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QUANTUM COMPUTING FOR EVERYONE

CHRIS BERNHARDT

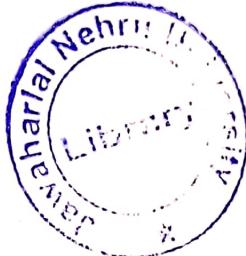
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