# FUNKTIONAL PROGRAMMING -- MONADS

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## Monads – what is the problem?

- The base problem: how to affect the world
- Problem is more prevalent in pure functional programming style
  - No side-effects
  - □ That's right: no side-effects!
- □ But you've all seen it too!

Consequence: expressing computation declaratively

# Example

```
def hypotenuse(x, y):
    return math.sqrt(math.pow(x, 2) + math.pow(y, 2))
```

Now we want to trace it, or affect the world in it:

```
def hypotenuse(x, y):
    h = math.sqrt(math.pow(x, 2) + math.pow(y, 2))
    print "x=" + str(x) + "; y=" + str(y) + "; h=" + str(h)
    return h
```



# Example

```
def hypotenuse(x, y):

h = math.sqrt(math.pow(x, 2) + math.pow(y, 2))
return h, "x=" + str(x) + ";y=" + str(y) + "h=" + str(h)
```

Signature was float, float -> float
Signature now is float, float -> float, string

> math.pow(hypotenuse(6, 16), 4);



pow is float, float -> float, not (float, string), float -> float

### Let's invent monads!

```
def hypotenuse (x, y):
           return math.sqrt(math.pow(x, 2) + math.pow(y, 2))
    Let's call functions (float, float) -> (float, string) Traceable f f
#((float, float) -> float) -> ((float, float) -> (float, string))
def makeTraceable f f(f):
    def traceable f f(x,y):
         h=f(x,y)
         return h, str(f) + " was called, result=" + str(h) + " n"
    return traceable f f
# Now let's make one of these! And call it
>> aTraceableHypo = makeTraceable f f(hypotenuse)
>> aTraceableHypo(3,4)
(5.0, '< function hypotenuse at <math>0xfff42a74> was called, result=5.0\n')
```

### Let's invent monads!

```
>>> math.pow(aTraceableHypo(3,4), 2)
TypeError: a float is required
```



It would be nice to trace math.pow too! Let's "lift" it Let's call functions (float, string), float -> (float, string) Traceable\_f\_s\_f

### Let's invent monads!

Still too tightly coupled, let's "bind" them externally instead:

```
>>> bind(aTraceableHypo(3,4), aTraceablePowOf2)
```

Exercise: write the function bind

```
# (t, (t->t')) -> t'
def bind(t, f):
    return f(t)
```

Voila! – our first monad!

#### What is a monad?

□ It's a container

- An active container... it has behavior to:
  - Wrap itself around a type
  - Bind functions together

#### What is a monad?

- A type constructor, m
- A function that builds values of that type
   a -> m a (makeX, previously)
- A function that combines values of that type with computations that produce values of that type to produce a new computation for values of that type m a -> (a -> m b) -> m b (bind, previously)

### Kinds of monads

- □ In Haskell
  - Identity
  - Maybe
  - Error
  - List

  - State
  - Reader
  - Writer
  - Continuation

# Identity monad

□ Simple function application

$$bind(x, f) = f(x)$$

# Maybe monad

- Functions that return either a value of a certain type (Something) or no value at all (Nothing)
- Nothing values stop the computation; Something values get passed on

A nice alternative to exceptions!

```
public interface Maybe<T>{}
public class Nothing<T> : Maybe<T>
    public override string ToString()
        return "Nothing";
public class Something<T> : Maybe<T>
    public T Value { get; private set; }
    public Something (T value)
        Value = value;
    public override string ToString()
        return Value. To String();
```

- Next, we need 2 operations:
  - One to construct Maybe's
  - One to bind Maybe's to the rest of the computation

#### Maybe type constructor:

```
public static Maybe<T> ToMaybe<T>(this T value)
{
    return new Something<T>(value);
}
```

#### Example:

```
3.ToMaybe();
"hello".ToMaybe();
```

#### Bind:

### Let's use it

```
public static Maybe<int> Div(this int numerator, int denominator)
    return denominator == 0
               ? (Maybe<int>) new Nothing<int>()
               : new Something<int>(numerator/denominator);
15.Div(3);
>> 5
15.Div(0);
>> Nothing
```

### But there's more

```
36. ToMaybe().Bind(n => Div(n, 3)).Bind(m => Div(m, 0)).Bind(p => Div(p, 9)); >> Nothing
```

Div(9) never happens