

Assignment 1AName :- Ghanshyam V. SanapClass :- B.F.Roll No. :- 56Subject :- A.T

DOP

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# Assignment 1A

Q.2] Consider following instance of 8 puzzle problem:-

8	7	6		-	8	7
2	1	5		2	3	6
3	4	-		3	4	5

Initial

Final Configuration

Consider Heuristic Functions defined below:-

$h_1$  = Misplaced files Count except space

$h_2$  = Currently placed files Count except space

$h_3$  = Sum of Manhattan distance between Current & Crossed position of all threes except

Answer the following questions:-

- (a) In 8 puzzle problem we are concerned with getting to goal Configuration within least no. of Stage, All moves are thus equally costly, Define  $g(n)$  in your own words. What will be the cost of 6 steps deviation to some arbitrary 8-puzzle instance?

Ans → The lowest path cost  $g(n)$  can be the cost to reach the goal Configuration in least steps. In our case, we can reach the final Configuration in at least 4 moves: UP, UP, LEFT, LEFT. Since all moves are equally costly, we concept  $g(n)$  as



$$g(n) = 1 + 1 + 1 + 1$$

$$g(n) = 4$$

consider the following arbitrary 8-puzzle instance which gives solution in 6 steps:-

8	7	6
2	1	5
-	3	4

The Solution can be represented as:-

$$\begin{aligned} &\{ \{ 8, 7, 6 \}, \{ 2, 1, 5 \}, \{ -, 3, 4 \} \} \rightarrow \{ \{ 8, 7, 6 \}, \{ 2, 1, 5 \}, \{ 3, -4 \} \} \\ &\{ \{ 8, 7, 6 \}, \{ 2, 1, 5 \}, \{ 3, 4, - \} \} \rightarrow \{ \{ 8, 7, 6 \}, \{ 2, 1, 3 \}, \{ 3, 4, 5 \} \} \\ &\{ \{ 8, 7, 3 \}, \{ 2, 1, 6 \}, \{ 3, 4, 5 \} \} \rightarrow \{ \{ 8, -7 \}, \{ 2, 1, 6 \}, \{ 3, 4, 5 \} \} \rightarrow \\ &\{ \{ -, 8, 7 \}, \{ 2, 1, 6 \}, \{ 3, 4, 5 \} \} \end{aligned}$$

Since all the moves are equally costly, the cost would be

$$g(n) = 6$$

(c) Draw exhaustive state space tree of depth limited to 4 for instance of 8-puzzle problem in the question.



Ans (c)

Initial Configuration

8	7	6
2	1	5
3	4	-

LEFT

8	7	6
2	1	5
3	-	4

UP

8	7	6
2	1	-
3	4	5

LEFT

8	7	6
2	1	5
-	3	4

UP

8	7	6
2	-	5
3	1	4

RIGHT

8	7	6
2	1	5
3	4	-

UP

8	7	-
2	1	6
3	4	5

LEFT

8	7	6
2	-	1
3	4	5

DOWN

8	7	6
2	1	5
3	4	-

LEFT

8	-	7
2	1	6
3	4	5

DOWN

8	7	6
2	1	-
3	4	5

LEFT

-	8	7
2	1	6
3	4	5

DOWN

8	1	7
2	-	6
3	4	5

RIGHT

8	7	-
2	1	6
3	4	5

final configuration



(e) Compute  $h_i(n)$  where  $i = 1, 2, 3$  &  $n =$  initial state, final/goal state from question.

→

for  $i = 1$ ,  $n =$  initial state

$h_1(\text{initial}) =$  Misplaced files count except space

$$h_1(\text{initial}) = 4$$

$n =$  goal state

$$h_1(\text{goal}) = 0$$

for  $i = 2$ ,  $n =$  initial state

$h_2(\text{initial}) =$  Currently placed files Count except space

$$h_2(\text{initial}) = 4$$

for  $n =$  goal state

$$h_2(\text{goal}) = 8$$

for  $i = 3$ ,  $n =$  initial state

$h_3(\text{initial}) =$  sum of Manhattan distance between current & pos. Current position of all times except space

$$h_3(\text{initial}) = 0 + 0 + 0 + 0 + 1 + 1 + 1 + 1 = 4$$

for  $n =$  goal state

$$h_3(\text{goal}) = 0$$