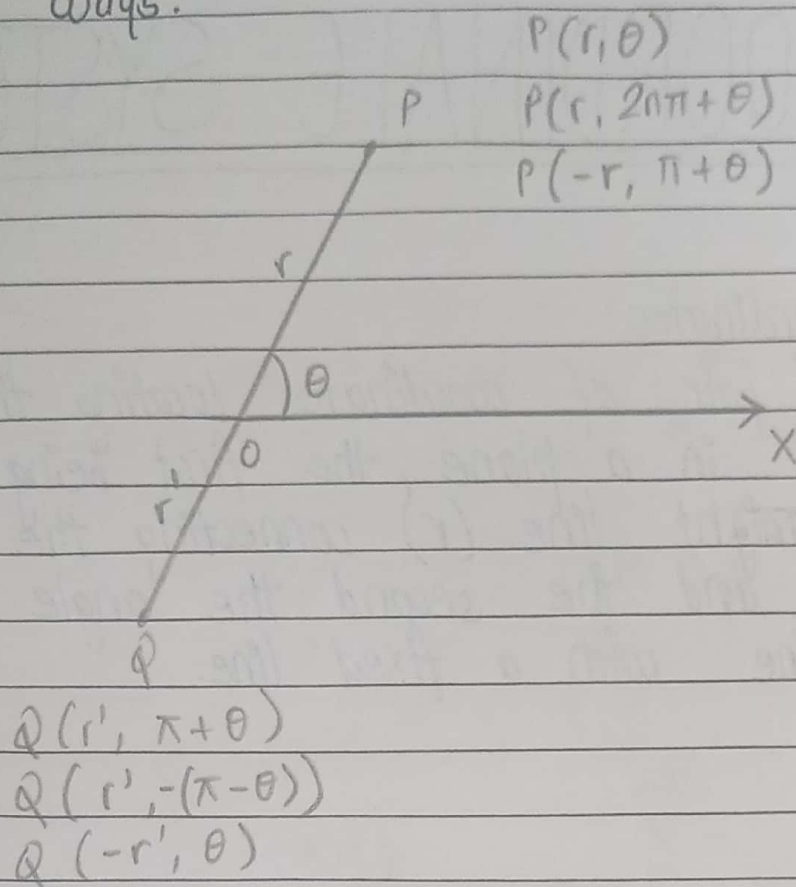
A pair of coordinates locating the position of a point in a plane, the first being the length of the straight line (r) connecting the point to the origin, and the second the angle (θ) made by this line with a fixed line.



* Needed things:

- i) Fixed point 'O' (origin) and the line OX
ie, positive x-axis is taken as reference line (initial ray).
- ii) Angle made ' θ ' by OP line ie, directed line with
 $OP = r$
- iii) The point P is denoted by (r, θ) .

→ Polar coordinates can be represented in many ways.



i) Moving θ degree in direction of point and move r magnitude. $P(r, \theta)$

ii) Moving $2n\pi + \theta$, $n \in \mathbb{Z}$ i.e., move θ direction and spin 2π degree and move in r magnitude. $P(r, \theta + 2n\pi)$

iii) Face towards opposite point to the original point in π direction and move in negative direction $P(-r, \theta)$

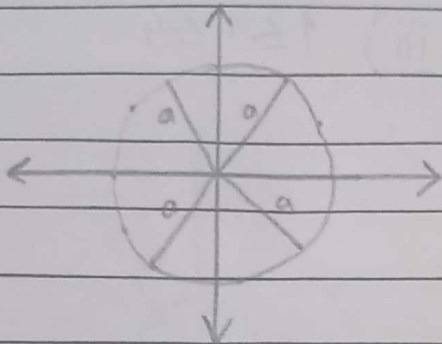
iv) Face towards point in negative direction and then move r' magnitude. $Q(r', -(\pi - \theta))$

* Note: Angle 1st, magnitude 2nd.

Graphing Polar Plot

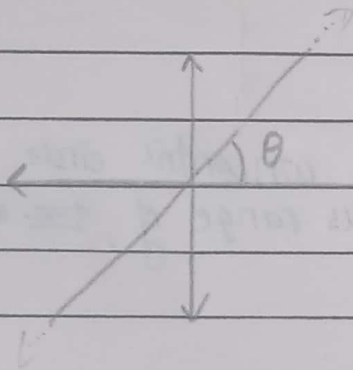
<Q>: What do the following represent?

(i): $r = a$ (const.)



Circle with center at origin with radius a .

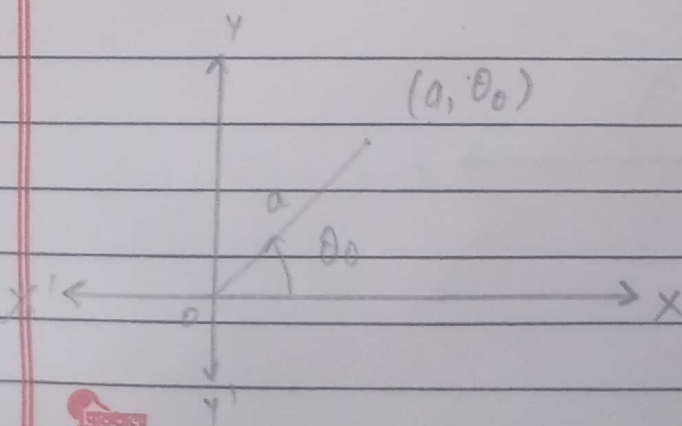
(ii) $\theta = \theta_0$ (const)



Gives straight line making angle θ_0 with reference line passing through origin.

(iii): $r = a$ (const), $\theta = \theta_0$ (const)

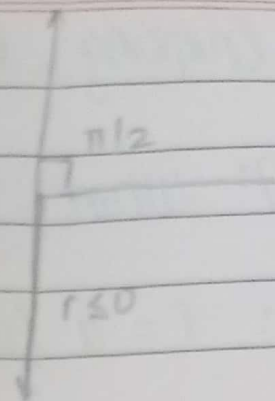
Gives a point.



Graph the following:

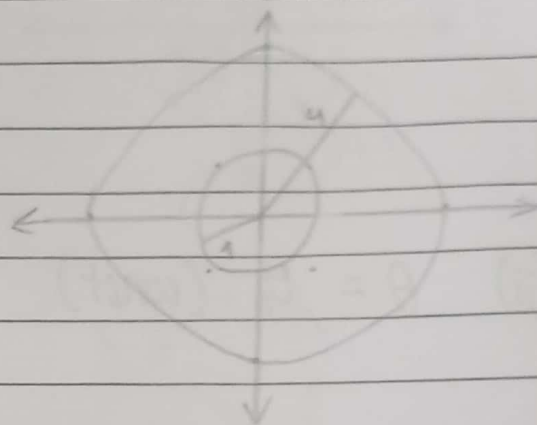
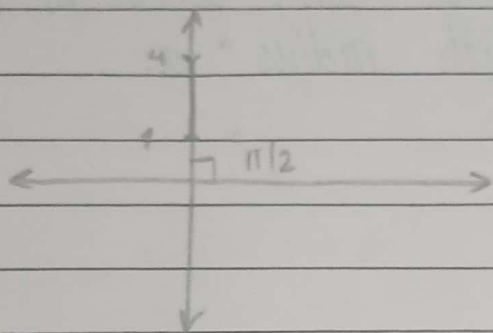
i) $\theta = \pi/2, r \leq 0$

↳ Represents negative y-axis.



ii) $\theta = \pi/2, 1 \leq r \leq 4$

iii) $1 \leq r \leq 4$



gives concentric circle with radius range of $1 \leq r \leq 4$

(iii): $\frac{\pi}{6} \leq \theta \leq \pi$

gives region of plane.

